

Energy-aware Trajectory Optimization of Connected and Automated Vehicle Platoons through a Signalized Intersection

A Research Report from the University of California Institute of Transportation Studies

Xiao Han, Postdoctoral Researcher, Department of Civil and Environmental Engineering, University of California, Davis

Rui Ma, Postdoctoral Researcher, Department of Civil and Environmental Engineering, University of California, Davis

H. Michael Zhang, Professor, Department of Civil and Environmental Engineering, University of California, Davis

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Energy-aware Trajectory Optimization of Connected and Automated Vehicle Platoons through a Signalized Intersection

UNIVERSITY OF CALIFORNIA INSTITUTE OF TRANSPORTATION STUDIES

June 2019

Xiao Han, Department of Civil and Environmental Engineering, University of California, Davis *Rui Ma,* Postdoctoral Scholar, Department of Civil and Environmental Engineering, University of California, Davis

H. Michael Zhang, Professor, Department of Civil and Environmental Engineering, University of California, Davis

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Energy-aware Trajectory Optimization of CAV Platoons through a Signalized Intersection

Xiao Han, Rui Ma, H. Michael Zhang^{*}

4 Department of Civil and Environmental Engineering, University of California, Davis, 95616, CA, United
 5 States

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Traffic signals, while serving an important function to coordinate vehicle movements through intersections, also cause frequent stops and delays, particularly when they are not properly timed. Such stops and delays contribute to significant amount of fuel consumption and greenhouse gas emissions. The recent development of connected and automated vehicle (CAV) technology provides new opportunities to enable better control of vehicles and intersections, that in turn reduces fuel consumption and emissions. In this paper, we propose platoon-trajectory-optimization (PTO) to minimize the total fuel consumption of a CAV platoon through a signalized intersection. In this approach, all CAVs in one platoon are considered as a whole, that is, all other CAVs follow the trajectory of the leading one with a time delay and minimum safety gap, which is enabled by vehicle to vehicle communication. Moreover, the leading CAV in the platoon learns of the signal timing plan just after it enters the approach segment through vehicle to infrastructure communication. We compare our PTO control with the other two controls, in which the leading vehicle adopts the optimal trajectory (LTO) or drive with maximum speed (AT), respectively, and the other vehicles follow the leading vehicle with a simplified Gipps' car-following model. Furthermore, we extend the controls into multiple platoons by considering the interactions between the two platoons. The numerical results demonstrate that PTO has better performance than LTO and AT, particularly when CAVs have enough space and travel time to smooth their trajectories. The reduction of travel time and fuel consumption can be as high as 40%and 30% on average, respectively, in the studied cases, which shows the great potential of CAV technology in reducing congestion and negative environmental impact of automobile transportation.

r Keywords: Connected-automated vehicle, platoon, fuel consumption, optimal control

8 1. Introduction

Transportation is a major consumer of non-renewable energy. In 2018, the U.S. trans portation sector alone consumed over 143 billion gallons of motor fuel, and it is predicted

^{*}Corresponding author: hmzhang@ucdavis.edu.

that the fuel consumption in transportation in the U.S. will remain at a high level in the 11 foreseeable future [1]. Furthermore, the world consumption of transportation fuel is forecast 12 to increase significantly with a steady increase in vehicle ownership as incomes in developing 13 countries rise [2]. There has been a practice of the so-called eco-driving among environmen-14 tally conscious drivers, which tries to avoid hard accelerations and decelerations based on 15 real-time driving conditions, particularly on urban streets with numerous traffic lights [3– 16 5]. This practice was shown to reduce personal fuel consumption, but without the advance 17 knowledge of traffic signal status, the practice is based on ad hoc rules and furthermore, its 18 impact on other drivers, and hence at a system level, is not certain. Fortunately, the rapidly 19 evolving connected and autonomous vehicle (CAV) technology can overcome these limita-20 tions of eco-driving through better communication and greater vehicle control, and hence 21 provides a powerful tool to reduce both fuel consumption and greenhouse gas emissions more 22 effectively [6–8]. 23

In the transportation system, intersections play a crucial role in assigning and controlling 24 traffic flow. In many cases, traffic streams on arterial roads are controlled by traffic signals at 25 intersections. Vehicles must stop at signals on red, which increases their fuel consumption, 26 emission levels and travel time due to acceleration/deceleration maneuvers and idling re-27 quired at traffic signals. In this paper, we propose a platoon-trajectory-optimization (PTO) 28 method, to control CAVs moving through a signalized intersection as so to minimize the 29 total fuel consumption of the platoon. In this method, we assume the CAV platoon knows 30 the traffic light's schedule before entering the approach of the intersection, and consider all 31 CAVs in one platoon as a whole, and classify the scenarios of CAVs passing a signalized 32 intersection into two categories according to whether all CAVs can cross the intersection 33 within one signal cycle or not, i.e., all CAVs passing the intersection within one green light 34 window (Scenario I) and the CAVs passing the intersection in two successive green light 35 windows (Scenario II). In Scenario I, the trajectory of the leading CAVs is copied by the 36 other ones in the platoon with reaction time delay and a safety space gap, enabled by vehicle 37 to vehicle communication. In Scenario II, the platoon must be split into two subplatoons, 38 and the other CAVs in each subplatoon follow the leading one with trajectory copying. 39

In addition, we compare PTO with other two methods based on a simplified Gipps' car-40 following model, i.e., leading-trajectory-optimization (LTO) and aggressive driving (AT). In 41 LTO method, we suppose the leading vehicle is a CAV, and the others are human-driven 42 vehicles. The strategy of the leading CAV is to minimize its fuel consumption with optimal 43 control and pass the signalized intersection without considering the following vehicles. The 44 human-driven vehicles travel across the intersection with a simplified Gipps' car-following 45 model and stop before the intersection when the red light is on. In AT method, we suppose 46 all vehicles in one platoon are human-driven. The leading vehicle travels with maximum 47 speed and stops before the intersection until the green light is on. As similar as LTO, the 48 other vehicles follow the leading vehicle with a simplified Gipps' car-following model in AT. 49 Furthermore, we apply the PTO method to control multiple platoons across a signalized 50 intersection in consideration of the intersections between two platoons. A virtual trajectory 51 generated based on the last CAV of the platoon in front is taken as a constraint of the back 52 platoon to ensure safety. The results of case studies and sensitivity analysis demonstrate 53

PTO outperforms LTO and AT in reducing both fuel consumption and travel time when the CAVs have enough space and traffic throughput to smooth their trajectories.

The rest of this paper is organized as follows. Section 2 reviews related literature. Section 3 presents the results of optimizing one vehicle with optimal control. In Section 4, the frameworks of PTO and the other two methods, LTO and AT, are described. Case studies and sensitivity analysis are conducted to compare the performance of the three methods. In Section 5, we extend the three methods into multiple platoons. As similar as Section 4, we conduct case studies and sensitivity analysis in the multiple-platoon level. Section 6 concludes the paper and discusses some further research directions.

63 2. Literature review

With the emergence of technologies, such as connected vehicle (CV), autonomous vehicle 64 (AV) and connected autonomous vehicle (CAV), vehicle trajectory control strategies have 65 been proposed to reduce fuel consumption for arterial roads controlled by speed limits or 66 traffic signals in recent years [9-17]. Liu et al. present a fuel-consumption-aware variable-67 speed limit (FC-VSL) traffic control scheme to minimize the fuel consumption on freeways 68 with the problem formulated as an optimal control problem [10]. He et al. propose a multi-69 stage optimal control formulation to optimize vehicle trajectory on signalized arterial roads 70 that considers both vehicle queue and traffic light status [11]. Ubiergo and Jin present a hi-71 erarchical green driving strategy based on feedback control to smooth stop-and-go traffic in 72 signalized networks with vehicle-to-infrastructure (V2I) communication [12]. With numeri-73 cal analysis, they demonstrate that their method can save about 15% in travel delays and 74 8% in fuel consumption and greenhouse gas emissions. Zhou et al. and Ma et al. propose 75 a parsimonious shooting heuristic algorithm to construct vehicle trajectories on a signalized 76 highway segment, in which the trajectories of each vehicle is broken into a few sections that 77 each one is analytically solvable [13, 14]. Li and Zhou propose an intersection automation 78 policy (IAP) to capture complex traffic dynamics and schedule resources (green lights) to 79 serve both CAV and human-driven vehicles [15]. Yao et al. present a trajectory smoothing 80 method based on individual variable speed limits with location optimization (IVSL-LC), 81 and compare the method with the individual advisory speed limits (IASL). They demon-82 strate IVSL-LC method can greatly increase traffic efficiency and reduce fuel consumption 83 in contrast to IASL [16]. Feng et al. propose a two-stage optimization framework that 84 combines trajectory smoothing and traffic signal control [17]. Simulation results show that 85 the framework can reduce 24% vehicle delay and 13.8% CO2 emissions. 86

The above studies mainly focus on solving the problem of trajectory smoothing across 87 a signalized intersection at the individual vehicle-level. Moreover, with the development of 88 CAV, it is possible to reduce fuel consumption and travel time at the platoon-level [18–20]. 89 Wei et al. present a set of integer programming and dynamic programming models for 90 scheduling longitudinal trajectories based on a space-time lattice [18]. By adjusting the lead 91 vehicle's speed and platoon-level reaction time at each time step, their framework can control 92 the complete set of trajectories in a platoon efficiently [18]. Lioris et al. assess the potential 93 mobility benefits of platooning with connected vehicle technology (CVT), and platooning 94

in CVT environment can double throughput in urban roads [19]. Stebbins et al. propose 95 a trajectory optimization method by optimizing for the delay over the entire trajectory 96 instead of suggesting an individual speed [20]. Moreover, they extend the framework to 97 platoon-level, in which other vehicles follow the leading vehicle with a car-following model. 98 In this paper, we develop a vehicle trajectory control framework for CAV platoons to re-99 duce fuel consumption and travel delay. To take advantage of vehicle to infrastructure (V2I) 100 and vehicle to vehicle (V2V) communication in a CAV traffic environment, traffic signal 101 timing status is transmitted to the leading CAV vehicle before it enters the intersection, and 102 the platoon leaves the intersection at free-flow speed (or the speed limit of the road), which 103 serves at the final state condition for our formulated optimal trajectory control problem. 104 Our approach first develops the optimal control policy for a single CAV, then extends it to 105 a vehicle platoon, and finally designs a mechanism to control multiple platoons traversing a 106 signalized intersection considering the interactions between platoons. 107

¹⁰⁸ 3. Optimal control of one CAV

First, let us optimize the trajectory of one CAV with optimal control from location s_0 to location s_1 ($s_1 > s_0$) without traffic signal. Suppose, at time t_0 , one CAV with maximum speed v_0 travel at location s_0 , and the vehicle must arrive at location s_1 at the maximum speed of v_0 . In this situation, we need to optimize one trajectory to minimize fuel consumption for the vehicle traveling from location s_0 to location s_1 with speed limit. The framework for solving this problem can be presented as follows.

(1) System Model: For a single vehicle, state vector x(t) is defined as,

$$\mathbf{x}(t) \stackrel{\Delta}{=} [x_1(t) \ x_2(t)]^T = [s(t) \ v(t)]^T, \tag{1}$$

where s(t) is the distance from s_0 , and v(t) is the speed of the vehicle. Those two variables denote the state of the vehicle. The control vector only contains one variable, i.e., the acceleration rate, which is defined as,

$$\mathbf{u}(t) \stackrel{\Delta}{=} [a(t)]^T. \tag{2}$$

¹¹⁹ Therefore, the dynamics of the system can be described with differential equations,

$$\dot{\mathbf{x}}(t) \stackrel{\Delta}{=} \left[\begin{array}{c} \dot{x}_1(t) = v(t) \\ \dot{x}_2(t) = a(t) \end{array} \right]$$
(3)

(2) Optimal Control Problem Formulation: The problem of controlling the CAV is formulated to minimize the fuel consumption as follows,

$$\mathbf{J} = \int_{t_0}^{t_f} c(v(t), a(t)) dt, \tag{4}$$

where t_0 and t_f are the corresponding time points of s_0 and s_1 , respectively; c(v(t), a(t)) is an instantaneous fuel consumption model presented at the Conference of Australian Institutes

of Transportation Research (CAITR) [10, 21], which is given by, 124

$$c(v(t), a(t)) = \begin{cases} \alpha, & a(t) \leq -\frac{R_a(t) + R_r(t)}{M_v} \\ \alpha + \beta_1 R_T(t) v(t), & a(t) \in (-\frac{R_a(t) + R_r(t)}{M_v}, 0) \\ \alpha + \beta_1 R_T(t) v(t) + \frac{\beta_2 M_v a(t)^2 v(t)}{1000}, & a(t) \geq 0 \end{cases}$$
(5)

where $R_T(t)$, $R_a(t)$, and $R_r(t)$ are the tractive force, air drag, and rolling resistance, respec-125 tively. They can be calculated as follows: 126

$$R_T(t) = M_v a(t) + R_a(t) + R_r(t) + R_g(t)$$
(6)

127

$$R_a(t) = \frac{\rho}{2} C_D A_f v(t)^2 \tag{7}$$

128

$$R_r(t) = 0.01 \frac{1 + v(t)}{44.73} M_v g \tag{8}$$

The definitions and values of the parameters from Eq. 5 to Eq. 8 are shown in Table 1. 129 Note that the default values of the parameters of the fuel consumption model assume the 130 vehicle travels in on a flat surface (i.e., grade force $R_q(t) = 0$) and neglect the wind pressure. 131 However, the fuel consumption model can easily be extended to more general scenarios that 132 can reflect a real environment by adjusting the values of the parameters of R_T . Here, for 133 the sake of simplification, we only consider the parameters shown in Table 1.

Tat	Table 1: Parameter definitions and values in the fuel consumption model.					
Parameter	Definition	Value				
α	Idle fuel consumption rate	0.375mL/s				
β_1	Efficiency parameter	0.09mL/kJ				
β_2	Energy-acceleration efficiency parameter	$0.03mL/(kJ.m/s^2)$				
M_v	Average vehicle mass	1400 kg				
ρ	Air density	$1.2256 kg/m^3$				
C_D	Drag coefficient	0.54				
A_f	Average vehicle frontal area	$2.1m^{2}$				
g	Standard gravity	$9.8m/s^{2}$				

134

The above optimal control problem is challenging to find analytical solutions [10]. In-135 stead, the numerical Gauss pseudospectral method (GPM) is used to discretize a continuous 136 optimal control problem into a nonlinear program (NLP) and obtain the optimal solution. 137 The technique is an orthogonal collocation method where the collocation points are the 138 Legendre-Gauss (LG) points [22]. Here, we employ the General Algebraic Modeling System 139 (GAMS) to obtain the optimal control solution [23]. 140

Figure 1 presents the optimal results with different travel distance, maximum speed, 141 deceleration/acceleration constraint, and LG points. Figure 1(a)-(d) show the relationship 142 between optimal fuel consumption and travel time. The corresponding travel time with 143

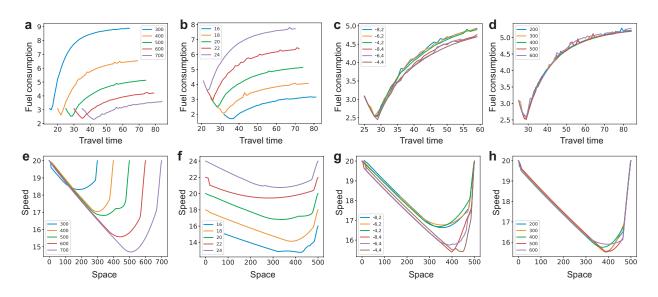


Figure 1: Optimal control outcomes of one CAV. (a-d) The relationship between optimal fuel consumption per 100 meters and travel time; (e-h) The relationship between travel speed and space for optimal trajectories with lowest fuel consumption. (a, e) Optimal results with different control space s_1 and the same maximum speed ($v_0 = 20m/s$) and deceleration/acceleration constraint ($a_{br} = -4m/s^2, a_{fw} = 2m/s^2$) and number of LG points ($N_{LG} = 200$). (b, f) Optimal results with different maximum speed and the same control space ($s_1 = 500m$) and deceleration/acceleration constraint ($a_{br} = -4m/s^2, a_{fw} = 2m/s^2$) and number of LG points ($N_{LG} = 200$). (c, g) Optimal results with different deceleration/acceleration constraint and the same control space ($s_1 = 500m$), maximum speed ($v_0 = 20m/s$) and number of LG points ($N_{LG} = 200$). (d, h) Optimal results with different number of LG points and the same control space ($s_1 = 500m$) and maximum speed ($v_0 = 20m/s$) and deceleration/acceleration constraint ($a_{br} = -4m/s^2, a_{fw} = 2m/s^2$).

the lowest fuel consumption is a little longer than the shortest travel time with constant 144 maximum speed. At a given travel distance, the optimal fuel consumption decreases firstly 145 and then increases over travel time. Figure 1(e)-(h) show the optimal trajectories with lowest 146 fuel consumption. The CAV traveling with lowest fuel consumption needs to decelerate 147 firstly, and then gradually accelerate to maximum speed. It is a bit counterintuitive at 148 first because it is generally believed that keeping a constant velocity would consume less 149 fuel in contrast to a trajectory with speed variations. However, a closer examination of the 150 fuel consumption model of Eq. 5 reveals the reason for this counterintuitive phenomenon. 151 When the acceleration $a \geq 0$, even though it has a high impact on the fuel consumption 152 in the third term, vehicle speed v(t) dominates in both the second and third terms. The 153 implication is that the effects of the lower speed could offset the impact of high acceleration 154 rate on fuel consumption. Besides, we find the deceleration/acceleration constraint and the 155 number of LG points do not have a significant influence on the performance of optimal 156 control. Therefore, in the following sections, we set the maximum brake deceleration as 157 $a_{br} = -4m/s^2$, maximum acceleration as $a_{fw} = 2m/s^2$ and the number of LG points as 158 $N_{LG} = 200.$ 159

160 4. Platoon optimization

161 4.1. The framework of PTO method

Based on the optimal control framework for one vehicle described in the above section, we propose the PTO method to optimize one platoon across a signalized intersection by considering all CAVs in the platoon as a whole. The components of the PTO method are described as follows.

Road: We only consider one single lane leading to a signalized intersection. The leading CAV in one platoon enters location s_0 and arrives location s_1 with maximum speed v_0 . The traffic signal is installed at location s_1 .

Traffic Signal: The traffic signal we consider here is a fixed signal timing including a sufficient length of G and an effective red time of R. Thus, the cycle length of the traffic signal is C := G + R.

Platoon: The number of CAVs in one platoon is N. The initial state of the platoon (the 172 leading CAV) arriving at location s_0 is that all CAVs have the same speed of v_0 and the space 173 between two vehicles in the platoon is same. Suppose the reaction time of CAV is τ and the 174 minimum gap between the two vehicles is d. The space between two CAVs at initial state 175 is $l = d + v_0 \tau$, and the total length of the platoon at initial state is $L_p = (d + v_0 \tau)(N - 1)$. 176 Moreover, we suppose all CAVs in one platoon can pass the green light windows if the leading 177 vehicle arrives the intersection at the beginning of the green light window, i.e., $G > \frac{(N-1)l}{m}$. 178 **Trajectory copying:** The basic idea of PTO method is that all vehicles can copy the 179 trajectory of the leading vehicles with reaction time delay and minimum gap delay. Figure 2 180 presents an illustration of trajectory copying, in which Trajectory 1 is the trajectory of the 181 leading CAV in one platoon, and the following CAV in the platoon can copy Trajectory 1 182 with time delay τ and minimum gap delay d, and travel along Trajectory 2. 183

Two scenarios: For one platoon across a signalized intersection, we divide the process into two scenarios according to whether the platoon can pass the signalized intersection in one green light window. The two scenarios are described as follows.

• Scenario I: The platoon can pass the signalized intersection within one green light window.

Scenario II: The CAVs in one platoon cannot pass the intersection within a green light window. The platoon must be split into two subplatoons, i.e., Subplatoon A (the former one) and Subplatoon B (the latter one), and pass the signalized intersection in two successive green light windows.

Figure 3 illustrates the operations of controlling one platoon across a signalized intersection with PTO. The platoon is composed of 6 CAVs, which can not pass the intersection within one green light window (Scenario II). The platoon is split into two subplatoons, and 3 CAVs in each subplatoon. As shown in Figure 3, the control space of Subplatoon A (blue trajectories) and Subplatoon B (black trajectories) are $s_1 - s_0$ and $s_1 - s_0 + 3(v_0\tau + d)$, respectively.

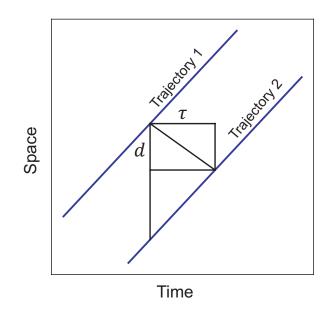


Figure 2: Illustration of trajectory copying.

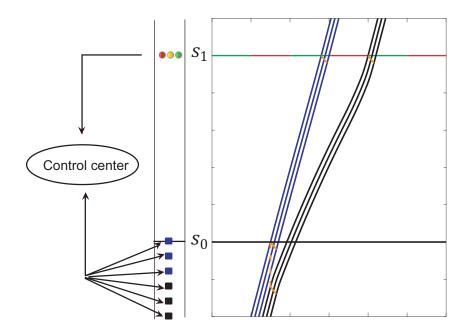


Figure 3: Illustration of control framework of PTO method.

Taking Scenario I and Scenario II into consideration, the total fuel consumption of one platoon with PTO method across a signalized intersection can be formulated as,

$$J_p = N_A J_A + N_B J_B, (9)$$

,

where $N_A \ge 0$ and $N_B \ge 0$; N_A (N_B) denotes the number of CAVs and J_A (J_B) the fuel consumption of one vehicle in Subplatoon A (B). Substituting J_A and J_B with Eq. 4, we can obtain,

$$J_p = N_A \left[\int_{t_0}^{t_f^A} c(v(t), a(t))dt + c(v_0, 0)L_p/v_0\right] + N_B \left[\int_{t_0}^{t_f^B} c(v(t), a(t))dt + c(v_0, 0)(L_p - (v_0\tau + d)N_A/v_0)\right]$$
(10)

where t_0 is the starting time of optimizing the leading CAV in Subplatoon A (B); t_f^A and t_f^B are the ending time of optimizing leading CAV in Subplatoon A and Subplatoon B, respectively. Unlike the optimal control of one CAV, the length of the platoon is considered in the control framework of one platoon. The locations of leading CAVs in Subplatoon A and Subplatoon B at t_0 are s_0 and $s_0 - N_A(v_0\tau + d)$, respectively. The locations of leading CAVs in the two subplatoons at t_f^A and t_f^B are both s_1 .

The platoon optimization of passing a signalized intersection is to minimize J_p with all CAVs traveling across the intersection in green light windows. The constraints of guaranteeing all vehicles crossing the intersection within green light windows can be described as,

$$\begin{cases} t_{f}^{A} \setminus C \leq G \\ (t_{f}^{A} + (N_{A} - 1)(\tau + d/v_{0})) \setminus C \leq G \\ \lfloor t_{f}^{A} \rfloor = \lfloor t_{f}^{A} + (N_{A} - 1)(\tau + d/v_{0}) \rfloor \\ t_{f}^{B} \setminus C \leq G \\ (t_{f}^{B} + (N_{B} - 1)(\tau + d/v_{0})) \setminus C \leq G \\ \lfloor t_{f}^{B} \rfloor = \lfloor t_{f}^{B} + (N_{B} - 1)(\tau + d/v_{0}) \rfloor \\ \lfloor t_{f}^{A} \rfloor + 1 = \lfloor t_{f}^{B} \rfloor \end{cases}$$
(11)

The first six equations in Eq. 11 can guarantee all CAVs in Subplatoon A (B) across one green light window, and the last equation can ensure Subplatoon A and Subplatoon B get through the intersection at two successive traffic signal cycles.

In combination of constraint conditions of Eq. 11 and fuel consumption of Eq. 5, we can obtain the optimization trajectories of all vehicles in one platoon with minimizing the total fuel consumption described in Eq. 10.

220 4.2. Two other methods for comparison

We compare our trajectory optimization framework PTO with two other methods that adopt a simplified Gipps' car-following model, namely leading-trajectory-optimization (L-TO) and aggressive-trajectory (AT). In the LTO method, we assume the leading vehicle in a platoon is a CAV, and optimize its trajectory based on the optimal control framework. The other vehicles in the platoon are human-driven ones and follow the leading vehicle with the simplified Gipps' car-following model [12, 24, 25]. If the following vehicles arrive at the signalized intersection in red, they need to stop until the green light is on. For the AT method, we assume there is no CAV in the platoon, and the leading vehicle travel from s_0 to s_1 with maximum speed v_0 . If the leading vehicle arrives at the intersection in red, it is forced to wait until the green light is on; otherwise, it travels through the intersection with maximum speed. The other vehicles in the platoon follow the leading vehicle with the simplified Gipps' car-following model and stop if the red light is on.

The upper limits of acceleration defined in simplified Gipps' car-following model includes two parts, i.e., free-flow and congested traffic acceleration, which is formulated as,

$$\begin{cases} a_i^{\text{free}} = 2.5a_{fw}(1 - \frac{v_i(t)}{v_0})\sqrt{0.025 + \frac{v_i(t)}{v_0}} \\ a_i^{\text{cong}} = \frac{1}{T} \left[\frac{1}{\tau_c} \left(s_{i-1}(t) - s_i(t) - d - \frac{v_{i-1}(t)^2 - v_i(t)^2}{2a_{br}}\right) - v_i(t)\right] \end{cases}$$
(12)

where T is the sensitivity coefficient, τ_c the drivers' time of reaction, and d the minimum gap between two adjacent vehicles. The acceleration of vehicle i at time t is,

$$a_i(t) = \max\{a_{br}, \min\{a_i^{\text{free}}(t), a_i^{\text{cong}}(t)\}\}.$$
(13)

The speed and location of one vehicle in the next time step with Gipps' car-following model are defined as,

$$\begin{cases} v_i(t + \Delta t) = \max\{0, \min\{v_i(t) + a_i(t)\Delta t, v_0\}\}\\ s_i(t + \Delta t) = \max\{s_i(t), \min\{s_i(t) + v_0\Delta t, s_i(t) + v_i(t)\Delta t + \frac{a_i(t)\Delta t^2}{2}\}\} \end{cases}$$
(14)

where Δt is the time step between iterations.

240 4.3. Case study

In this section, we conduct one case study to illustrate the performance of our proposed platoon optimization method PTO and the other two methods, LTO and AT. The parameters in the case study are set as follows: enter location $s_0 = 0$, traffic signal location $s_1 = 500m$, maximum speed $v_0 = 20m/s$, CAV reaction time $\tau = 1.5s$, and driver's reaction $\tau_c = 2s$. The number of vehicles in the platoon is N = 6, and the length of the platoon is $L_p = 200m$ at the initial state. The cycle length of traffic signal is C = 40s, and R = G. The parameters in the fuel consumption model are shown in Table 1.

Figure 4 displays trajectories of all vehicles in one platoon with different entry time 248 at location s_0 . The first, second and third row denote the results of PTO, LTO and AT, 240 respectively. The first two columns are illustrations of Scenario I, in which all vehicles 250 can pass the intersection at one green window. The trajectories in the last column belong 251 to Scenario II, in which one platoon needs to split into two subplatoons and passes the 252 signalized intersection in two successive green light windows. Table 2 shows the average fuel 253 consumption and travel time per vehicle per 100 meters for the platoons shown in Figure 4. 254 We calculate the fuel consumption and travel time of each vehicle from location $s_0 - L_p$ to 255 location $s_1 + (v_0^2)/2a_f w$ with considering the length of a platoon and the acceleration space 256 of human-driven vehicles to compare the performance of PTO, LTO and AT. When entry 257

time $t_0 = 5$, the trajectories with AT are blocked by a red signal and need to wait before 258 the intersection until the light is on green, however, the vehicles with PTO and LTO can 259 adjust their trajectories to avoid stopping before the signalized intersection. In this case, the 260 trajectories with LTO consumes less fuel than PTO and AT because the following vehicles 261 with LTO have more space and time to smooth their trajectories than PTO. When entry 262 time $t_0 = 15s$, all vehicles can pass the signalized intersection without the influence of red 263 light, and PTO outperforms LTO and AT in fuel consumption. Because all vehicles with 264 AT can travel from s_0 to s_1 and cross the intersection with maximum speed, the travel time 265 of AT is lowest among the three methods. When the entry time $t_0 = 30s$, the trajectories 266 with PTO are optimized in each subplatoon and pass the intersection with maximum speed. 267 In this case, the PTO method can reduce both fuel consumption and travel time in contrast 268 to the other two methods. 269

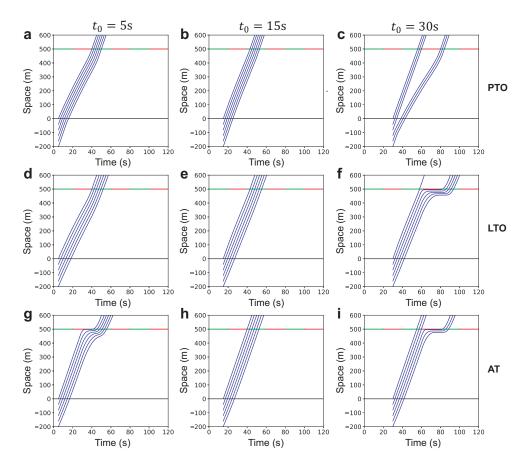


Figure 4: Trajectories of one platoon entering at different times. (a-c) Trajectories with PTO, (d-f) trajectories with LTO and (g-i) trajectories with AT.

Figure 5 (a) presents average fuel consumption per vehicle per 100 meters for one platoon entering location s_0 at different times t_0 . Overall, the performance of PTO is better than LTO and AT in fuel consumption. The mean values of fuel consumption per vehicle per

	Fuel consumption (ml)			Travel time (s)		
t_0	5	15	30	5	15	30
PTO	3.39	2.74	3.15	6.25	5.38	6.25
LTO	3.08	3.12	4.34	6.41	5.53	8.12
AT	5.17	3.54	4.58	7.04	5.16	6.59

Table 2: Average fuel consumption and travel time per vehicle per 100 meters shown in Figure 4.

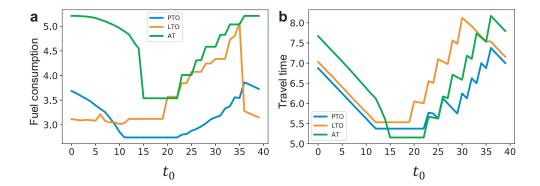


Figure 5: The performance of fuel consumption (ml) and travel time (s) per vehicle per 100 meters with PTO, LTO and AT methods for different entry time. The parameters are set for simulation: $s_1 = 500m$, $v_0 = 20m/s$, N = 6, and C = 40s.

100 meters over different entry times in one cycle of traffic signal with PTO, LTO and AT 273 are 3.14, 3.54 and 4.59 ml, respectively. In contrast to LTO and AT, the fuel consumption 274 with PTO method falls by about 11.30% and 31.59%, respectively. When all vehicles are 275 blocked by red light and need to pass the intersection at next traffic signal cycle, the fuel 276 consumption with LTO may outperform PTO. In this condition, the following vehicles with 277 a simplified Gipps' car-following model have more space and travel time to smooth their 278 trajectories. Figure 5 (b) depicts the results of average travel time per vehicle per 100 279 meters. The mean values of travel time over different entry times in one cycle of traffic 280 signal with PTO, LTO and AT are 6.06, 6.60 and 6.52 seconds, respectively. Even though 281 we only take fuel consumption as our optimization objective, the performance of PTO in 282 reducing travel delay is better than LTO and AT because CAVs have less reaction time and 283 pass the signalized intersection with maximum speed in PTO method. Compared with LTO 284 and AT, the travel time reduced about 8.18% and 7.06% in PTO method, respectively. All 285 in all, from the case study, we find the PTO method can not only reduce fuel consumption 286 but also ease traffic congestion and increase traffic efficiency. 287

288 4.4. Sensitivity analysis

From the previous case study, we find our PTO method is beneficial for reducing fuel consumption and travel delay. In this section, we analyze how the values of the critical parameters influence the performance of PTO, LTO and AT methods. Figure 6 presents the results of sensitivity analysis about different control space s_1 , maximum speed v_0 , the number of vehicles in one platoon N, and the length of traffic signal cycle C.

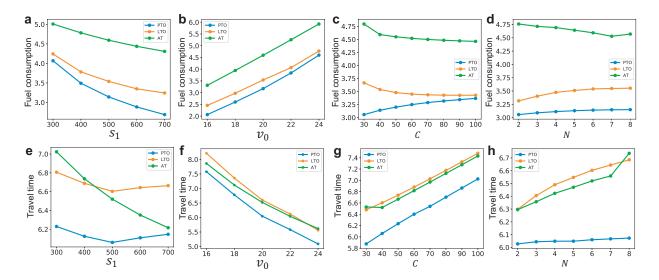


Figure 6: Sensitivity analysis of one platoon across a signalized intersection with different parameters. (a-d) Fuel consumption and (e-h) travel time per vehicle per 100 meters. The parameters except for parameters analyzed are set as: $s_1 = 500m$, $v_0 = 20m/s$, N = 6 and C = 40s. All data points are calculated over different entry times in one traffic signal cycle.

As shown in Figure 6 (a), the average fuel consumption of the three methods all decreas-294 es with the increase of control space. The gap in fuel consumption between PTO and the 295 other two methods also increases with the increase of control space. Figure 6 (b) shows the 296 average fuel consumption with different maximum speeds. The average fuel consumption of 297 the three methods all increases with the maximum speed, because travel speed contributes 298 positively to the second and third terms in the fuel consumption model in Eq. 5. Figure 6 (c) 299 shows the sensitivity of the length of the traffic signal cycle on fuel consumption. The fuel 300 consumption of the PTO method increases with the increase of the cycle length. However, 301 for the other two methods, the fuel consumption decreases with the increase of the length 302 of the traffic signal cycle. It is because the fuel consumption with optimal control increases 303 with travel time (see Figure 1). When the traffic signal has a significantly long cycle, the 304 PTO method, by requiring the CAV platoon to arrive at the start of the green interval, 305 does not take full advantage of the long green time window. Figure 6 (d) shows that 306 the fuel consumption increases slightly with large platoon size, and the number of vehicles 307 in one platoon does not have a significant influence on the fuel consumption of PTO. Fig-308 ure 6 (e-h) show the results of travel time in different conditions. Even though we only 309

take fuel consumption as our optimization objective, the PTO method is also beneficial to 310 reduce travel time compared with LTO and AT methods. In summary, our PTO method 311 considerably outperforms the LTO method in reducing fuel consumption and increasing 312 traffic throughput in the situation with longer control distance, lower maximum speed and 313 shorter traffic signal cycle. Moreover, even though only the leading vehicle is CAV in LTO 314 method, it can improve the performance in fuel consumption and travel time in comparison 315 with AT, which is consistent with both theoretical and experimental found in the literature 316 results [12, 16, 26]. 317

³¹⁸ 5. Optimization of multiple platoons

319 5.1. The constraint between two platoons

The previous results are for one platoon with different entry times, and no interaction between two platoons is considered. Therefore, in this section, we extend our PTO method to multiple platoons. The probability of the leading vehicle in platoon k entering location s_0 at time $t_{k,1}$ according to the time of the last vehicle in platoon k-1 entering location is described as,

$$p(t_{k,1}) = \lambda e^{-\lambda [(t_{k,1} - t_{k-1,N}) - \tau_p]},$$
(15)

where λ is the average event rate, τ_p is minimum time headway between two platoons, and $t_{k,1}$ and $t_{k-1,N}$ denotes the time of the leading vehicle in platoon k and the last vehicle in platoon k-1 entering location s_0 , respectively.

For multiple platoons, the behaviors of one platoon will affect the performance of the next platoon. If we optimize the trajectory of platoon by platoon, the trajectory of the last vehicle in platoon k-1 may cross with the trajectory of the leading vehicle in platoon k. To avoid a crash between two platoons, we suppose one virtual vehicle follow the last vehicle in platoon k-1 with time delay τ and space delay d. The trajectory of the virtual vehicle in platoon k-1 is the constraint of the leading vehicle in platoon k, which can be described as,

$$s_{k-1}^{\text{virtual}}(t) \ge s_{k,1}(t),\tag{16}$$

where $s_{k-1}^{\text{virtual}}(t)$ and $s_{k,1}(t)$ denote the locations of virtual vehicle in platoon k-1 and the leading vehicle in platoon k at time t, respectively. Moreover, the constraint between two platoons also is applied to avoid a crash between two subplatoons.

338 5.2. Case study

In this section, a case study is conducted to compare the performance of PTO, LTO and AT for multiple platoons. The parameters in the case study are set as follows: the number of platoons $N_p = 10$, the average event rate $\lambda = 0.2$, and the minimum time difference between two platoons $\tau_p = 10s$. The other parameters are the same as the case mentioned above for one platoon.

Figure 7 illustrates trajectories of multiple platoons. Overall, the PTO method can reduce congestion and let more vehicles cross the signalized intersection in less traffic signal cycles in contrast to LTO and AT. According to the trajectories of multiple platoons in Figure 7, we can obtain the average fuel consumption and travel time per vehicle per 100 meters which are shown in Table 3. We can see that more than 30% of fuel consumption and 40% of travel time are reduced with PTO method in contrast to LTO and AT method. However, because LTO only has a local influence on multiple platoons across a signalized intersection, the fuel consumption of the LTO method is not significantly reduced in comparison with AT. In some cases, compared with AT, LTO method may increase traffic congestion.

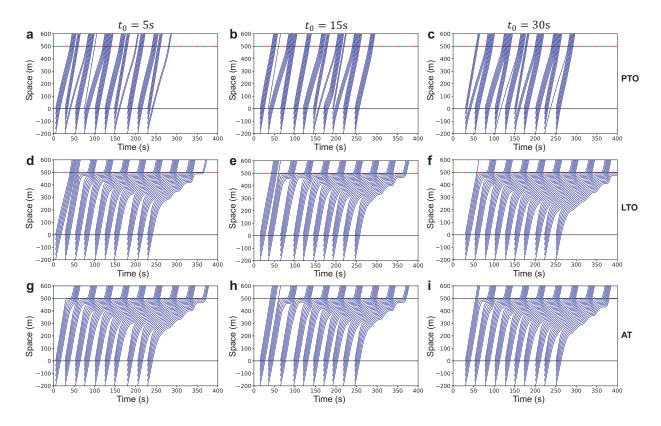


Figure 7: Trajectories of multiple platoons across a signalized intersection. (a-c) Trajectories with PTO, (d-f) trajectories with LTO and (g-i) trajectories with AT.

Table 3: Average fuel consumption and travel time per vehicle per 100 meters shown in Figure 7.

	Fuel consumption (ml)			Travel time (s)		
t_0	5	15	30	5	15	30
PTO	3.21	3.35	3.38	5.73	5.72	5.84
LTO	4.84	4.89	4.92	11.06	10.48	13.72
AT	5.00	4.89	4.95	12.43	10.44	12.23

Figure 8 shows the cumulative distribution function (CDF) of fuel consumption and 353 travel time. In Figure 8 (a), the mean values of fuel consumption are 3.32, 4.94 and 4.99 ml 354 per vehicle per 100 meters with PTO, LTO and AT, respectively. In contrast to LTO and 355 AT, the fuel consumption with PTO method falls by about 32.79% and 33.47%, respectively. 356 It is clear that the fuel consumption of most vehicles is less than 4 ml with the PTO method. 357 However, the fuel consumption of most vehicles with LTO and AT is more than 4 ml. In 358 Figure 8 (b), the mean values of travel time are 5.73, 10.97 and 11.10 seconds with PTO, 359 LTO and AT, respectively. In comparison with LTO and AT, the travel time with PTO 360 method decreases about 47.8% and 48.4%, respectively. The travel time of most vehicles is 361 less than 8 seconds with PTO; however, the cumulative probabilities of travel time with LTO 362 and AT are gradually increasing with travel time, indicating PTO method can effectively 363 reduce traffic congestion. 364

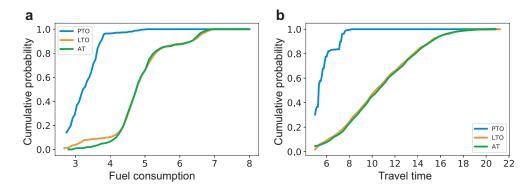


Figure 8: Cumulative probability of fuel consumption (ml) and travel time (s). The data is generated by 50 independent simulations.

365 5.3. sensitivity analysis

From the above case study, we find our PTO method can reduce more than 30% fuel 366 consumption and 40% travel time than the other two methods. In this section, we analyze the 367 influence of key parameters on the performance of PTO, LTO and AT methods. Figure 9 368 and Figure 10 show the fuel consumption and travel time with different parameters. As 369 shown in Figure 9, some parameters, e.g., v_0 , C, N and λ , have negative impacts on the fuel 370 consumption of PTO for multiple platoons. As similar as one platoon, in those parameters, 371 it is obvious that the increase of v_0 and C will contribute more to the fuel consumption. 372 As shown in Figure 9 (c), when the length of traffic signal C is large enough, The unit 373 fuel consumption of PTO method gradually approaches those of the other two methods, 374 which indicate that our PTO method is better suited for short and moderately long cycles 375 (less than 90 seconds). Moreover, in Figure 9 (d) and (f), more vehicles in one platoon and 376 higher arrival rate of platoons cause the increase of the density of vehicles, leading more 377 fuel consumption. Combing the results in Figure 9 and Figure 10, we find the increase of 378 the length of traffic signal cycle and the density of vehicles go against the performance of 379

PTO in both fuel consumption and traffic throughput. In general, the PTO method can significantly improve the performance of fuel consumption and traffic throughput in contrast to LTO and AT when vehicles have enough space to smooth their trajectories. However, for multiple platoons, the performance of LTO cannot be significantly improved in comparison with AT in most cases because the impact of CAV would be non-existent or substantially lessened [27].

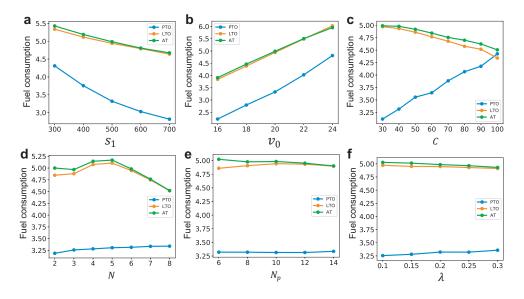


Figure 9: Fuel consumption (ml) per vehicle per 100 meters for multiple platoons across a signalized intersection. The parameters except for parameters analyzed are set as: $s_1 = 500m$, $v_0 = 20m/s$, N = 6, C = 40s, $N_p = 10$, $\lambda = 0.2$ and $\tau_p = 10s$. All data points are calculated over 50 independent simulations.

386 6. Conclusions and Discussions

In this paper, we propose a platoon-based trajectory optimization method, i.e., PTO, 387 to reduce fuel consumption of vehicles passing through a signalized intersection. In the 388 PTO method, all vehicles are CAVs, and the CAVs in one platoon follow the leading one 389 with a reaction time delay and safety space gap. The method can smooth the trajectories 390 of vehicles, eliminate full stops, economize fuel consumption, and ease traffic congestion. 391 Moreover, we compare the PTO method with the other two methods, LTO and AT. In 392 LTO, only the leading vehicle is a CAV with optimized trajectory, and the other vehicles 393 follow the leading CAV with Gipps' car-following model. In AT, we simulate the condition 394 that all vehicles are human-driven and no optimization is applied. 395

Through a series of case studies and sensitivity analysis, we verify that our PTO method has advantages in economizing fuel consumption and reducing travel time over the other two methods. We find there are negative relationships between fuel consumption and the length of the traffic signal cycle, maximum speed, the density of vehicles. Because when those factors have large values, it is equivalent to reducing the space used for trajectory

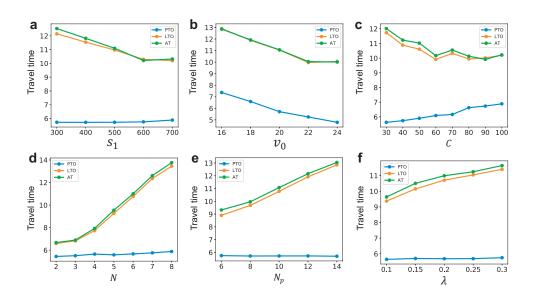


Figure 10: Travel time (s) per vehicle per 100 meters for multiple platoons across a signalized intersection. The parameters except for parameters analyzed are set as: $s_1 = 500m$, $v_0 = 20m/s$, N = 6, C = 40s, $N_p = 10$, $\lambda = 0.2$ and $\tau_p = 10s$. All data points are calculated over 50 independent simulations.

Table 4: Average fuel consumption and travel time per vehicle per 100 meters shown in Figure 11.

	Fuel consumption (ml)			Travel time (s)		
t_0	5	15	30	5	15	30
PTO	3.16	3.25	3.27	5.48	5.44	5.52
LTO	4.77	4.77	4.85	9.14	8.74	10.77
AT	4.90	4.76	4.84	9.99	8.71	9.86

optimization. From this perspective, the PTO method needs enough space to let all CAVs
take optimal trajectories. When the traffic is heavy, and there is not enough space for CAVs
to smooth their trajectories, the performance of the PTO method degrades and approaches
those of LTO and AT. This indicates that the PTO method is best suited to undersaturated
traffic conditions with shorter or moderately long cycles.

In the above analysis, we only consider multiple platoons across an isolated signalized 406 intersection. However, in general, traffic signals are usually coordinated based on a time-407 distance (T-D) diagram so that platoons can pass the intersections along with a "green 408 wave" without the influence of red light [28]. Figure 11 illustrates the trajectories of multiple 409 platoons across two successive signalized intersections. The offset between the two traffic 410 signals is set as $T_C = (s_2 - s_1)/v_0$, where s_2 is the location of the second intersection. 411 As shown in Figure 11 (a-c), all platoons with the PTO method can travel from the first 412 intersection to the second intersection with maximum speed and pass the second intersection 413

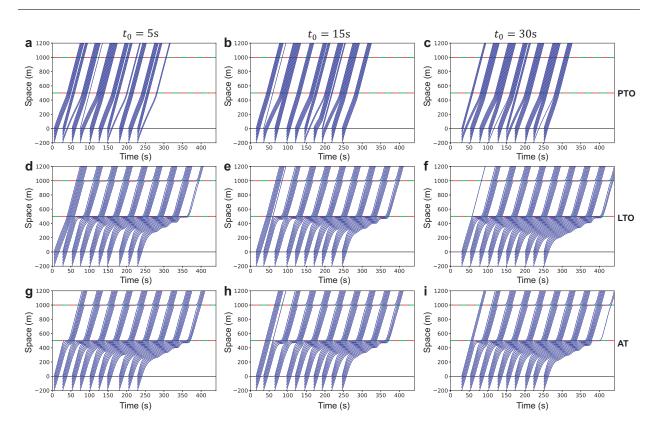


Figure 11: Trajectories of multiple platoons across two signalized intersections. (a-c) Trajectories with PTO, (d-f) trajectories with LTO and (g-i) trajectories with AT.

without stopping. In the case of LTO and AT (Figure 11 (d-i)), however, there are some vehicles that cannot cross the second intersection along with the "green wave", and need to stop before the second intersection until the light turns green. This highlights the added advantage of the PTO method over LTO and AT methods when traffic lights are coordinated. The results of average fuel consumption and travel time per vehicle per 100 meters for multiple platoons across two intersections in Figure 11 are shown in Table 4.

Several research directions can be pursued to extend this research, which includes, but is not limited to (1) to develop a PTO method for electric vehicles (EV), (2) to extend the PTO method for a network of traffic intersections, and (3) to extend the PTO method with actuated control traffic signals.

424 7. Acknowledgements

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