

NHI Course No. 13063

# ***Seismic Bridge Design Applications***

25 July 1996

Part Two

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16. Abstract Seismic Bridge Design Applications, Parts One and Two, contains the material used in two one-day national satellite seminars broadcast from the University of Maryland to provide seismic design application instruction. Mr. Robert Mast and Dr. Lee Marsh of BERGER/ABAM Engineers, Inc., were the instructors and developed the course materials. Part One includes seven sessions covering basic seismic principles, one complete seismic analysis and design example, modeling guidelines, multimodal analysis, and column design features. Part Two includes "homework problems" assigned after the first seminar as well as specific topics requested by participants of the first seminar.					
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# Seismic Design of Bridges

## Seminar No. 2 – Outline

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Session No.	Topic	Reference Example
1	Practice Problem No. 1 Spread Footings	Concrete Box Girder Bridge (Design Example No. 1)
2	Abutments	
3	Practice Problem No. 2 Conceptual Design Steel Superstructure Issues	Steel Plate Girder Bridge (Design Example No. 2)
4	Skew Structure Issues Elastomeric Bearings	
5	Curved Structure Issues Piles	Curved Box Girder Bridge (Design Example No. 6)

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# Seismic Design of Bridges

## Seminar No. 2 – Outline (continued)

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Session No.	Topic	Reference Example
6	Drilled Shafts	Curved Box Girder Bridge (Design Example No. 6)
	Pile Bents	Pile Bent Bridge (Design Example No. 7)
	Joint Design	Other Topics
7	Existing Bridge Assessment and Retrofit	
	Questions and Answers	

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# **Session 1**

## **Concrete Box Girder Bridge Example**

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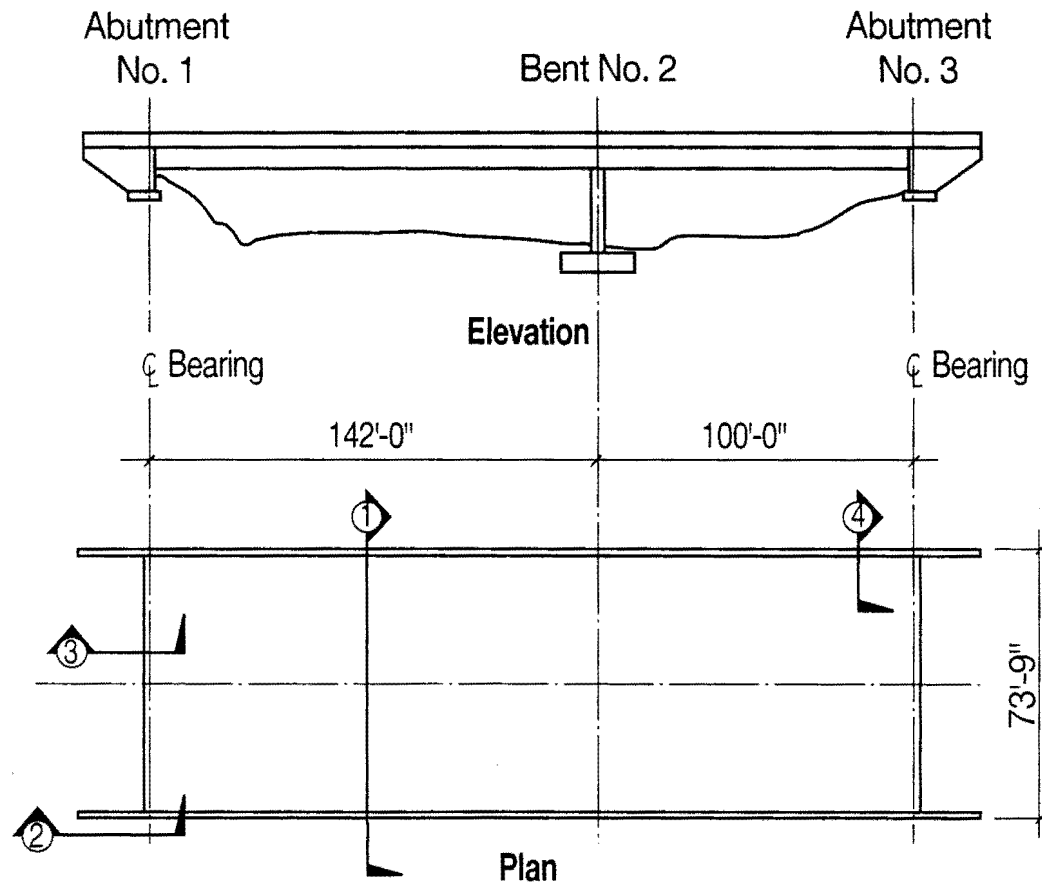
### **Session 1**

- **Practice Problem No. 1**
- **Spread Footings**

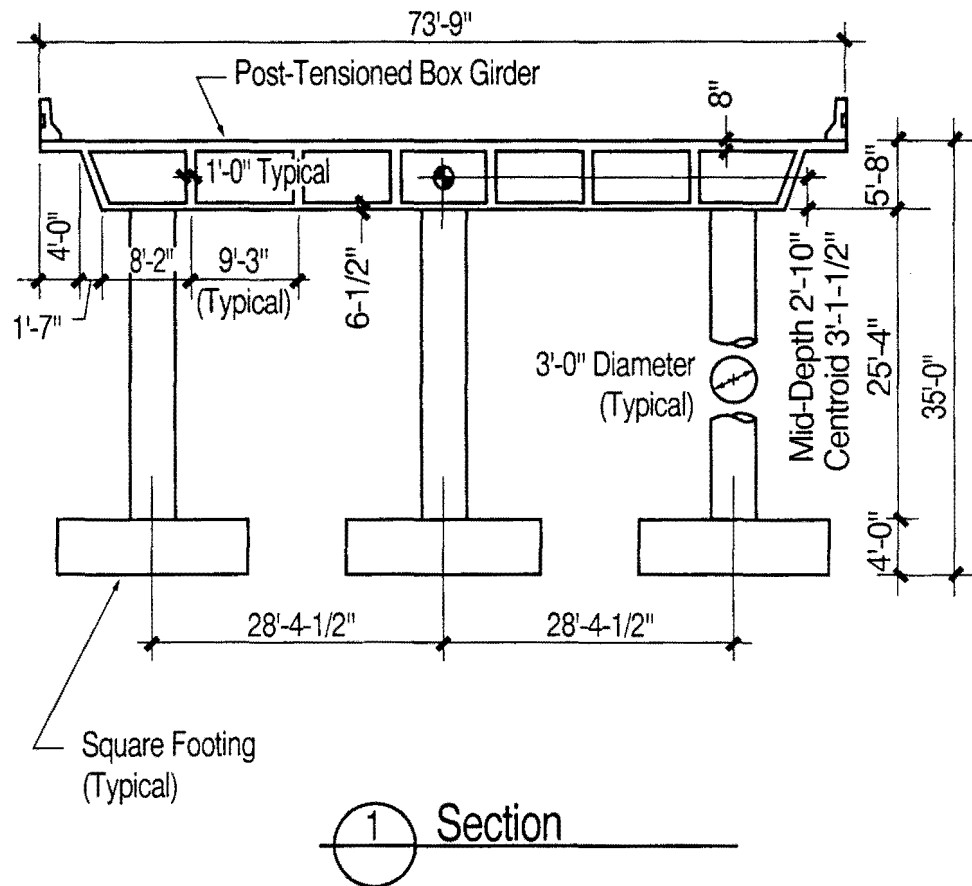
### **Session 2**

- **Abutments**

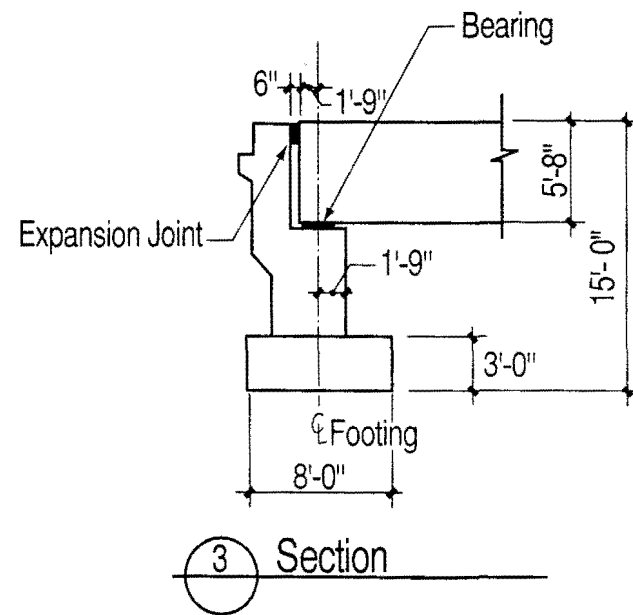
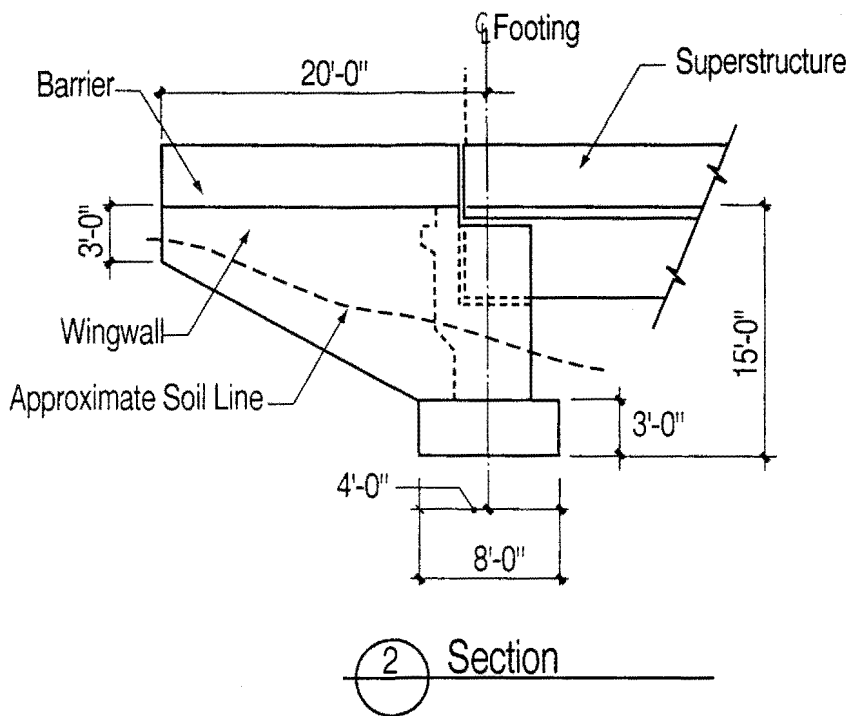
# Bridge Layout / Plan and Elevation



# Layout / Preliminary Bent Details

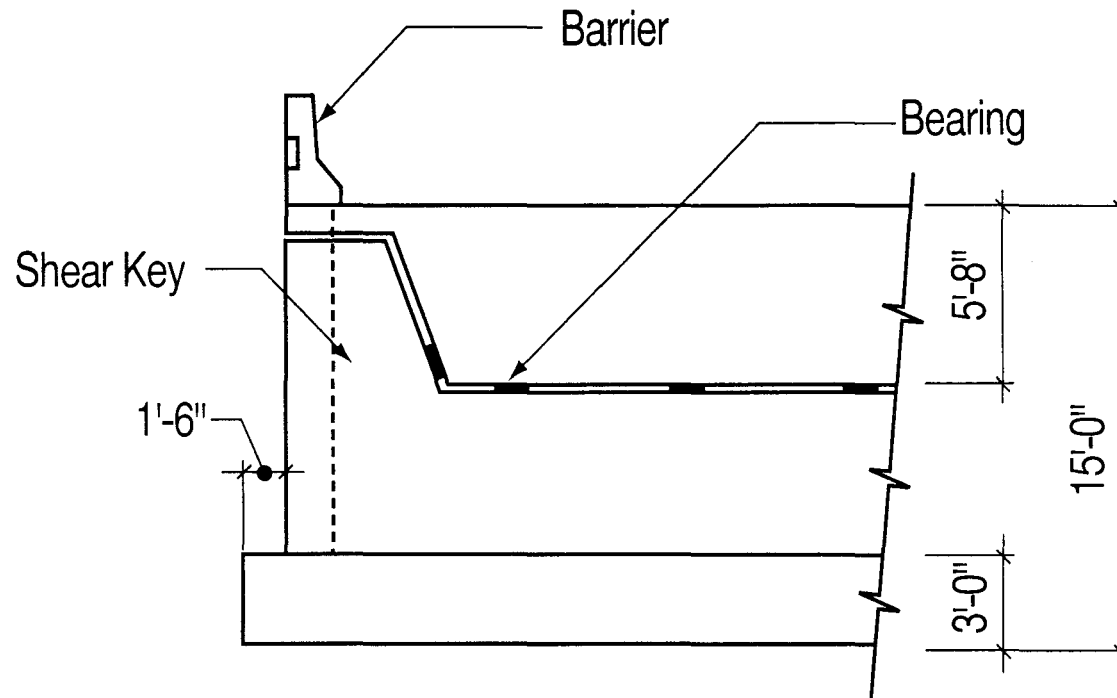


# Bridge Layout / Abutment Details





# Layout / Shear Key at Abutments



4 Section

# **Session 1**

## **Required / Practice Problem No. 1**

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- **Calculate the Longitudinal Period**
- **Calculate the Longitudinal Forces and Displacements**
- **Design the Column Reinforcement**
- **Size Column Footing**
- **Assess the Effects of Plastic Hinging**

# Basic Data for Bridge

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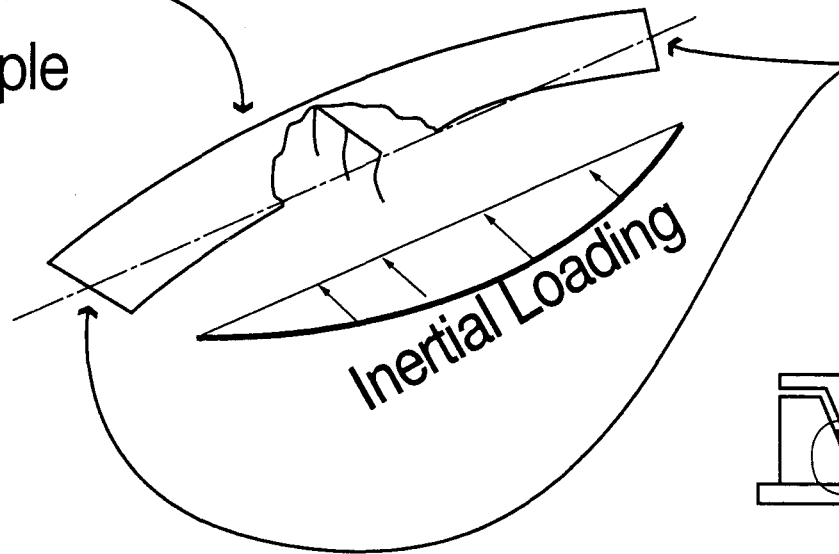
- Acceleration Coefficient,  $A = 0.15g$
- Seismic Performance Category,  $SPC = B$
- Soil — 250 ft Deep Glacial Sand and Gravel

$$S = 1.2$$

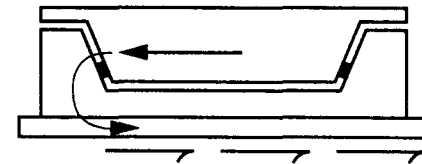
$$f_{ult} = 24 \text{ ksf}$$

# Transverse Lateral Load Behavior

Superstructure  
Acts as a Simple  
Beam in Plan

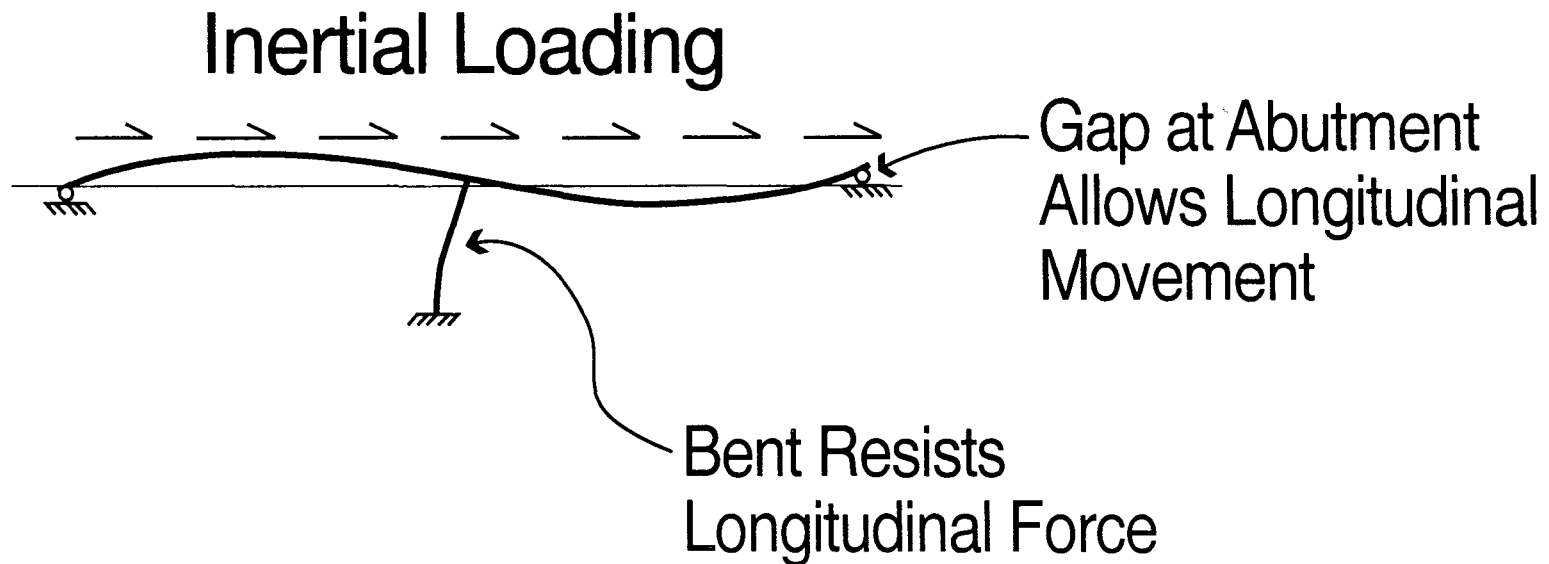


Abutments  
Resist Most  
of the Force



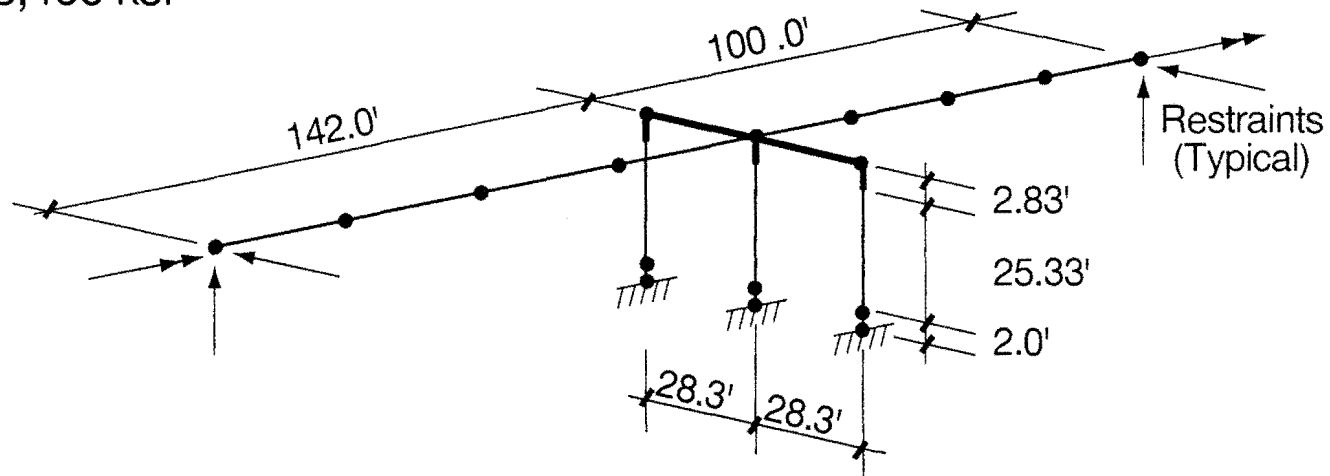
# Longitudinal Lateral Load Behavior

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# Analytical Model and Properties

$E = 518,400 \text{ ksf}$



## Superstructure

$A = 120 \text{ ft}^2$   
 $I_{\text{str}} = 51,000 \text{ ft}^4$   
 $I_{\text{weak}} = 575 \text{ ft}^4$

## Capbeam

$A = 25 \text{ ft}^2$   
 $I_{\text{str}} = I_{\text{weak}} = 10^7 \text{ ft}^4$

## Column

$A = 7.07 \text{ ft}^2$   
 $I = 3.98 \text{ ft}^4$

# Longitudinal Period

---

**Stiffness**  
(Bent Only)

$$K = 3 \left( \frac{12EI}{H^3} \right) = 3 \left( \frac{12(518,400)3.98}{(25.33 + 2.0)^3} \right)$$

$$K = 3639 \text{ kip/ft}$$

**Weight**

$$W = 4842 \text{ kip}$$

**Period**

$$T = 2\pi \sqrt{\frac{4842}{32.2 (3639)}} = 1.28 \text{ sec}$$

$$T_{\text{modal}} = 1.32 \text{ sec (3\% Difference)}$$

# Longitudinal Shear and Moment

---

- **Total Base Shear**

$$C_s = \frac{1.2AS}{T^{2/3}} = \frac{1.2(0.15)(1.2)}{(1.28)^{2/3}} = 0.183 < 0.375 = 2.5A$$

$$V_{\text{base}} = C_s W = 0.183 (4842) = 886 \text{ kip}$$

Assumes All Mass Moves Equally

- **Column Forces**

$$V_{\text{col}} = \frac{V_{\text{base}}}{3} = \frac{886}{3} = 295 \text{ kip vs. } V_{\text{modal}} = 288 \text{ kip}$$

$$M_{\text{col}} = V_{\text{col}} \left( \frac{H}{2} \right) = 295 \left( \frac{27.33}{2} \right) = 4031 \text{ kip ft vs. } M_{\text{modal}} = 3856 \text{ kip ft}$$





# Column Design Forces

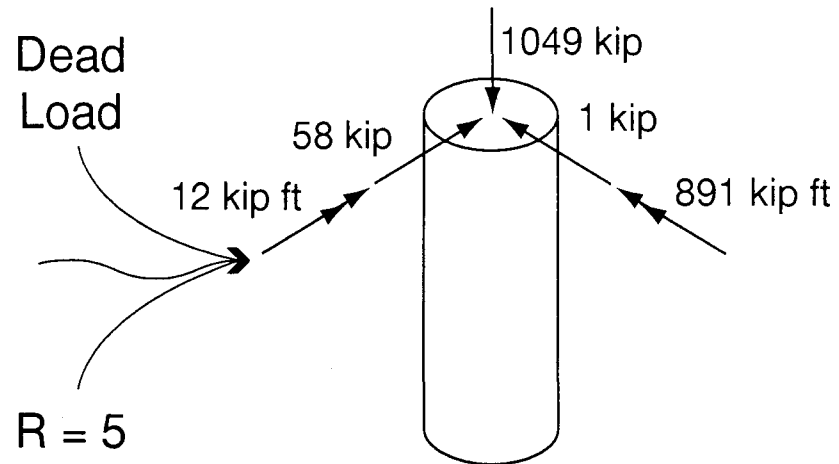
- **Outboard Column**

Longitudinal  
Earthquake

LC1

Transverse  
Earthquake

LC2



$$M_{\text{result}} = 891 \text{ kip ft}$$

$$V_{\text{result}} = 58 \text{ kip}$$

# Column Flexural Design

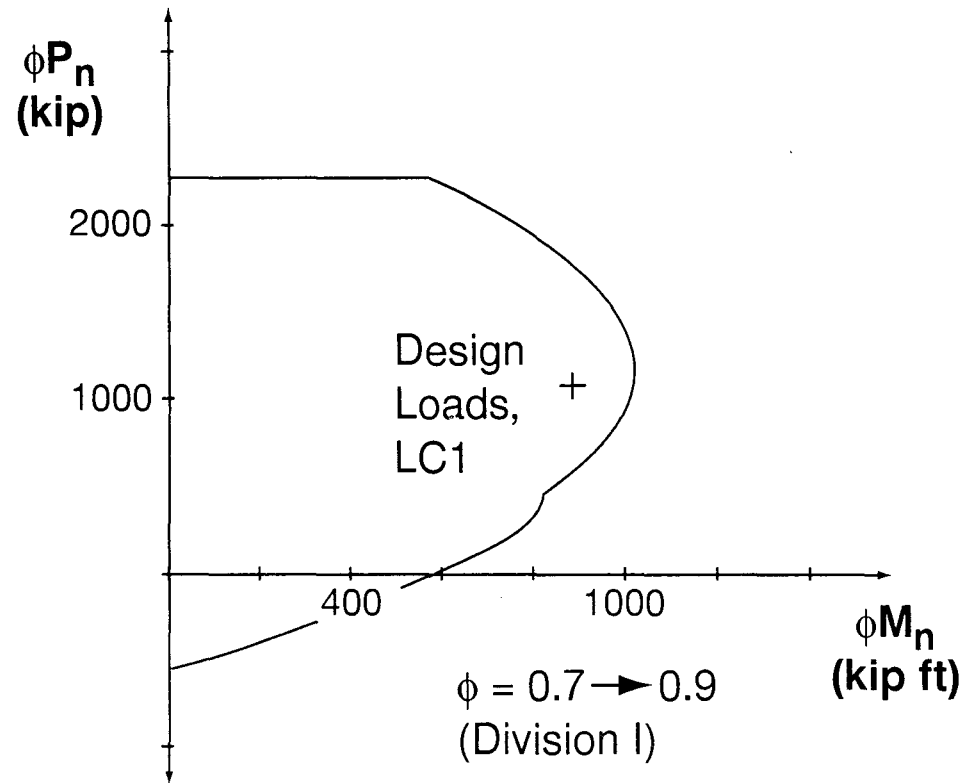
Try:

8 #10 Bars

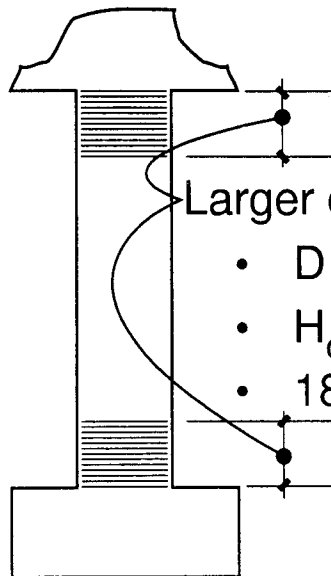
$\rho_g = 1.00\%$

$f_y = 60$  ksi

$f'_c = 4$  ksi



# Hinge Zone Confinement



Larger of:

- D = 36"
- $H_{clr}/6 = 51"$
- 18"

$$\rho_s = 0.45 \left( \frac{A_g}{A_{core}} - 1 \right) \frac{f'_c}{f_{yh}} = 0.008$$

Minimum:

$$\rho_s \geq 0.12 \frac{f'_c}{f_{yh}} = 0.008$$

$$\text{Try } A_{sp} = 0.31 \text{ in}^2 \text{ (#5)}$$

$$s = \frac{4 A_{sp} d_s}{\rho_s d_{core}^2} = \frac{4 (0.31)(32 - 0.625)}{0.008(32)^2} = 4.75"$$

Use #5 @ 4.5 in. for 60 in.

# Shear Strength

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SPC B — Shear Strength Same as Division I

$$V_u = 58 \text{ kip} \quad \phi V_c = (0.85) \frac{2\sqrt{4000}}{1000} 36(28) = 109 \text{ kip}$$

$$\text{Use } A_{V_{\min}} = \frac{50(36)12}{60,000} = 0.36 \text{ in}^2$$

$$\text{Use \#5 @ 12 in.} \quad V_s = 2(0.31) \frac{28}{12} 60 = 87 \text{ kip}$$

$$\phi V_n = 109 + 0.85(87) = 183 \text{ kip}$$

# Footing Design Forces

- **Outboard Column**

Longitudinal  
Earthquake

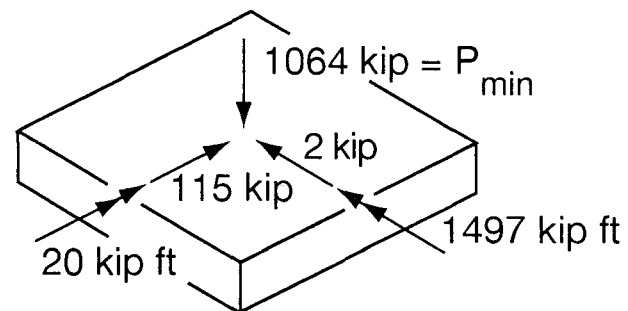
LC1

Transverse  
Earthquake

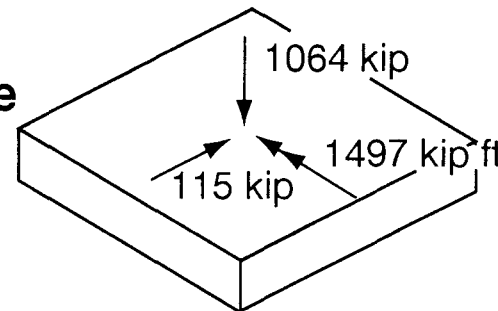
LC2

Dead  
Load

$$R = \frac{5}{2} = 2.5$$

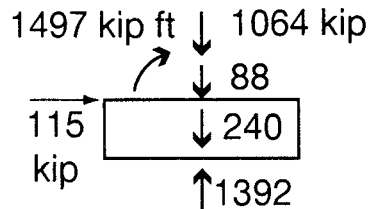


**Resultant Forces Essentially Are**



# Footing Size

- If  $B = L = 20$  ft



$$P = P_{D+LC1/R} + P_{\text{footing}} + P_{\text{soil}}$$

$$P = 1064 \text{ kip} + 240 \text{ kip} + 88 \text{ kip} = 1392 \text{ kip}$$

$$M = 1497 + 115(4) = 1957 \text{ kip ft}$$

$$e = \frac{M}{P} = \frac{1957}{1392} = 1.4 \text{ ft} \ll \frac{L}{3} = \frac{20}{3} = 6.7 \text{ ft}$$

- If  $B = L = 15$  ft (Gravity Loads Control)

$$P = 1255 \text{ kip}$$

$$e = \frac{1957}{1255} = 1.6 \text{ ft} < \frac{15}{3} = 5 \text{ ft}$$

$$q = 9.5 \text{ ksf} < 24 \text{ ksf}$$

∴ 1/2 Uplift  
Will Not  
Control

Use 15 ft  
Square Footing

# Check the Effects of Plastic Hinging

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**Not Required in SPC B**

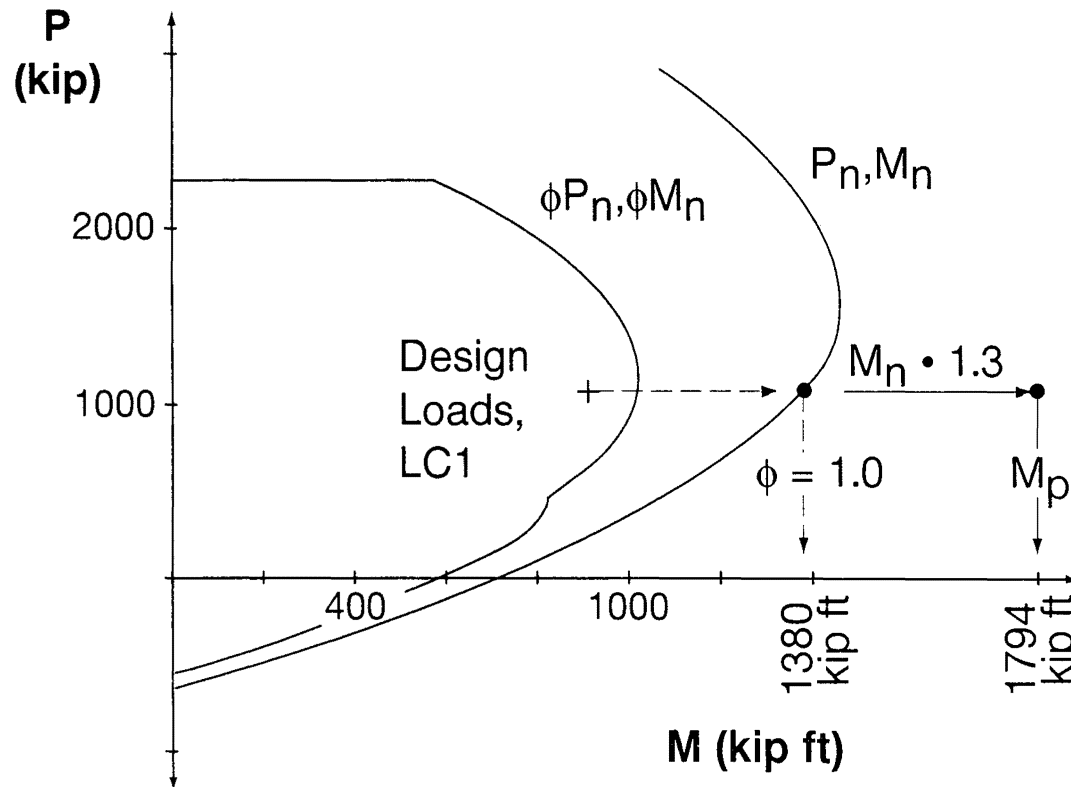


# Column Nominal and Overstrength Properties

8 #10 Bars

$f_y = 60$  ksi

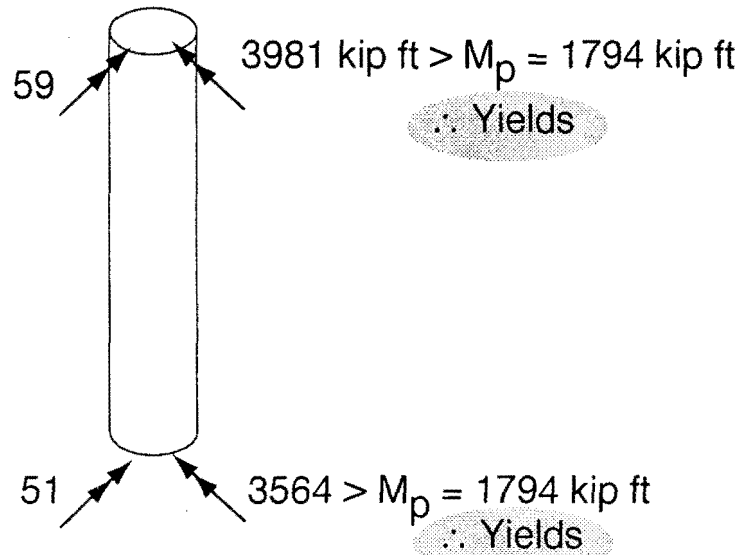
$f'_c = 4$  ksi



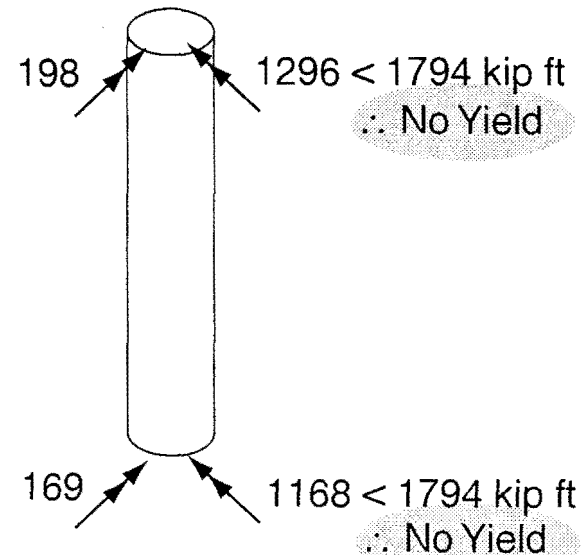
# Will Column Develop Plastic Hinge?

## Outboard Column

### Elastic Forces LC1 + DL

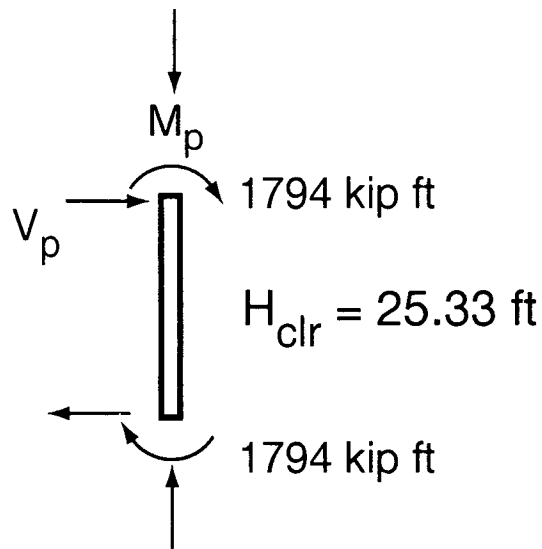


### Elastic Forces LC2 + DL



# Maximum Column Shear

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$$V_{\text{elastic}} = 288 \text{ kip}$$

$$V_p = \frac{2(1794)}{25.33} = 142 \text{ kip}$$

$$\phi V_n = 183 \text{ kip} \quad \therefore \text{OK}$$

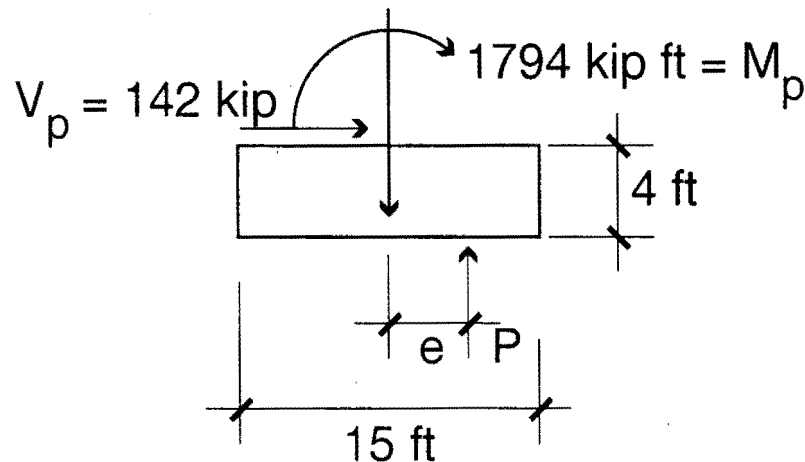
Because We Provided  
Minimum Steel

# Plastic Hinging Effects on Footing

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$$e = \frac{M}{P} = \frac{1794 + 142(4)}{1255} = 1.88 \text{ ft} < 5 \text{ ft}$$

and  $q = 9.9 \text{ ksf} < 24 \text{ ksf}$



$\therefore$  OK  
for Plastic  
Hinging

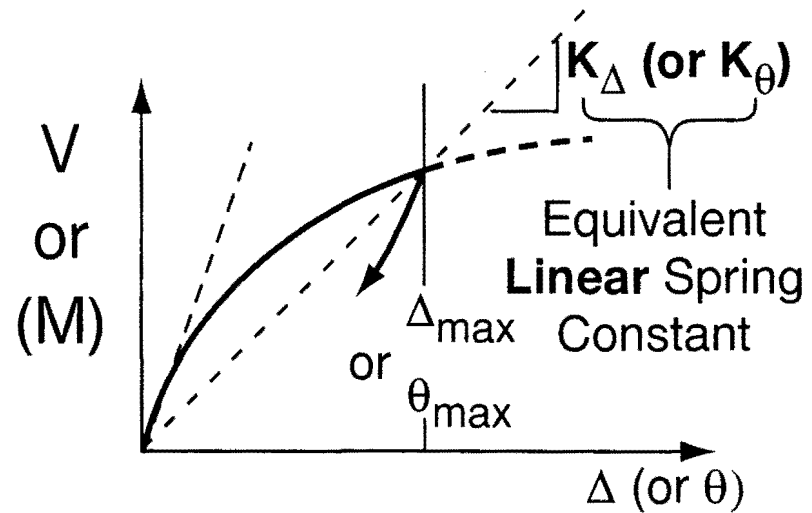
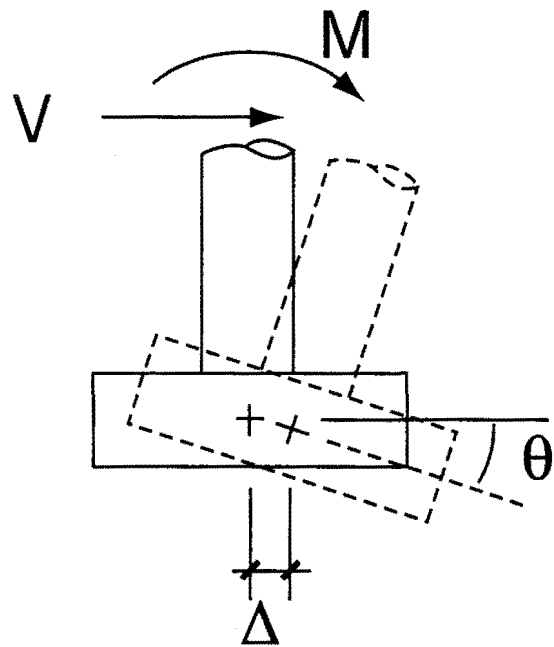
# Session 1

## Spread Footings

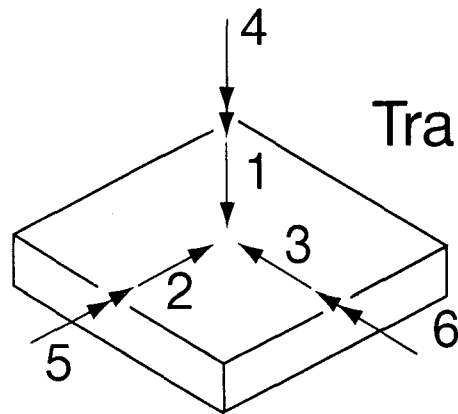
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- **Including Flexibility**
- Overturning and Sliding
- Pinned Base Columns

# Conceptual Behavior



# Degree-of-Freedom / Importance



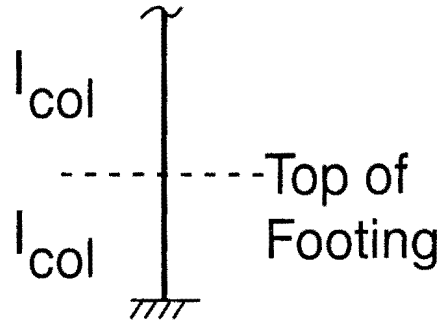
Translation {  
1. Vertical  
2. Lateral  
3. Lateral

Rotation {  
4. Torsion  
5. Rocking  
6. Rocking } Most Important  
to Include

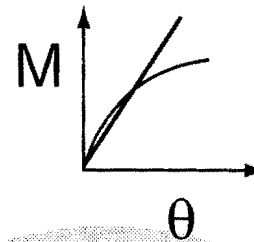
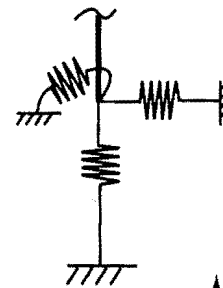
# Modeling Foundation Flexibility



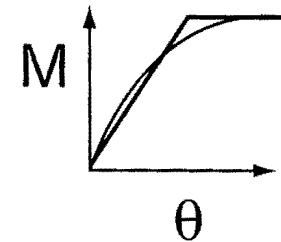
**Fixed / Free**



**Equivalent Column**



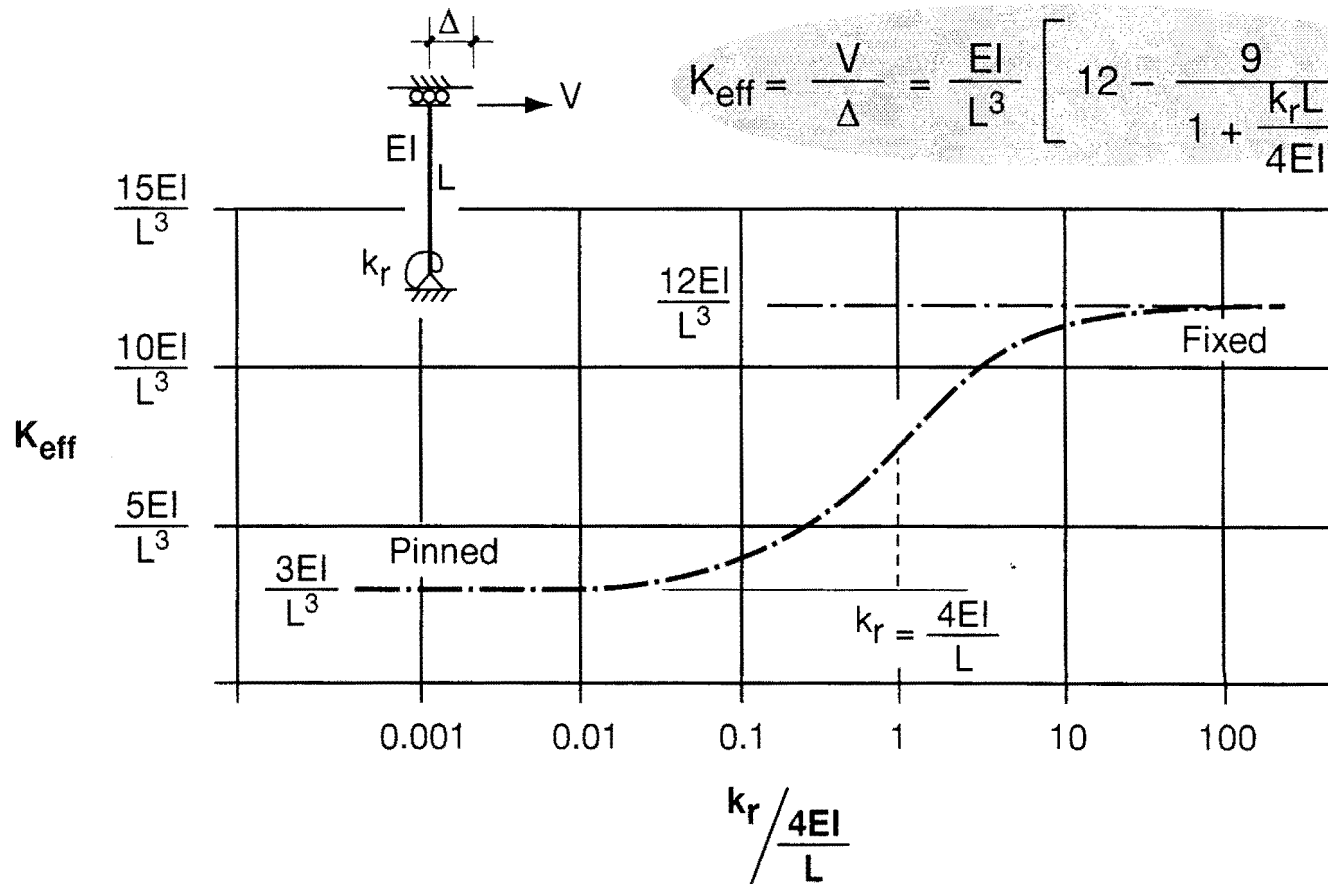
**Linear Soil Springs**



**Nonlinear Springs**



# Rotational Flexibility / Fixed or Not?

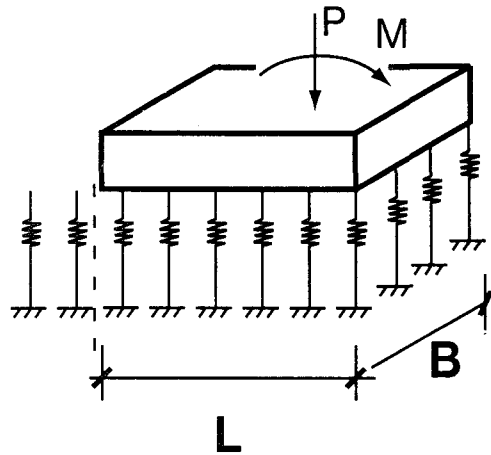


# Determining Foundation Stiffness

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- **Elastic Foundation Methods**
- **'Elastic Half-Space' Methods**

# Elastic Foundation Method

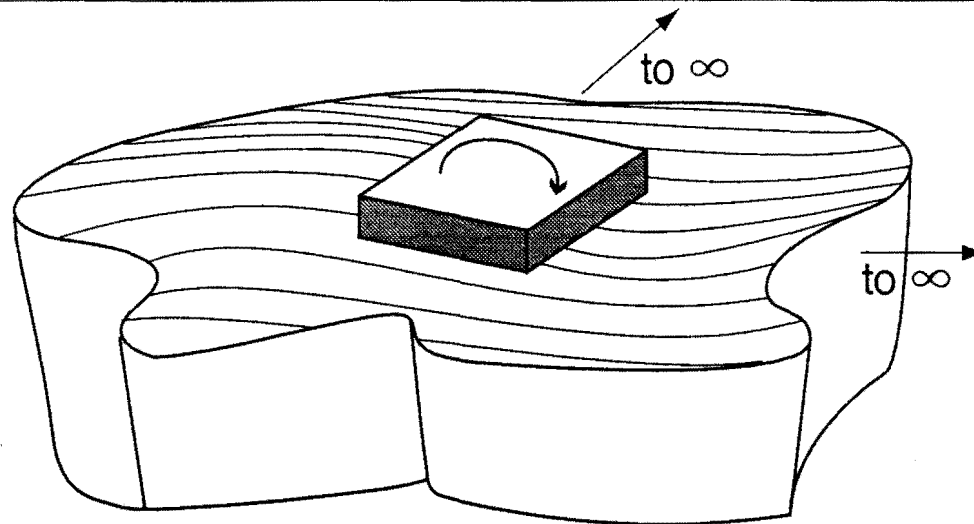


$k_S$ , Subgrade Reaction Coefficient

$$\left( \frac{\text{kip}}{(\text{ft}^2 \text{ of Area})(\text{ft of Deflection})} = \text{kcf} \right)$$

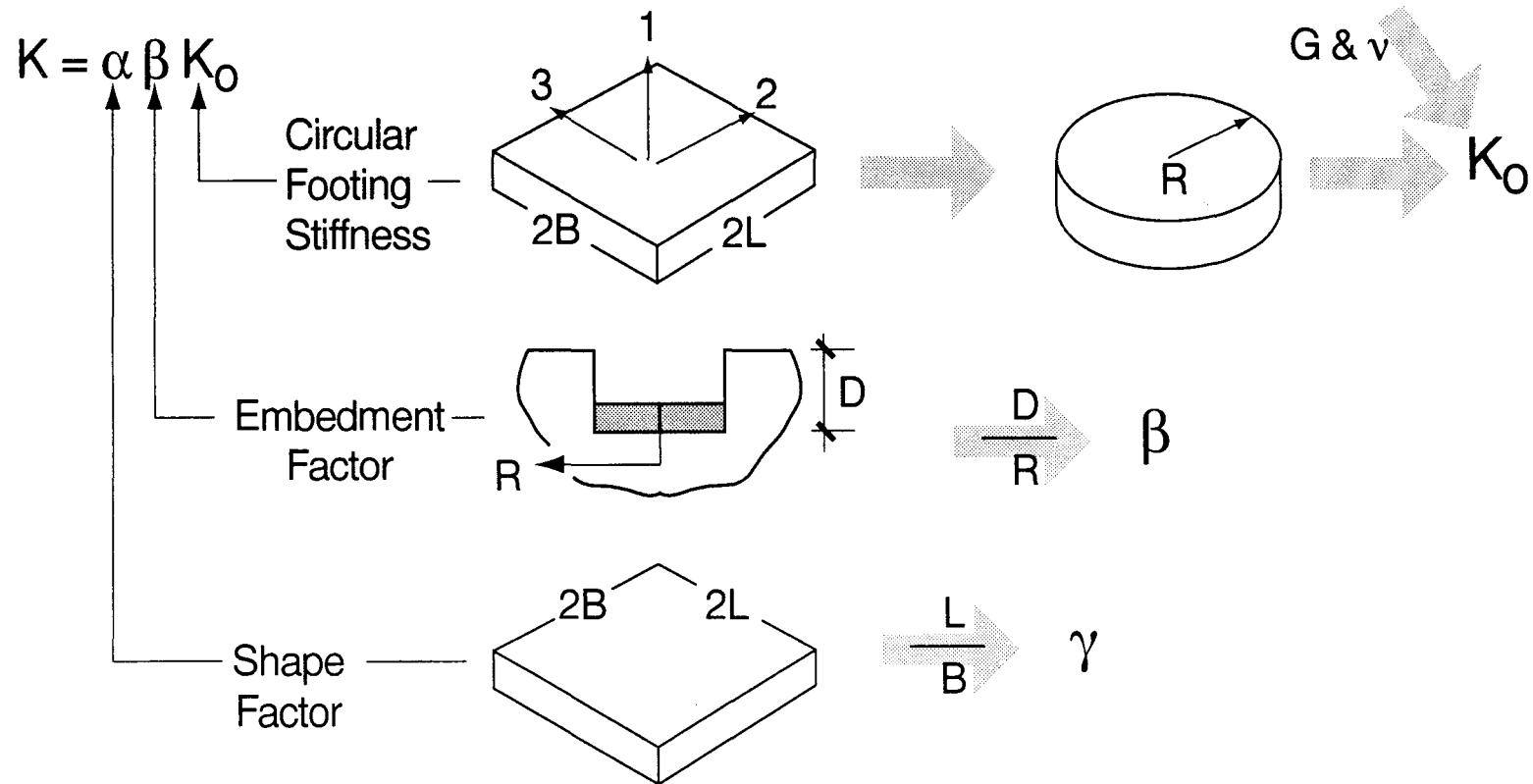
- 'Springs' Are Independent (Winkler Foundation)
- Footing Rigid Relative to Soil
- Rotational Stiffness,  $k_r = k_S \frac{L^3 B}{12} \frac{\text{kip ft}}{\text{rad}}$

# Half-Space Method



- Footing (Rigid) Bonded to Elastic Half-Space Medium
- Must Use Theory of Elasticity Methods to Determine K's  
(Standard Non-Dimensional Solutions)

# Half-Space Method for Spread Footings



Adapted from : FHWA-IP-87-6

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UMD-ITV

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# Stiffness of Circular Surface Footing

Degree of Freedom	Equivalent Radius	Stiffness $K_0$
Vertical Translation	$R_0 = \sqrt{\frac{4BL}{\pi}}$	$4GR/1 - \nu$
Lateral Translation (Both)	"	$8GR/2 - \nu$
Torsion Rotation	$R_1 = \left[ \frac{4BL (4B^2 + 4L^2)}{6\pi} \right]^{1/4}$	$16GR^3/3$
Rocking About 2	$R_2 = \left[ \frac{(2B)^3 (2L)}{3\pi} \right]^{1/4}$	$8GR^3/3(1 - \nu)$
Rocking About 3	$R_3 = \left[ \frac{(2B) (2L)^3}{3\pi} \right]^{1/4}$	"

Adapted from: FHWA-IP-87-6

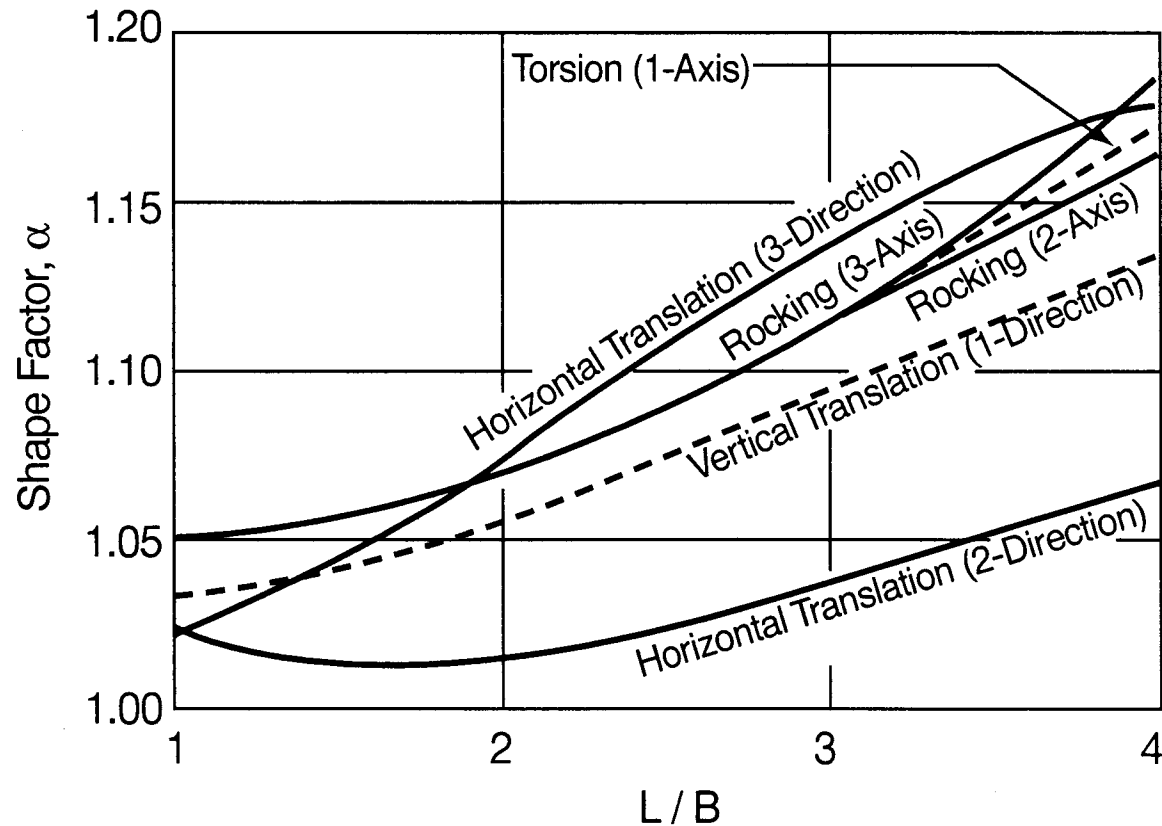
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UMD-ITV

Seismic Bridge Design Applications

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# Shape Factor for Rectangular Footing



Adapted from : FHWA-IP-87-6

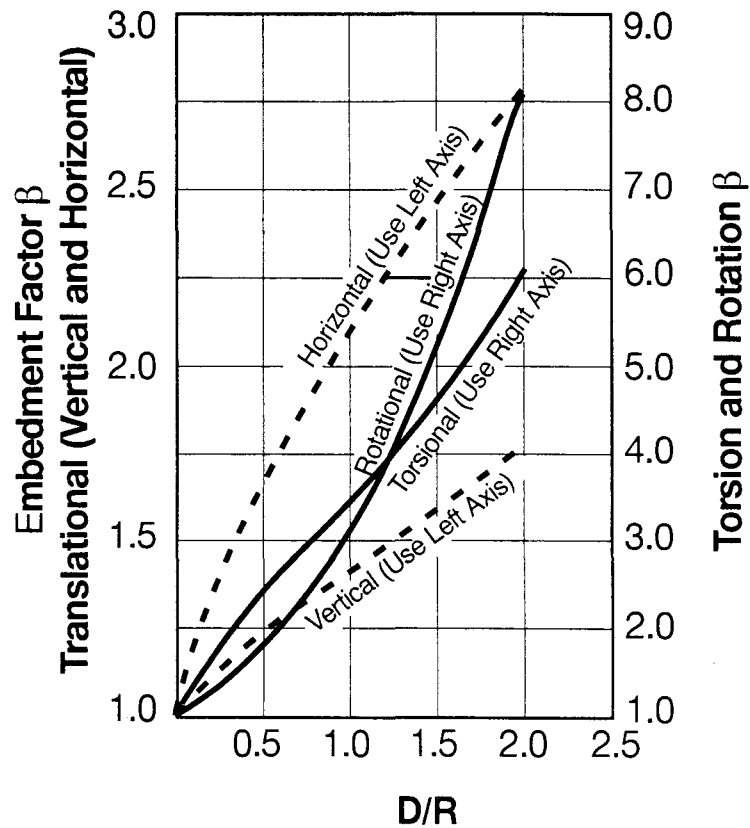
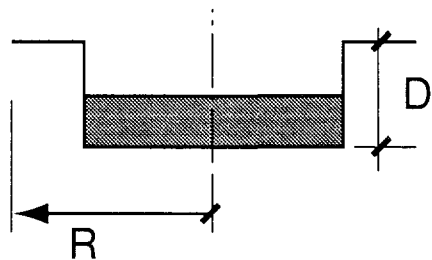
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UMD-ITV

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# Embedment Factor



Adapted from : FHWA-IP-87-6

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 UMD-ITV

Seismic Bridge Design Applications  
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# Representative\* Soil Properties

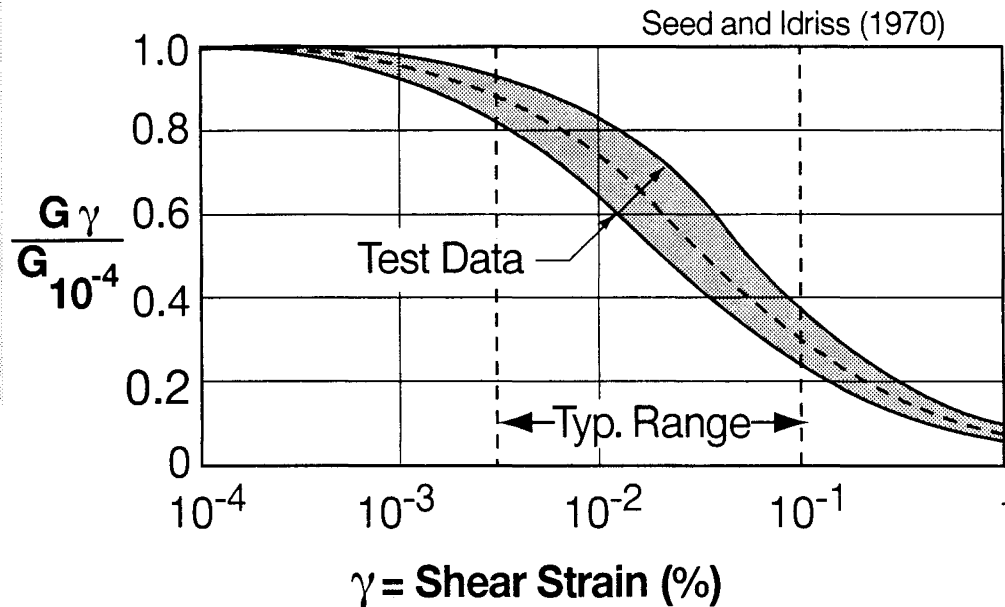
- **Shear Modulus, G**

Material	G(ksi)
Clean dense quartz sand	1.8-3 <sup>+</sup>
Micaceous fine sand	2.3
Berlin sand (e=0.53)	2.5-3.5
Loamy sand	1.5
Dense sand-gravel	10 <sup>+</sup>
Wet soft silty clay	1.3-2
Dry soft silty clay	2.5-3
Dry silty clay	5-5
Medium clay	2-4
Sandy clay	2-4

Bowles (1988)

- **Poisson's Ratio**  $\nu = 0.3$  Cohesionless  
 $\nu = 0.4 - 0.5$  Cohesive

- **Shear Modulus vs. Strain**



\* Consult Your Geotech!

# Example / Rocking Stiffness / Half-Space

- Consider Practice Problem No. 1

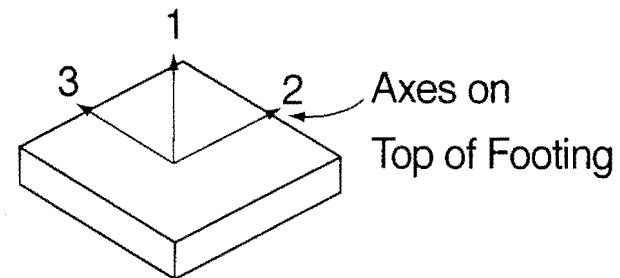
**Footing:**  $2B = 2L = 15 \text{ ft}$   $D = 6 \text{ ft}$

**Soil:** From Geotechnical Engineer,  $G = 400 \text{ ksf}$   $\nu = 0.3$

**Rotational**

**Stiffness:**  $K_{r3} = \alpha \beta K_0$

(Rocking About Axis 3)



## Example / Rocking Stiffness (continued)

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- Equivalent Radius,  $R_3 = \left[ \frac{(15)(15)^3}{3\pi} \right]^{1/4} = 8.56 \text{ ft}$

- Rocking,  $K_0 = \left[ \frac{8(400)(8.56)^3}{3(1 - 0.3)} \right] = 955,600 \frac{\text{kip ft}}{\text{rad}}$

- Shape Factor,  $\alpha$   $\frac{L}{B} = 1 \rightarrow \alpha = 1.05$

- Embedment Factor,  $\beta$   $\frac{D}{R} = \frac{6}{8.56} = 0.70 \rightarrow \beta = 2.3$

## Example / Rocking Stiffness (continued)

- $$K_{r3} = \alpha\beta K_0 = 1.05(2.3) 955,600 = 2,308,000$$

$$\frac{\text{kip ft}}{\text{rad}}$$

- How Important Is This Stiffness on the Lateral Behavior of the Structure?

Column Properties

$$E = 518,400 \text{ ksf}$$

$$I = 3.98 \text{ ft}^4$$

$$H_{\text{clr}} = 25.33 \text{ ft}$$

$$K_{\text{eff}} = \frac{EI}{H^3} \left[ 12 - \frac{9}{1 + \frac{K_r L}{4EI}} \right]$$

$$\frac{K_{03} H}{4EI} = 7.08 \quad \Rightarrow \quad K_{\text{eff}} = 10.9 \frac{EI}{H^3}$$

vs. 12!  $\therefore$  Essentially Fixed

# Example / Footing Rocking – Practice No. 1

---

- Effective Longitudinal Stiffness Including Rocking

$$K_{\text{eff}} = 3 \left( 10.9 \frac{EI}{H^3} \right) = 4146 \text{ kip/ft}$$

- Previously in Practice No. 1  $K = 3639 \text{ kip/ft}$  (Top Half of Footing Included with  $I_{\text{col}}$  to Approximate Footing Flexibility)
- New Results

$$T = 1.20 \text{ sec (vs. 1.28 sec)}$$

$$C_s = 0.192$$

$$V = 928 \text{ kip}$$

$$\Delta_{\text{long}} = 2.7 \text{ in vs. } \begin{cases} 2.9 \text{ in with } I_g \\ 4.6 \text{ in with } I_g / 2 \end{cases}$$

# Session 1

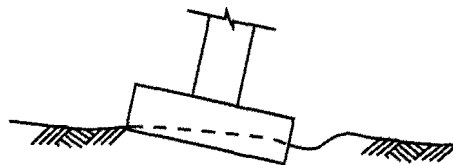
## Spread Footings

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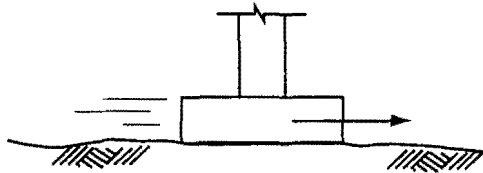
- Including Flexibility
- **Overturning and Sliding**
- Pinned Base Columns

# Spread Footing Failure Modes

- **Soil Failure**



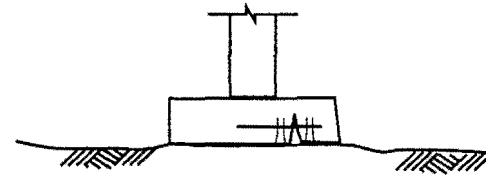
**Soil Bearing Failure  
(Overturning)**



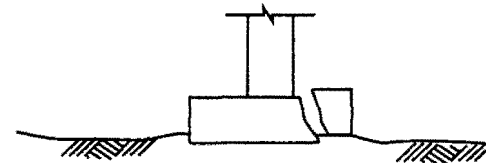
**Sliding Failure**

- **Footing Failure**

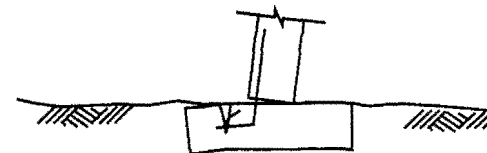
(All Types Aggravated by Large Overturning)



**Flexural Yielding of Reinforcing**



**Concrete Shear Failure**



**Anchorage Failure**

# Overturning

---

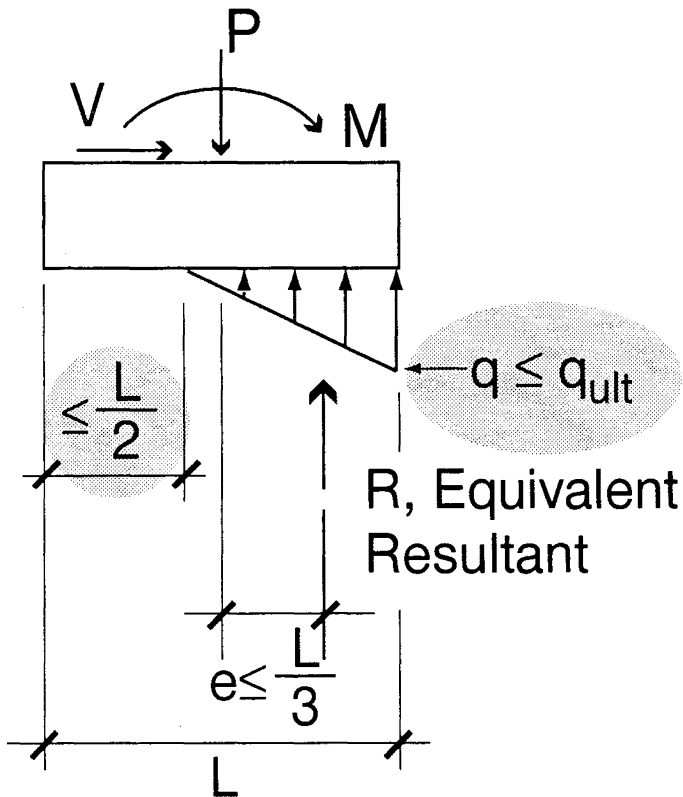
## **Division I-A, Articles 6.4.2(B) and 7.4.2(B)**

“Because of the dynamic cyclic nature of seismic loading, the ultimate capacity of the foundation medium should be used ...”

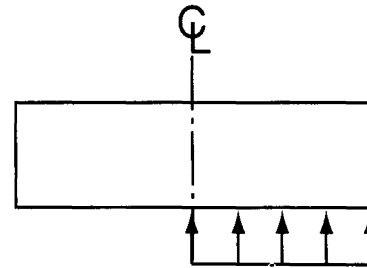
“Transient foundation uplift or rocking involving separation ... up to one-half of ... pile group or ... contact area is permitted ... provided that ... soils are not susceptible to loss of strength ...”



# Overturning Comparisons



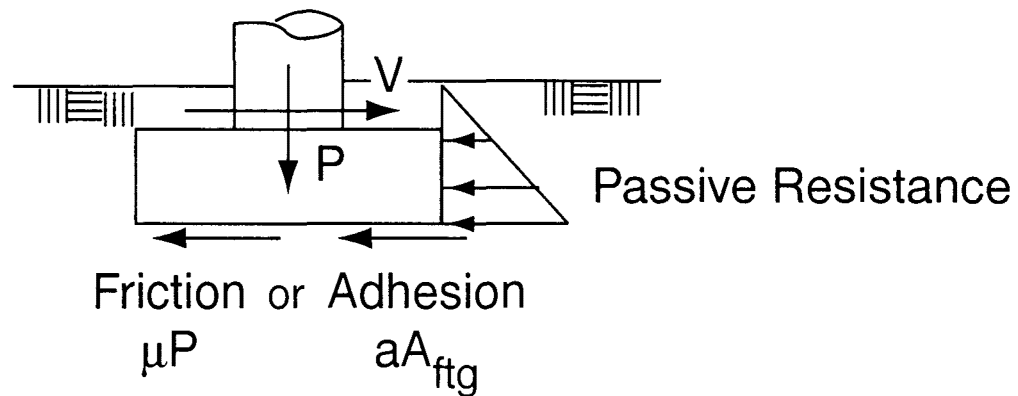
- Triangular Stress Distribution  
Recommended for Now
- Rectangular Stress Distribution



Under Development,  
Better Correlation with  
Test Results?  
Better for Soft Soils?

# Sliding

- Make Comparisons at Impending Sliding Condition
- Neglect Passive Resistance? (Consult Your Geotech)
- If Soil Is Adhesive, Use Larger of Friction or Adhesion
- Consider Jointing Effect in Rock



# Representative\* Ultimate Values of Coefficient of Friction for Concrete Foundations on Rock / Soil

Material	Relative Density/ Consistency	Coefficient of Friction <sup>1</sup>	Adhesion <sup>1</sup> (PSF) <sup>2</sup>
Clean, Sound Rock <sup>3</sup>	Not Applicable	0.70 - 0.80	—
Clean Gravel, Gravel-Sand Mixtures	Dense to Very Dense Medium Dense	0.55 - 0.70 0.55 - 0.65	—
Clean to Slightly Silty / Clayey Sand with or without Gravel	Dense to Very Dense Medium Dense	0.45 - 0.60 0.45 - 0.55	— —
Silty / Clayey Sand and Sandy Silt with or without Gravel	Dense to Very Dense Medium Dense	0.40 - 0.55 0.35 - 0.50	— —
Silty Clay and Clayey Silt with or without Sand and Gravel (low plasticity) <sup>4</sup>	Very Stiff to Hard Medium Stiff to Stiff	0.40 - 0.50 0.30 - 0.45	1000 - 1500 500 - 1000

(After Potyondy, 1961; Goh and Donald, 1984; U.S. Department of the Navy, 1986) For Notes 1 through 4, See Design Example No. 3

\* Consult Your Geotechnical Engineer

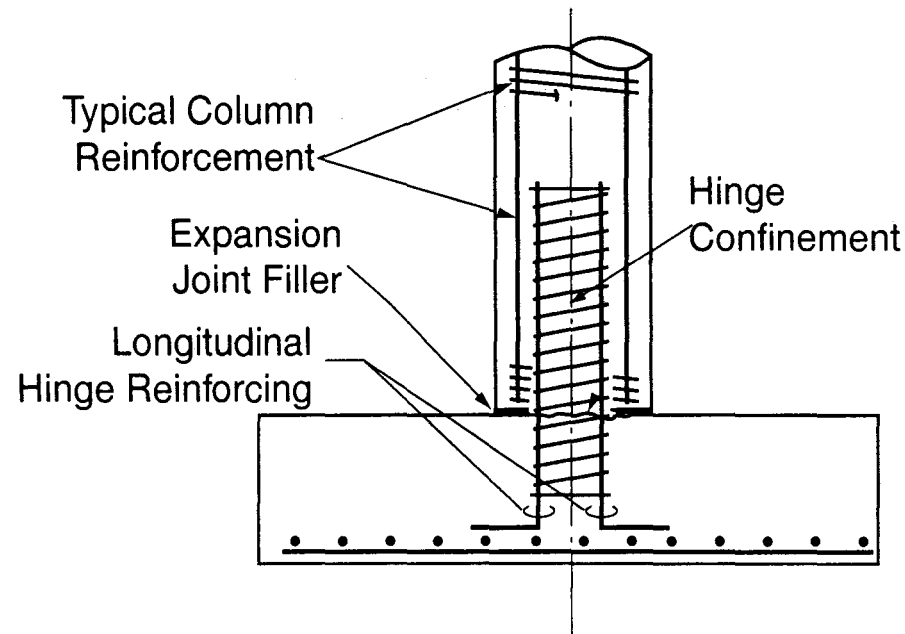
# Session 1

## Spread Footings

---

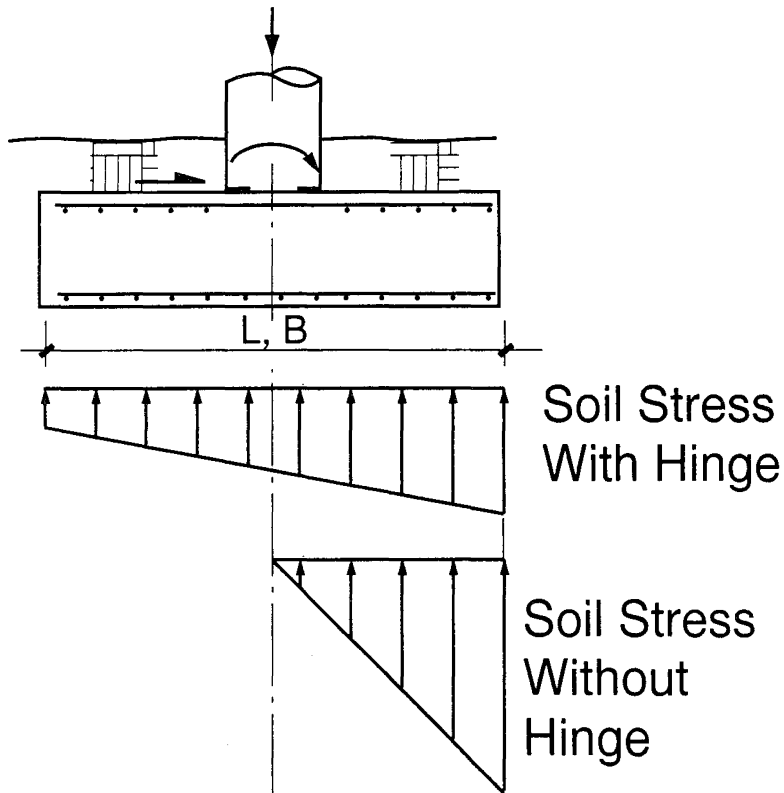
- **Including Flexibility**
- **Overturning and Sliding**
- **Pinned Base Columns**

# Limiting the Moment Transferred to a Footing



**Seismic  
Hinge Detail**

# Effects of Limiting Foundation Moments



With a Hinge:

- Soil Contact Stress Lower
- Internal Forces Lower
- Structure More Flexible  
(Displacements Larger)
- Can Reduce Footing Size
- May Increase Column Size

# Design of Pinned Bases

---

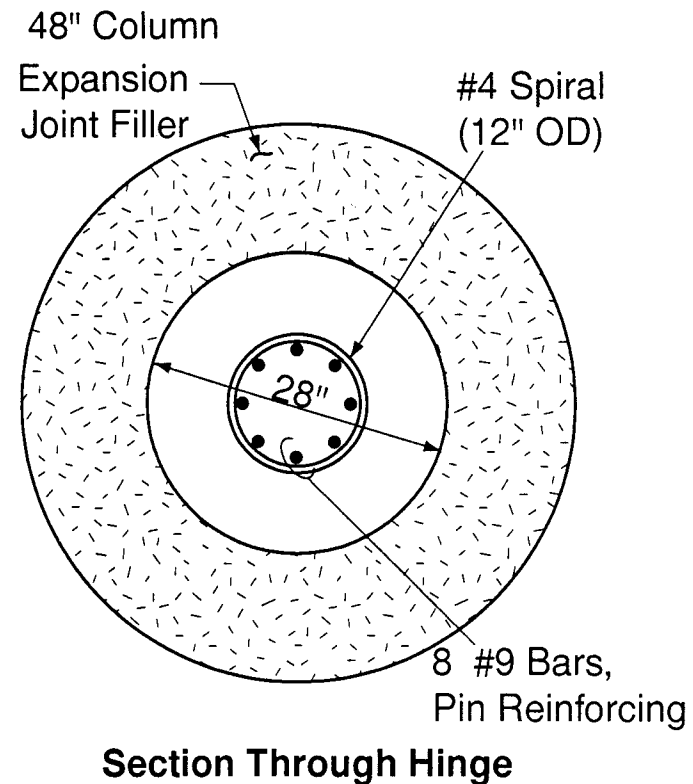
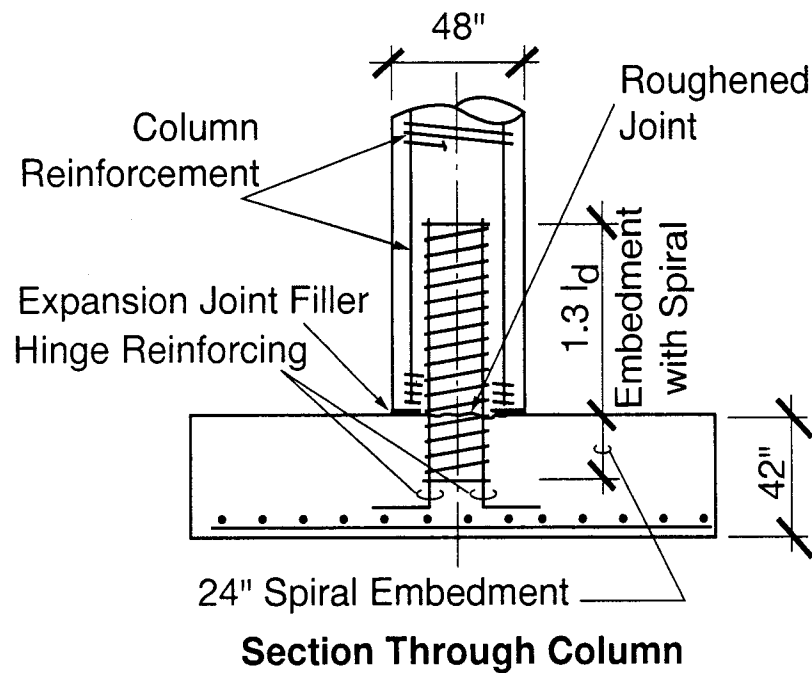
- Use 1/2 in. or More Expansion Joint Filler for Rotation Capacity
- Size Contact Area Using Shear Friction
- Ensure Area Can Carry Group VII Loads Based on

$$\phi P_o = 0.85\phi f'_c (A_g - A_{st}) + A_{st} f_y$$

Caltrans (1995)

- Centralize Longitudinal Steel to Minimize Actual Moment
- Develop Longitudinal Steel on Both Sides of Hinge
- Use a Nominal Spiral Over Half the Column Dimension  
Above and Below Hinge

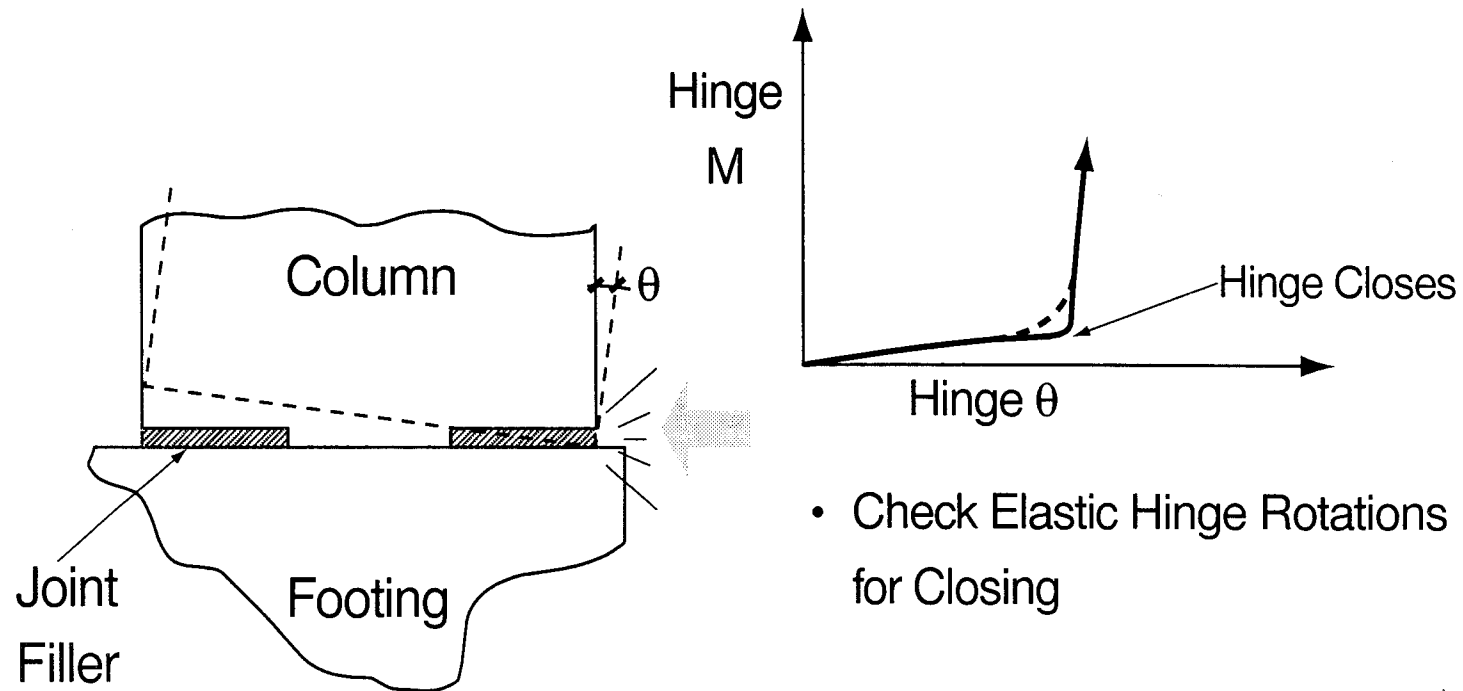
# Example Detailing / 4 ft Diameter Column



Reference: Design Example No. 4



# Limit Behavior / Pinned Base Columns



- Check Elastic Hinge Rotations for Closing



# **Session 2**

## **Concrete Box Girder Bridge Example**

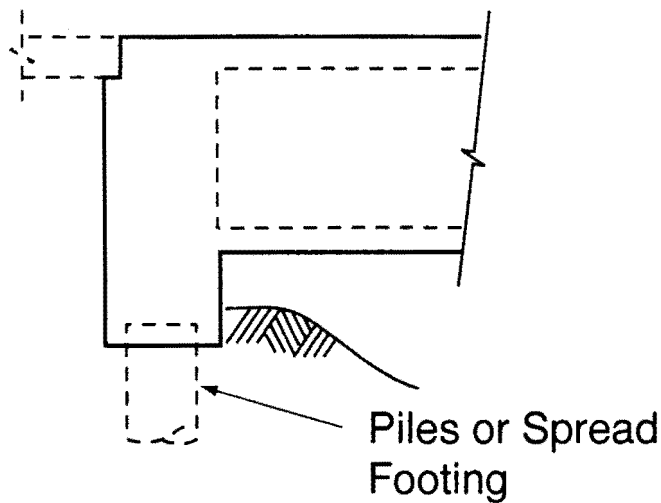
### **Abutments**

---

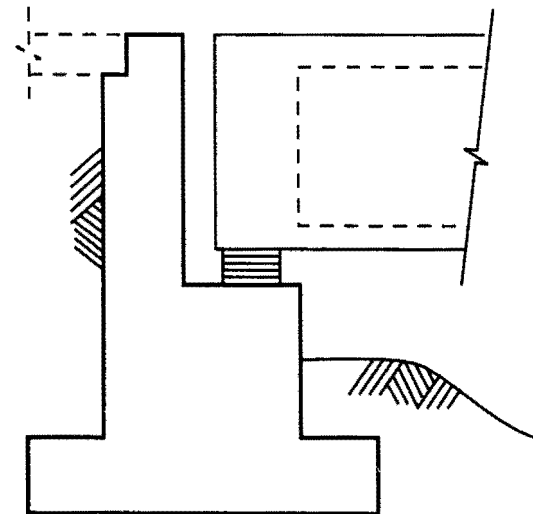
- **Conceptual Behavior**
- **Modeling Soil Flexibility**
- **Nonlinear Effects**
- **Mononobe-Okabe Analysis**
- **Design Issues, Force Transfer,  
and Fuse Elements**

# Types of Abutments

---

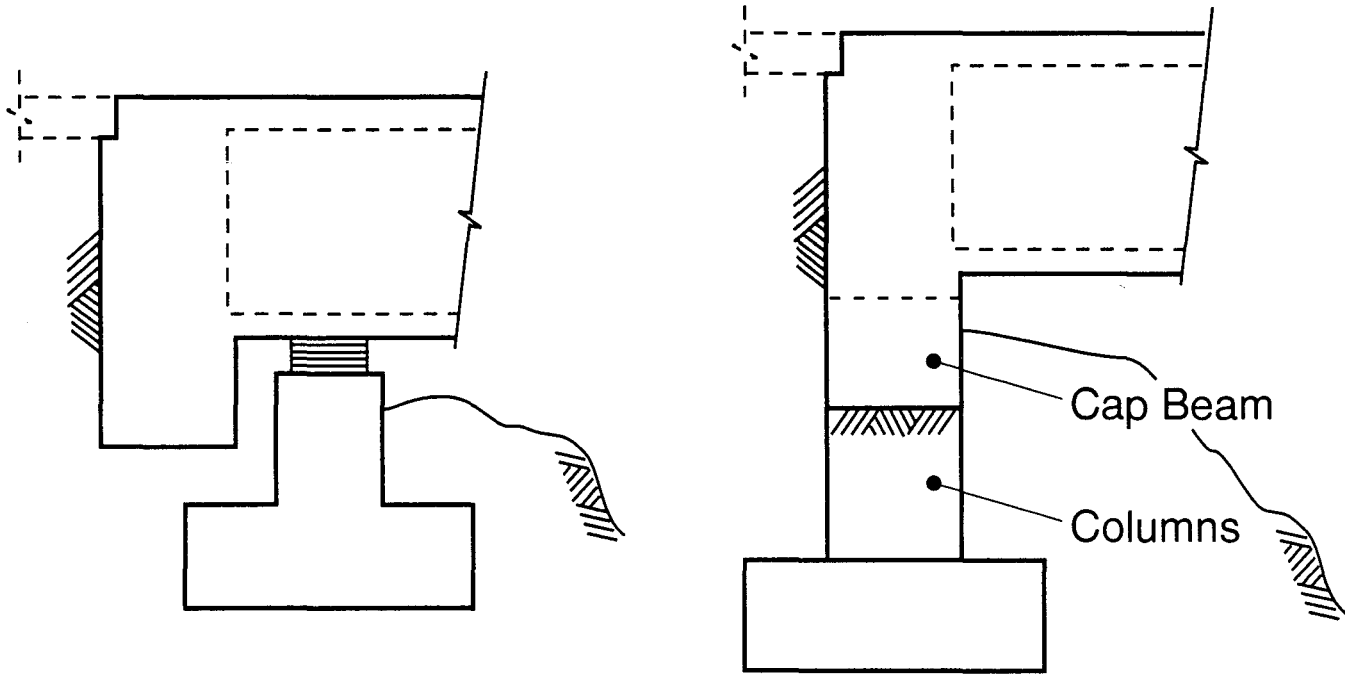


**Integral Abutment**  
(Monolithic)



**Seat Abutment**  
(Free-Standing)

# Variations of the Integral Abutment

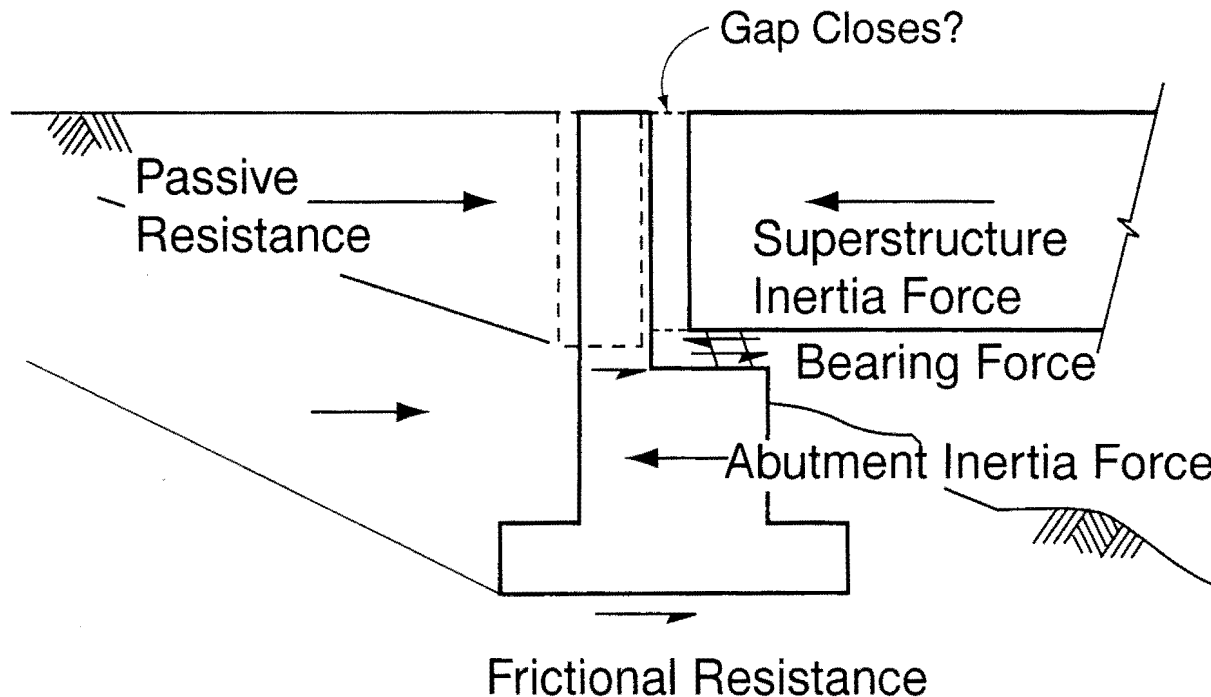


**Stub Abutment**  
(Semi-Integral)

**Spill-Through Abutment**

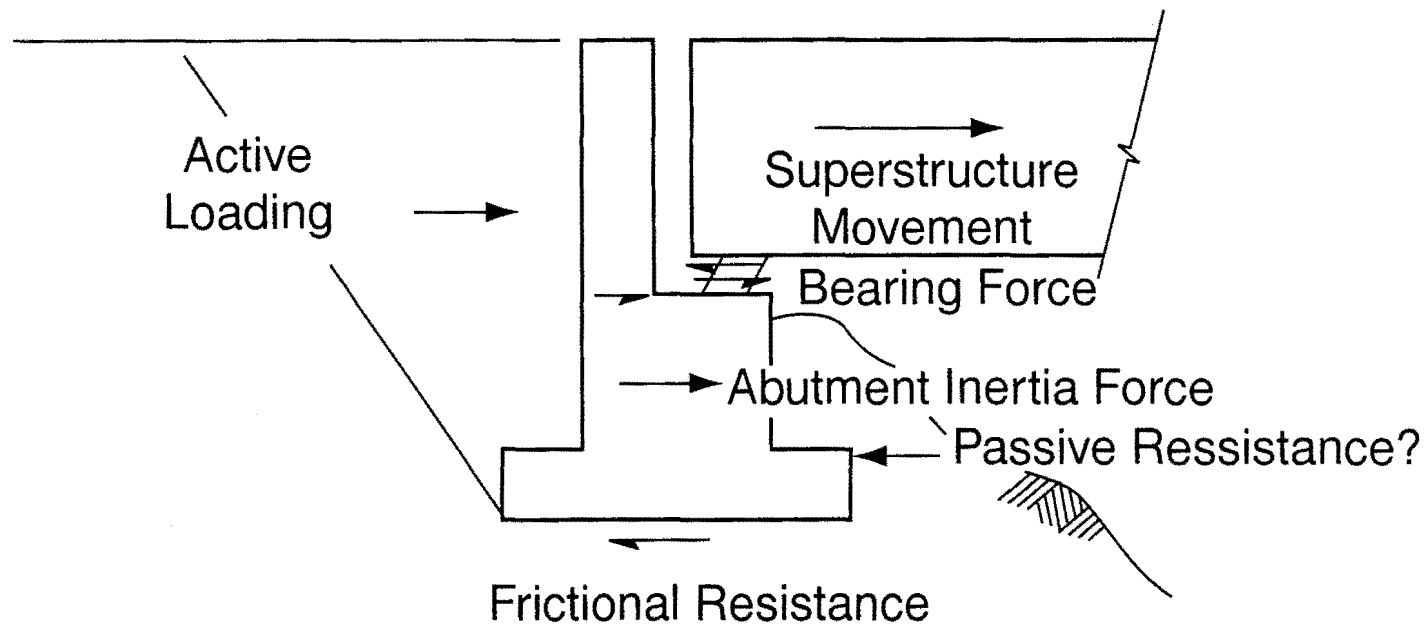
# Seat Type / Longitudinal Behavior

Superstructure Moves **Toward** Backfill

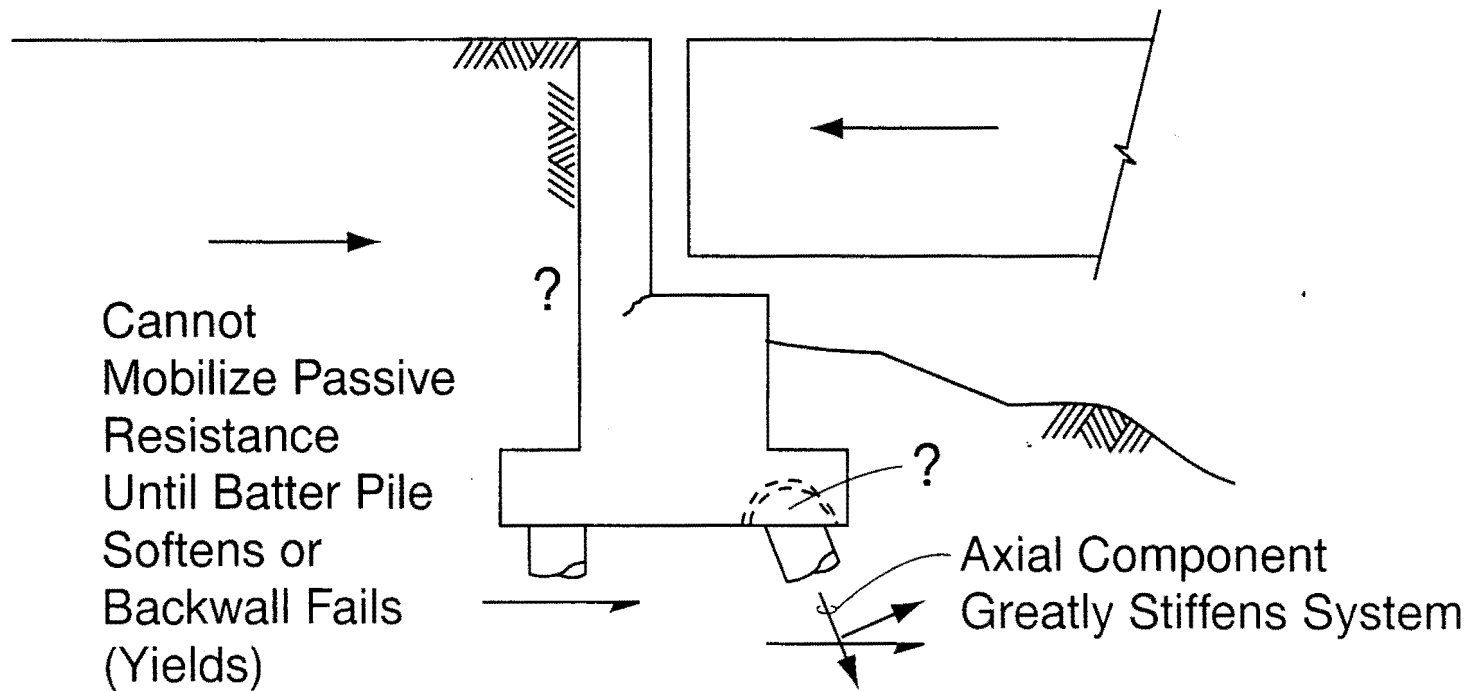


# Seat Type / Longitudinal Behavior (continued)

Superstructure Moves **Away** from Backfill

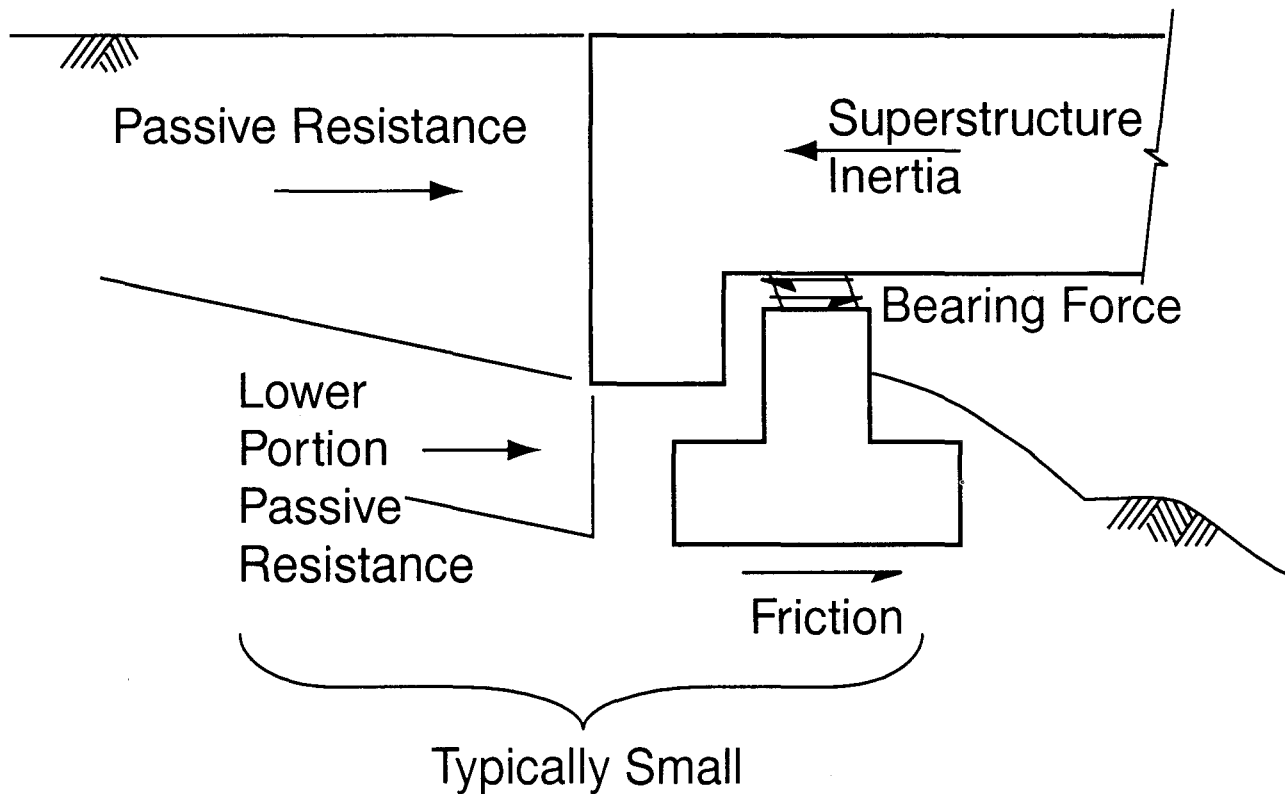


# Effect of Piles Supporting Abutment

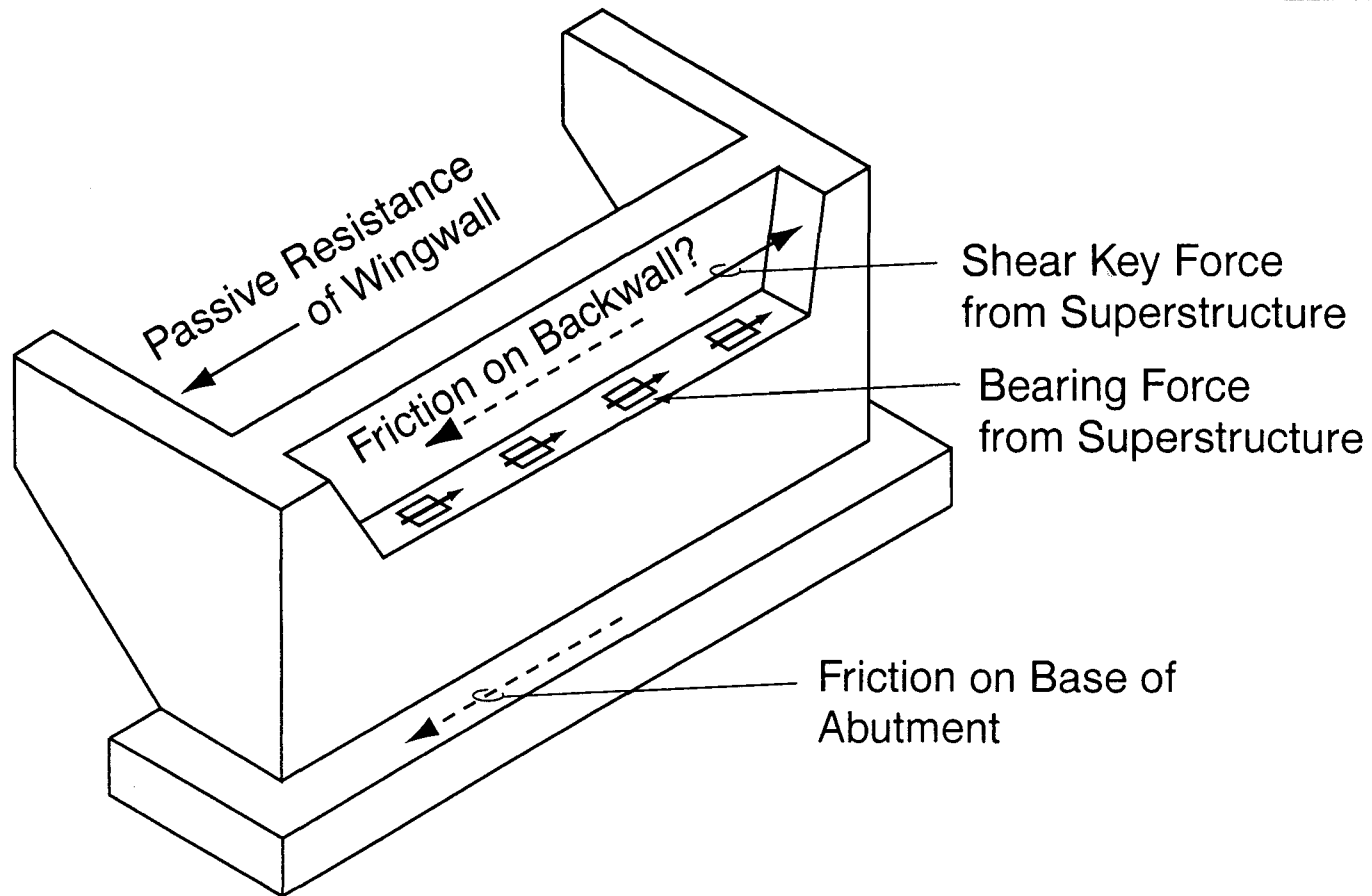




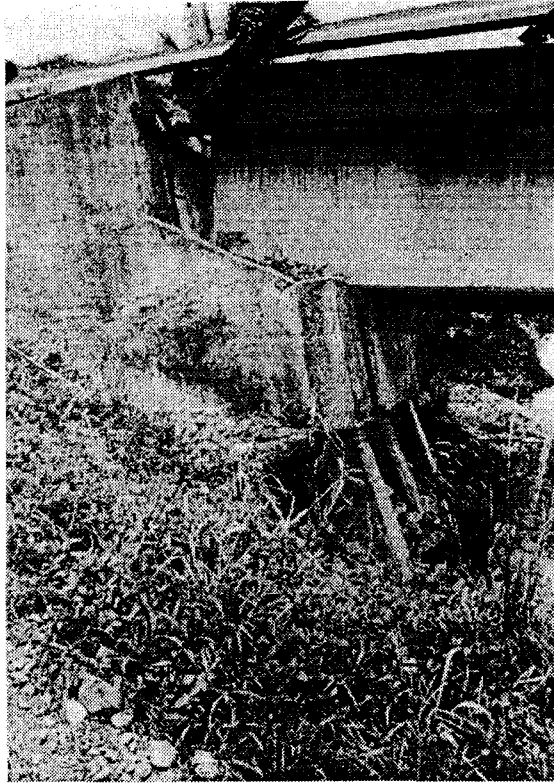
# Integral Type / Longitudinal Behavior



# Transverse Behavior

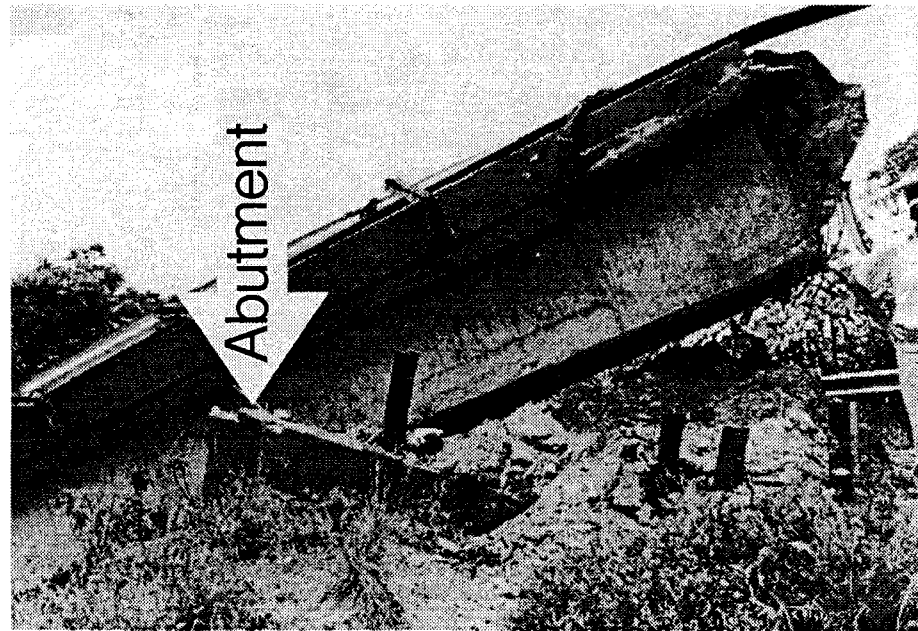


# Abutment Damage



**Abutment Slumping  
and Rotation**

Costa Rica, 1991



**Passive Failure**

Priestley, Seible, Calvi (1996)

Session 2 Page 9 of 45  
UMD-ITV

Seismic Bridge Design Applications  
25 July 1996, NHI Course Code No. 13063

# Session 2

## Abutments

---

- Conceptual Behavior
- **Modeling Soil Flexibility**
- Nonlinear Effects
- Mononobe-Okabe Analysis
- Design Issues, Force Transfer, and Fuse Elements

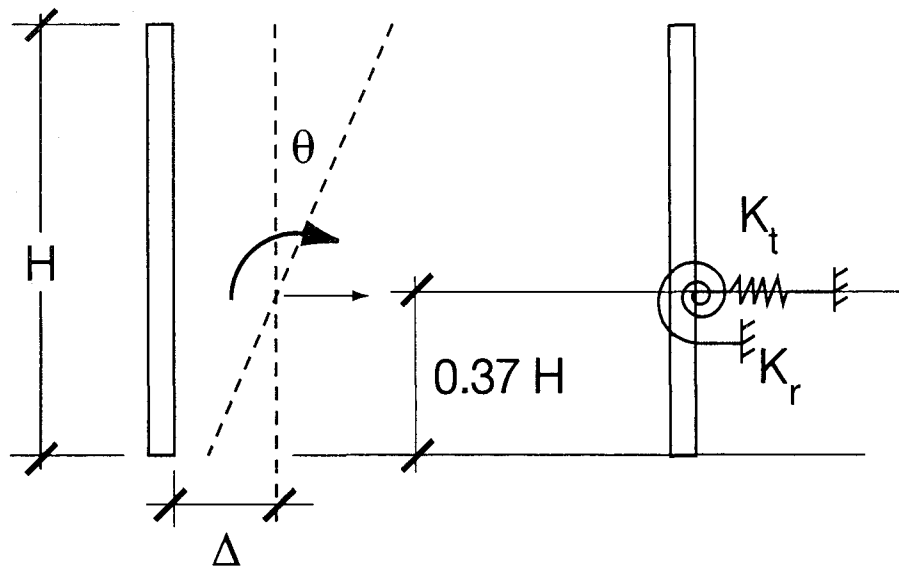
# Methods of Determining Stiffness

---

- Elasticity — FHWA / RD-86 / 101 (1986)
- Empirical — Caltrans

Focus on Elastic Stiffness First, Then Incorporate  
Nonlinear Behavior

# FHWA Method



$$K_t = 0.425 E_s B$$

$$K_r = 0.072 E_s B H^2$$

$E_s$  = Elastic Modulus of  
Backfill

$B$  = Width of Wall

$H$  = Height of Wall

FHWA (1986)

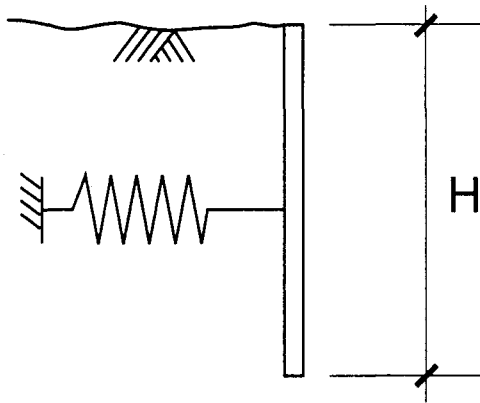
Session 2 Page 12 of 45

UMD-ITV

Seismic Bridge Design Applications  
25 July 1996, NHI Course Code No. 13063

# Caltrans Method

- **Basic Stiffness**



$$K_{\text{abut}} = 200 \frac{\text{kip/in.}}{\text{ft of Width}}$$

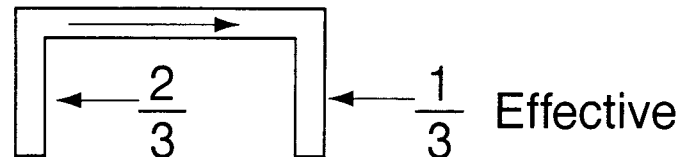
(8 ft High Wall)

- **Wall Height  $\neq$  8 ft**

Linearly Prorate

- **Wingwalls**

Assume  $\frac{2}{3}$  Effective into Backfill,  
and  $\frac{1}{3}$  Effective Away from Backfill



# Caltrans Method (continued)

- Maximum Soil Capacity = 7.7 ksf (Passive)

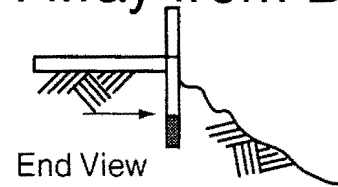
Based on

- Properly Compacted and Drained Backfill
- Maximum Static = 5.0 Amplified by 1/0.65 for Dynamic Effects

- Thoughts on Wingwalls

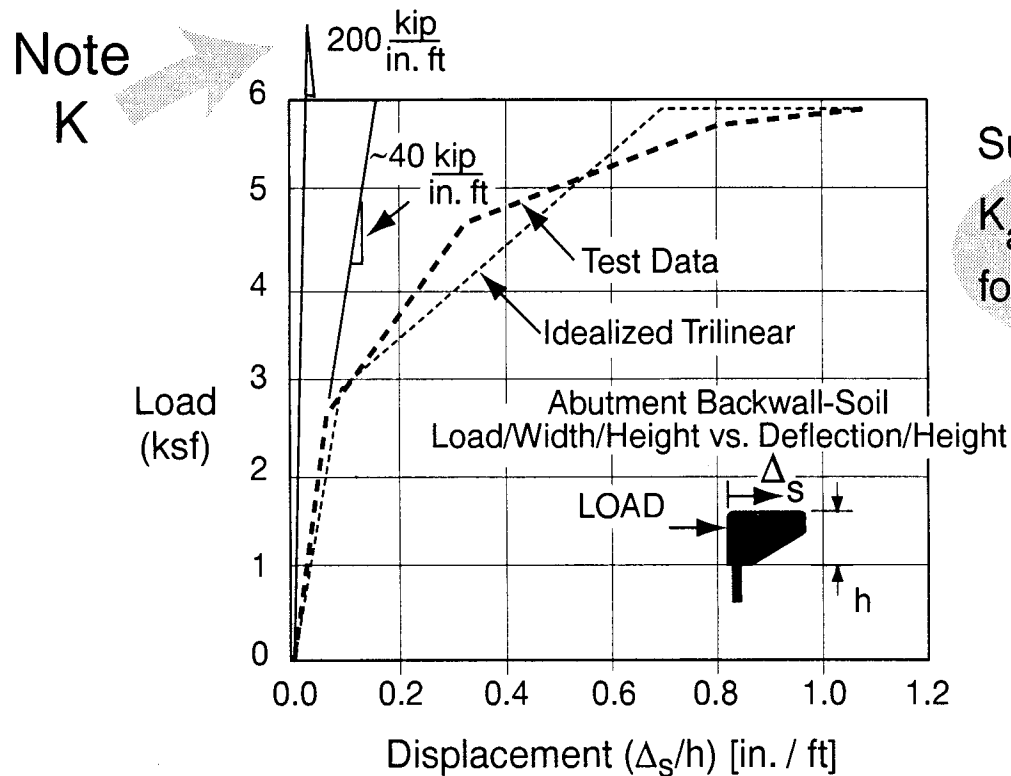
- Effectiveness Acting Away from Backfill

$$\frac{1}{3} \longrightarrow 0 ?$$





# Test Data / Large Scale Abutment Tests



Suggest:

$K_{\text{abut}} \approx 40 - 50 \frac{\text{kip}}{\text{in. ft}}$   
for an 8 ft High Wall

Priestly, Seible, Calvi, 1996

Session 2 Page 15 of 45

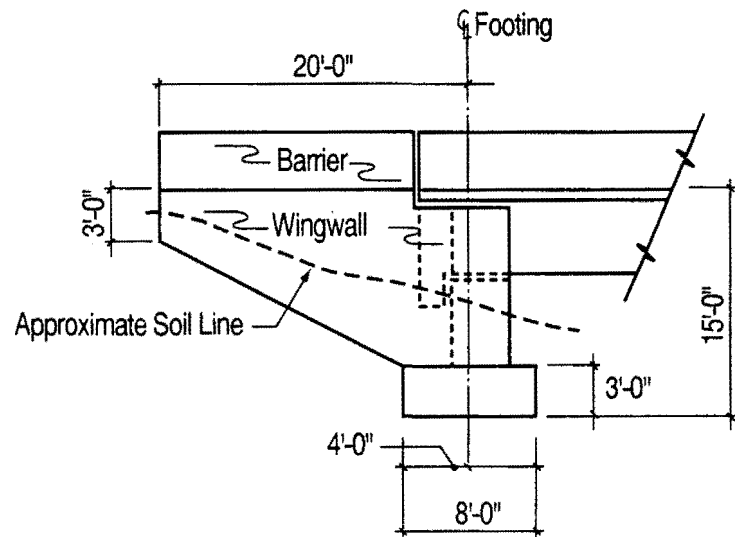
UMD-ITV

Seismic Bridge Design Applications

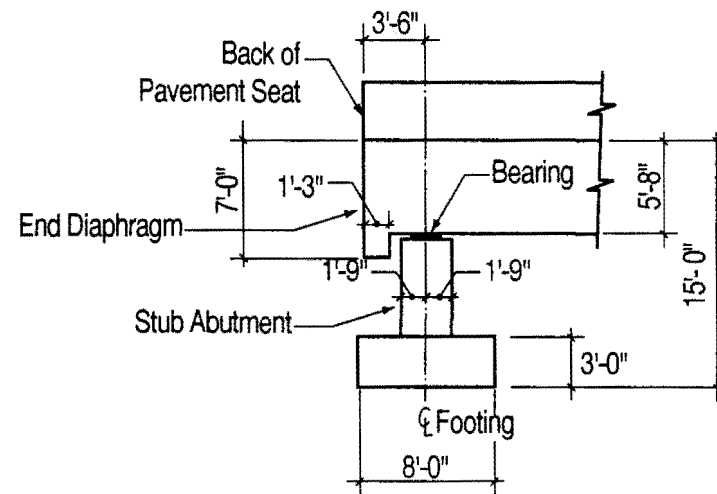
25 July 1996, NHI Course Code No. 13063

# Example / Calculation of Abutment Stiffnesses

Consider Practice Problem No. 1 with an Integral Abutment



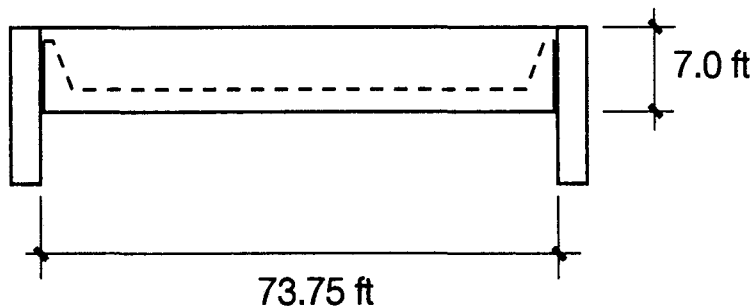
**Elevation**



**Interior Section**

## Example / Abutment Stiffness (continued)

Assume the Following Geometry Between the Wingwalls



- Caltrans  $K_{\text{abut}} = 40(73.75) \frac{7}{8} (12) = 30,975 \text{ kip/ft}$   
 $\frac{\text{kip/in.}}{\text{ft}}$

# Example / Effect of Abutment Stiffness On Seismic Forces

---

- Recall  $K_{bent} = 3639 \text{ kip/ft}$   
 $W = 4842 \text{ kip}$
  - New Stiffness (Caltrans)  $K_{total} = K_{bent} + K_{abut}$   
 $K_{total} = 34,614 \text{ kip/ft}$
  - New Values  $V = 1816 \text{ kip}$   
 $\Delta = 0.63 \text{ in.}$
- } Session 1  
 Consider One Abutment Acts at a Time
- { 191 kip to Bent vs. 886 kip Before!  
 1625 kip to Soil

# Example / Check of Abutment Behavior

---

- Determine Backfill Pressure

$$p = \frac{1625}{7(73.75)} = 3.15 \text{ ksf} < 7.7 \text{ ksf Capacity}$$

∴ OK!

Soil Can Withstand Forces  
in Longitudinal Direction

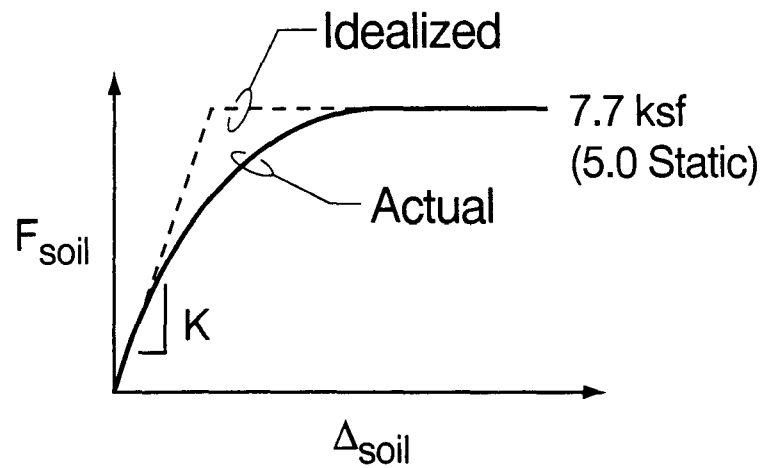
# Session 2

## Abutments

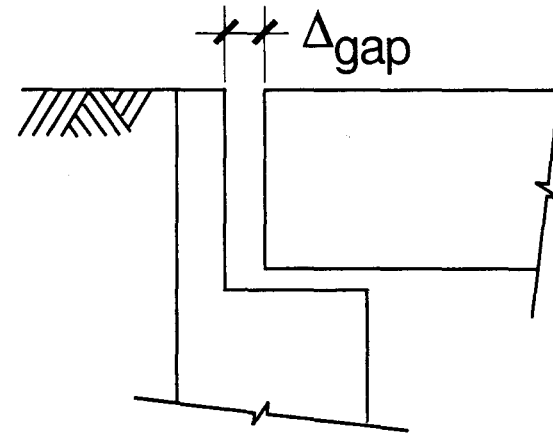
---

- Conceptual Behavior
- Modeling Soil Flexibility
- **Nonlinear Effects**
- Mononobe-Okabe Analysis
- Design Issues, Force Transfer, and Fuse Elements

# Sources of Nonlinearity

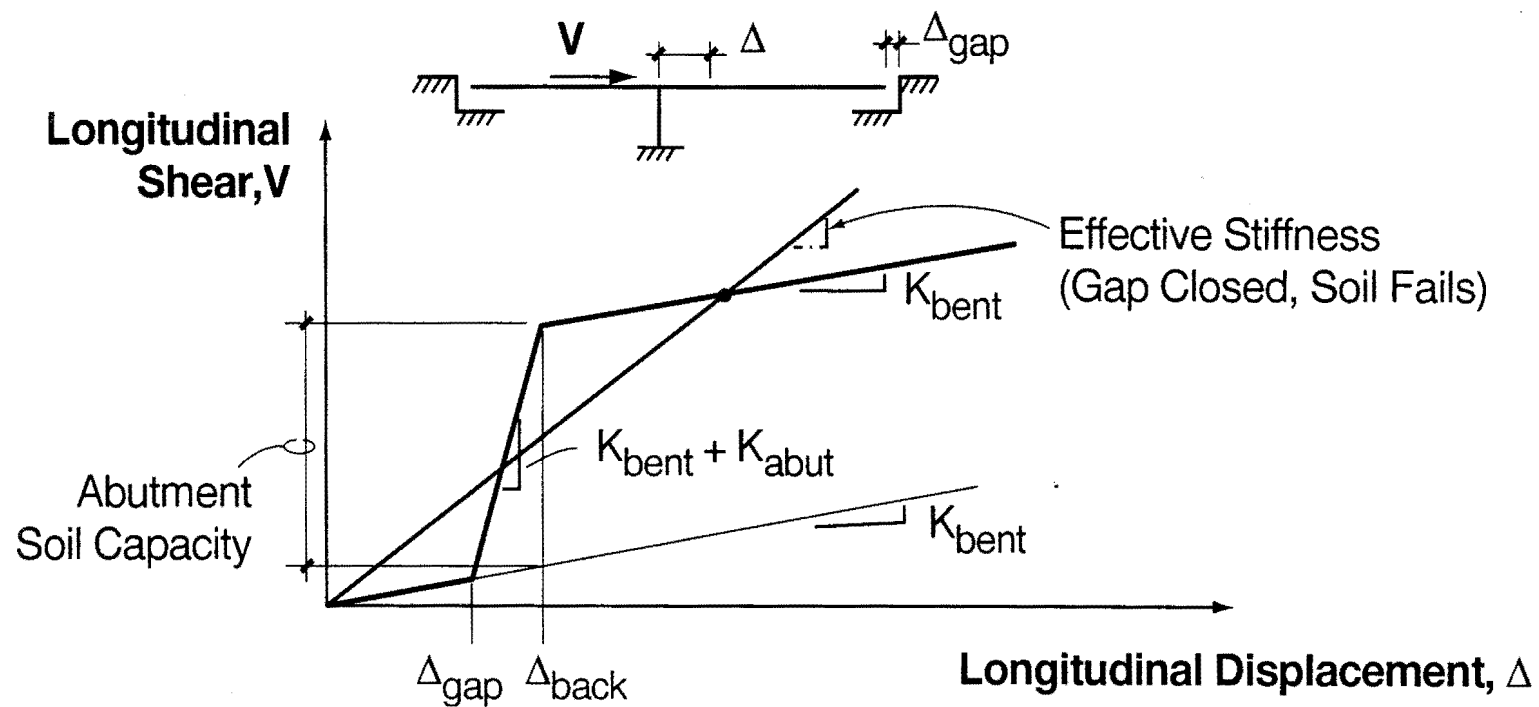


**Soil Behavior**



**Movement Joints**

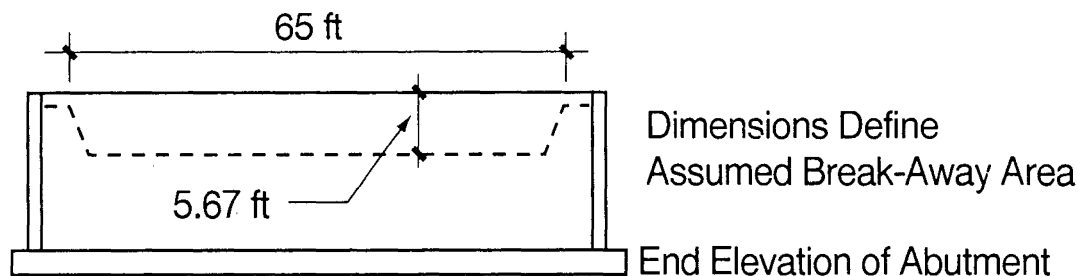
# Overall Structure Stiffness





# Example / Abutment Nonlinearities (1 of 7)

- Use Seat Abutment Detail Given with Practice Problem No. 1
- Leave Columns at 3 ft Diameter
- Assign  $A = 0.40g$  (In Order to Be Well into Nonlinear Range)
- Assume Backwall Breaks Away Around Perimeter of Box Girder
- Recall  $K_{bent} = 3639 \frac{\text{kip}}{\text{ft}}$ ,  $\Delta_{gap} = 6 \text{ in.}$ ,  $S = 1.2$ , and  $W = 4842 \text{ kip}$



## Example / Abutment Nonlinearities (2 of 7)

---

- Longitudinal Stiffness of Abutment (Caltrans)

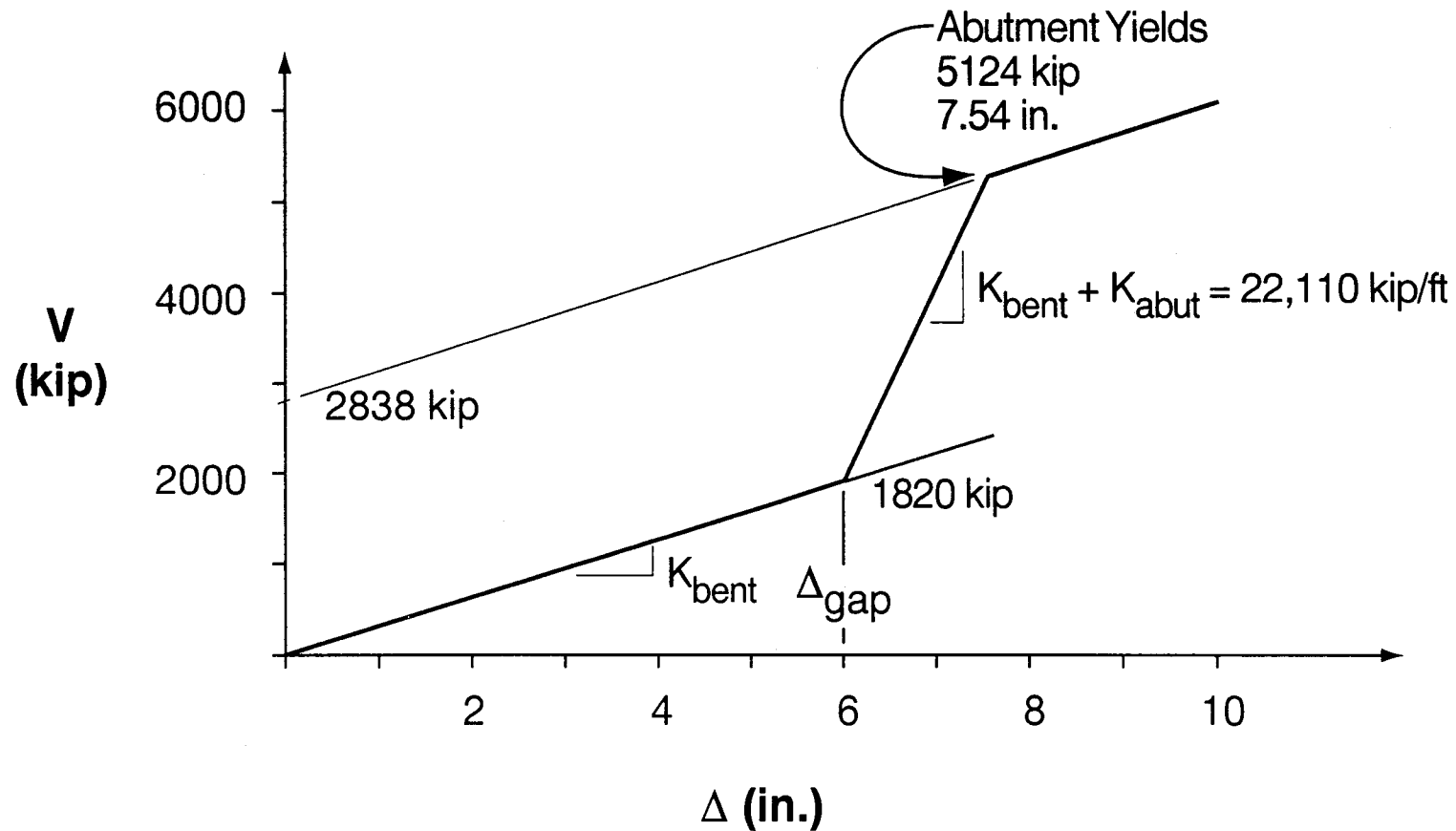
$$K_{\text{abut}} = 40 (65) \frac{5.67}{8} (12) = 22,110 \text{ kip/ft}$$

- Abutment Backfill Capacity (Caltrans)

$$P_{\text{max}} = 7.7(65)5.67 = 2838 \text{ kip}$$

- Construct V vs.  $\Delta$  Curve for Structure (Longitudinal)

# Example / Abutment Nonlinearities (3 of 7)



## Example / Abutment Nonlinearities (4 of 7)

---

- Check  $\Delta$  with Only Bent

$$K = 3639 \text{ kip/ft} \longrightarrow T = 2\pi \sqrt{\frac{4842}{32.2(3639)}} = 1.28 \text{ sec}$$

$$C_s = \frac{1.2 (0.4) 1.2}{1.28^{2/3}} = 0.49 < 1.00 \longrightarrow V = 0.49(4842) = 2373 \text{ kip}$$

$$\Delta = \frac{2373}{3639} (12) = 7.8 \text{ in.} > 6 \text{ in.} \quad \therefore \text{Into Nonlinear Range}$$

- Iterative Approach — Guess K, Determine V and  $\Delta$ , Revise
- Direct Approach — Plot Spectral V vs.  $\Delta$

# Example / Abutment Nonlinearities (5 of 7)

---

## Direct Spectral Approach

- $V = f(C_s) \quad C_s = f(T) \quad T = f(W/K) \quad K = f(V/\Delta) \quad \therefore \mathbf{V = f(\Delta)}$

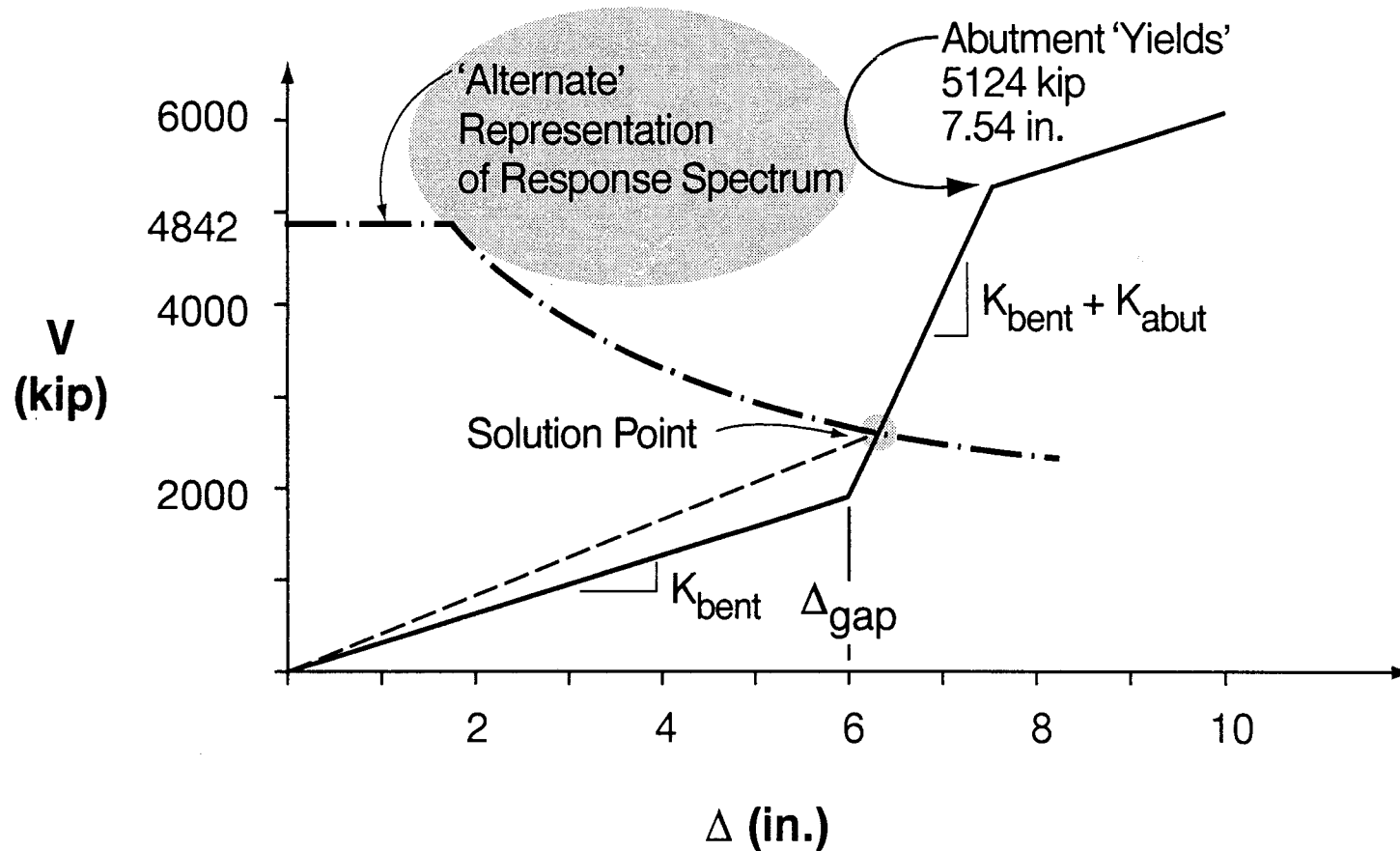
- For a SDOF System with Full Mass Participation ( $V = C_s W$ )

$$V = \frac{(1.2AS)^{3/2} W g^{1/2}}{2\pi} \frac{1}{\Delta^{1/2}} \leq 2.5 AW$$

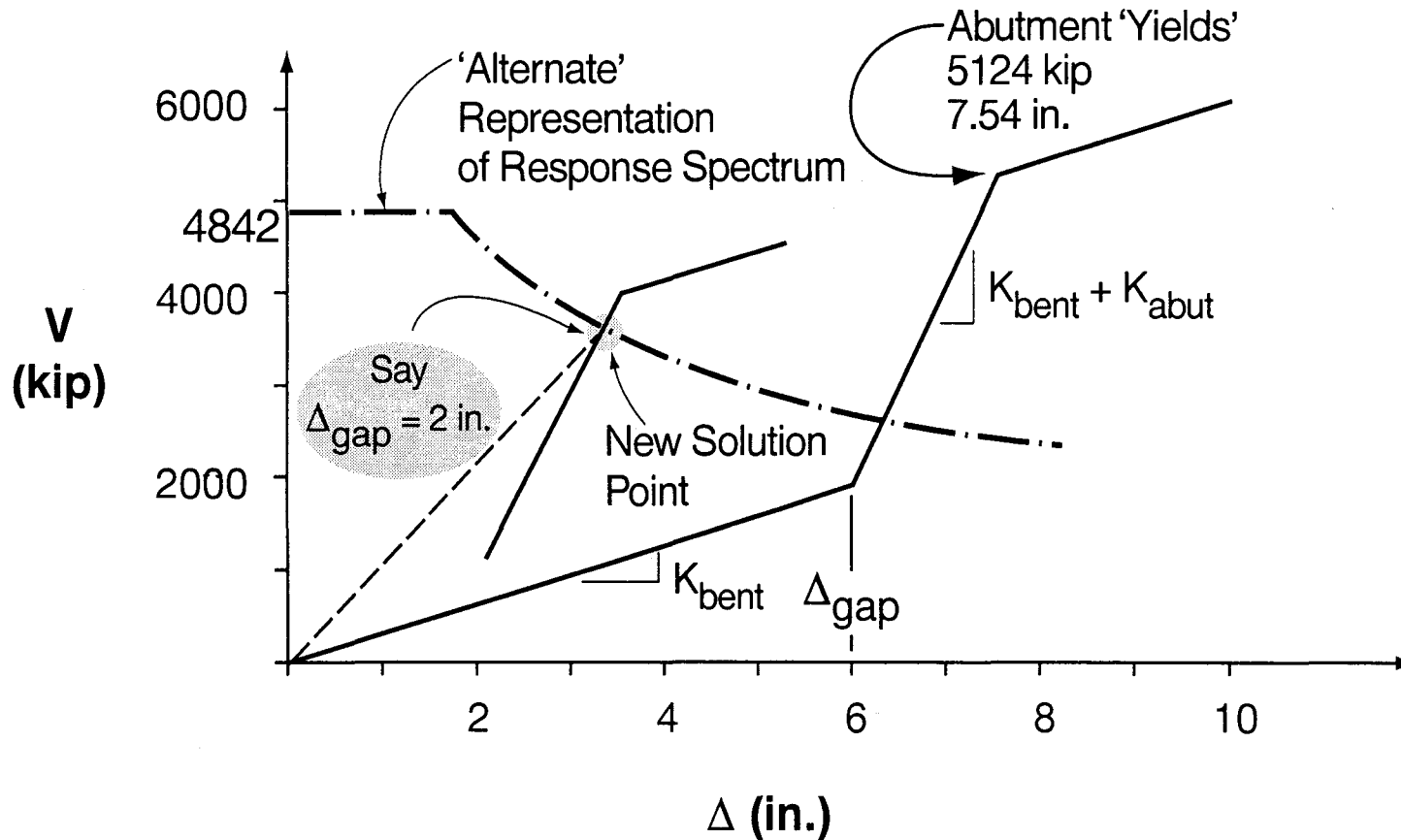
- For This Example

$$V = 1912 \frac{1}{\Delta^{1/2}} \leq 4842 \text{ kip} \quad (\Delta \text{ in ft})$$

# Example / Abutment Nonlinearities (6 of 7)



# Example / Abutment Nonlinearities (7 of 7)



# Session 2

## Abutments

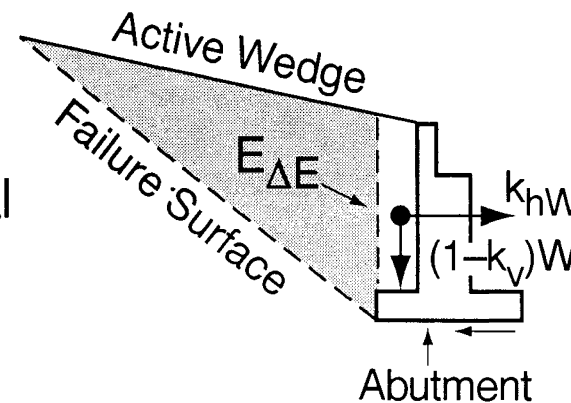
---

- Conceptual Behavior
- Modeling Soil Flexibility
- Nonlinear Effects
- **Mononobe-Okabe Analysis**
- Design Issues, Force Transfer, and Fuse Elements



# Pseudostatic Approach / Yielding Abutments

- Applies to Seat-Type (Freestanding) Abutments that Are Not Restrained by Superstructure
- Cohesionless Backfill with Friction Angle  $\phi$
- Unsaturated / No Liquefaction
- Coulomb Sliding Wedge + Vertical and Horizontal Inertia Effects



# Calculation of Active Seismic Loading on Wall

---

$$E_{AE} = \frac{1}{2} \gamma H^2 (1 - k_v) K_{AE}$$

- Inertial Effect Increases Forces

$\gamma$  = Soil Unit Weight

H = Wall Height

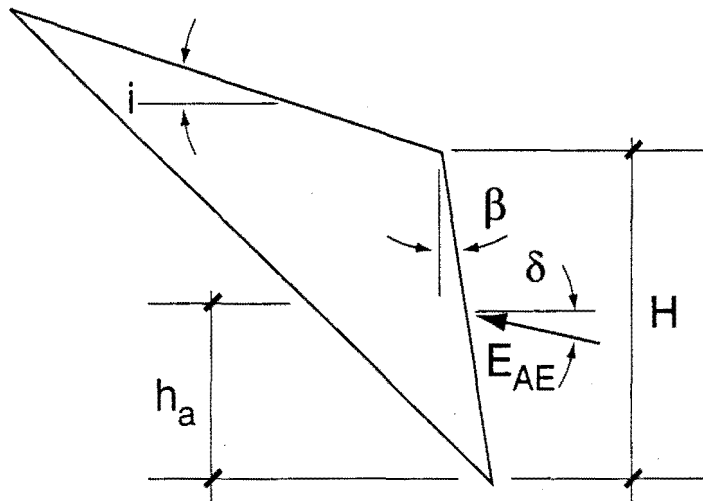
$k_v$  = Vertical Acceleration Coefficient

$k_h$  = Horizontal Acceleration Coefficient

Typically  $\left. \begin{array}{l} k_v = 0 \\ k_h = 0.5A \end{array} \right\} \begin{array}{l} \text{Division I-A} \\ 6.4.3(A) \text{ and } 7.4.3(A) \end{array}$

# Active Seismic Loading (continued)

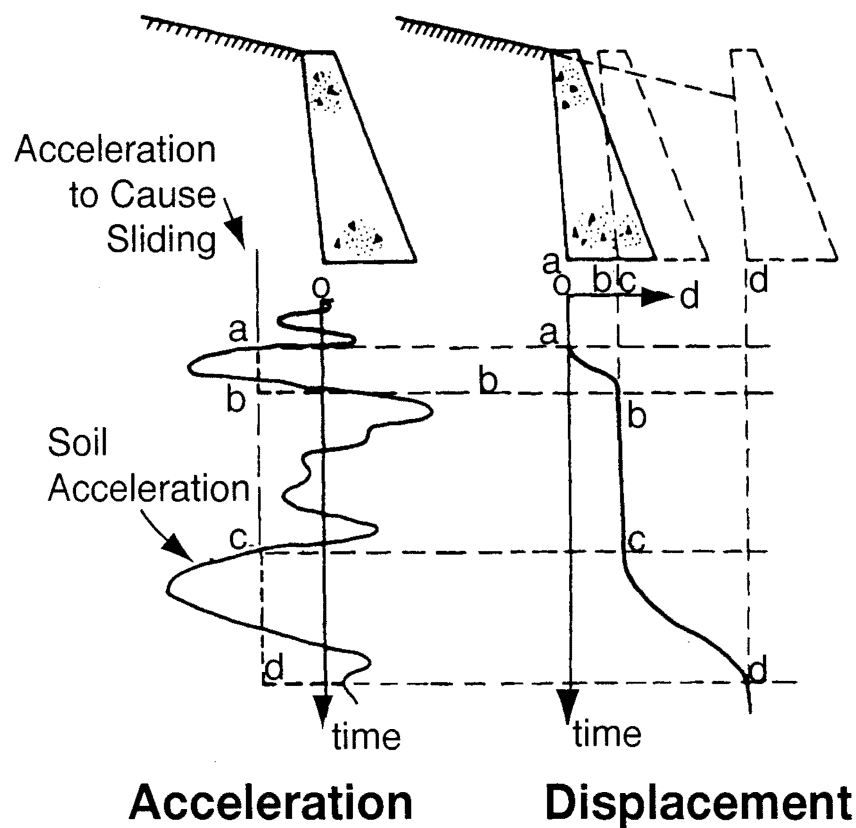
$$K_{AE} = \frac{\cos^2(\phi - \theta - \beta)}{\cos\theta \cos^2\beta \cos(\delta + \theta + \beta) \left[ 1 + \sqrt{\frac{\sin(\theta + \delta) \sin(\phi - \theta - i)}{\cos(\delta + \beta + \theta) \cos(i - \beta)}} \right]^2}$$



$$\theta = \tan^{-1} \left( \frac{k_h}{1 - k_v} \right)$$

$$\delta = \frac{\phi}{2} \text{ (Typical Approximation)}$$

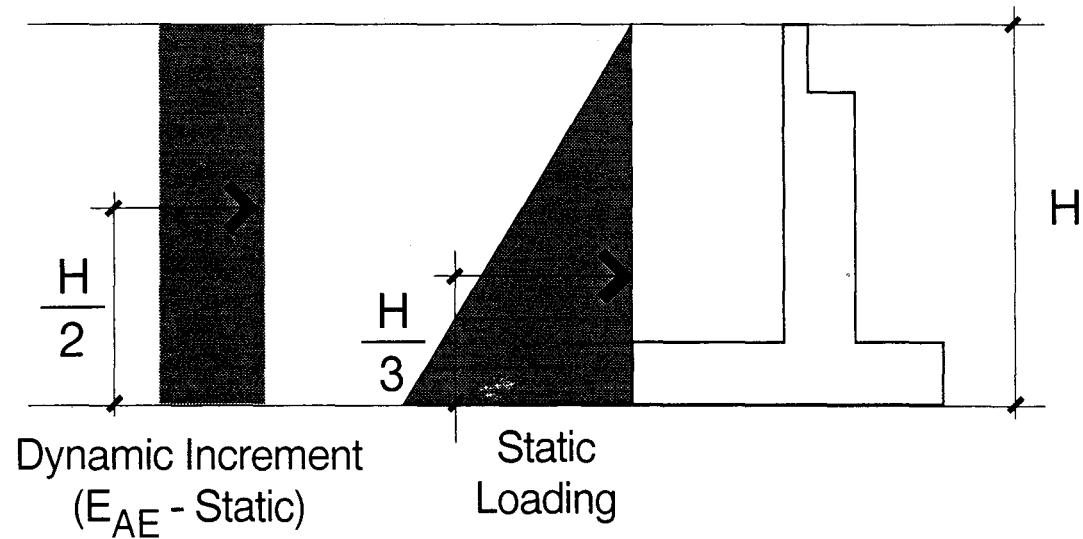
# Allowing Some Wall Movement



- By Allowing Some Movement,  
 $k_h = 0.5 A$  (Instead of  $A$ )
- Expect Displacements to  $10 \cdot A$  (in.)
- Also Basis of 7.7 ksf vs. 5.0 ksf Used by Caltrans

# Distributing the Force

- M-O Expression Includes the Static Active Load
- Obtain Static Force by Using  $k_h$  (or  $\theta$ ) = 0



# Other Conditions

---

- Abutments Restrained by Soil Anchors or Battered Piles,  
Use  $k_h = 1.5A$
- Abutments Moving into Soil, — Could Use  
M-O Passive, But No Experimental Verification

# Using the Concepts

---

<u>Abutment Type / Condition</u>	<u>Method</u>	<u>...</u>	<u>Product</u>
• Seat / Gap Open	M-O Active	...	Loading
• Seat / Gap Closed	or Caltrans	...	Stiffness / Capacity
	FHWA	...	Stiffness
• Integral	or Caltrans	...	Stiffness / Capacity
	FHWA	...	Stiffness

# Session 2

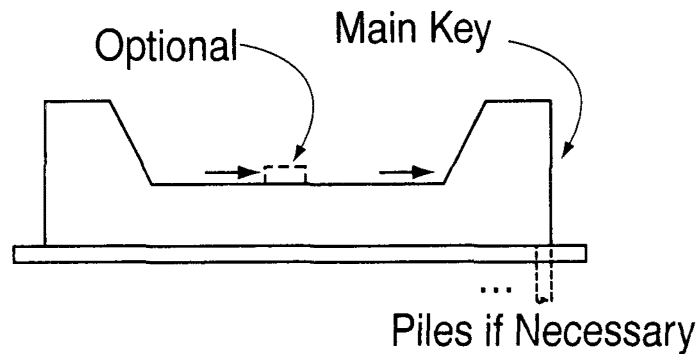
## Abutments

---

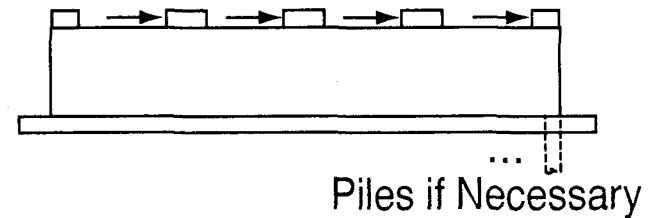
- Conceptual Behavior
- Modeling Soil Flexibility
- Nonlinear Effects
- Mononobe-Okabe Analysis
- **Design Issues, Force Transfer, and Fuse Elements**



# Transverse Loading of Abutments / Shear Keys



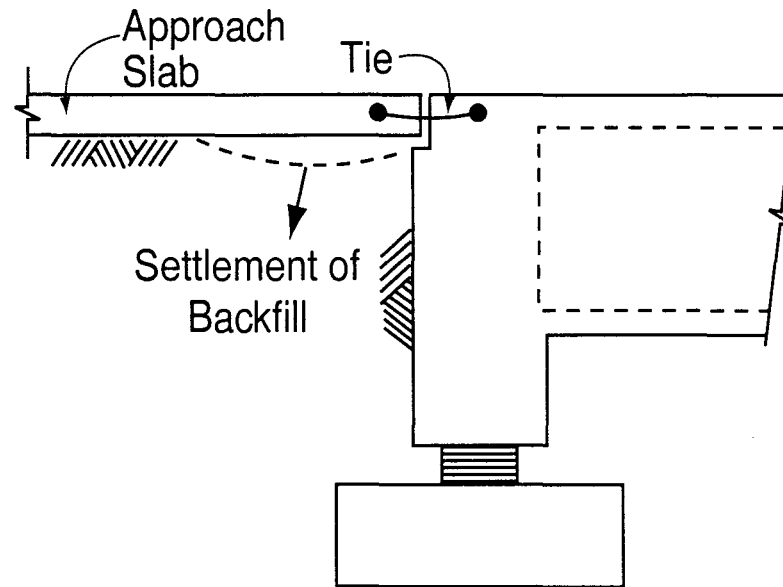
**Box Girder  
Arrangement**



**Precast or Steel  
Girder Arrangement**

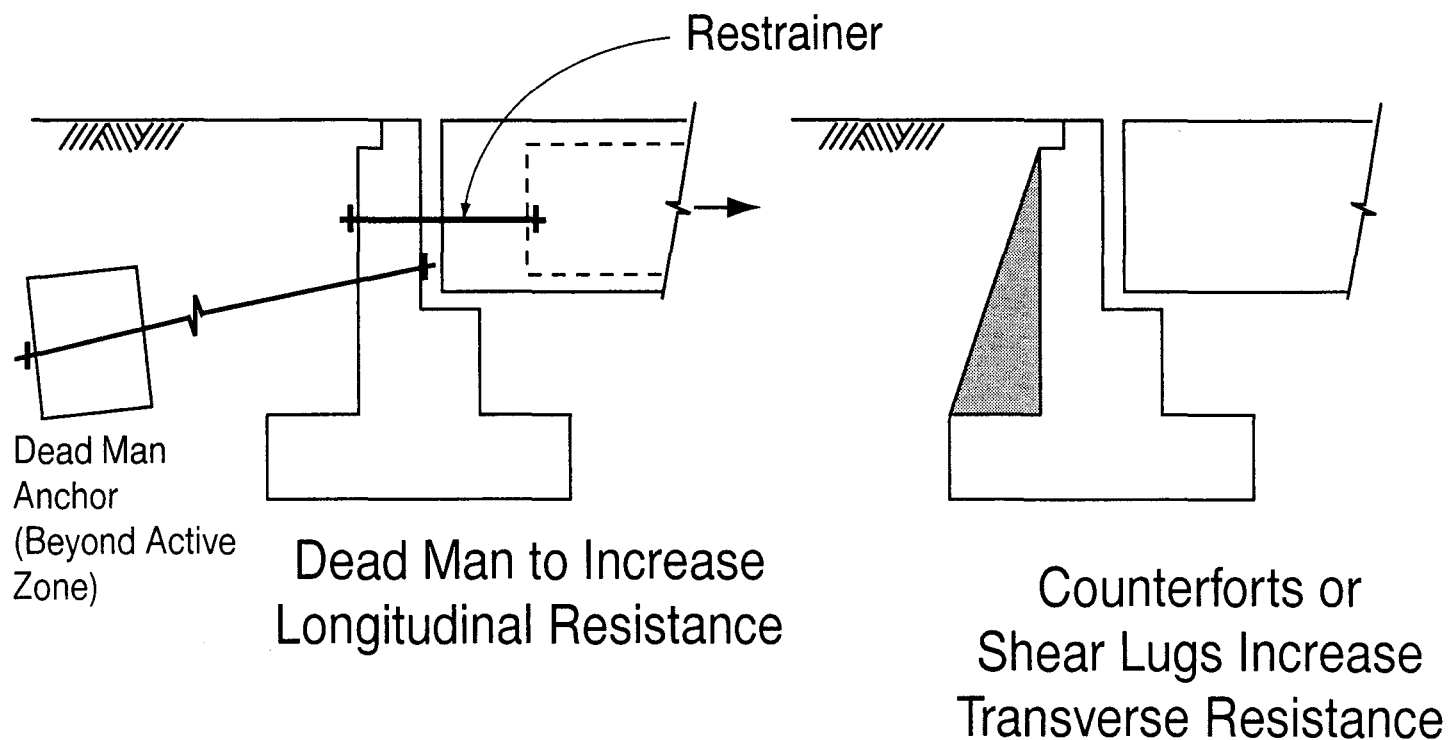
- Interior Keys for Box Girders Difficult to Inspect and Repair
- Multiple Keys May Not Load Evenly (Be Conservative / Ductile)
- Consider 'Fusing' Keys to Fail Before Damaging Piles

# Approach Slabs



- If Settlement Occurs, Approach Slab Provides Access to Bridge (Required for SPC **D**, Emergency Response)
- Tie to Superstructure to Prevent Unseating

# Enhancements for Force Transfer



# External Shear Key Damage

---

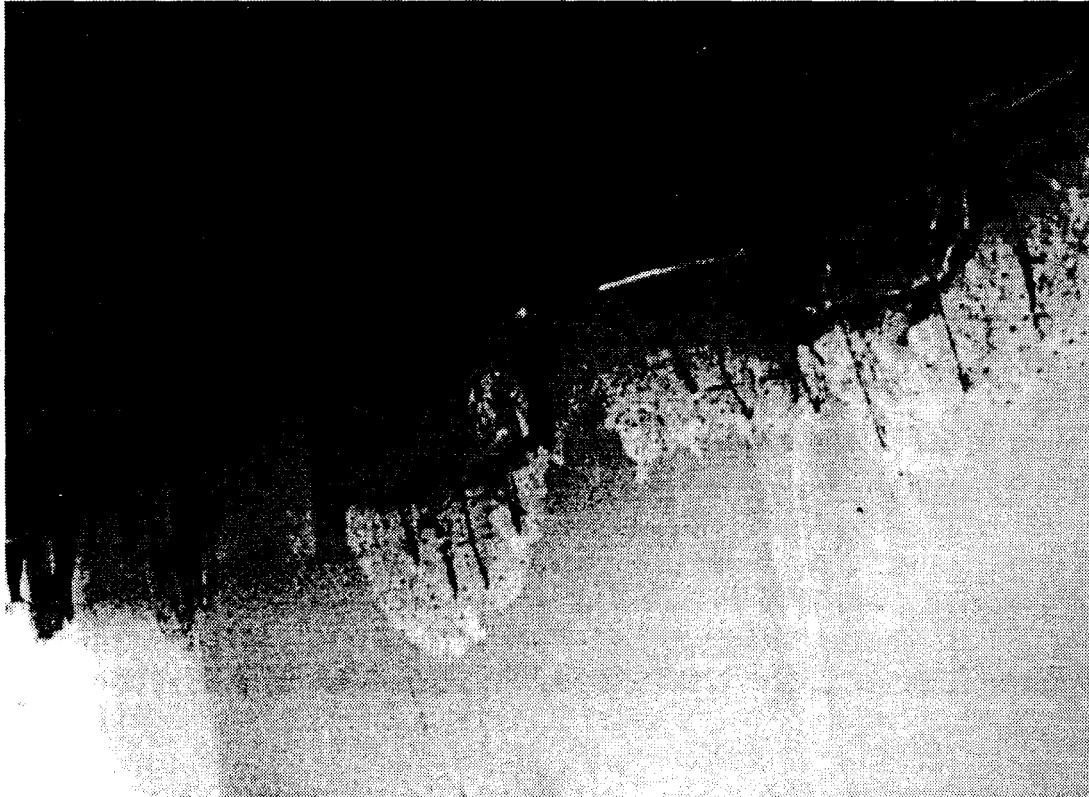


Northridge,  
1994

EERI (1995)

# Internal Shear Key Damage

---



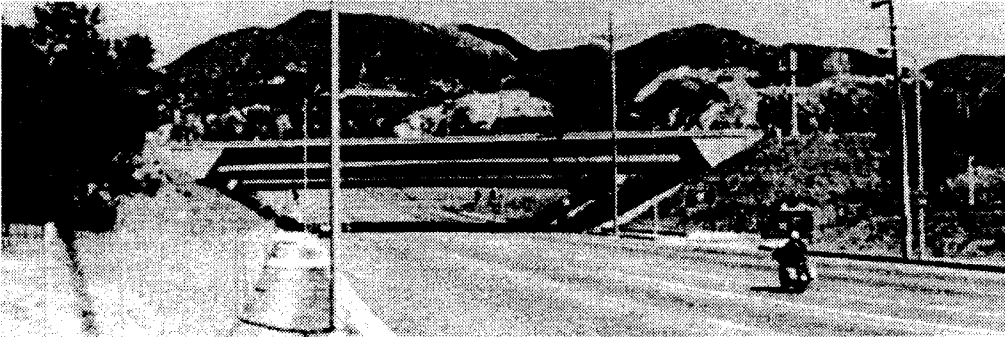
Northridge,  
1994

EERI (1995)

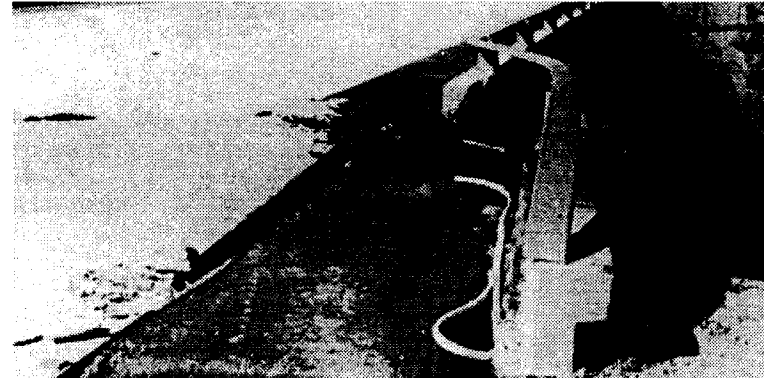
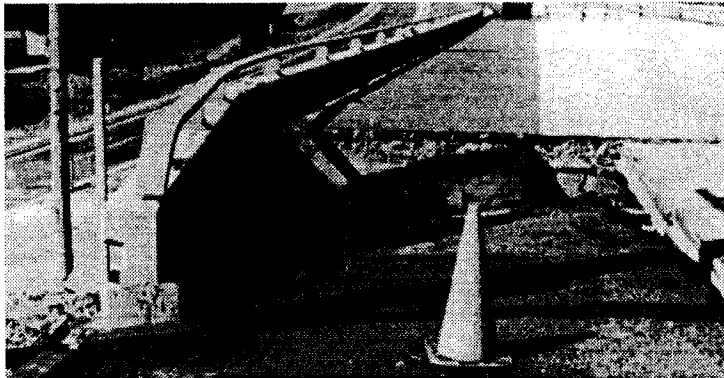
Session 2 Page 43 of 45  
UMD-ITV

Seismic Bridge Design Applications  
25 July 1996, NHI Course Code No. 13063

# Transverse Response and Backfill Settlement Issues

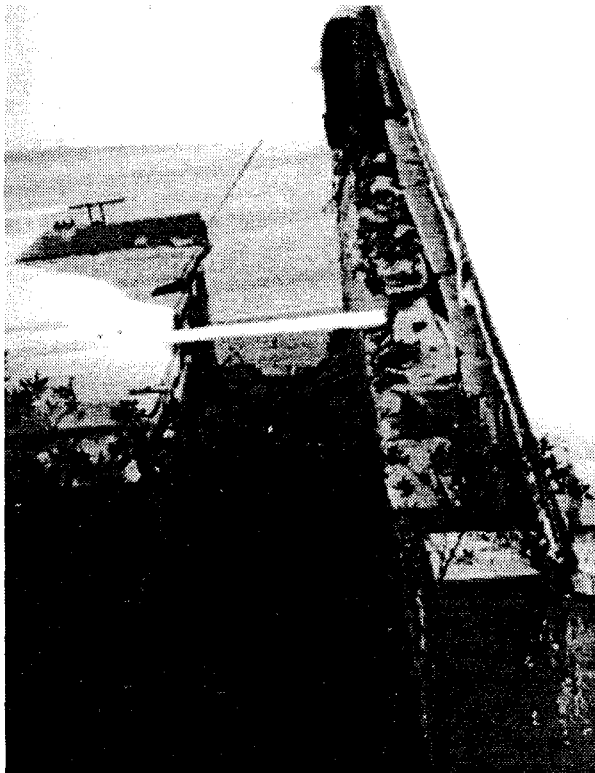


San Fernando,  
1971



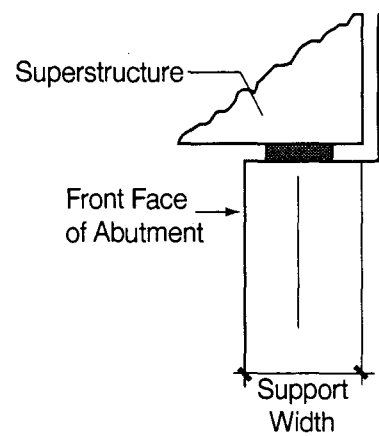
Caltech (1971)

# Most Important of All – Seat Width

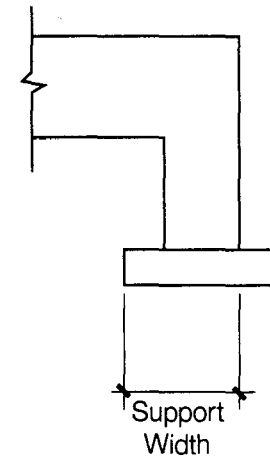


EERI (1995)

## Northridge, 1994



**Seat Abutment**



**Integral Abutment**





# **Session 3**

## **Steel Plate Girder Bridge Examples**

---

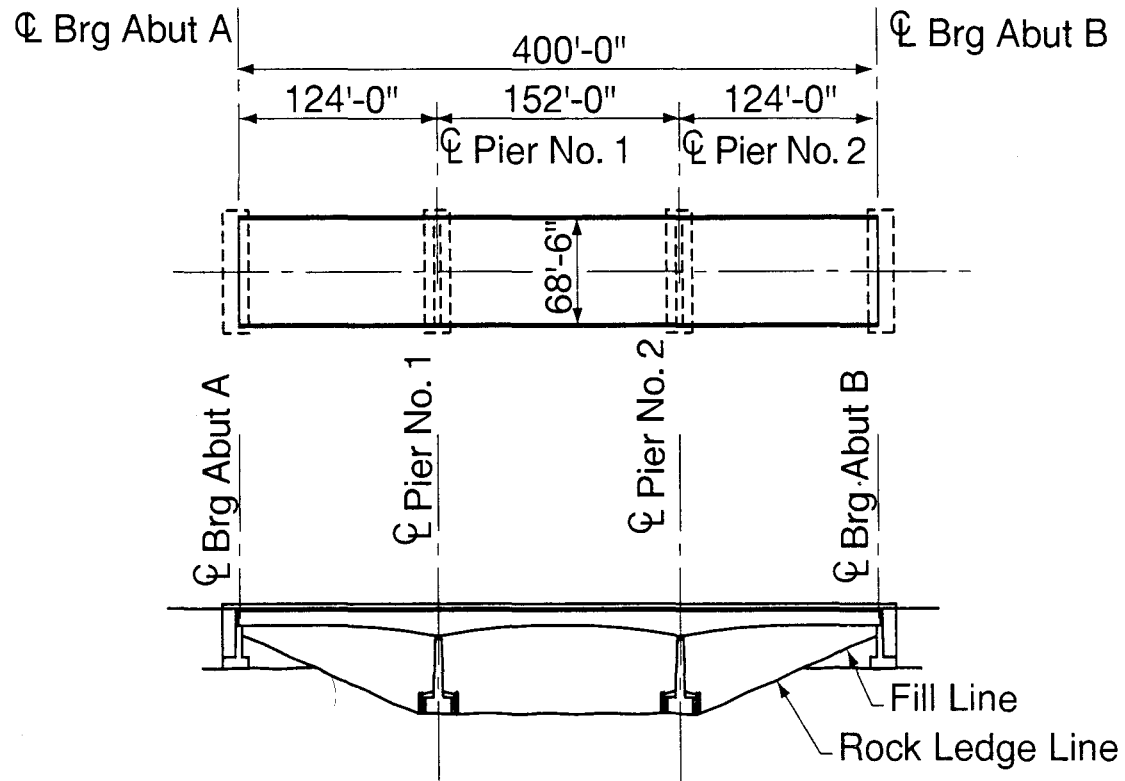
### **Session 3**

- **Practice Problem No. 2**
- **Conceptual Design Considerations**
- **Steel Superstructure Issues**

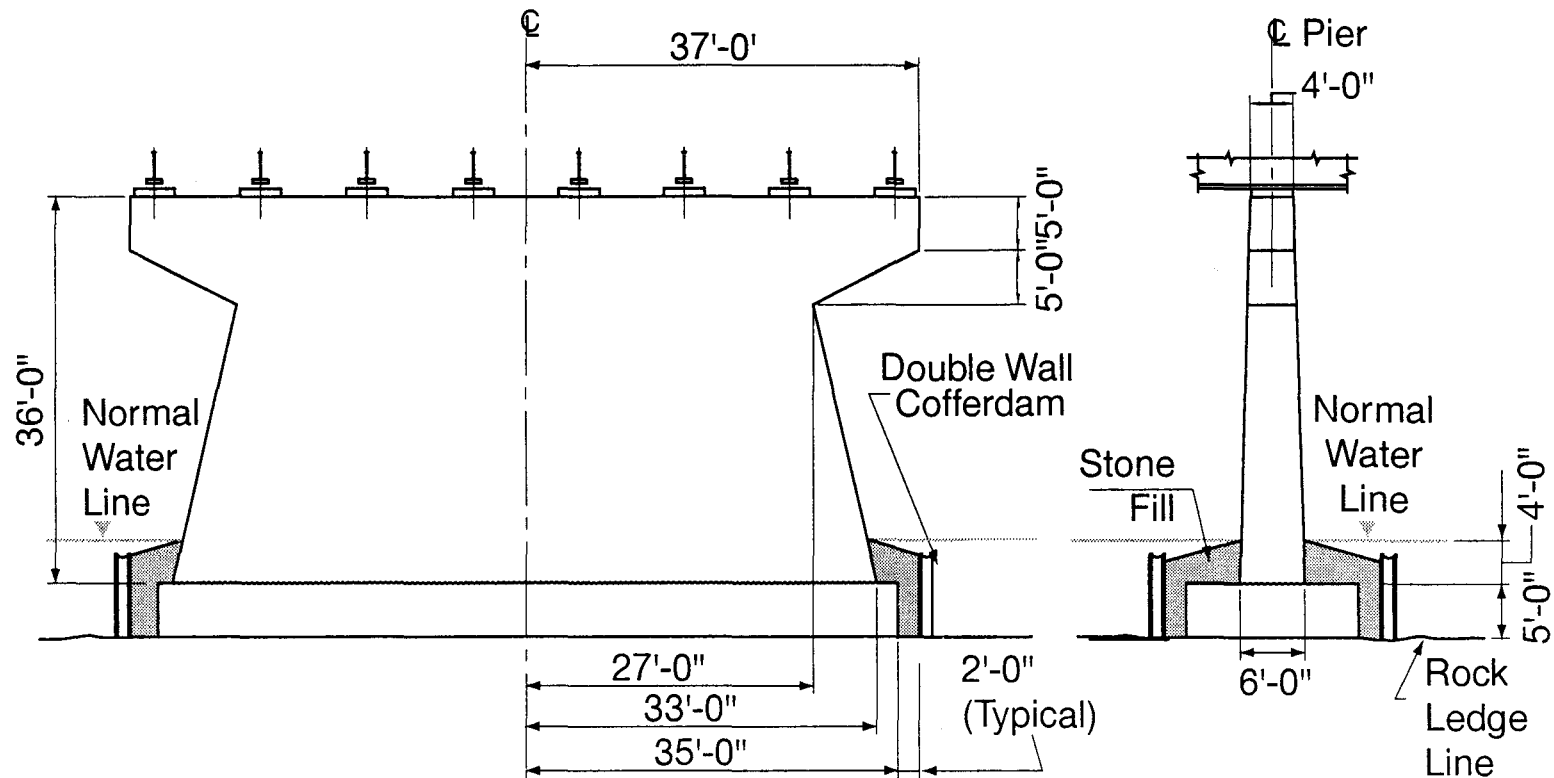
### **Session 4**

- **Skew Structure Issues**
- **Elastomeric Bearing Modeling**

# Steel Plate Girder Bridge / Layout



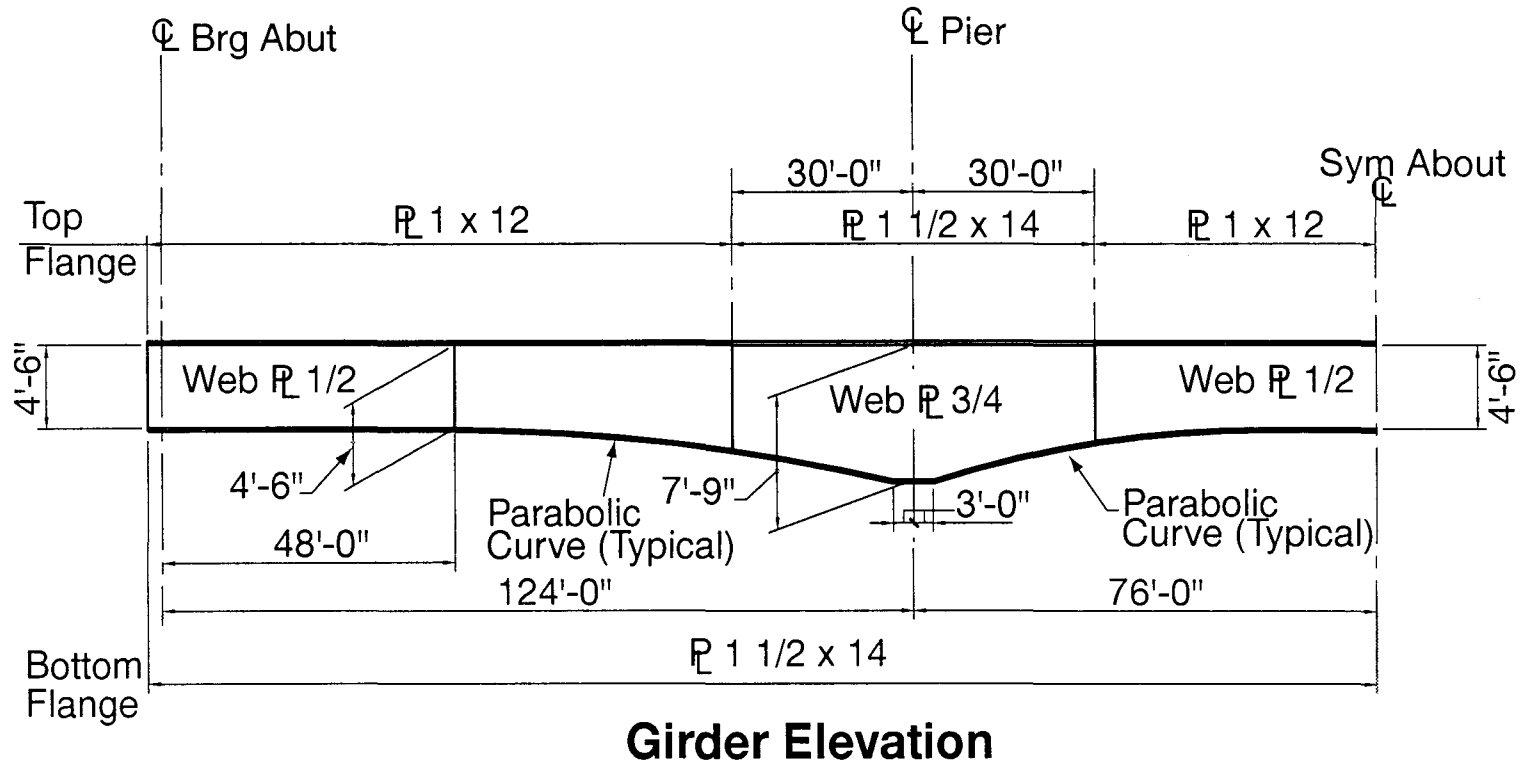
# Steel Plate Girder Bridge / Wall Pier



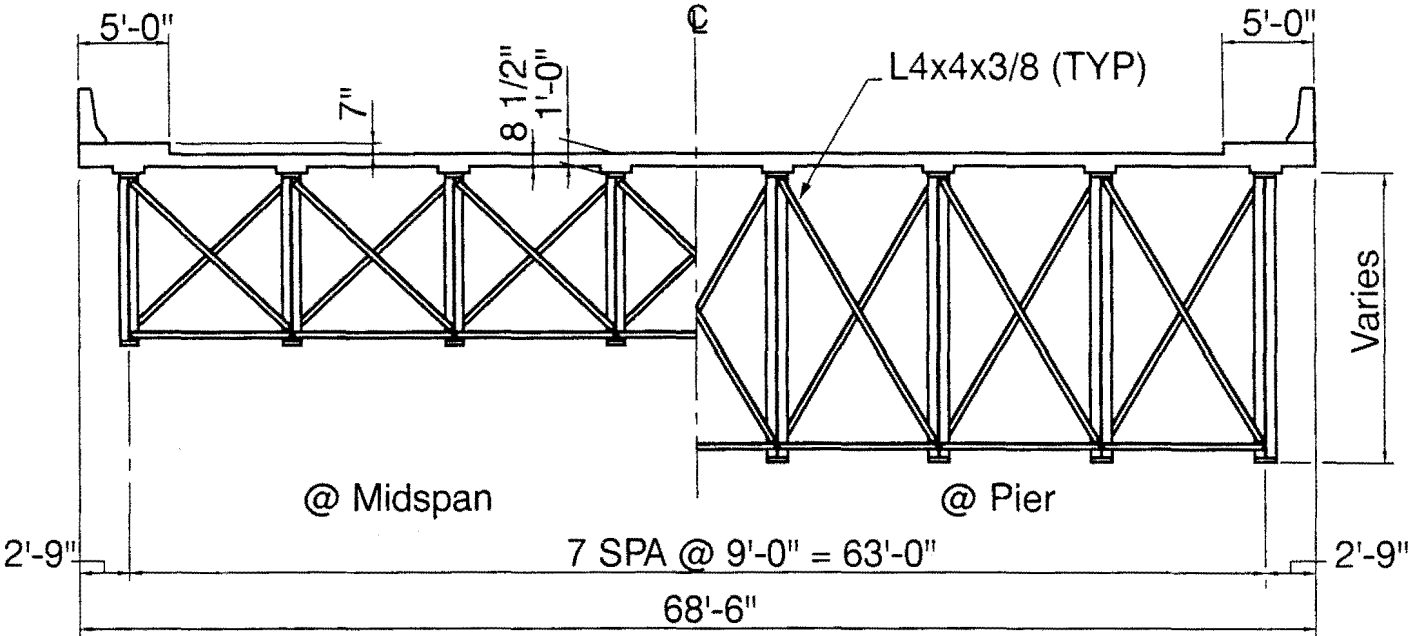
**Pier Elevation**

**End Elevation**

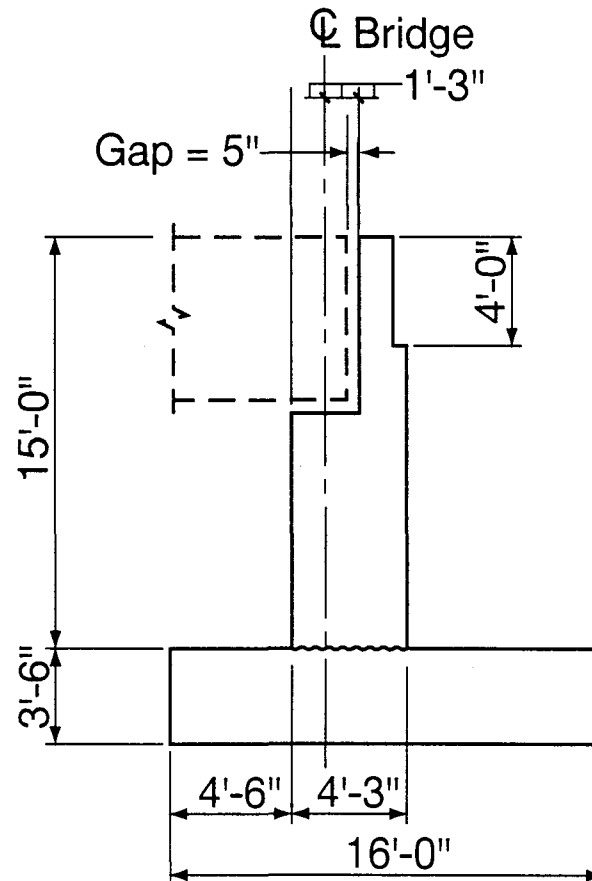
# Steel Plate Girder Bridge / Girder Elevation



# Steel Plate Girder Bridge / Superstructure Section



# Steel Plate Girder Bridge / Abutment Section



# **Session 3**

## **Required / Practice Problem No. 2**

---

- **Calculate Longitudinal Period**
- **Calculate Elastic Longitudinal Shear, Moment, and Displacement of Pier No. 1**
- **Design Pier No. 1 Reinforcement**
- **Size Footing**
- **Consider Alternatives**

# Basic Data for Bridge

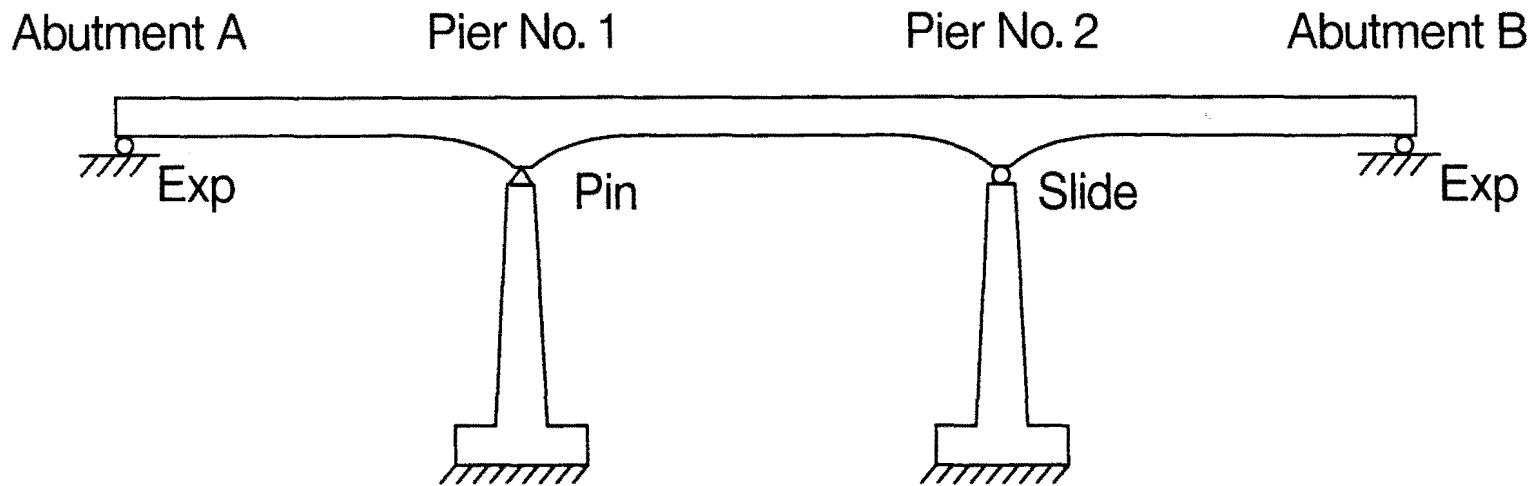
---

- Acceleration Coefficient,  $A = 0.15g$
- Seismic Performance Category,  $SPC = B$
- Soil — Rock
  - $S = 1.0$
  - $f_{ult} = 50 \text{ ksf}$  Ultimate Bearing Capacity

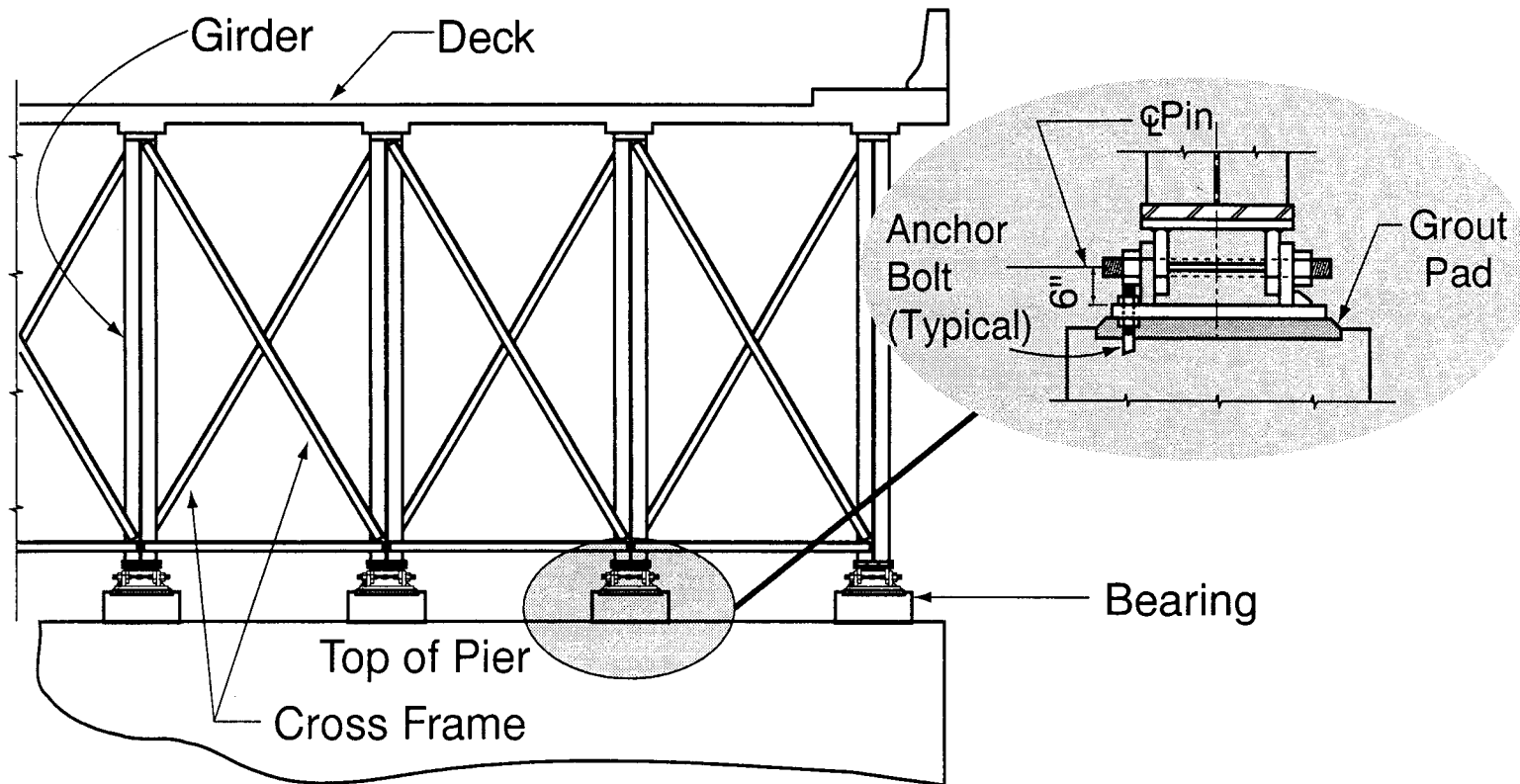


# Bearing Conditions – Longitudinal

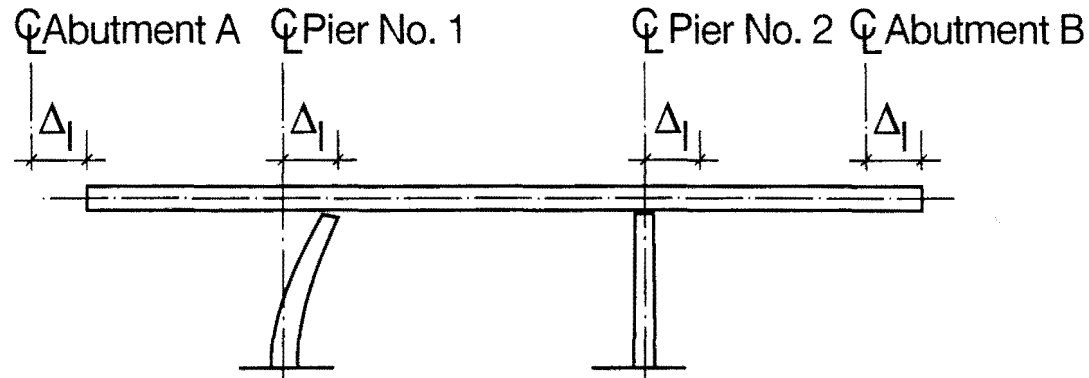
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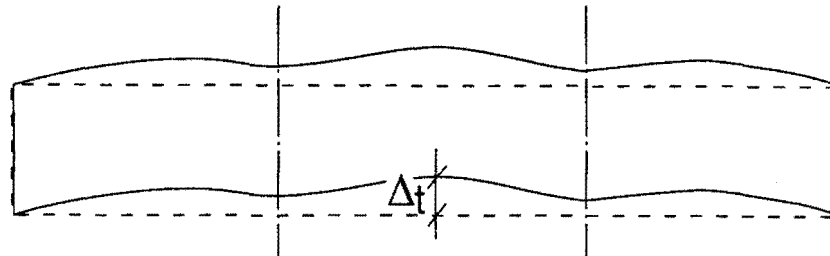
# Bearing Conditions – Transverse



# Expected Lateral Seismic Behavior

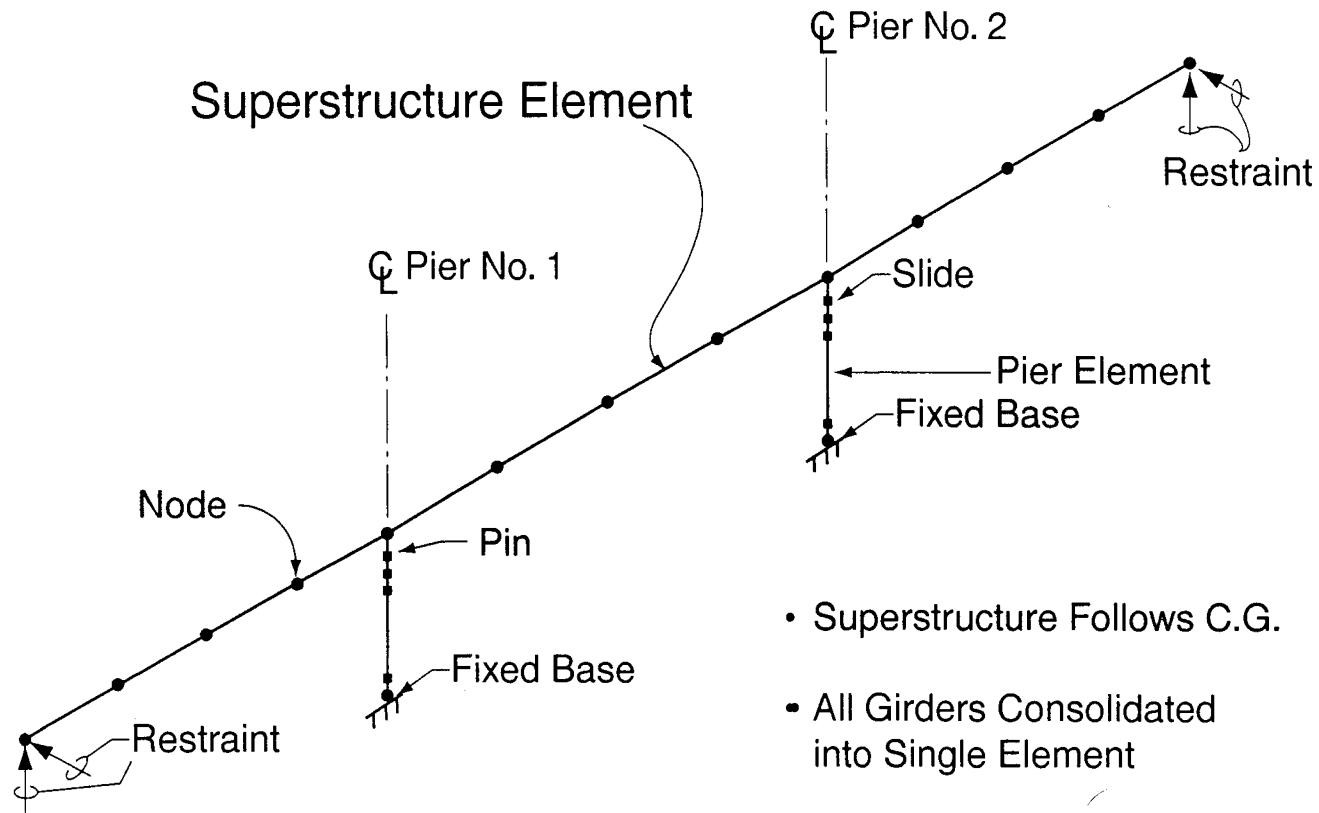


**Longitudinal Behavior — One Column Resists Loads**



**Transverse Behavior — Piers and Abutments Resist Loads**

# Seismic Analysis Model



# Superstructure Properties

Location	Area A (ft <sup>2</sup> )	Effective Density $\gamma^a$ (k/ft <sup>3</sup> )	Moment of Inertia		
			Bending in Horiz. Plane	Bending in Vert. Plane	
			I horiz <sup>b</sup> (ft <sup>4</sup> )	y bar <sup>c</sup> (ft)	I vert <sup>b</sup> (ft <sup>4</sup> )
Abutment	81.0	0.166	36207	1.377	296
End Span 1/4 Pt	81.0	0.166	36207	1.377	296
1/2 Pt	81.0	0.166	36353	1.407	311
3/4 Pt	84.3	0.162	36607	1.698	473
Pier	104.0	0.143	45988	2.477	996
Center Span 1/4 Pt	83.4	0.163	37206	1.603	417
1/2 Pt	81.0	0.166	36207	1.377	296

- a. Includes Weight of Barriers, Overlay, Forms, Stiffeners, and Cross Frames
- b. I Based on Full Composite Action of Deck and Girders
- c. 'y bar' Is Measured from the Top of the 9 in. Deck

# Superstructure Specifics

---

- Properties Based on Equivalent Concrete

- Weights Include

Concrete  $w_C = 8.16$  kip/ft

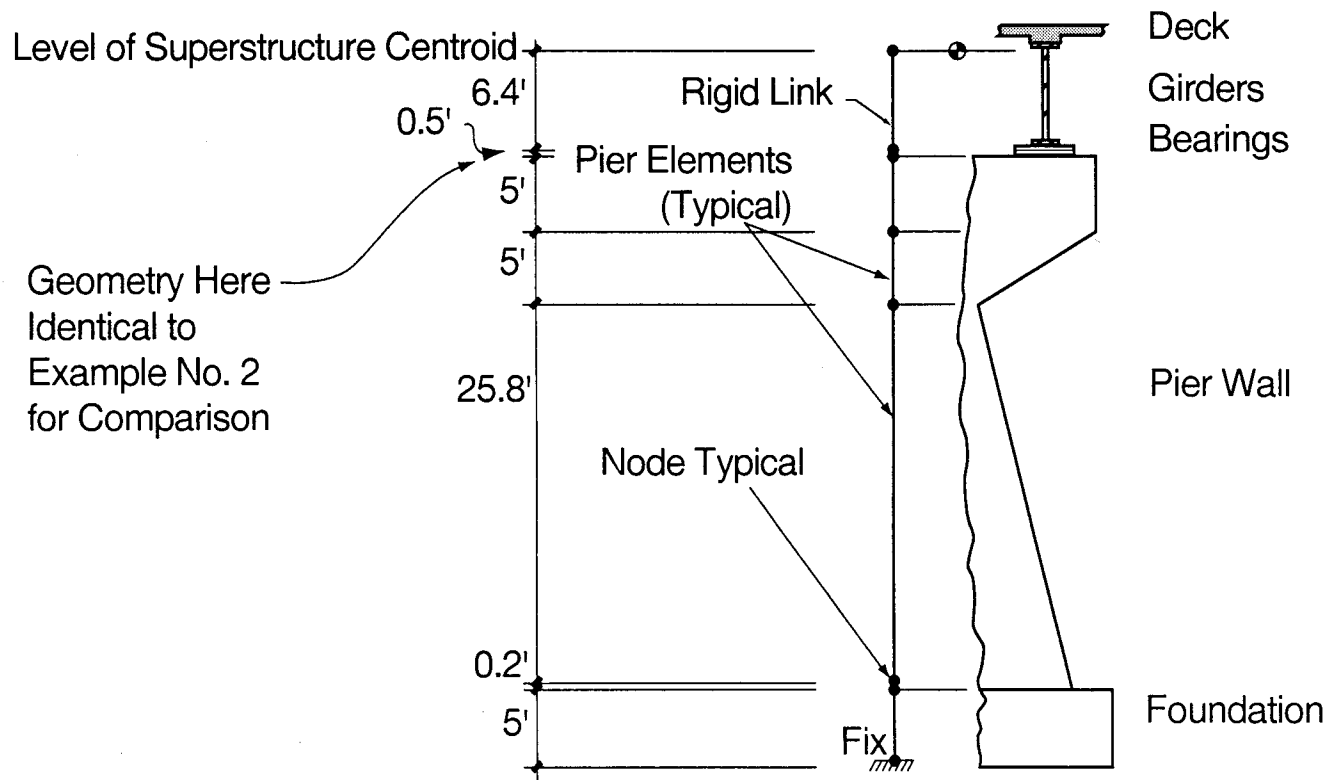
Girders  $w_g = 3.04$  kip/ft to 1.63 kip/ft

Barrier Overlay, Stay-in-Place Forms, Allowance  
for Cross Frames and Stiffeners

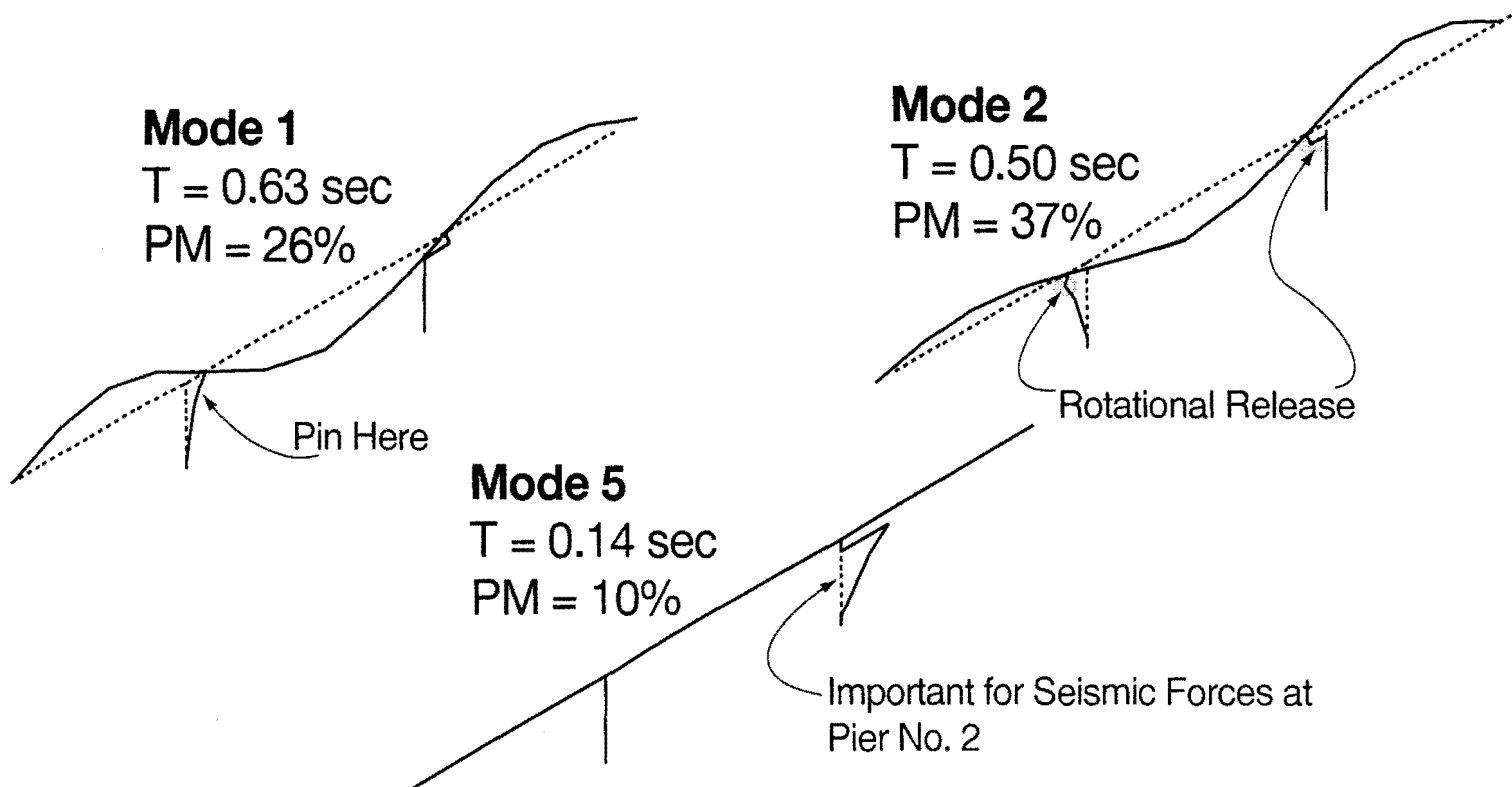
$w_m = 3.69$  kip/ft

- Full Composite Action Assumed

# Pier Geometry



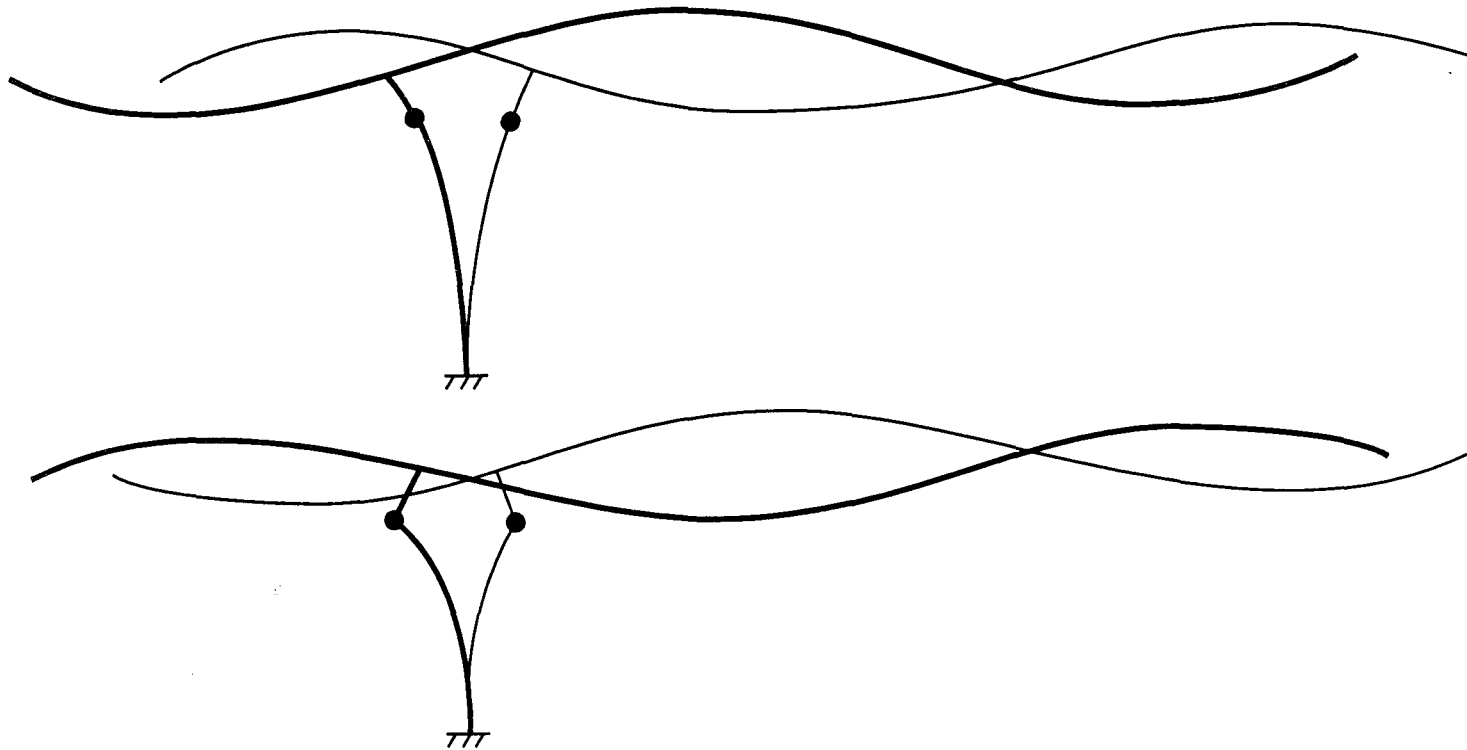
# Longitudinal Mode Shapes



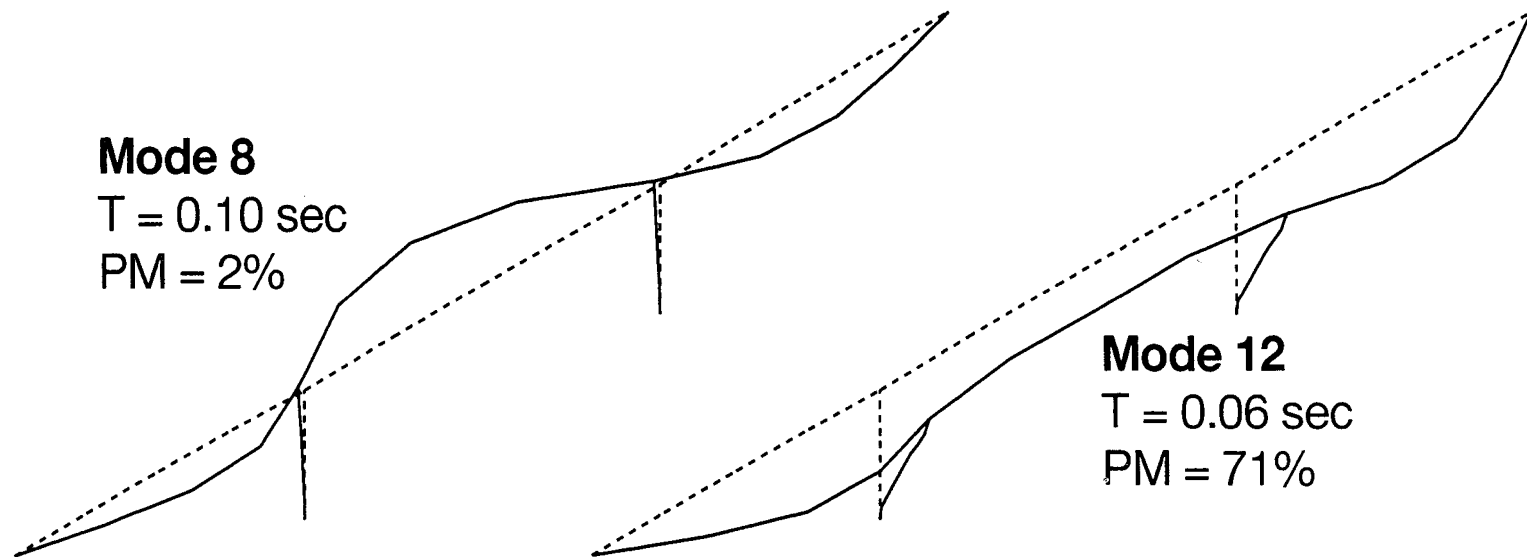


# Reasons for Two Longitudinal Modes

---

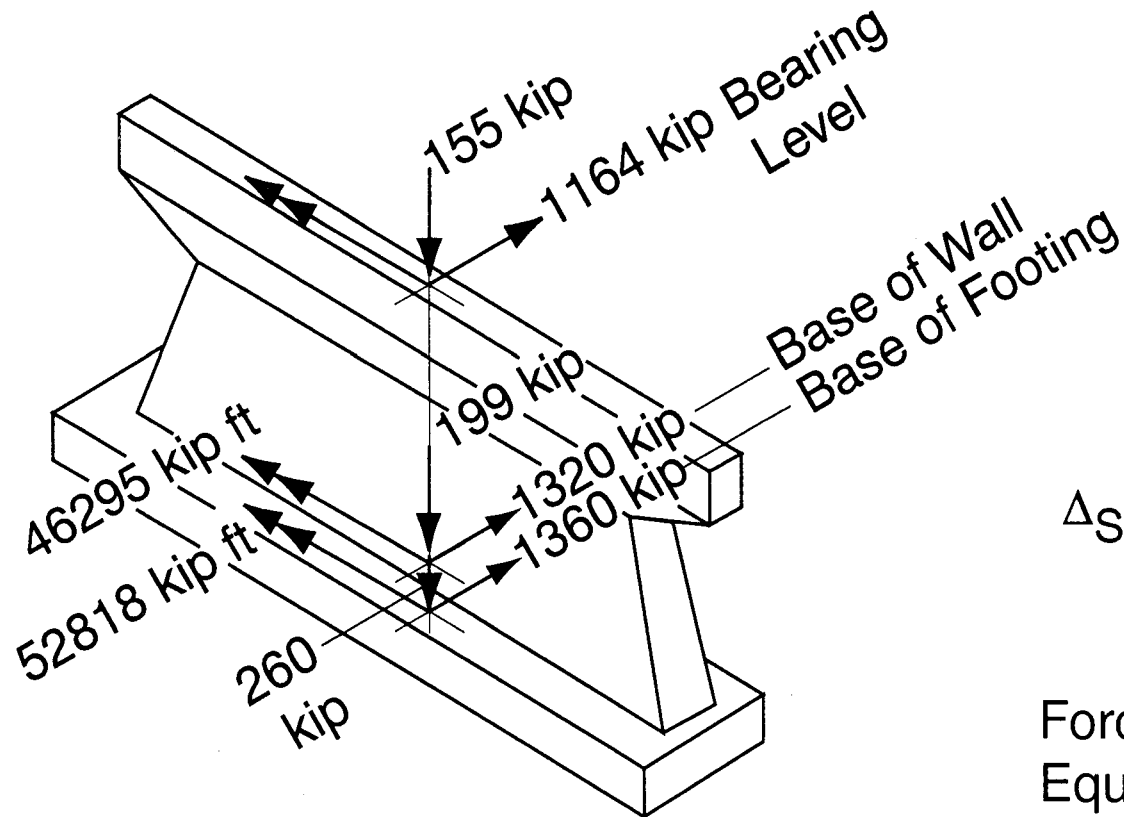


# Transverse Mode Shapes



(Recall 3 • No. of Spans = 9)

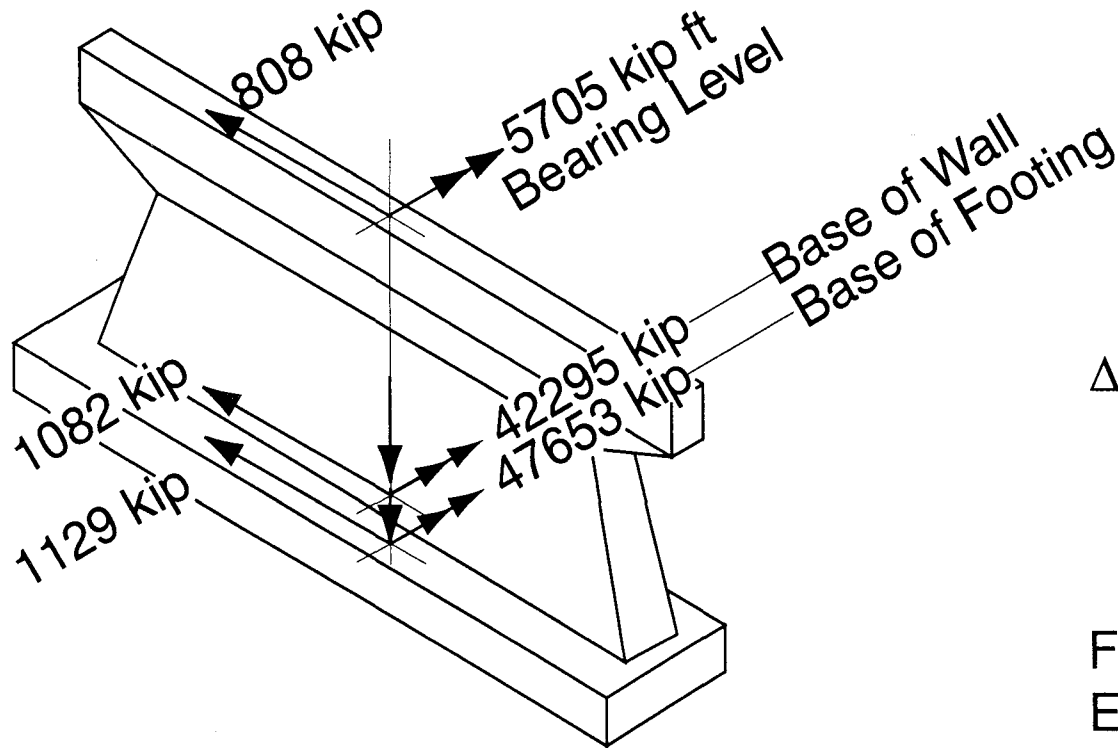
# Longitudinal Modal Analysis Results



$$\Delta_{\text{Super}} = 0.61 \text{ in.}$$

Forces Not Shown  
Equal Zero

# Transverse Modal Analysis Results

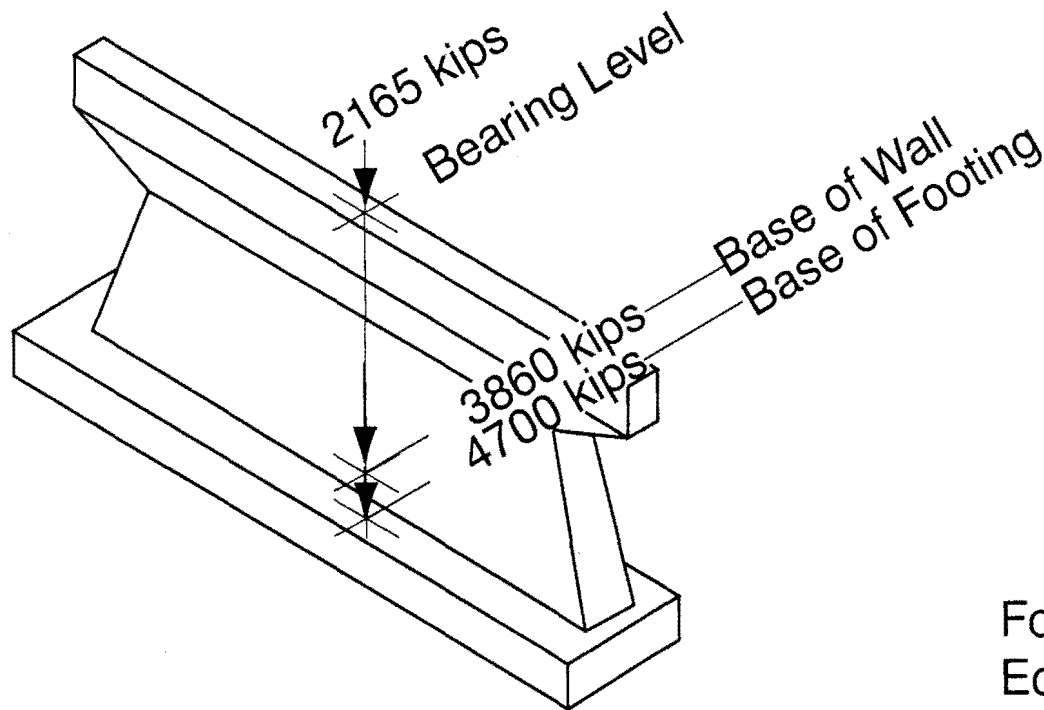


$$\Delta_{\text{Super}} = 0.014 \text{ in.}$$

Forces Not Shown  
Equal Zero

# Dead Load Analysis Results / Spine Model

---



Forces Not Shown  
Equal Zero

# Check of Results / Hand and Computer

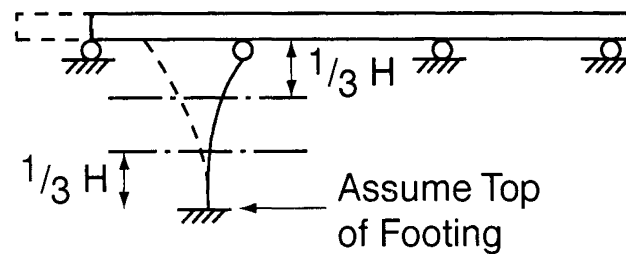
---

**Strategy:** • Compare Period and Base Shear

**Use:**

- Hand Model with Rigid Superstructure
- Computer Model with Rigid Superstructure  
(Only Change from Previous Modal Analysis)

# Hand Check



- **Seismic Weight**

$$W_{\text{super}} = 5525 \text{ kip}$$

$$W_{1/3} = 517 \text{ kip}$$

---


$$W_{\text{total}} = 6041 \text{ kip}$$

- **Stiffness**

Use Stiffness at  $1/3$  of Height of Tapered Wall Above the Footing

$$K = \frac{3(519000)764}{(36)^3} = 25508 \text{ kip/ft}$$

$B = 60.46 \text{ ft} \quad T = 5.333 \text{ ft}$

## Hand Check (continued)

---

• **Period** 
$$T_{\text{Long}} = 2 \pi \sqrt{\frac{W}{g K}} = 2 \pi \sqrt{\frac{6041}{32.2 (25508)}}$$

$$T_{\text{Long}} = 0.54 \text{ sec} \quad \text{Bracketed by Mode 1 and 2 Periods}$$

• **Base Shear** 
$$V_{\text{Long}} = C_s W = \frac{1.2(0.15)1.0}{(0.54)^{2/3}} (6041)$$

$$V_{\text{Long}} = (0.272)(6041) = 1642 \text{ kips}$$



# Computer Model with 'Rigid' Superstructure

---

Let:

$$I_{\text{super}} \rightsquigarrow 10^7 \cdot I_{\text{super}} \rightsquigarrow T_{\text{long}} = 0.53 \text{ sec}$$

Then:

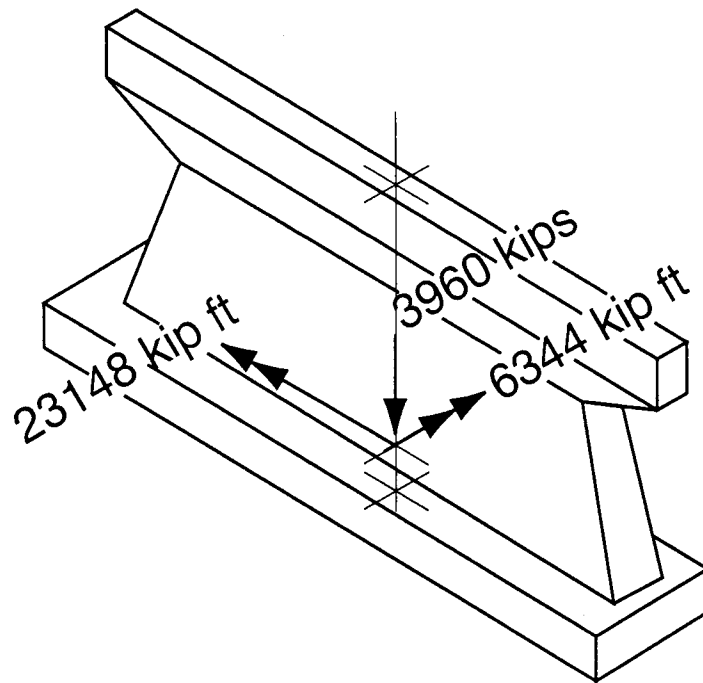
$$V_{\text{long}} = 1776 \text{ kip}$$

# Comparison of Results and Checks

---

- **Basic Model**                       $V = 1320$  kip at Base of Wall
- **Hand Check**                       $V = 1642$  kip ... Higher Due to Single  
Mode Contributing All  
Response
- **Rigid Superstructure  
Computer Model**       $V = 1776$  kip ... Higher Than Hand Check  
Due to Contribution of  
Lower Part of Pier  
(~ 90 kip)

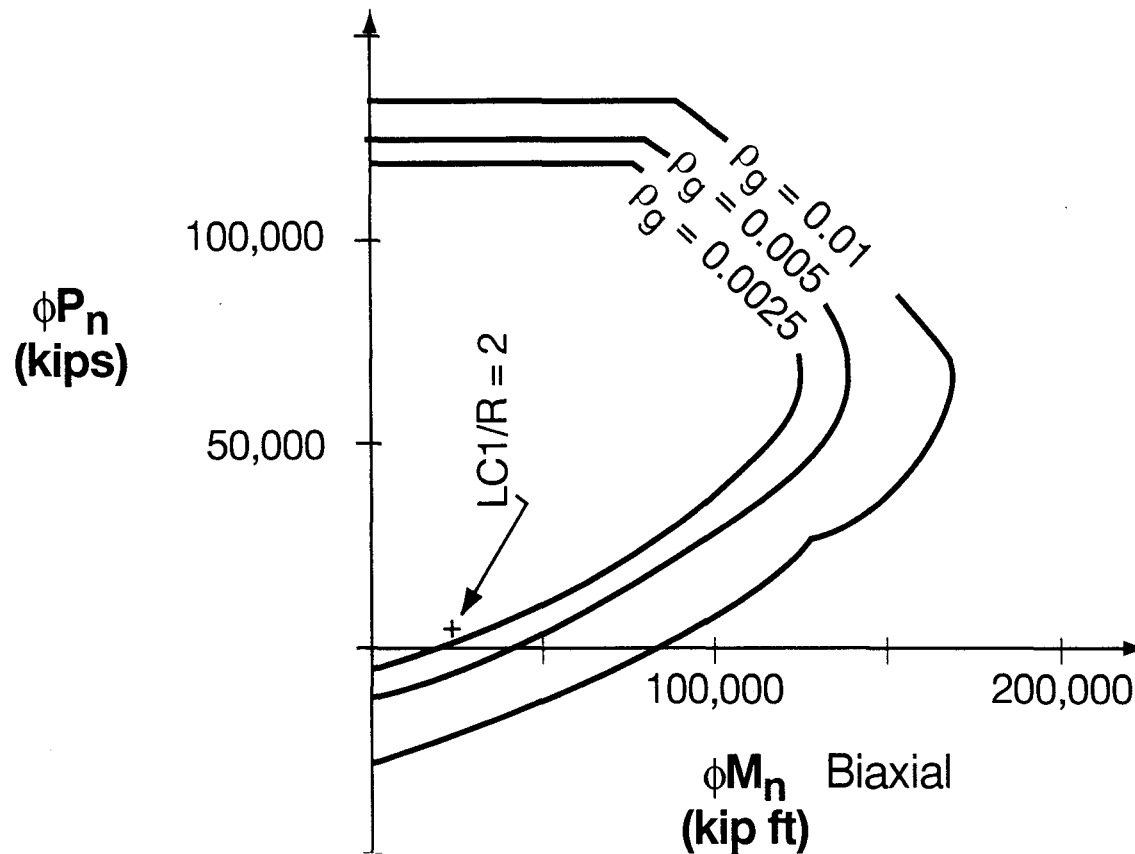
# Design Forces at Base of Wall



R = 2 Weak

R = 2 Strong

# Vertical Reinforcement Options



# Minimum Vertical Steel Considerations

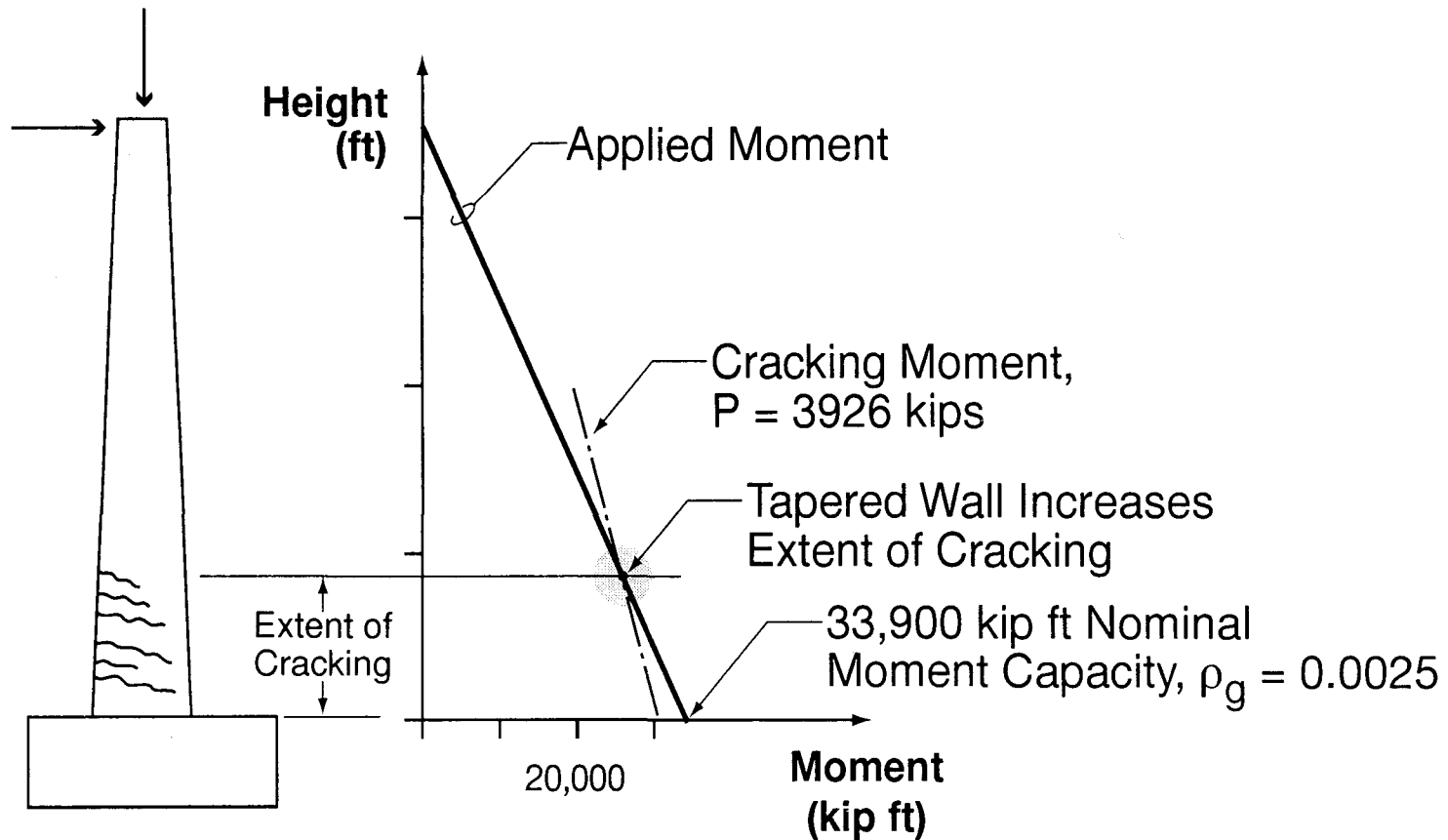
---

- a) Wall —  $\rho_g \geq 0.0025$  SPC C & D Div. I-A. 7.6.3  
b)  $\phi M_n \geq 1.2 M_{crack}$  (Flexural Members) Div. I 8.17.1.1

## This Wall:

- $\rho_g = 0.0025$  Can Satisfy a) Since  $R = 2$
- Consider b) for Crack Distribution

# Distribution of Cracking



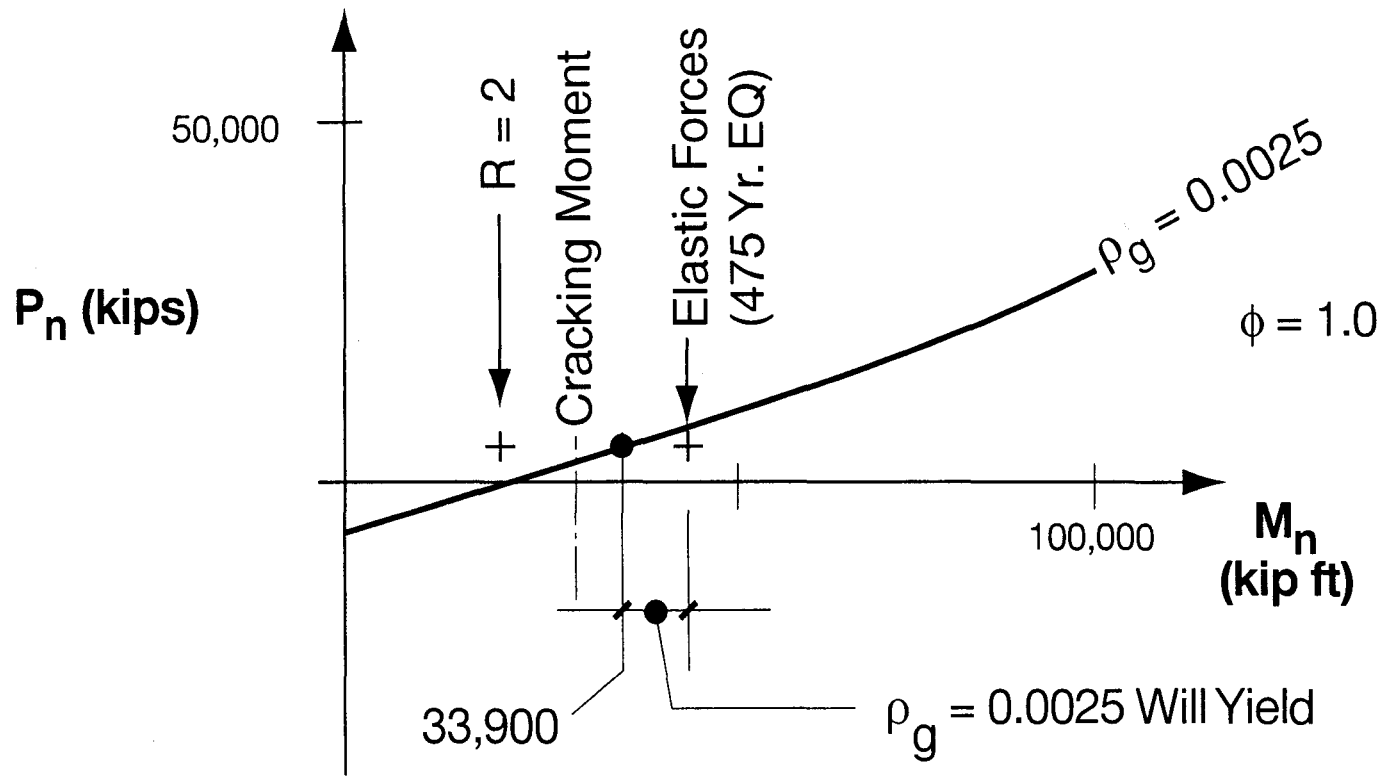
# Selection of Vertical Reinforcement

---

Use  $\rho_g = 0.0025$   $\rightsquigarrow$  142 #9 Bars

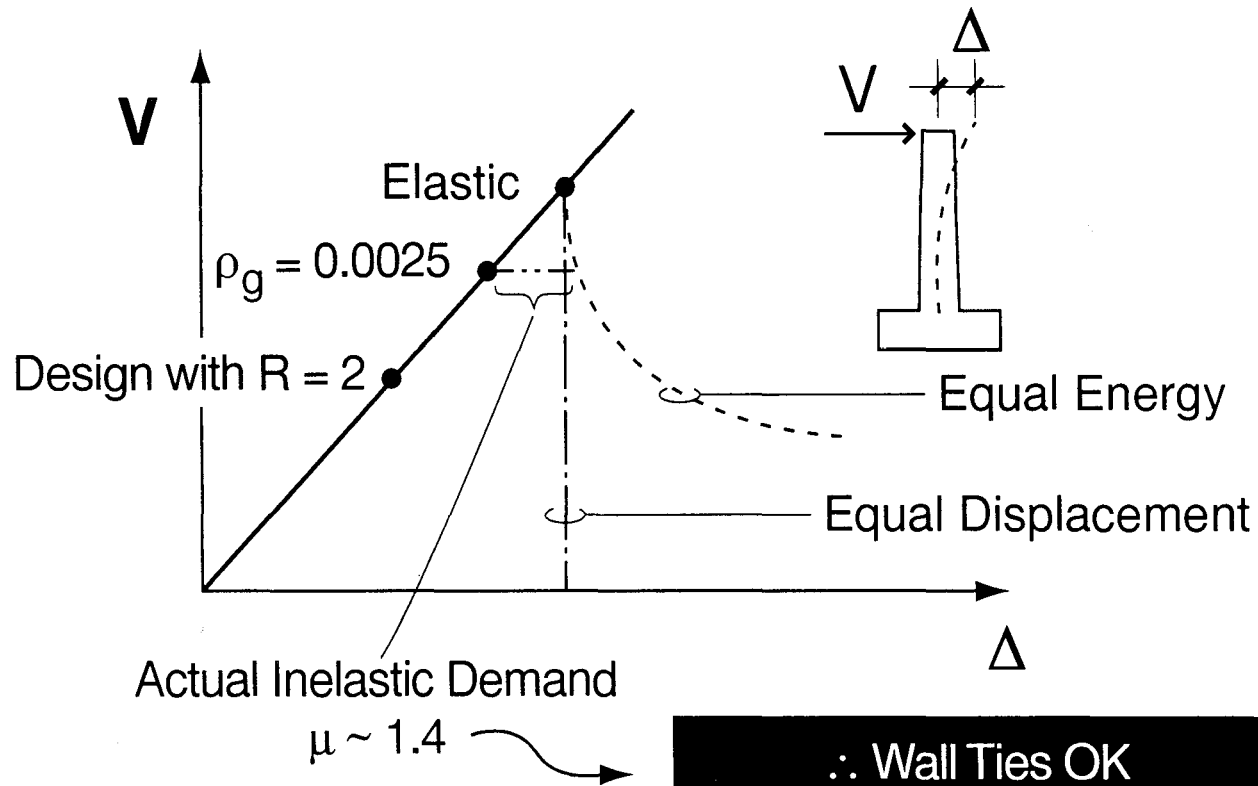
- This Will Work for  $R = 2$
- Wall Is Expected to Yield During 475 Year Earthquake, but Ductility Demand Will Be Low ( $M_{elas} \sim 1.2 M_n$ )
- Even Though  $M_n \sim 1.10 M_{cr}$ , Cracking Will Be Distributed Due to Wall Taper

# Nominal Capacity of Wall in Weak Direction





# Expected Inelastic Demands



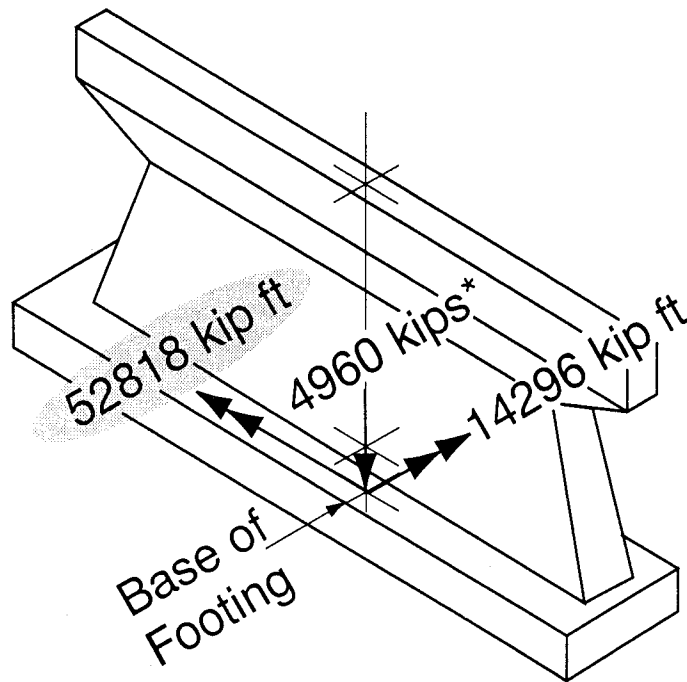
# Wall Cross Ties

---

Weak Direction / Designed as a Column /  $R = 2$

Use #4 at 2 ft O.C. Horizontal and 8 in. Vertical  
See Design Example No. 2

# Foundation Design Forces / Controlling Case LC1



$$R = \frac{2}{2} \text{ Weak}$$

$$R = \frac{2}{2} \text{ Strong}$$

\*Does Not Include  
Buoyancy and Stone Fill

# Foundation Behavior / 33' Footing

## Results for:

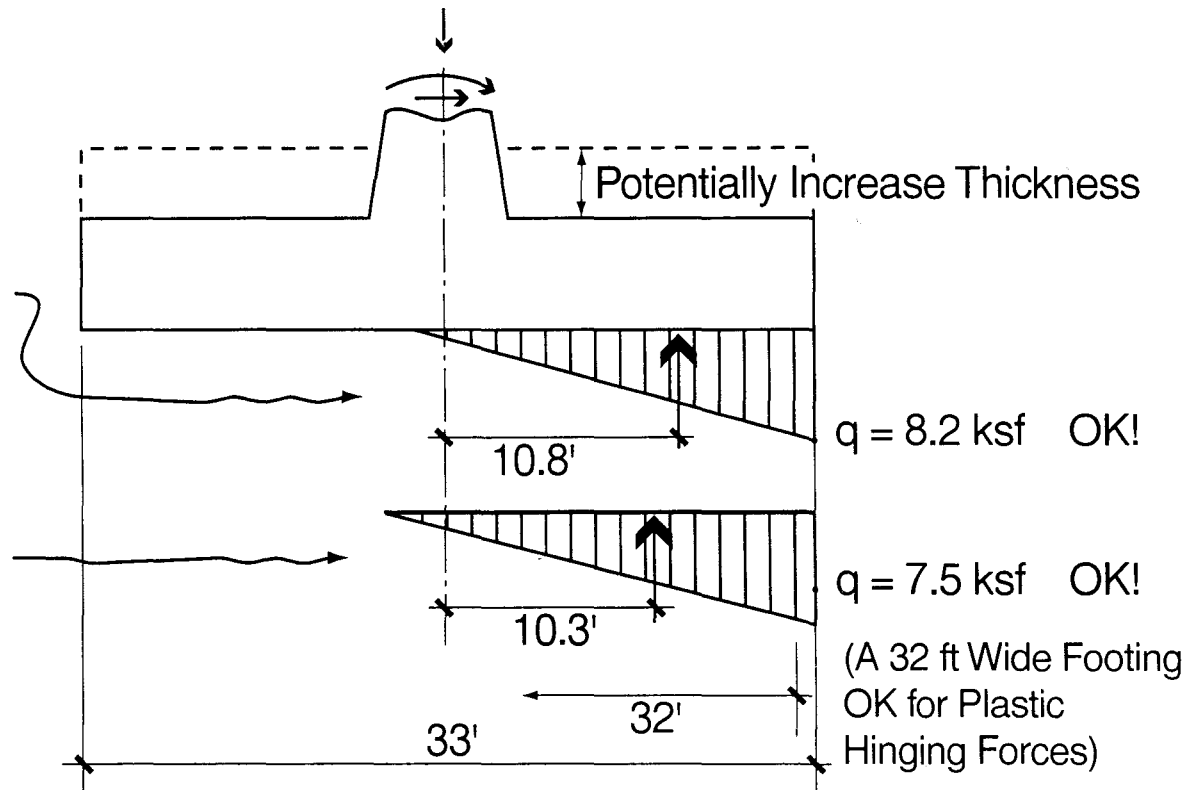
- Design Forces

$$R = \frac{2}{2}$$

(Elastic)

- Plastic Hinging Forces

$$\rho_g = 0.0025$$



# Choices and Implications / Flexural Design

---

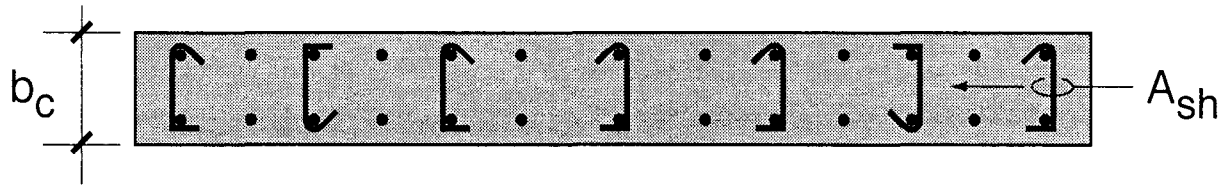
## SPC B Weak Direction

	R = 2 (Wall)	R = 3 (Column) 1% Vertical Steel
Wall:	Less Vertical Steel ( $\rho_g = 0.0025$ )	More Cross Ties in Hinge Zone
Foundation:	Larger Footing	Smaller Footing

# Cross Ties

Weak Direction / Designed as a Column / R = 3

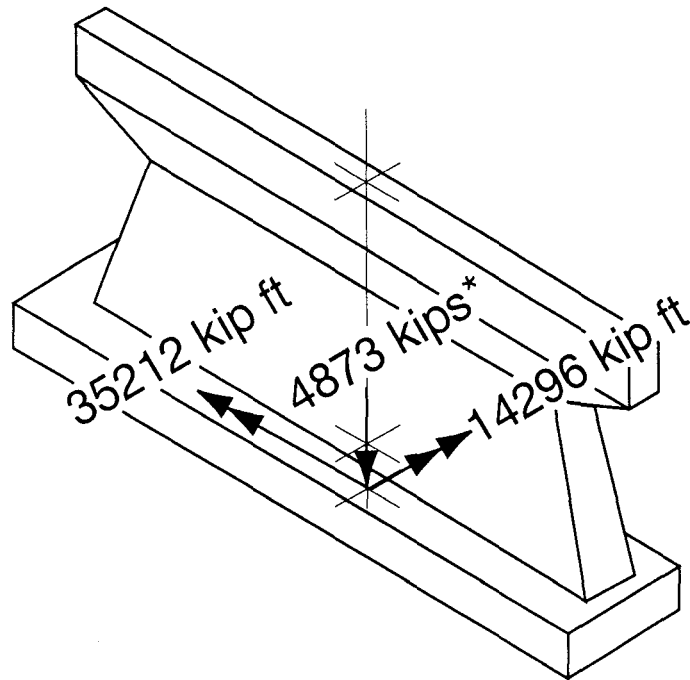
$$I-A / 6.6.2 \quad A_{sh} = 0.3ah_c \left[ \frac{A_g}{A_{core}} - 1 \right] \geq 0.12ah_c \frac{f'_c}{f_{yh}}$$



Try #7 → 63 Required / Use 67 #7 Cross Ties, One for Each Vertical, at 6 in. Vertical Spacing

Cross Ties Required Over Lower 6 ft ~ Plastic Hinge Zone

# Foundation Design Forces



Design as a Column

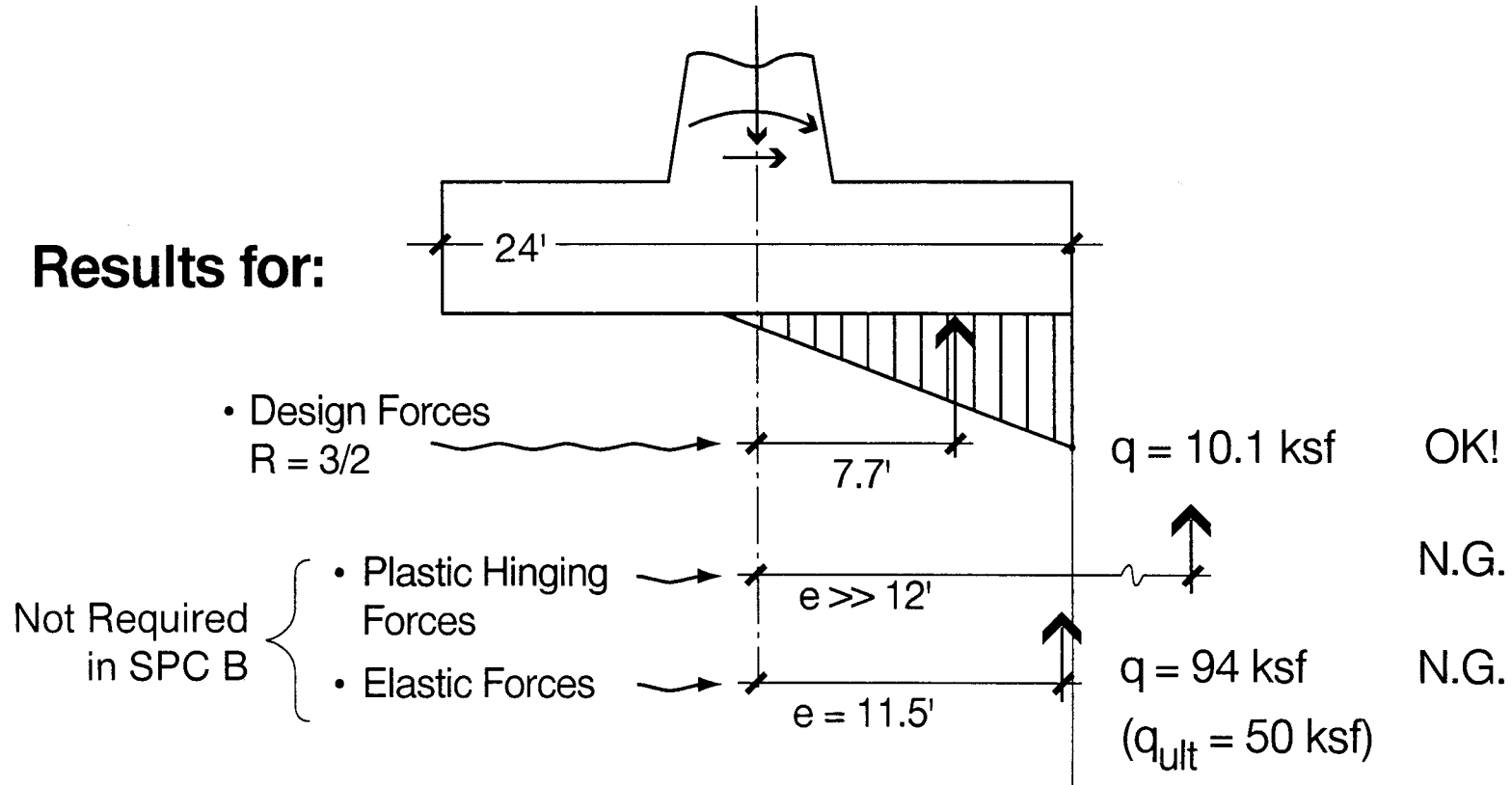
$R = \frac{3}{2}$  Weak

$R = 1$  Strong

\*Does Not Include  
Buoyancy and Stone Fill

# Foundation Behavior / 24' Footing

Results for:





# Summary

---

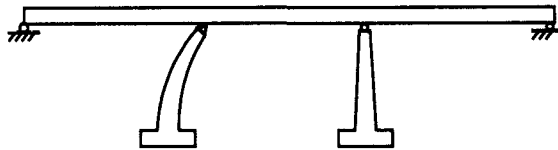
	Designed As:	
	Wall	Column
Vertical Reinforcement .....	10 Tons	40 Tons ( $\rho_g = 0.01$ )
Cross Ties .....	0.6 Tons	4.6 Tons
Footing Width.....	33 ft	24 ft*

\* Permitted by Code for SPC B, But if Designed for Elastic or Hinging Forces 33 ft Would Be Required

# Choices and Implications

---

## 1. Use 33 ft Footing ... Design as a Wall

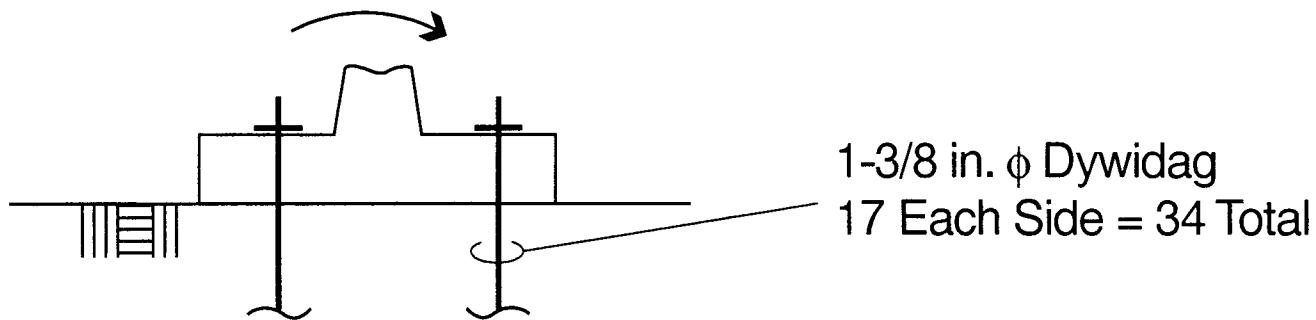


- Best Solution for Single Conventional Bearing Configuration
- No Foundation Damage

# Alternative

---

2. Use 16 ft Footing ... Use Rock Anchors to Prevent Overturning



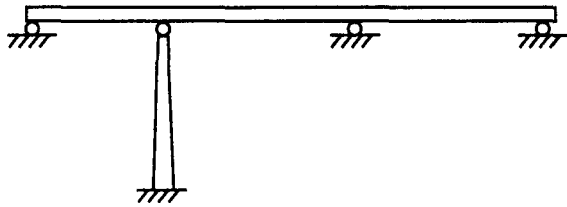
# **Session 3**

## **Conceptual Design Considerations**

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- **Conventional vs. Elastomeric Bearings**
- **Longitudinal Releases and Restraints**

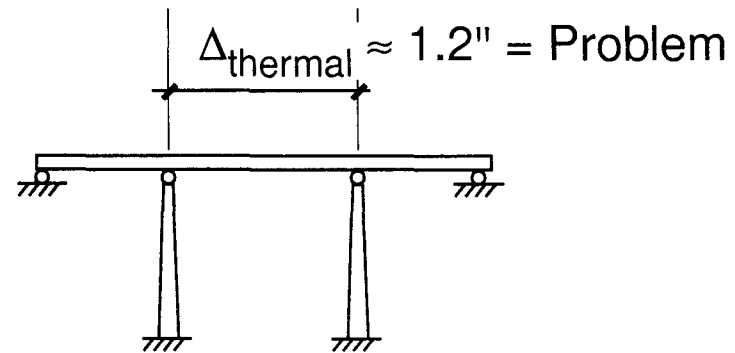
# Conventional Bearings



$$T = 0.52 \text{ sec}$$

$$\Delta = 0.74 \text{ in.}$$

**One Restraint**



$$T = \frac{0.52}{\sqrt{2}} = 0.37 \text{ sec}$$

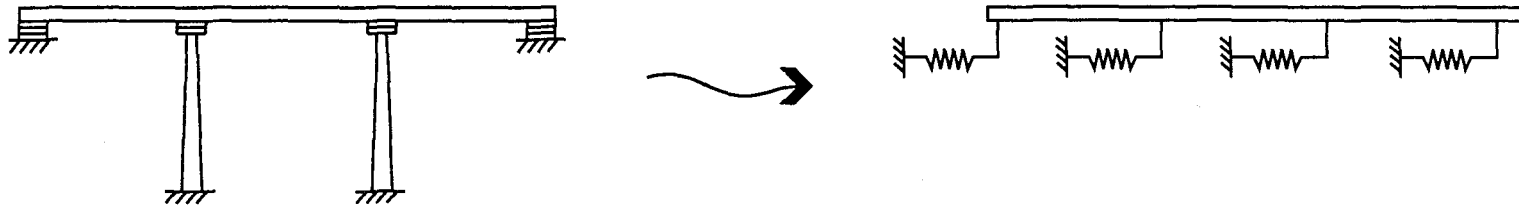
$$\Delta = 0.74 \text{ in.} \left( \frac{1}{\left(\frac{1}{\sqrt{2}}\right)^{2/3}} \right) \frac{1}{2} = 0.47 \text{ in.}$$

No. of Piers

**Two Restraints**

# Elastomeric Pads at Each Support

---

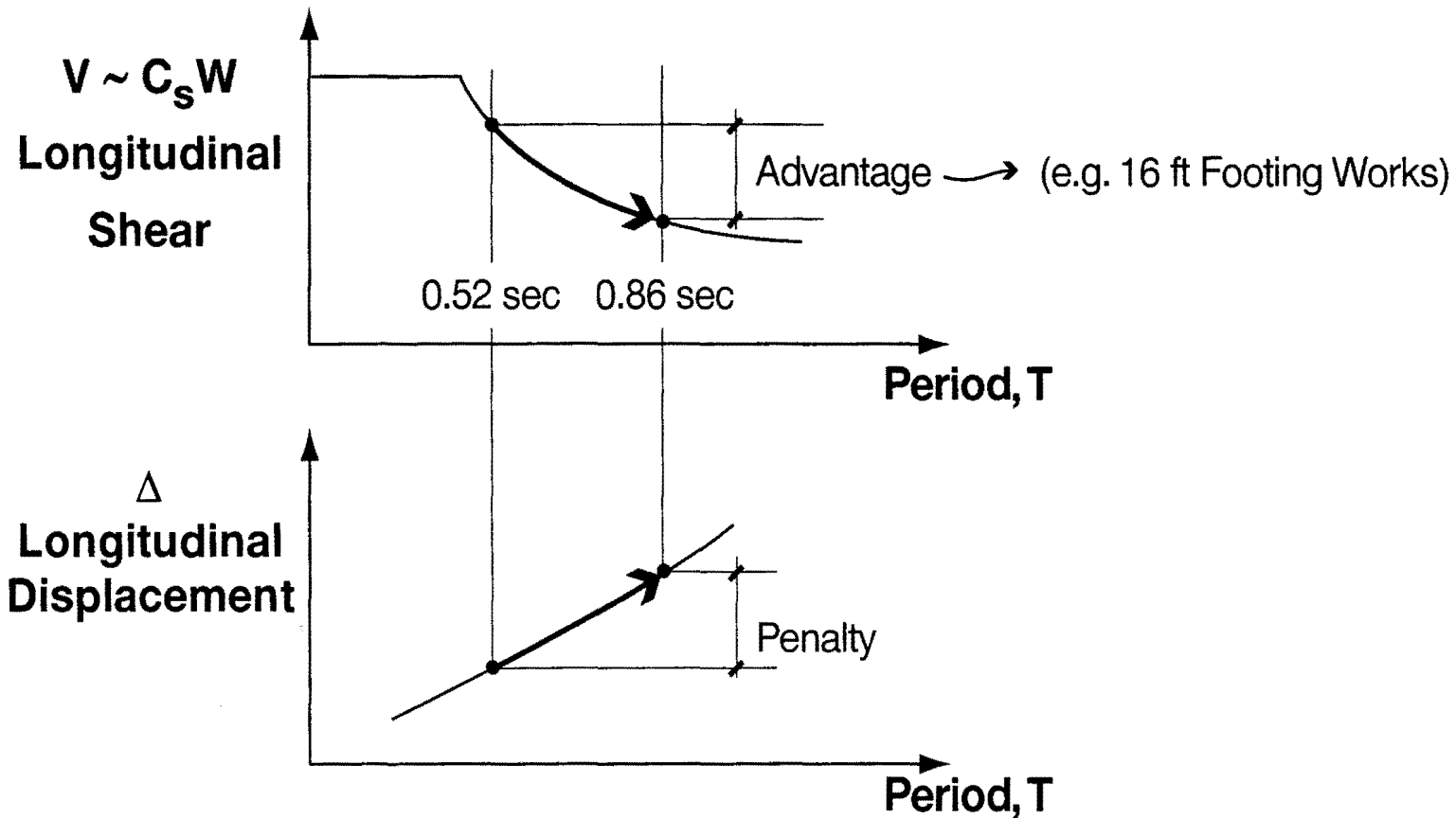


Incorporate  
Flexibility of  
Elastomeric Pads

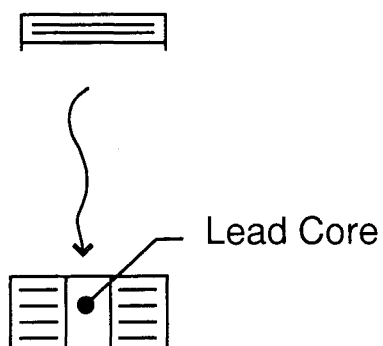
$T \rightarrow 0.86 \text{ sec}$

$\Delta \rightarrow 1.44 \text{ in.}$

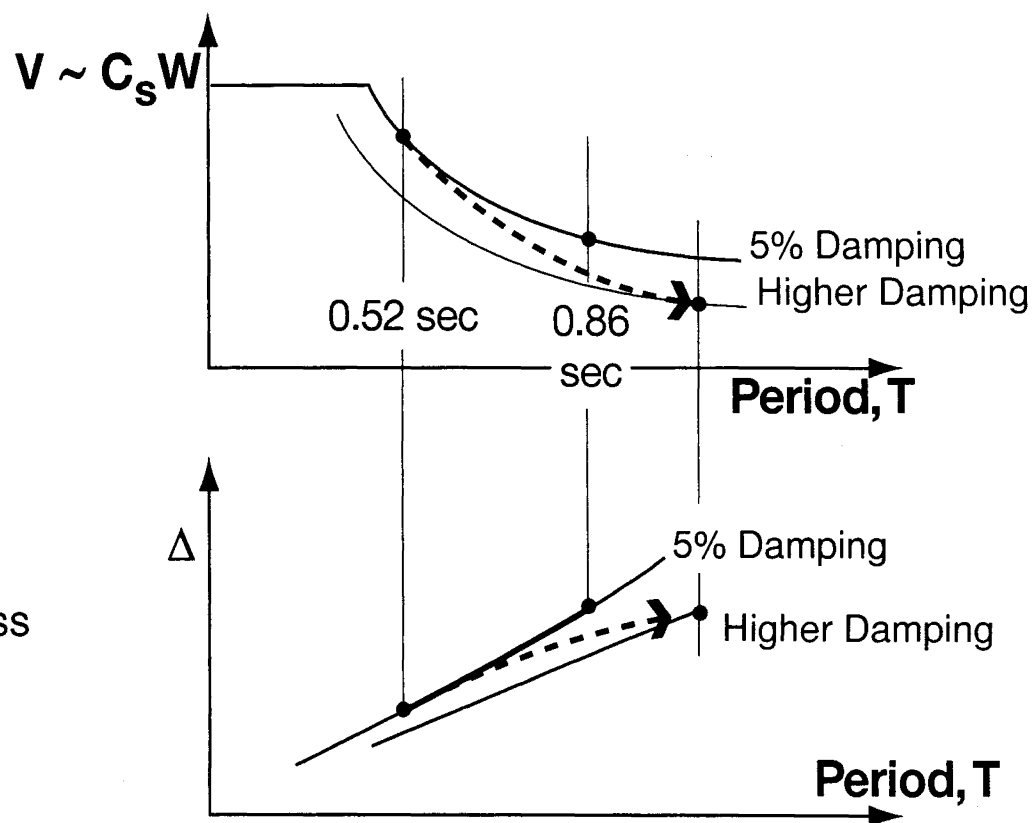
# How the Elastomeric Pads Affect the System



# How a 'Base Isolated' Concept Would Affect System



- **Lead Core**  
Damping  
Low Amplitude Stiffness
- **Increased Height**  
Added Flexibility





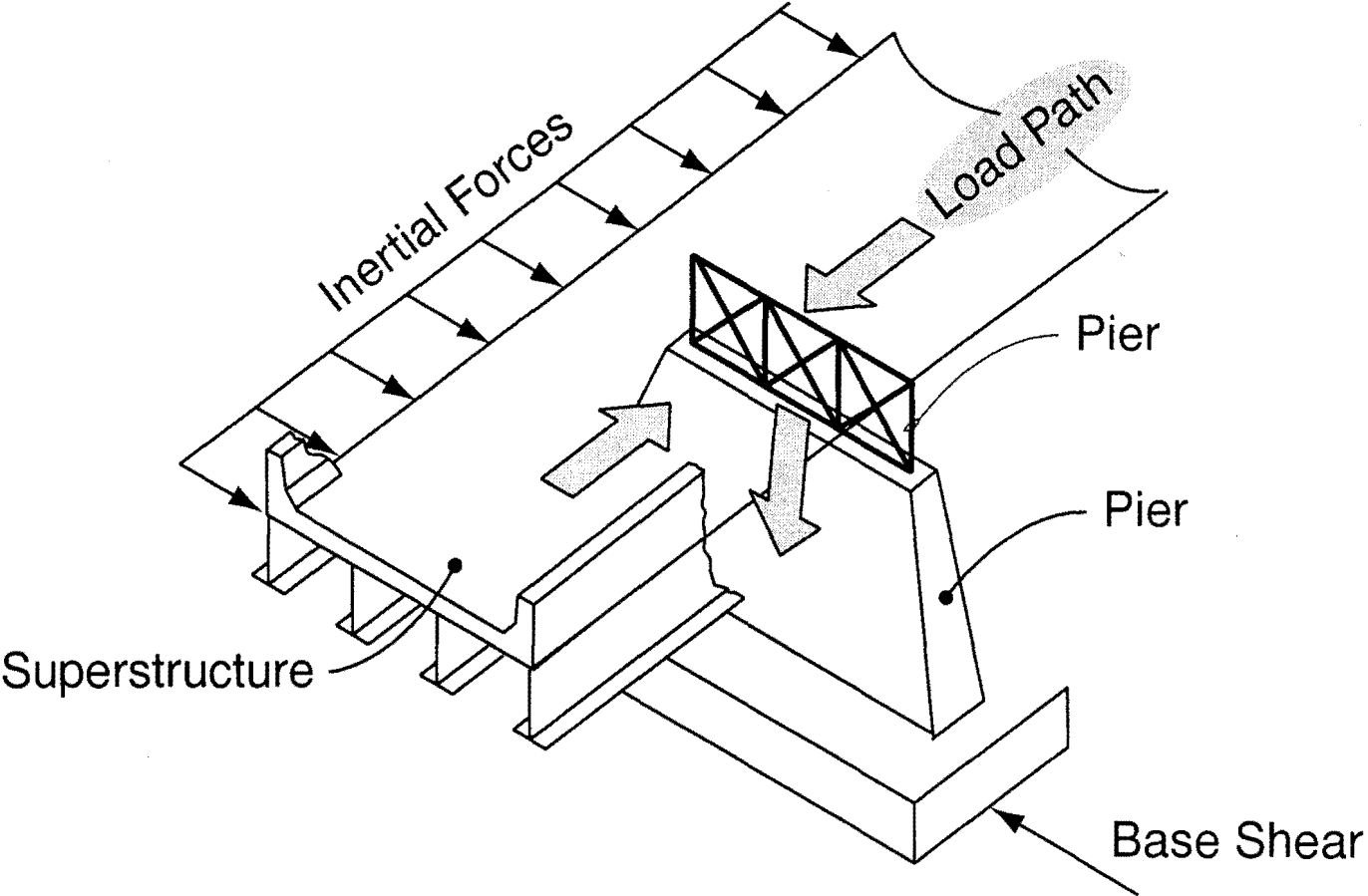
# **Session 3**

## **Steel Superstructure Issues**

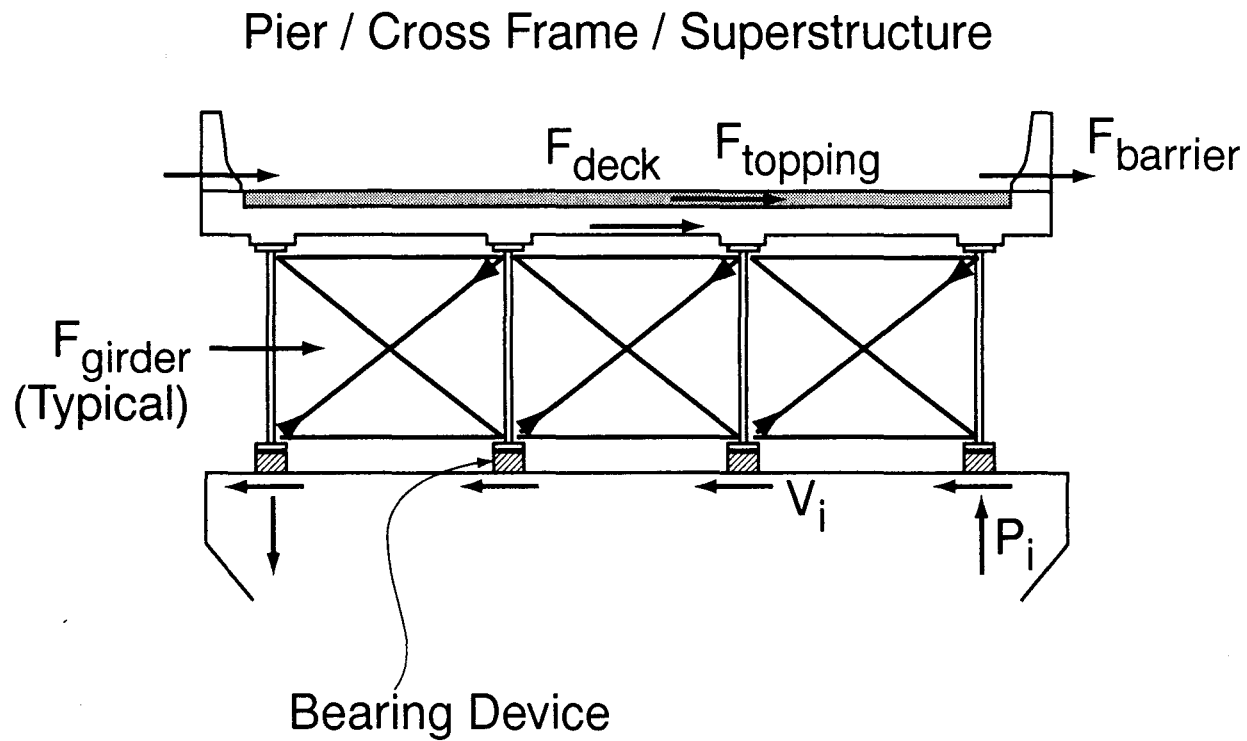
---

- **Cross Frame Design**
- **Shear Key Considerations**

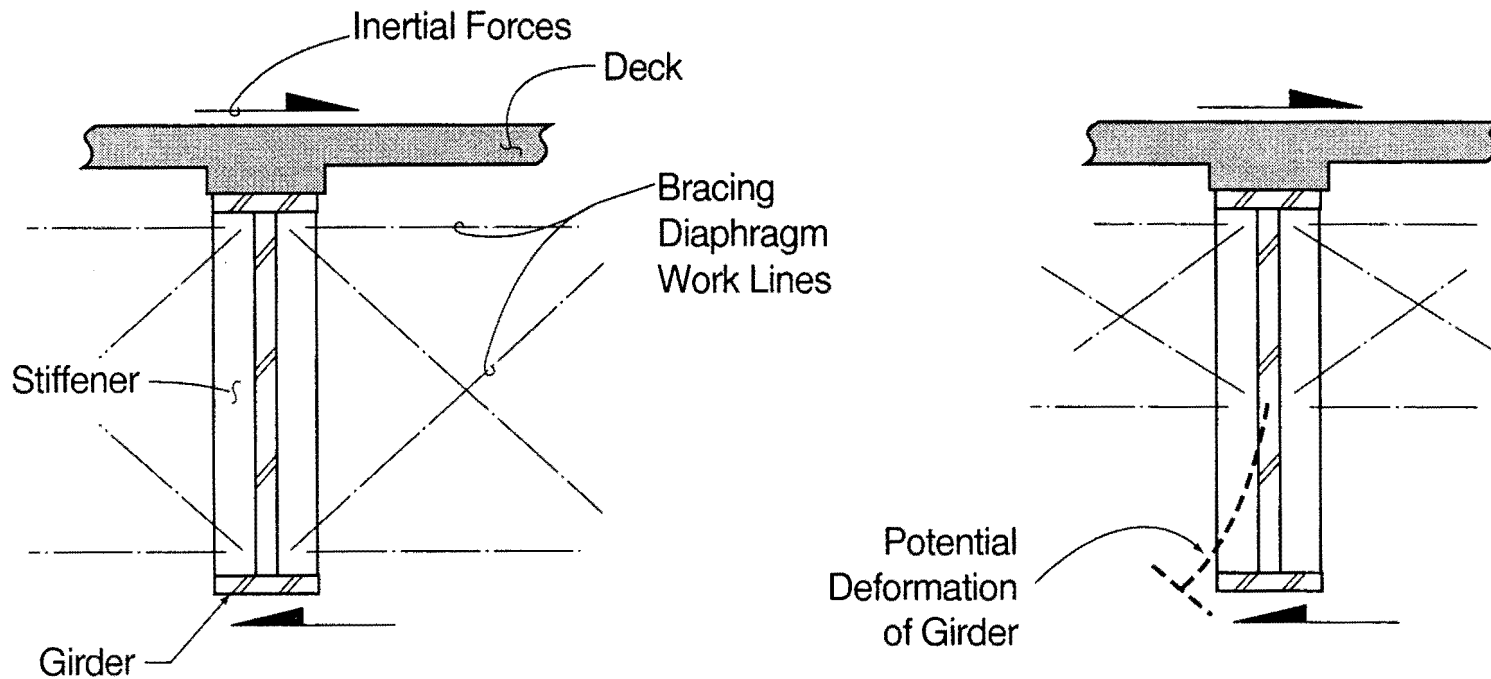
# Inertial Forces and Lateral Load Path



# Cross Frame Forces



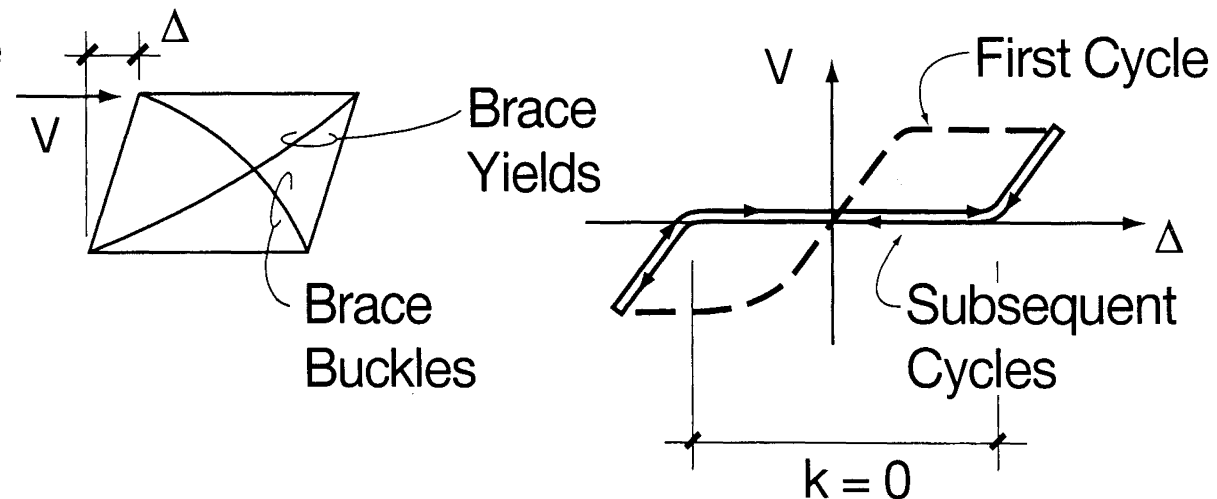
# Failure Mode / Lateral Bending



Lateral Rigidity vs. Service Load (Fatigue) Performance

# Failure Mode / Tensile Yielding

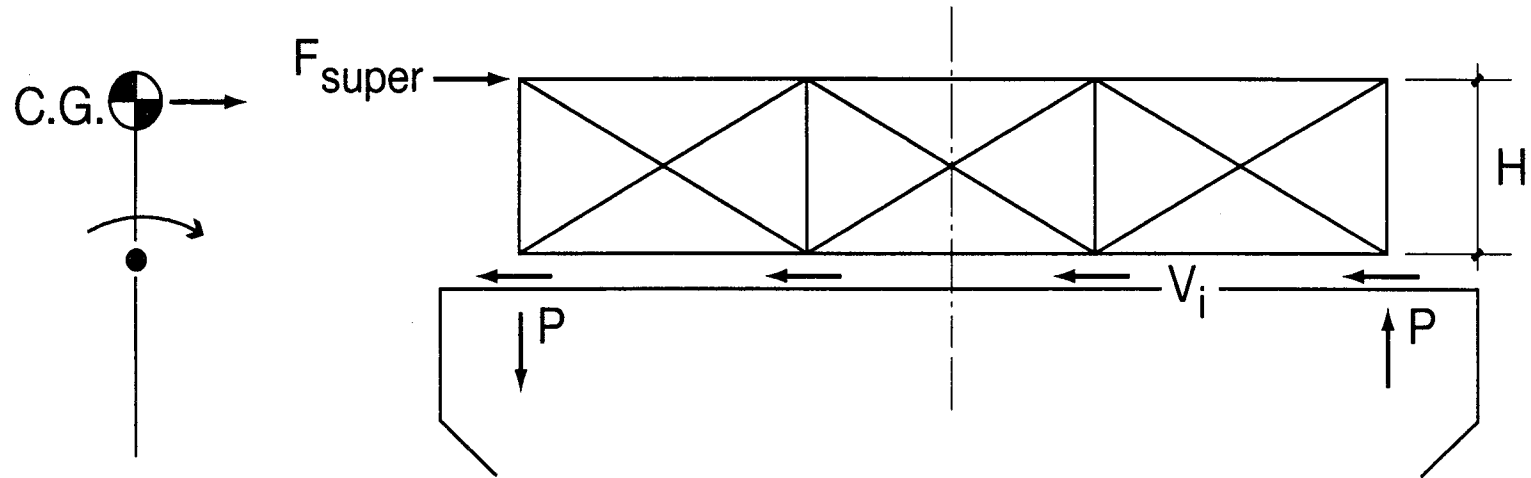
Problem with  
Cross Frame  
Yielding



Code Specifies  $R = 1.0$  to Prevent Yielding

- Preserves Elastic (Tight) Response
- Preserves Lateral and Gravity Load Paths

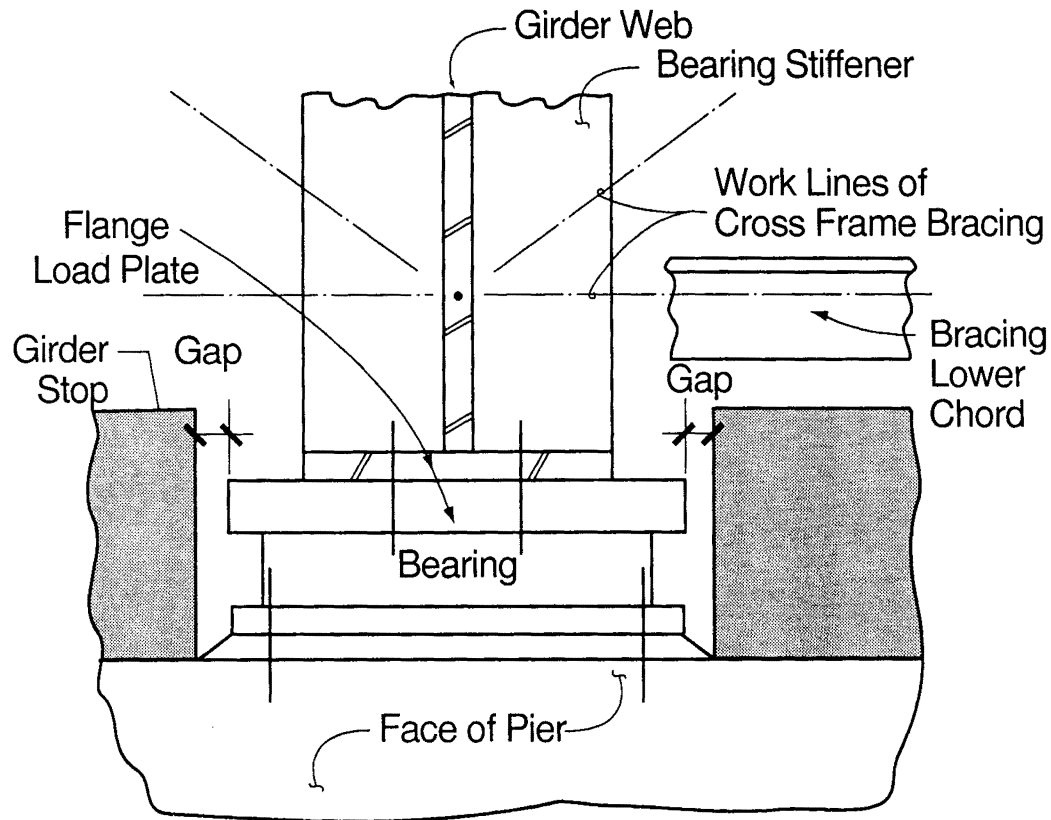
# Seismic Model vs. Actual Structure



$$V_i \approx \frac{F_{\text{super}}}{n} \quad \dots \quad \text{Actual May Be Higher Due to Tolerances}$$

For Relatively Flexible Superstructure Overturning Is Resisted Primarily at Exterior Bearings

# Shear Keys / Girder Stops



- Failsafe Load Path for Bearing
- Load May Not Be Even Due to Construction Tolerances (Unbuttoning)
- Design to Fail in Ductile Manner





# **Session 4**

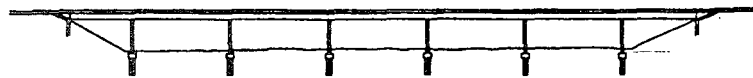
## **Steel Plate Girder Bridge Example**

### **Skew Structure Issues**

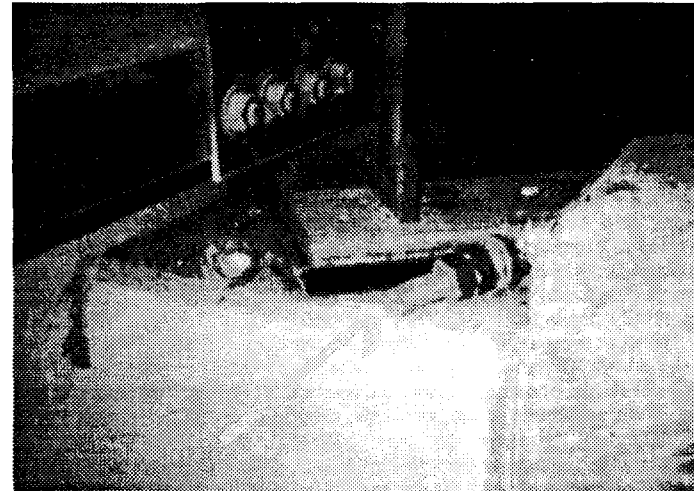
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- **Conceptual Behavior**
- **Stiffness Considerations**
- **Bearing Orientation and Releases**
- **Effects on Lateral Behavior**

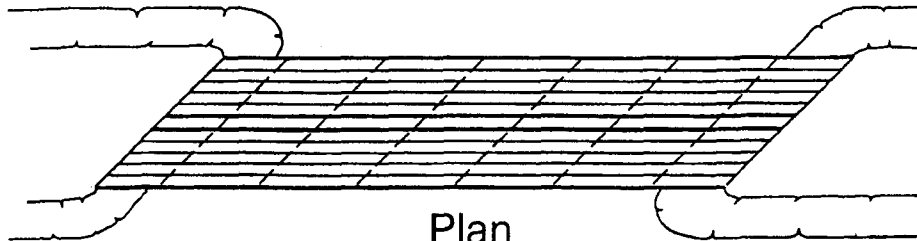
# Damage to Steel Superstructure Bridge



Elevation



Sheared Anchor Bolts



Plan

EERI (1995)

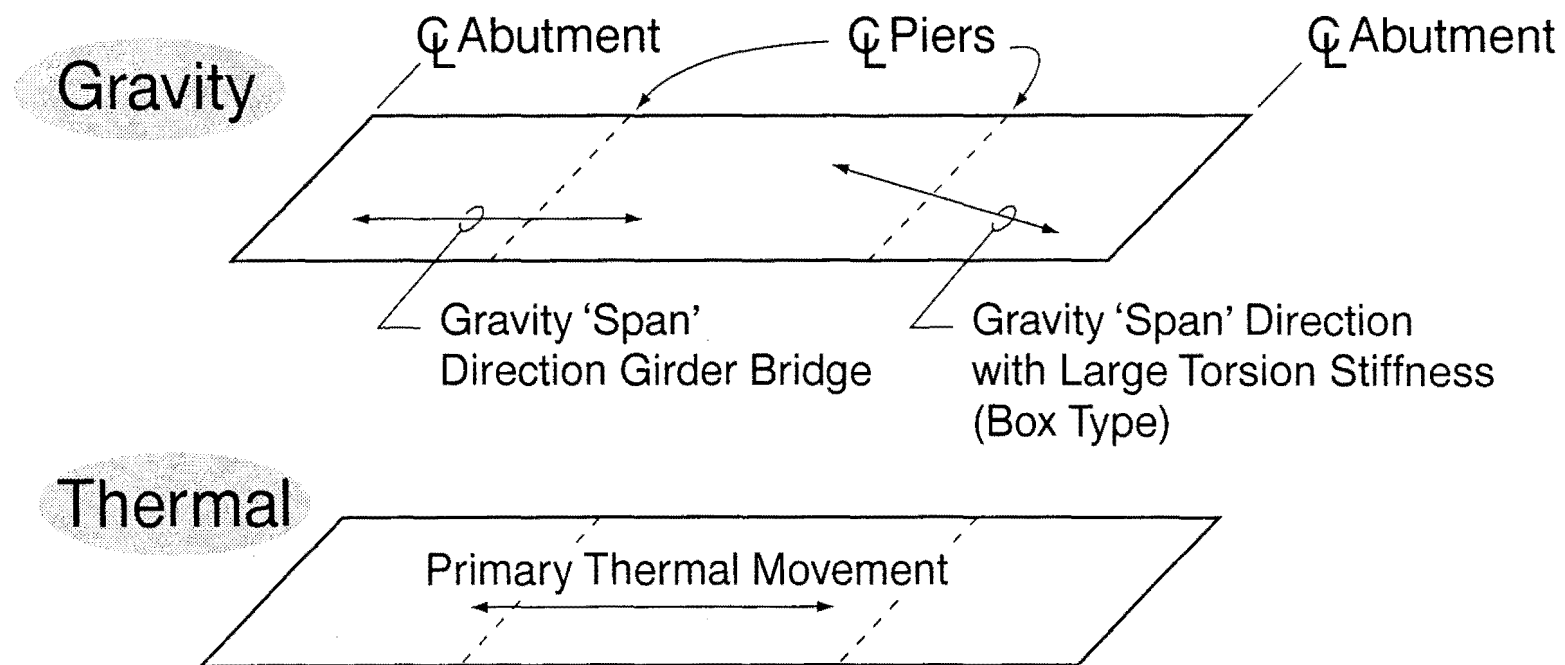
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UMD-ITV

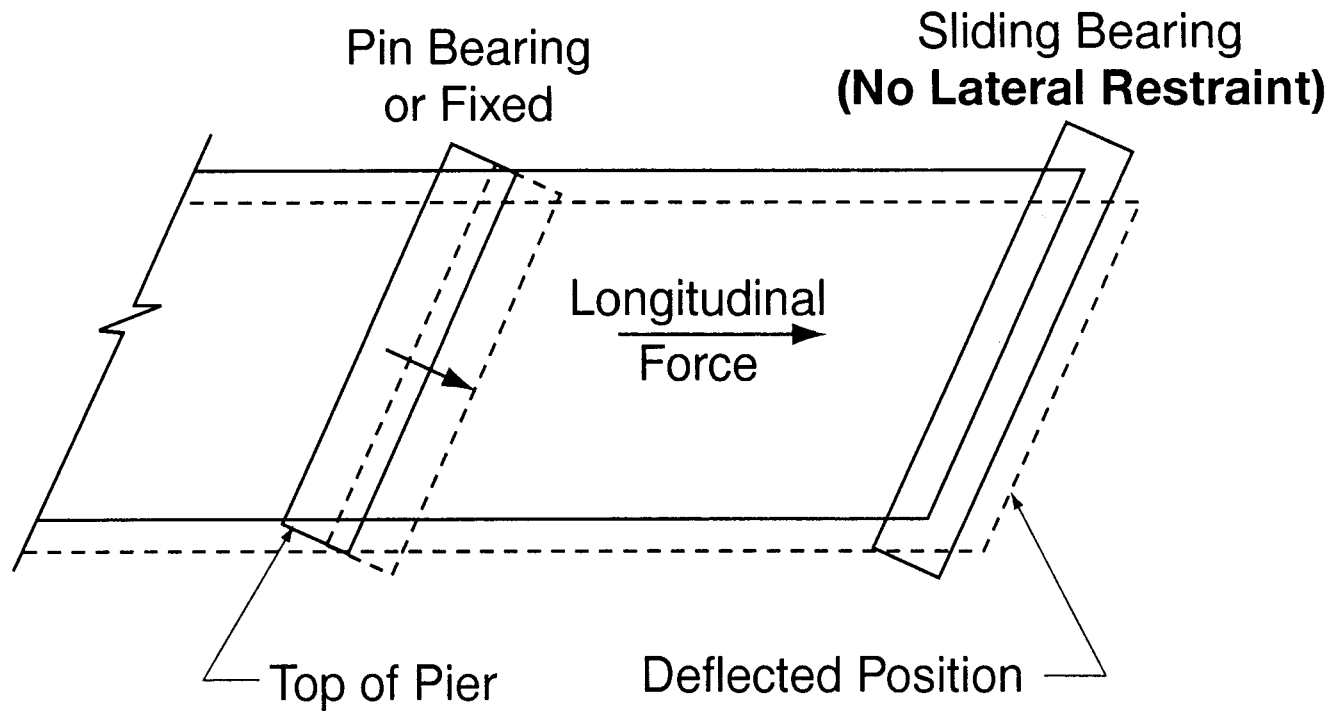
Seismic Bridge Design Applications

25 July 1996, NHI Course Code No. 13063

# Skew Behavior Under Gravity and Thermal Loads

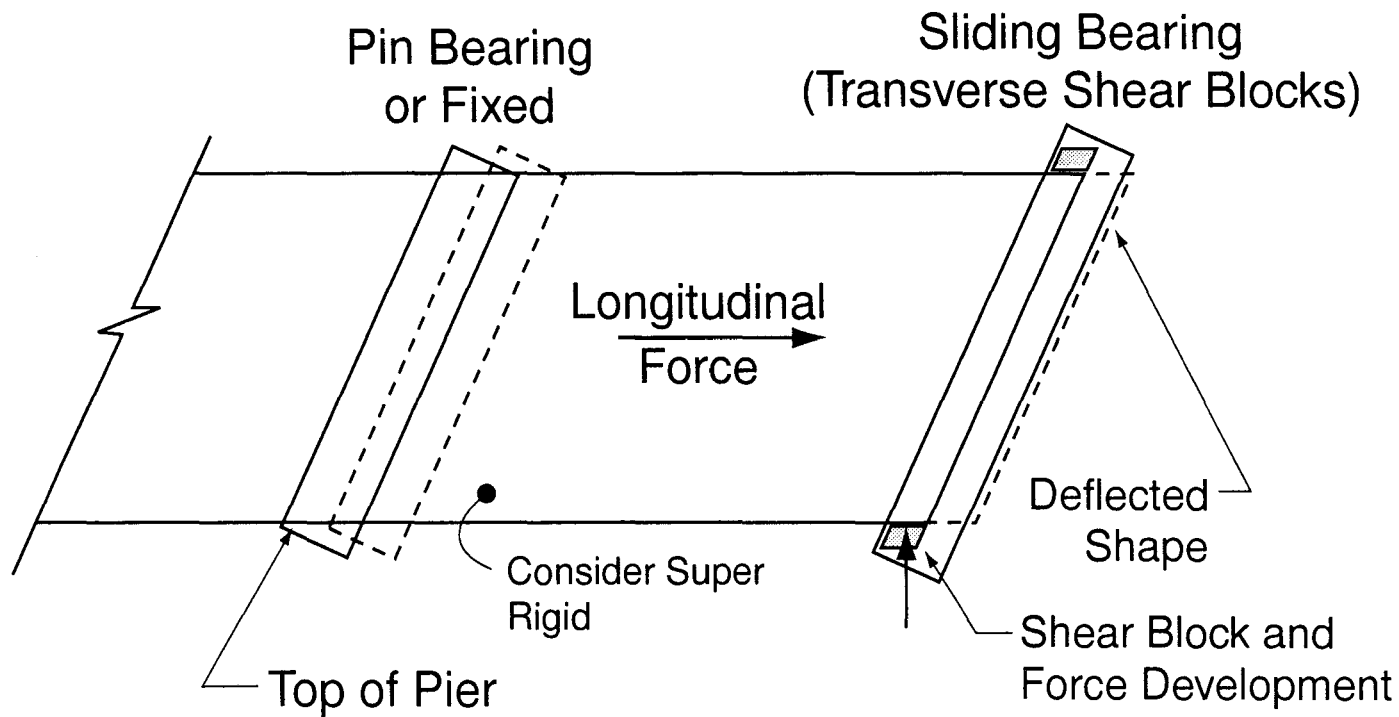


# Lateral Loading Concepts



**Plan View**

# Lateral Loading Concepts (continued)



**Plan View**

# Lateral Behavior Observations

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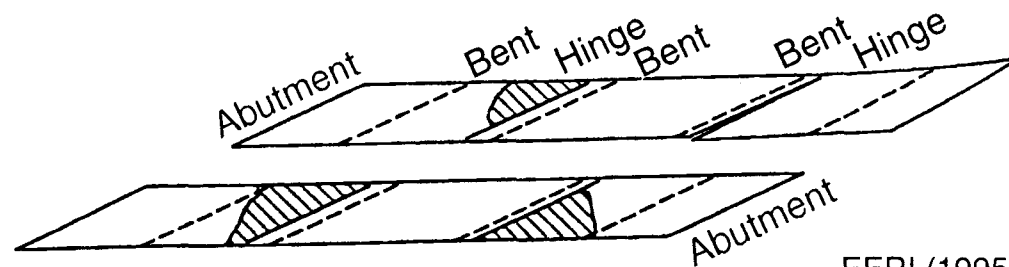
- Bridge Would Like to Move Along Weak Axis of Piers
- Shear Blocks Oriented Transversely Prevent Such Movement  $\rightsquigarrow$  Large Transverse Forces?

- Behavior Coupled in Orthogonal Plan Directions

$$F_{\text{long}} \rightsquigarrow F_{\text{trans}} \text{ and } F_{\text{trans}} \rightsquigarrow F_{\text{long}}$$

- Twisting Also Likely if Mass and Stiffness Centers Are Not Coincident

# Damage to Skewed Box Girder Bridge



EERI (1995)



USCD (1994)

- End Spans Have Large Eccentricity Between C.M. and C.S.

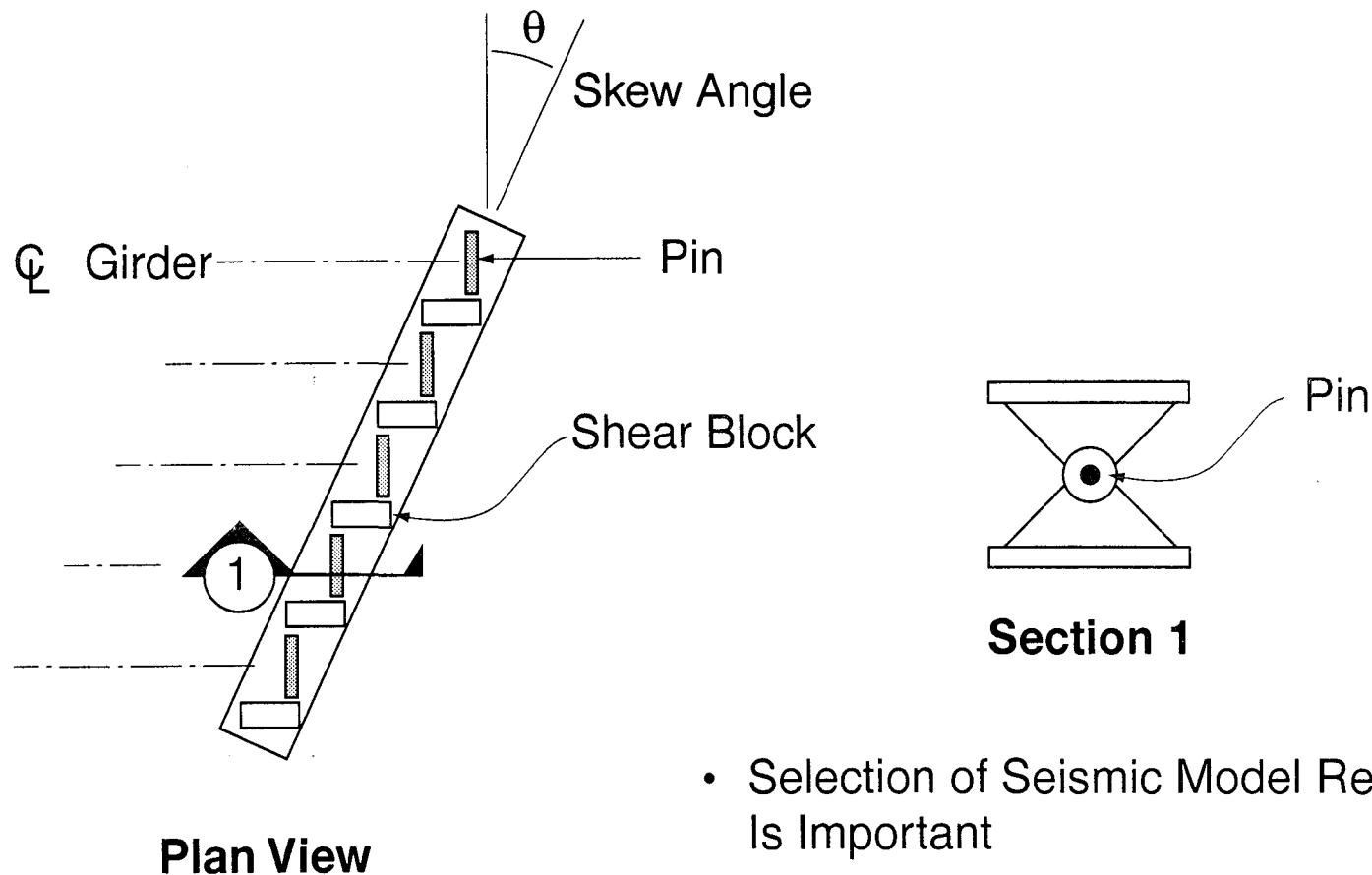
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UMD-ITV

Seismic Bridge Design Applications

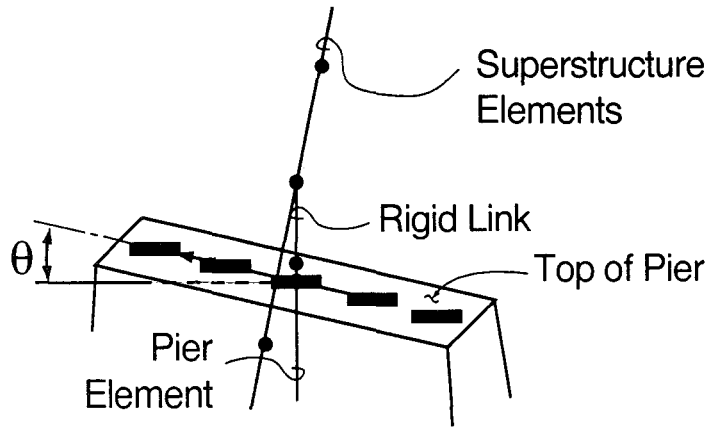
25 July 1996, NHI Course Code No. 13063

# Steel Superstructure Bearing Orientation

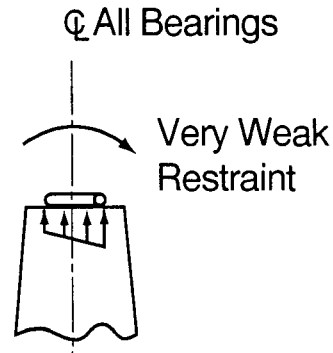




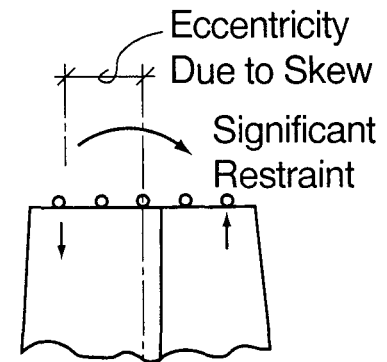
# Release Directions for Bearings



**Rotational Release  
for Pin Bearings**



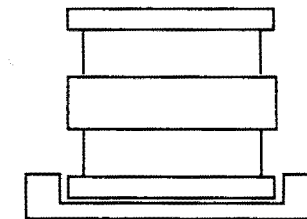
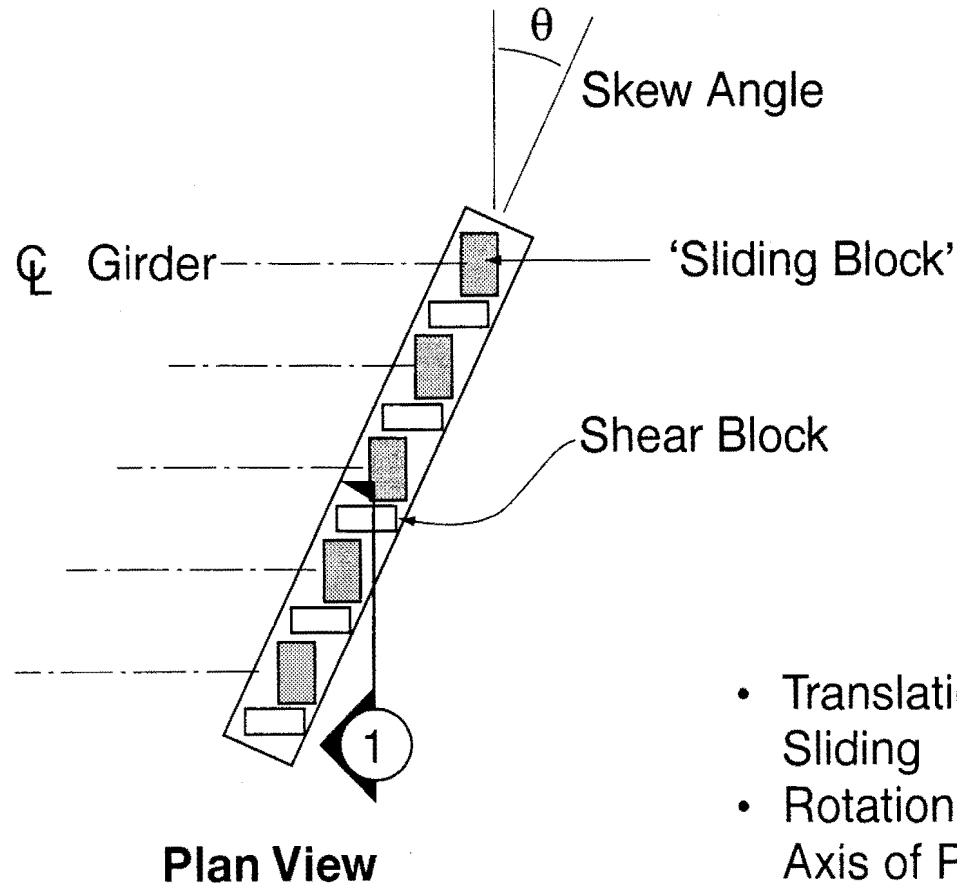
**Looking Along Weak  
Axis of Pier**



**Elevation from  
Side of Bridge**

Use Rotational Release About Weak Axis of Pier

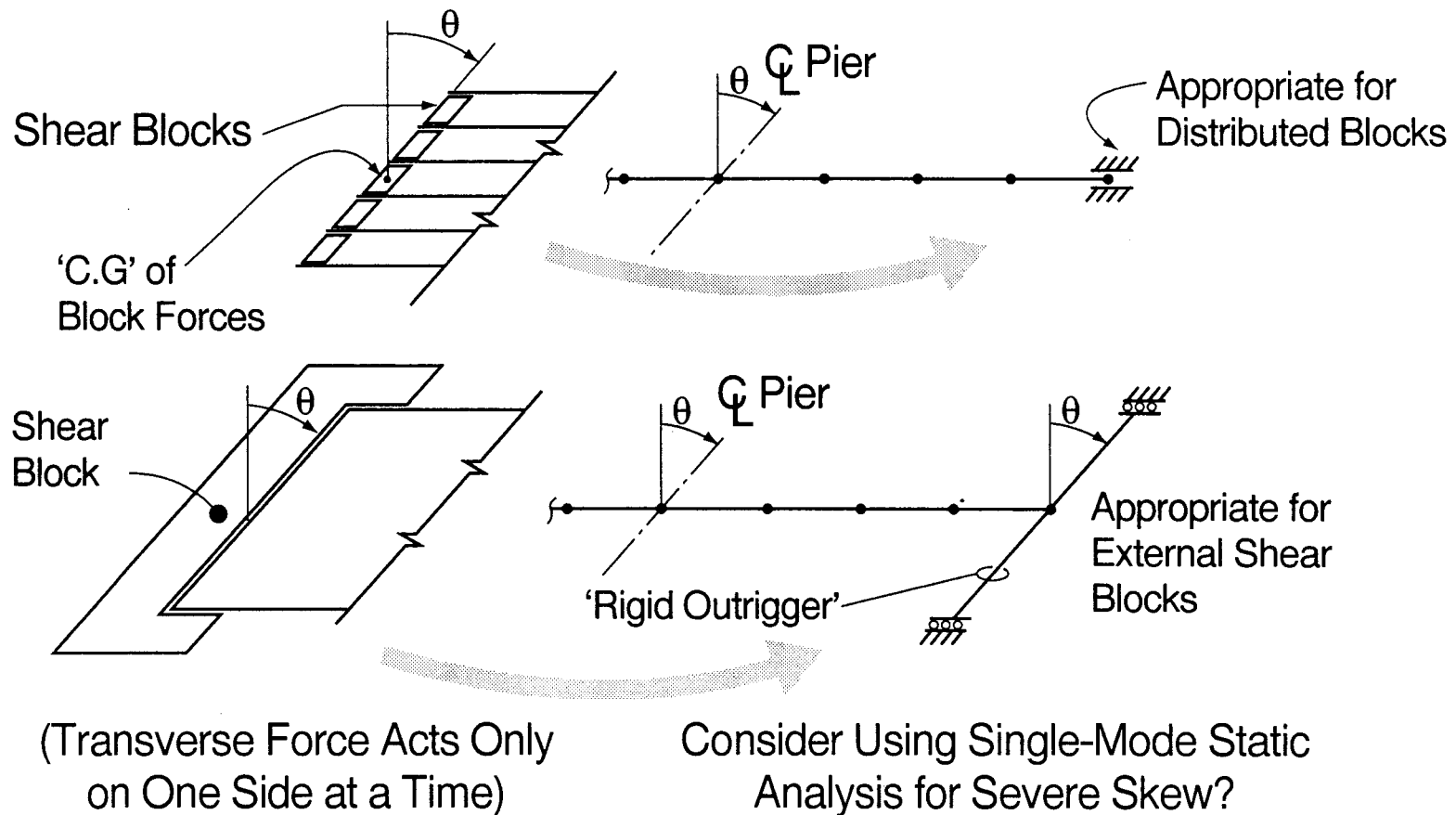
# Sliding Bearing Orientation



**Section 1**

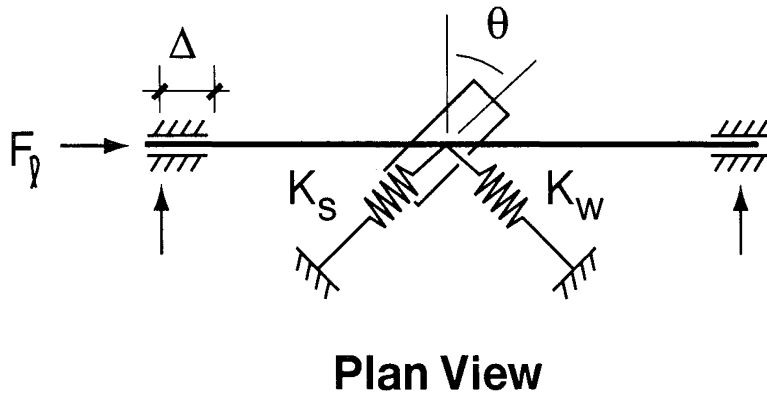
- Translational Release in Direction of Sliding
- Rotational Release About Weak Axis of Pier

# Modeling Considerations for Shear Blocks



# Stiffness Considerations (1 of 3)

Consider a Two-Span **Rigid Deck System** as Shown



- For a Given Longitudinal Displacement, the Transverse Forces Developed by  $K_s$  and  $K_w$  Are Not Equal
- ∴ Transverse Reactions Are Required

## Stiffness Considerations (2 of 3)

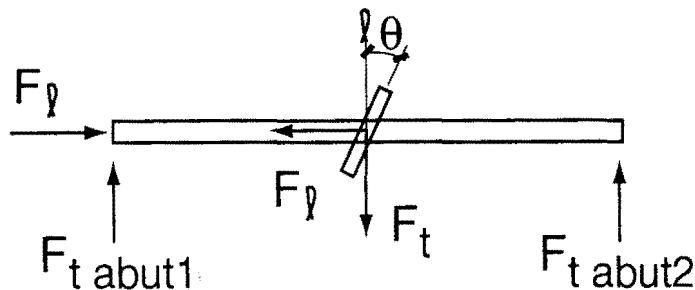
- It Can Be Shown That

$$K_{\parallel} = K_S \sin^2\theta + K_W \cos^2\theta$$

Structure Stiffness in  
Longitudinal Direction

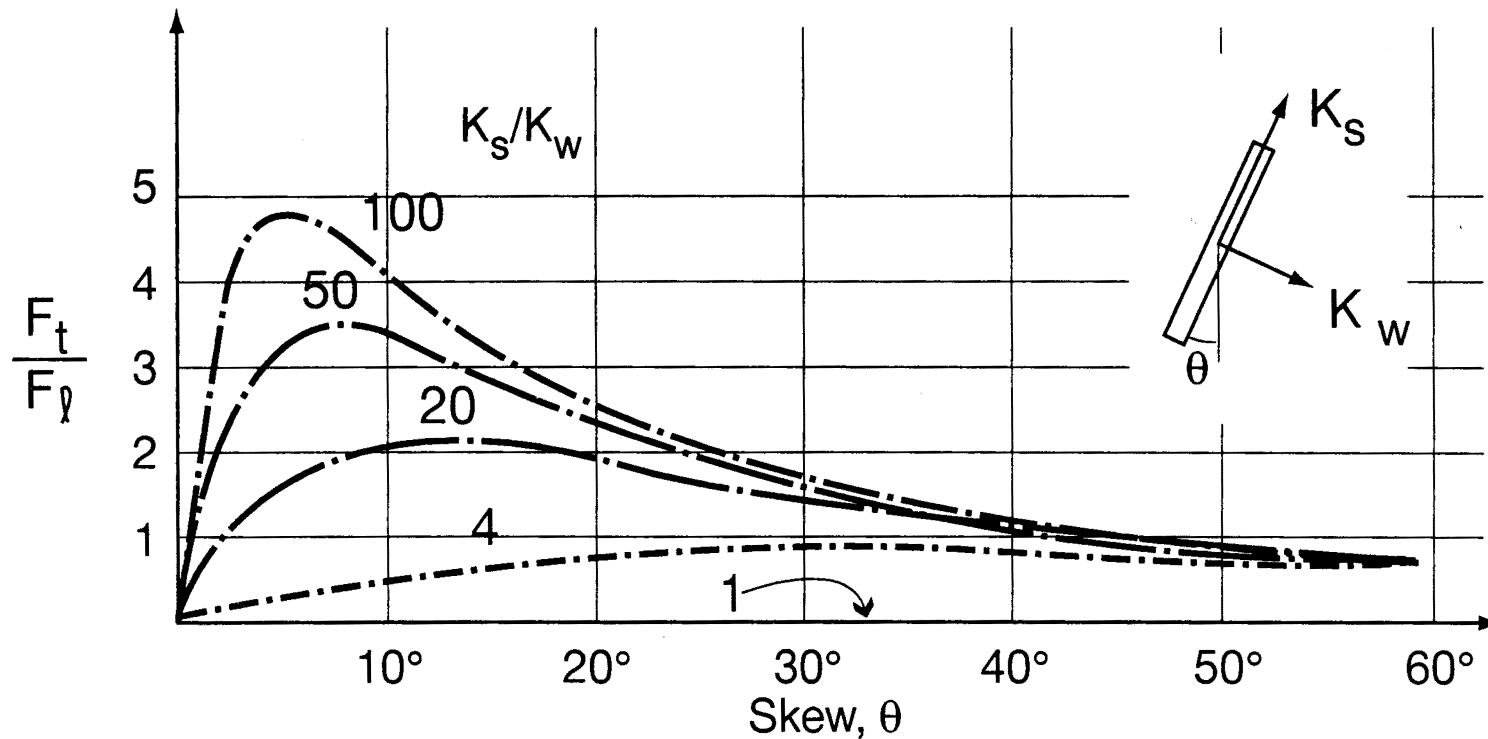
$$\frac{F_t}{F_{\parallel}} = \frac{(K_S - K_W) \sin\theta \cos\theta}{(K_S \sin^2\theta + K_W \cos^2\theta)}$$

Ratio of Transverse  
Force to Longitudinal Force  
for a Given Displacement



Plan View

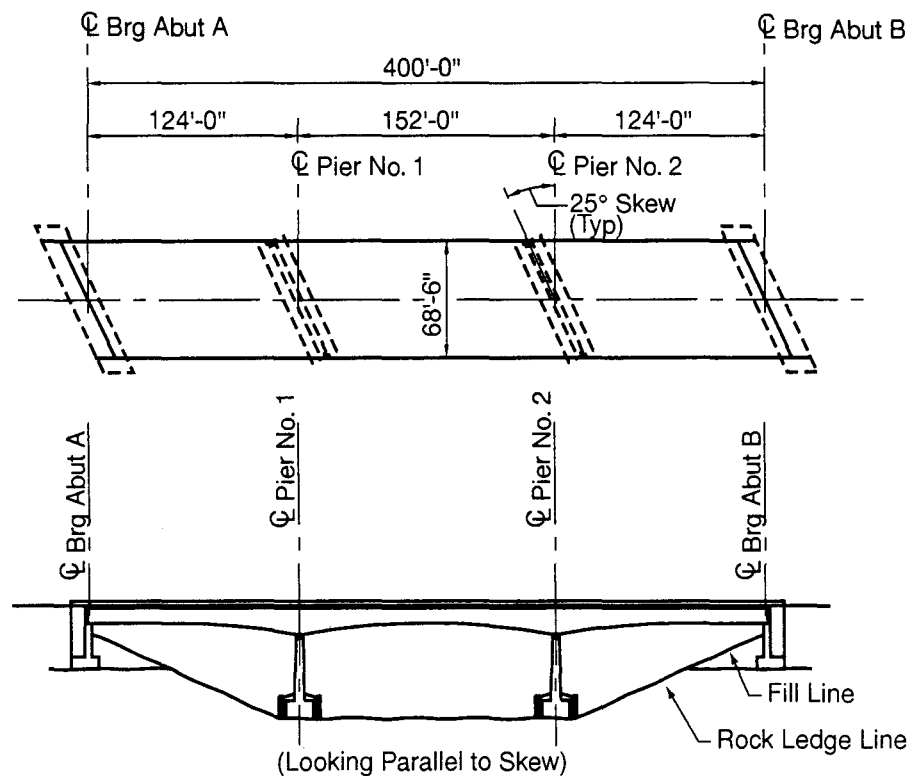
## Stiffness Considerations (3 of 3)



- For Infinitely Stiff Superstructures, Large Transverse Forces May Develop!

# Example / Effects of Skew (1 of 6)

- Consider Practice Problem No. 2 with 25° Skew



## Example / Effects of Skew (2 of 6)

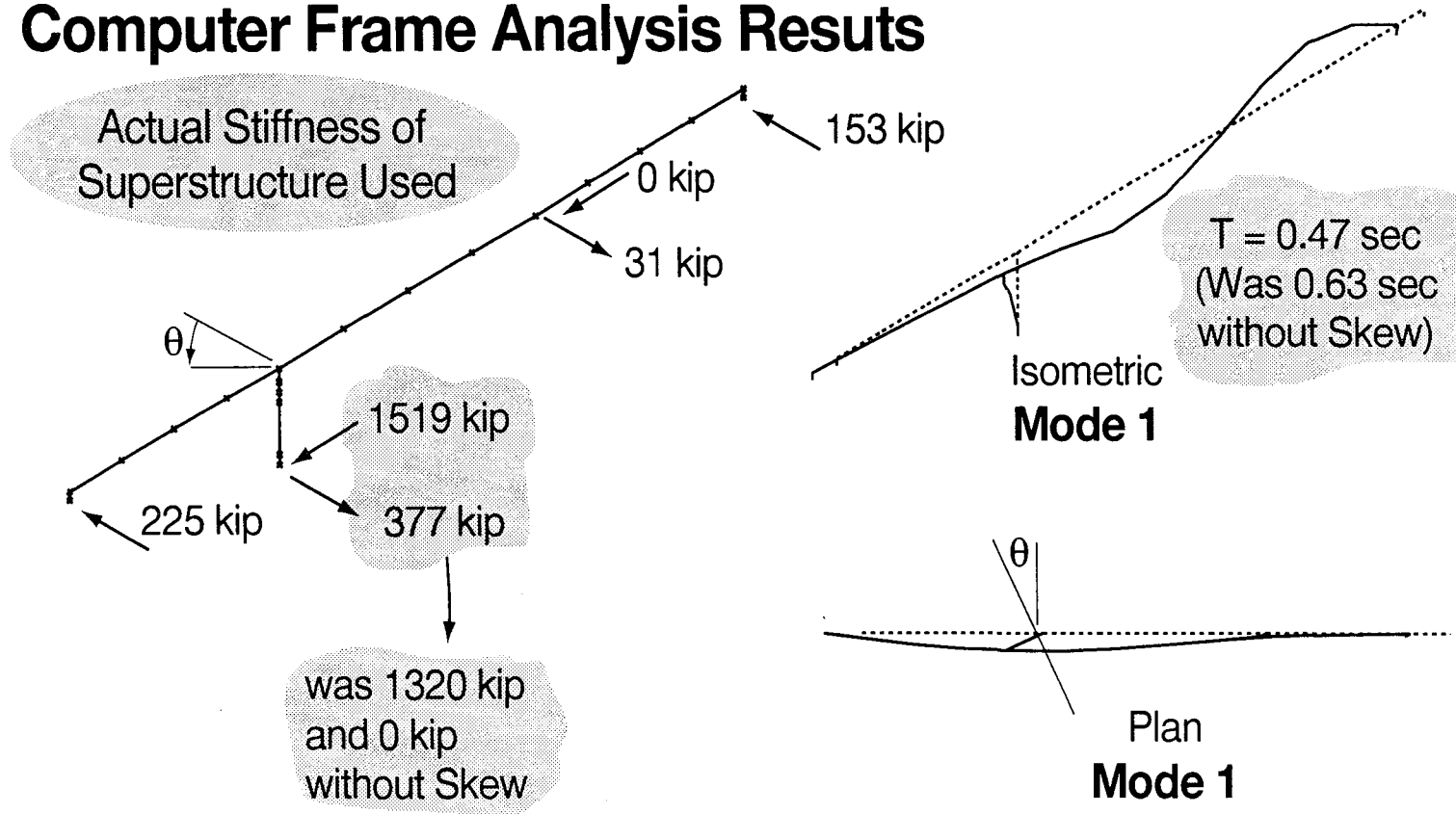
---

Determine the Longitudinal Base Shear and Transverse Restraint Forces by Frame Analysis and by Hand for Longitudinal Earthquake



# Example / Effects of Skew (3 of 6)

## Computer Frame Analysis Results



## Example / Effects of Skew (4 of 6)

---

### Hand Analysis (Assume Rigid Superstructure)

Recall Pier Stiffness,  $K_{\text{weak}} = 27150 \text{ kip/ft}$

Seismic Weight,  $W = 6041 \text{ kip}$

Strong Direction  
Pier Stiffness } Approximate Using:

Width = 60 ft, Thk = 5 ft

H = 36 ft

E = 519,000 ksf G = 220,000 ksf

## Example / Effects of Skew (5 of 6)

---

$$K_{\text{strong}} = 1,140,000 \text{ kip/ft} \quad \frac{K_S}{K_W} = \frac{1140000}{27150} = 42$$

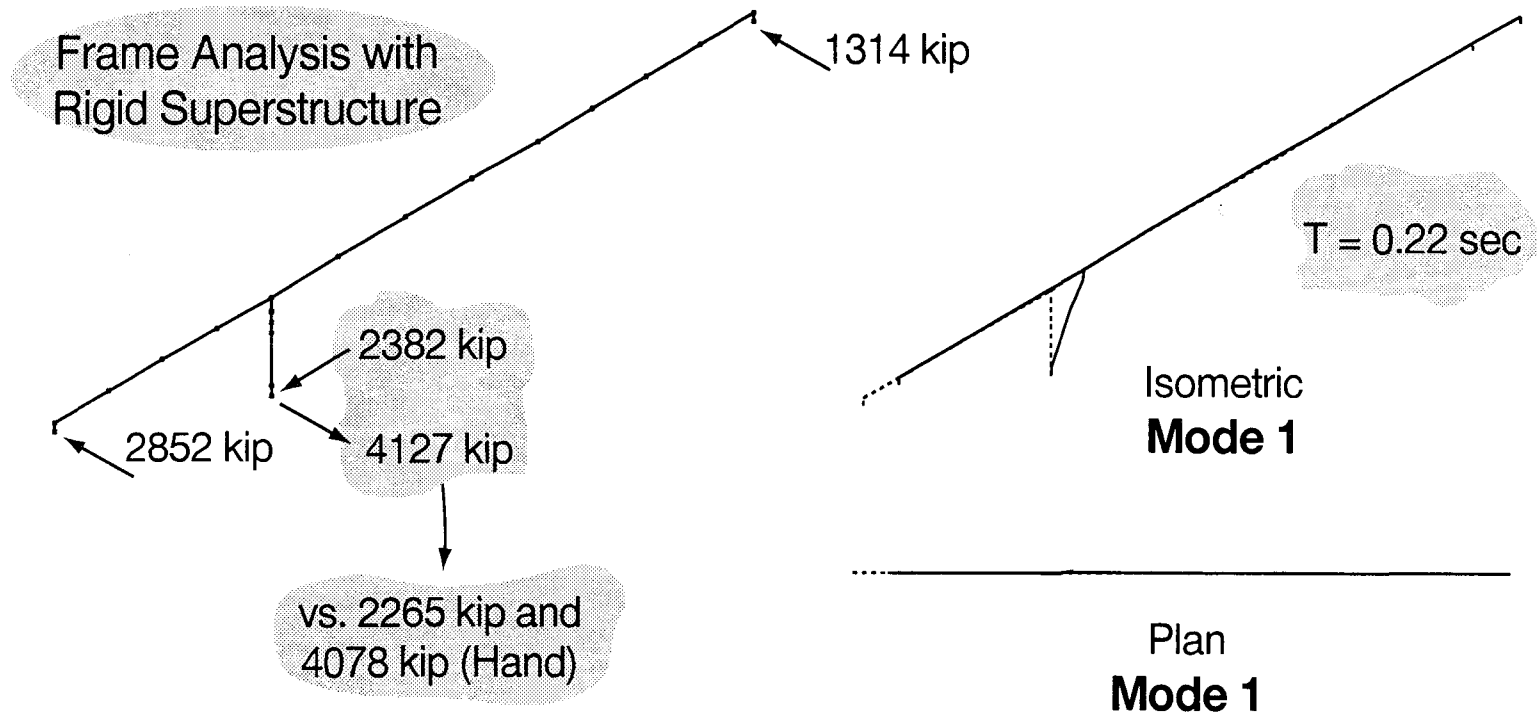
$$\text{Using Plot, } \theta = 25^\circ \quad \frac{F_t}{F_\lambda} = 1.8$$

$$K_{\text{long}} = K_S \sin^2 \theta + K_W \cos^2 \theta = \underbrace{205,200 + 22,300}_{9.2/1} = 227,500 \text{ kip/ft}$$

$$T = 0.18 \text{ sec} \quad C_S = 0.375 \quad V_\lambda = 2265 \text{ kip}$$

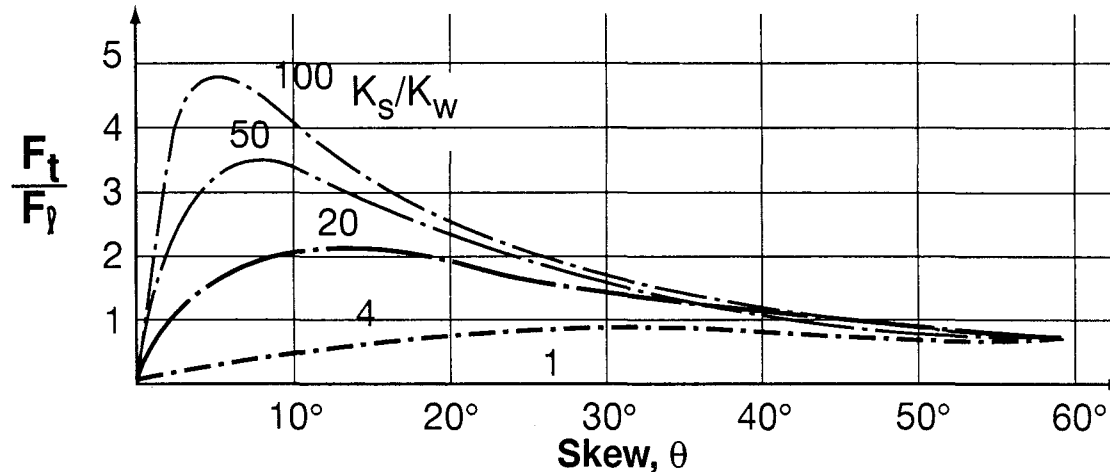
$$F_t = 1.8 (2265) = 4078 \text{ kip (vs. 377 from Frame Analysis)}$$

# Example / Effects of Skew (6 of 6)

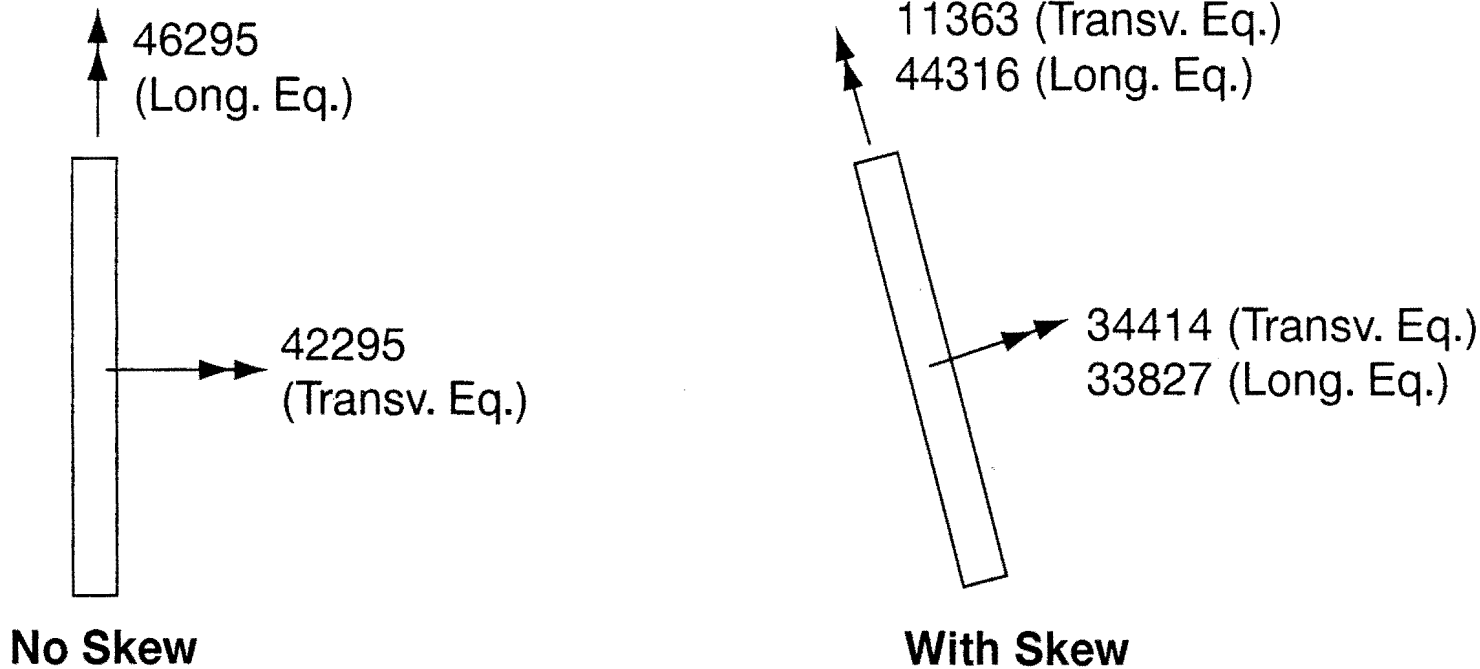


# Relative Stiffnesses

- $K_S/K_W = 1$  ..... Round Columns Fixed Top and Bottom  
 $K_S/K_W = 4$  ..... Columns Fixed Top in Strong Direction and Free Top in Weak Direction  
 $K_S/K_W = 20$  ..... Rectangular Columns or Walls  
 $K_S/K_W = 50+$  ..... Walls, But Superstructure Not Rigid, Relative to Stiff Walls, Need Frame Analysis

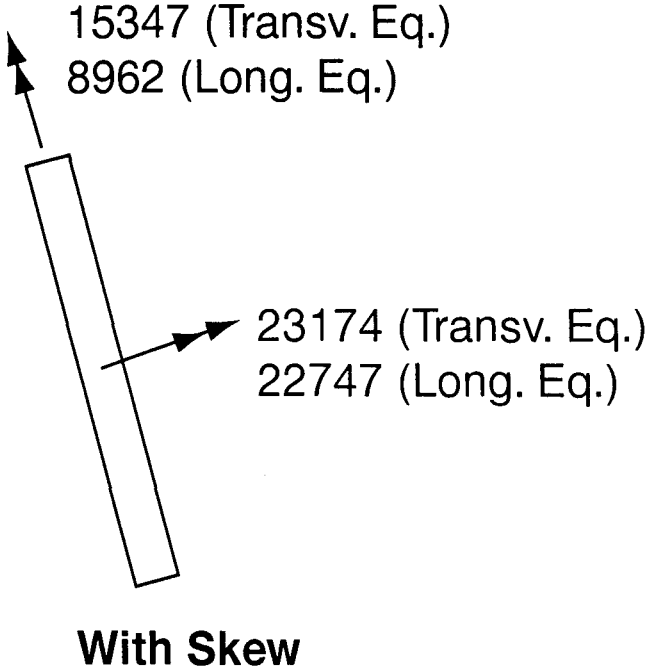
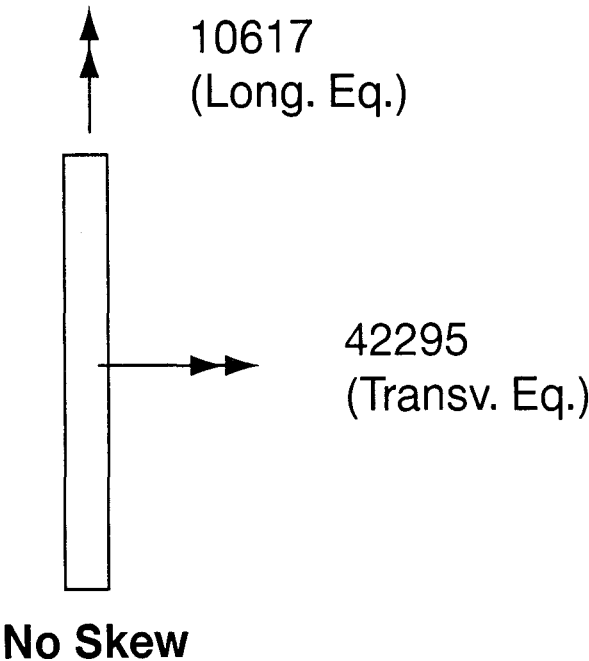


# Example Pier No. 1 – Moments of Base of Wall



Moments in kip ft

# Example Pier No. 2 – Moments of Base of Wall



Moments in kip ft

# Example / Effects of Skew

---

## Summary

- Coupling of Longitudinal and Transverse Forces Can Be Significant
- Coupling Very Sensitive to Relative Stiffness of Superstructure and Piers

## Implications

- For Stiff Superstructure / Flexible Pier Bridges, Shear Block Forces Can Be Quite High
- Failure of Shear Blocks Will Induce Torsional Response (Worsens: Seating and Outer Column / Pier Response)



# Minimizing Effects of Skew

---

- Elastomeric Bearing Pads, Which Can Have Omnidirectional Flexibility for Both Translation and Rotation, Can Help Minimize Effects of Skew
- For Example, See Design Example No. 2

# **Session 4**

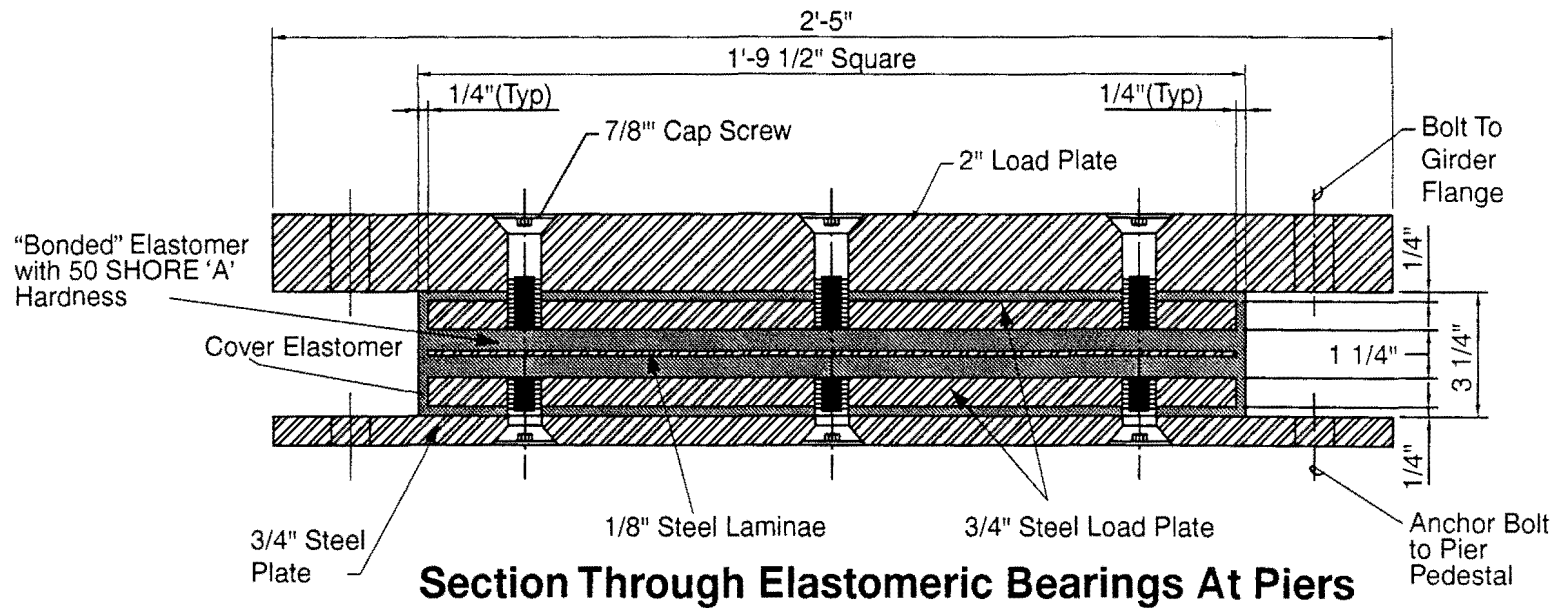
## **Elastomeric Bearing and Modeling Design**

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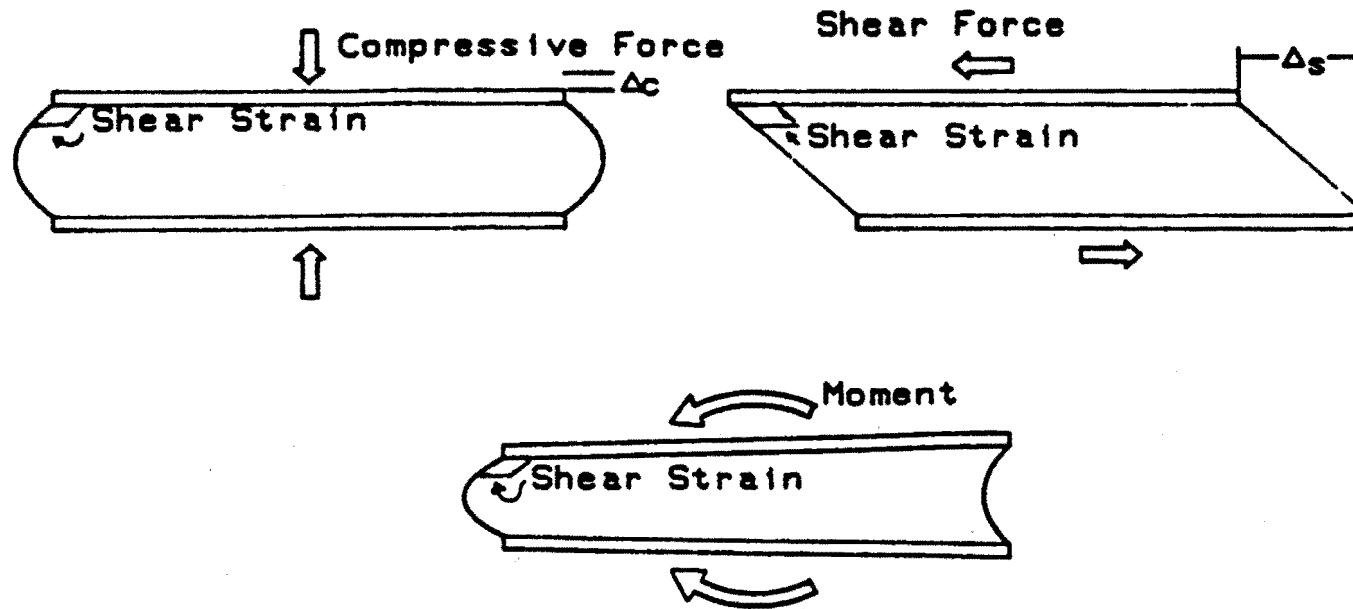
- **Concepts and Configuration**
- **Stiffness Calculations**
- **Limiting Strain**
- **Details**

(These Are Not Seismic Isolation Bearings)

# Bearing Configuration



# Conceptual Behavior



- All Loadings Induce Shear Strains

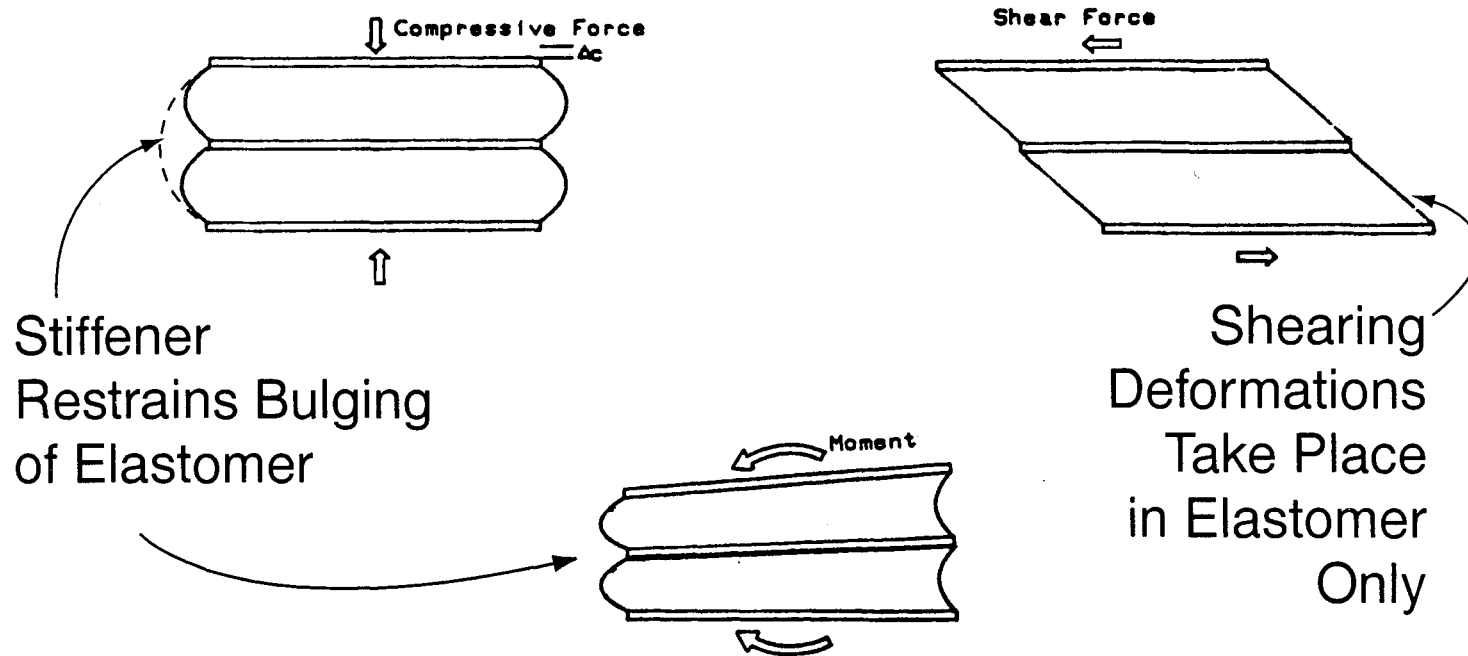
Roeder and Stanton (1990)

Session 4 Page 28 of 42

UMD-ITV

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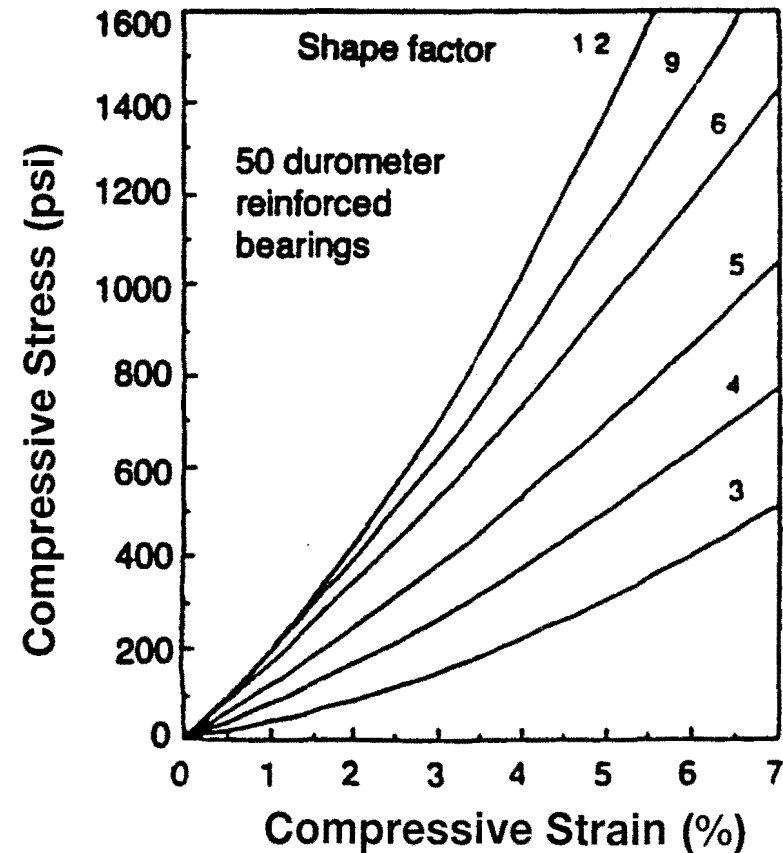
# Behavior with Stiffeners



# Properties of Elastomer

Hardness (Shore 'A')	Elastomer Shear* Modulus, G (psi)
50	95 - 130
60	130 - 200
70	200 - 300

\* Coordinate with Supplier



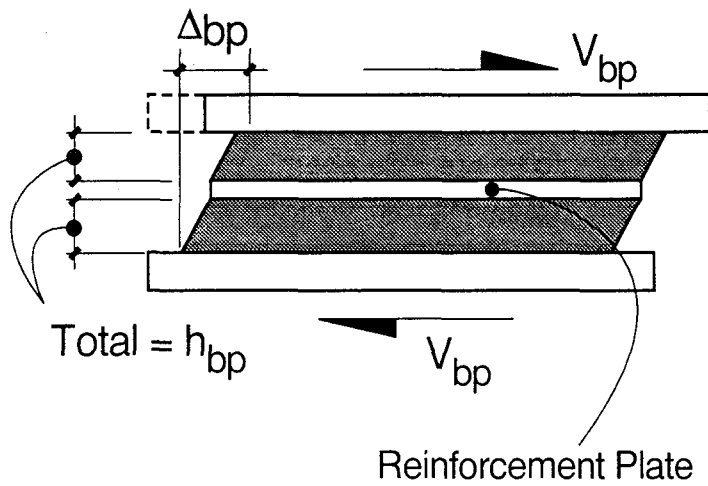
AASHTO (1995) (Division I)

Session 4 Page 30 of 42

UMD-ITV

Seismic Bridge Design Applications  
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# Stiffness Calculation for Lateral Loads



$$K_h = \frac{V_{bp}}{\Delta_{bp}} = \frac{GA}{h_{bp}}$$

$A$  = Area of Bonded Elastomer

$h_{bp}$  = Total Height of Elastomer

(Do Not Include Reinforcement Plates)

# Stiffness Calculation for Vertical Loads

---

- Shape of Bearing Affects Stiffness

$$\text{Shape Factor, } S = \frac{\text{Plan Area}}{\text{Perimeter Area Free to Bulge}} = \frac{LW}{2h_{ri}(L + W)}$$

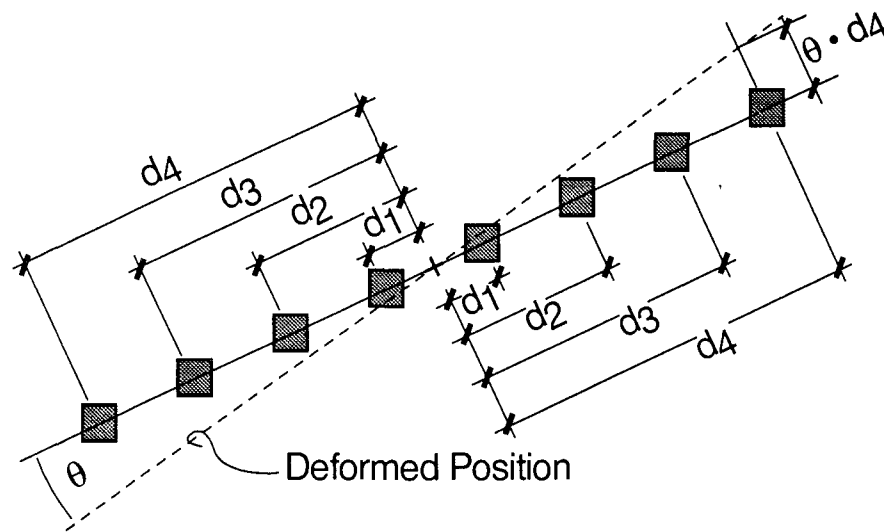
L = Length  
W = Width

$h_{ri}$  = Height of Layer

- Based on Compressive Stress and Shape Factor, Calculate Strain and Then Displacement
- Find Stiffness from Compression Force and Displacement



# Rotational Stiffness of Group



**Plan View  
Bearing Pads on Skew Pier**

$$K_{rot} = \frac{M}{\theta} = \sum_{i=1}^n K_{brg_i} d_i^2$$

$K_{brg_i}$  = Individual Bearing  
Translational  
Stiffness

$d_i$  = Distance from  
Centroid to  
Bearing  $i$

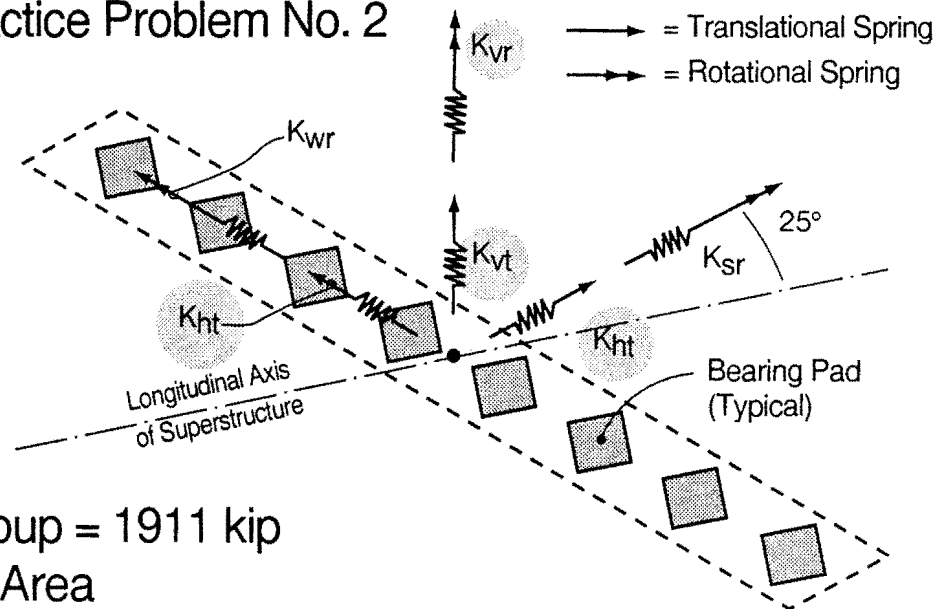
- Vertical Rotational  
Stiffness Similar

# Example / Elastomeric Bearing Stiffness (1 of 5)

- Consider Bearing Shown at Beginning of Section and 25° Skew Bridge of Practice Problem No. 2

- Calculate Stiffness Shown in Shaded Bubbles

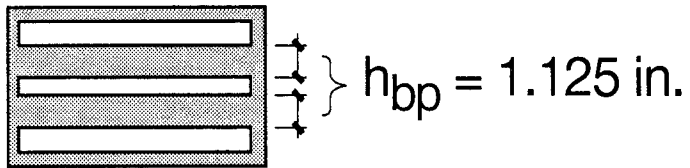
- Use  $G = 115$  psi  
Weight on Bearing Group = 1911 kip  
21 in. x 21 in. Bonded Area



Configuration at Pier

## Example / Elastomeric Bearing Stiffness (2 of 5)

---



- One Pad:  $k_{ht} = \frac{GA_{bp}}{h_{bp}} = \frac{115(21)^2 12}{1.125 (1000)} = 541$  kip/ft
- Eight Pads:  $K_{ht} = 8 (541) = 4328$  kip/ft
- Note that Stiffness Is the Same in All Directions

## Example / Elastomeric Bearing Stiffness (3 of 5)

- Stress on Individual Bearings

$$\sigma = \frac{1911 (1000)}{8(21)^2} = 542 \text{ psi}$$

- Shape Factor

$$h_{ri} = \frac{1.125}{2} = 0.563 \text{ in.}$$

$$S = \frac{LW}{2h_{ri}(L+W)}$$

$$S = \frac{(21)^2}{2(0.563)(21+21)} = 9.3$$

- From AASHTO Plot (50 Durometer)

Compressive Strain  $\epsilon_c = 0.025$  (Use Manufacturer's Data if Available)

## Example / Elastomeric Bearing Stiffness (4 of 5)

---

- **One Pad**

$$k_{vt} = \frac{AE}{h_{bp}} \cdot \frac{A \sigma/\epsilon}{h_{bp}} = \frac{(21)^2 \left( \frac{0.542}{0.025} \right) (12)}{(1.125)}$$

$$k_{vt} = 102,000 \text{ kip/ft}$$

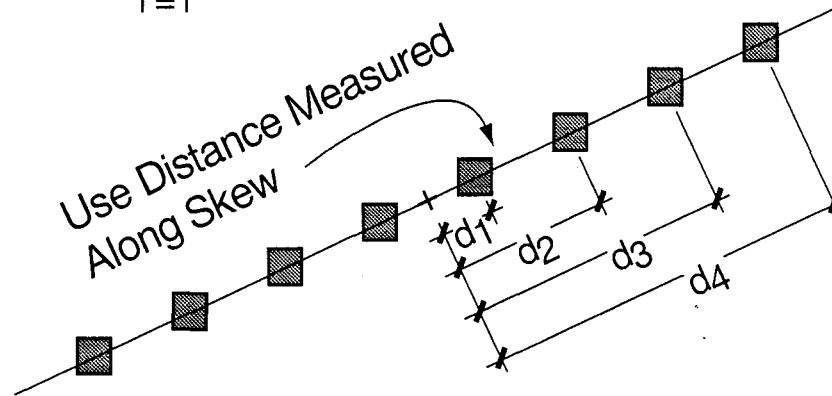
- **Eight Pads**

$$K_{vt} = 8(102,000) = 816,000 \text{ kip/ft}$$

# Example / Rotational Stiffness About Vertical Axis (5 of 5)

$$K_{rv} = \sum_{i=1}^8 k_{ht} d_i^2 = 2 k_{ht} \sum_{i=1}^4 d_i^2$$

$$\begin{aligned} d_1 &= 4.5 \text{ ft} \\ d_2 &= 13.5 \text{ ft} \\ d_3 &= 22.5 \text{ ft} \\ d_4 &= 31.5 \text{ ft} \end{aligned}$$



Plan View

$$K_{rv} = 2(541)[4.5^2 + 13.5^2 + 22.5^2 + 31.5^2] = 1,841,000 \frac{\text{kip ft}}{\text{rad}}$$

# Assessing Seismic Performance

---

- **Conventional (Division I)** → **Limit Service Shear Displacement**  
(To 1/2 Elastomer Height)
- **Seismic Loadings** → **Assess Against Ultimate Resistance**  
(Not Service Allowable)
- **Suggest AASHTO's Guide Specification for Seismic Isolation Design**  
(Use Article 14.6, Seismic Load Combinations, Even Though We Are Considering Only Conventional Elastomeric Bearings in This Section)

# Assessing Seismic Performance of Conventional Elastomeric Bearings

**Limit Strains to:**  $0.75 \epsilon_U > \epsilon_{SC} + \epsilon_{eq} + \epsilon_{sr}$  AASHTO Seismic Isolation Guide Specification / §14.6

$\epsilon_U$  = Minimum Elongation-At-Break of Elastomer  
(From AASHTO or Preferably Supplier)

Example, Table 18.2.3.1 Division II  
50 Durometer Neoprene  $\epsilon_U = 400\%$

$\epsilon_{SC}$  = Shear Strain Due to Compression =  $65 S \epsilon_C$  ← Compressive Strain

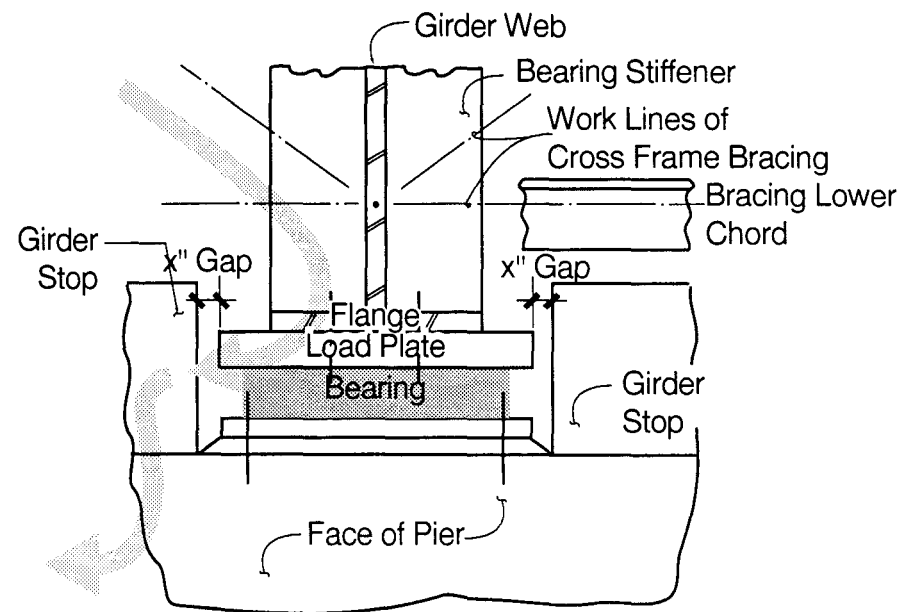
$\epsilon_{eq}$  = Shear Strain Due to Earthquake =  $\Delta_{eq} / h_{elastomer}$

$\epsilon_{sr}$  = Shear Strain Due to Rotation =  $\frac{B^2 \theta}{2h_{ri} \cdot h_{bp}}$  ← Load Direction Dimension



# Fail-Safe Issues

- Consider an Additional Load Path in Case of Bearing Failure
- Engage Alternate Path After Bearing Deformation Occurs



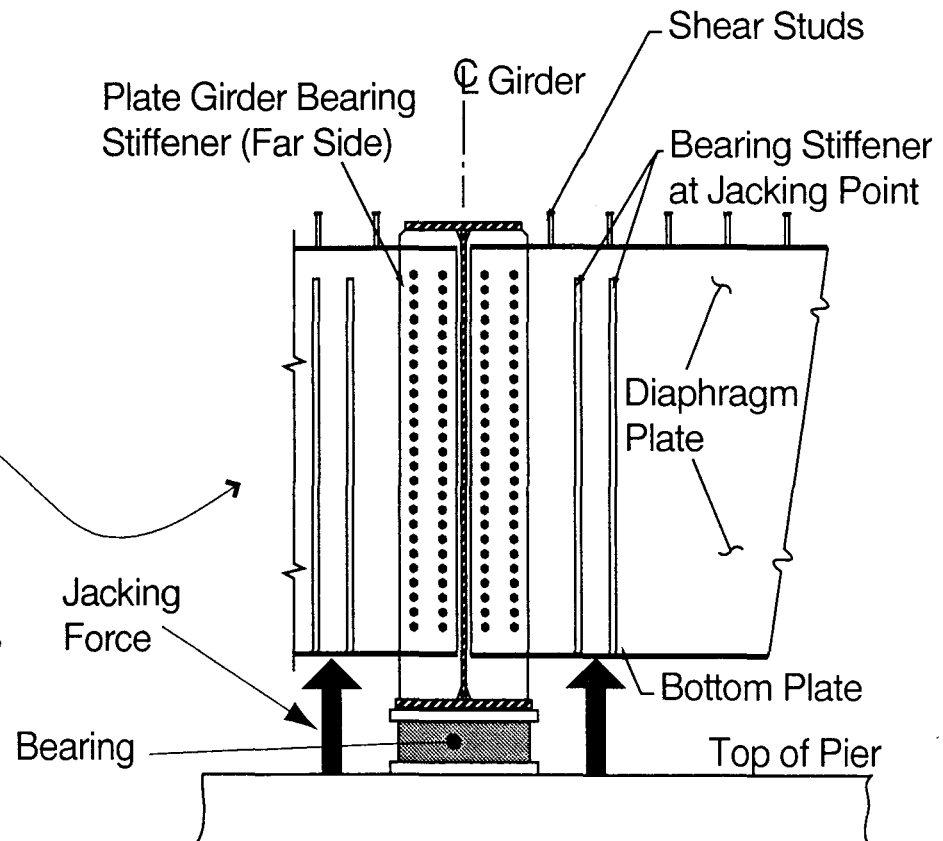
# Consider Method of Bearing Replacement

- Lift Along Girder  
(Previous Sketch)

or

- Lift Along Solid  
Diaphragm-Type  
Cross Frame

Interior Support Cross  
Frame Elevation



# **Session 5**

## **Curved Box Girder Bridge Example**

---

### **Session 5**

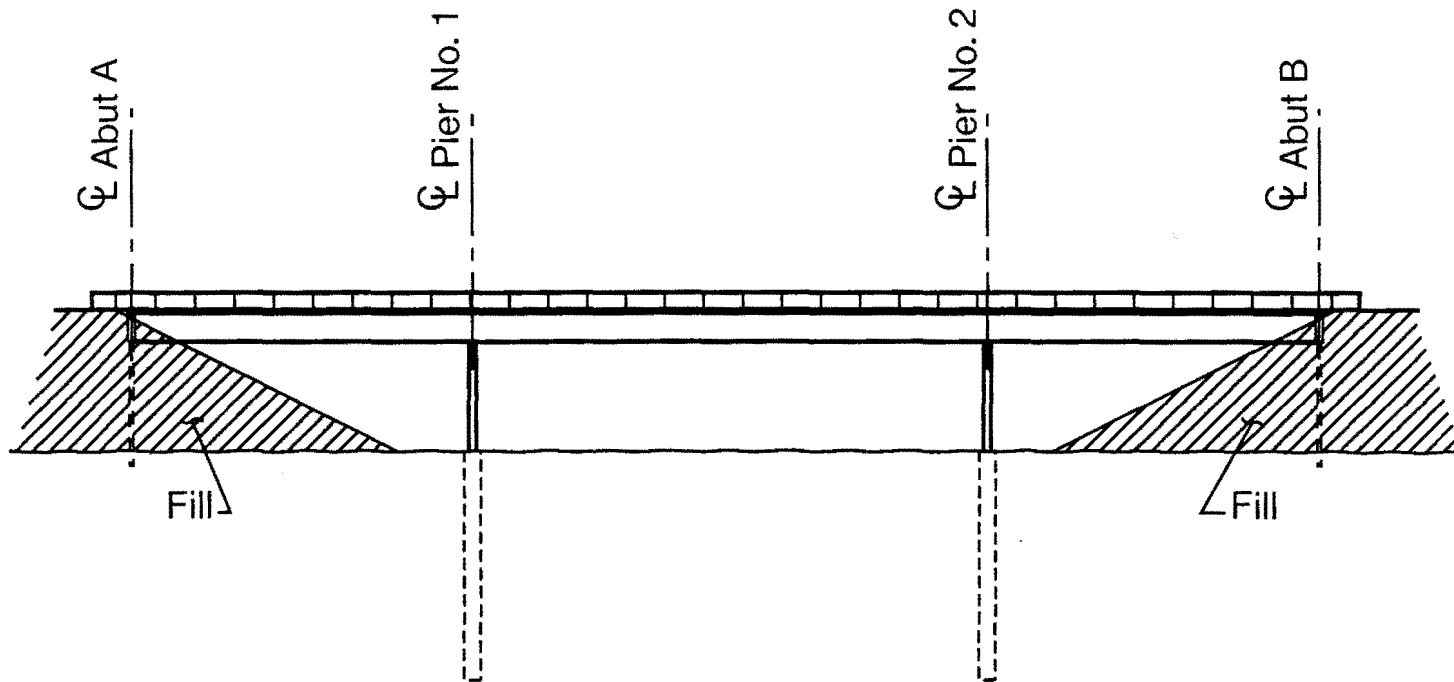
- **Curved Structure Issues**
- **Piles**

### **Session 6**

- **Drilled Shafts**

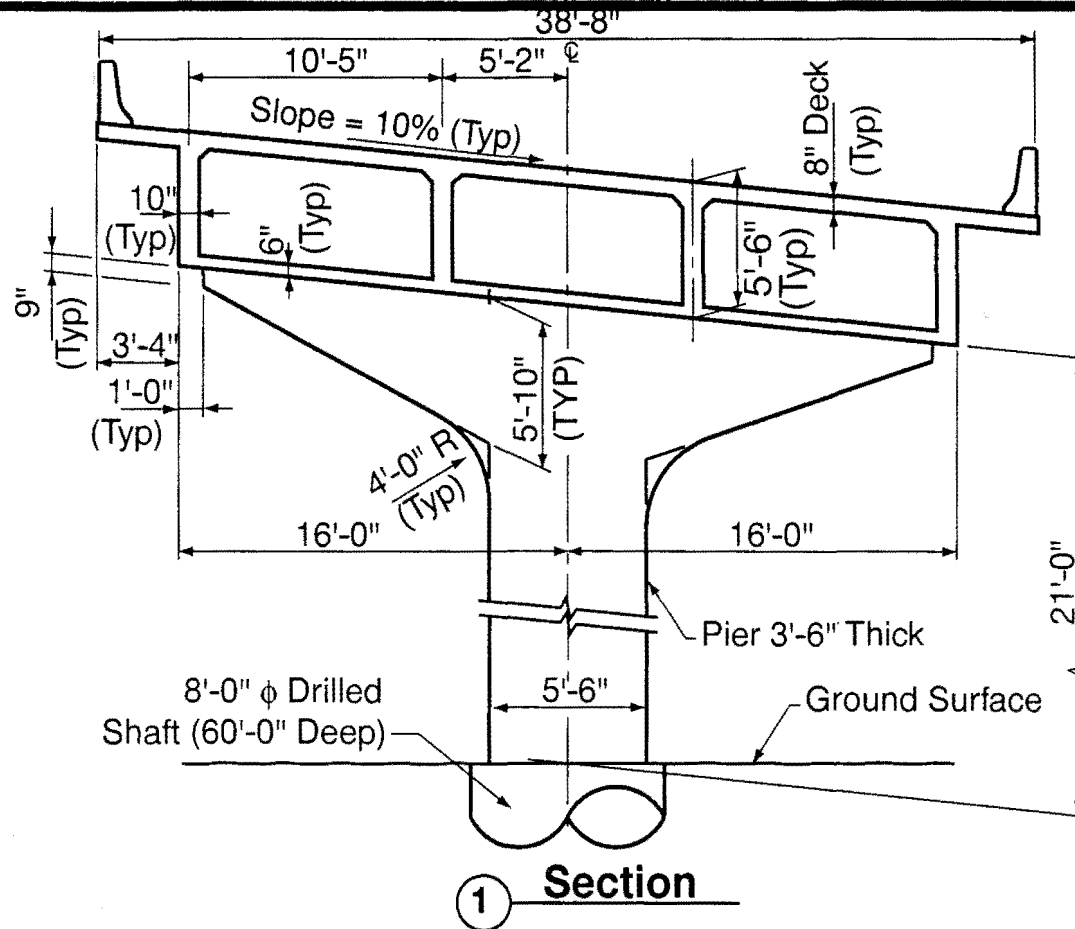


# Concrete Curved Box Girder Bridge / Elevation

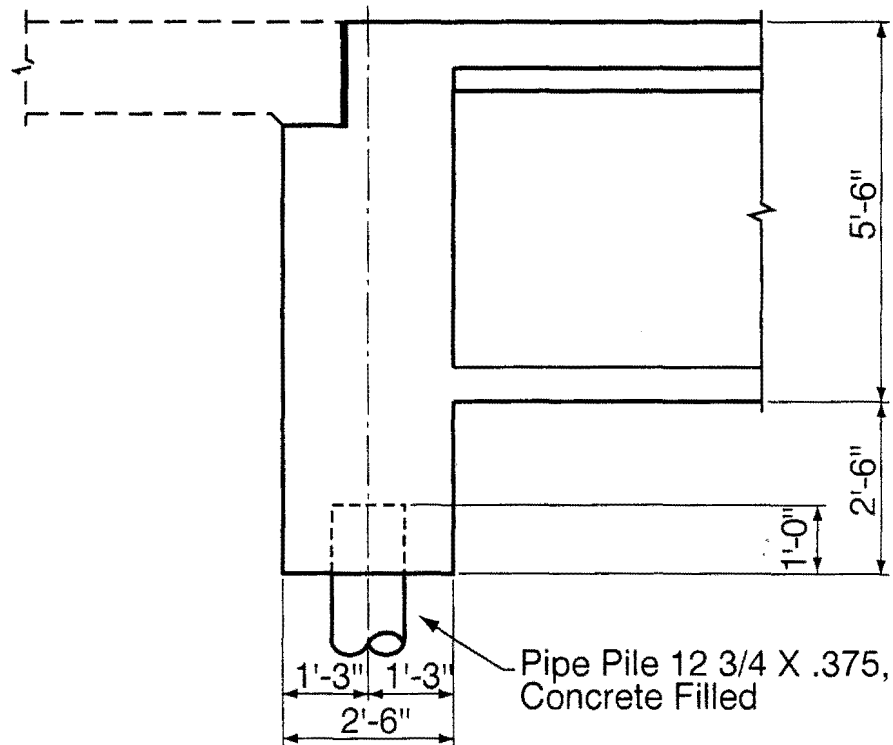


**Developed Elevation**

# Concrete Curved Box Girder Bridge / Pier

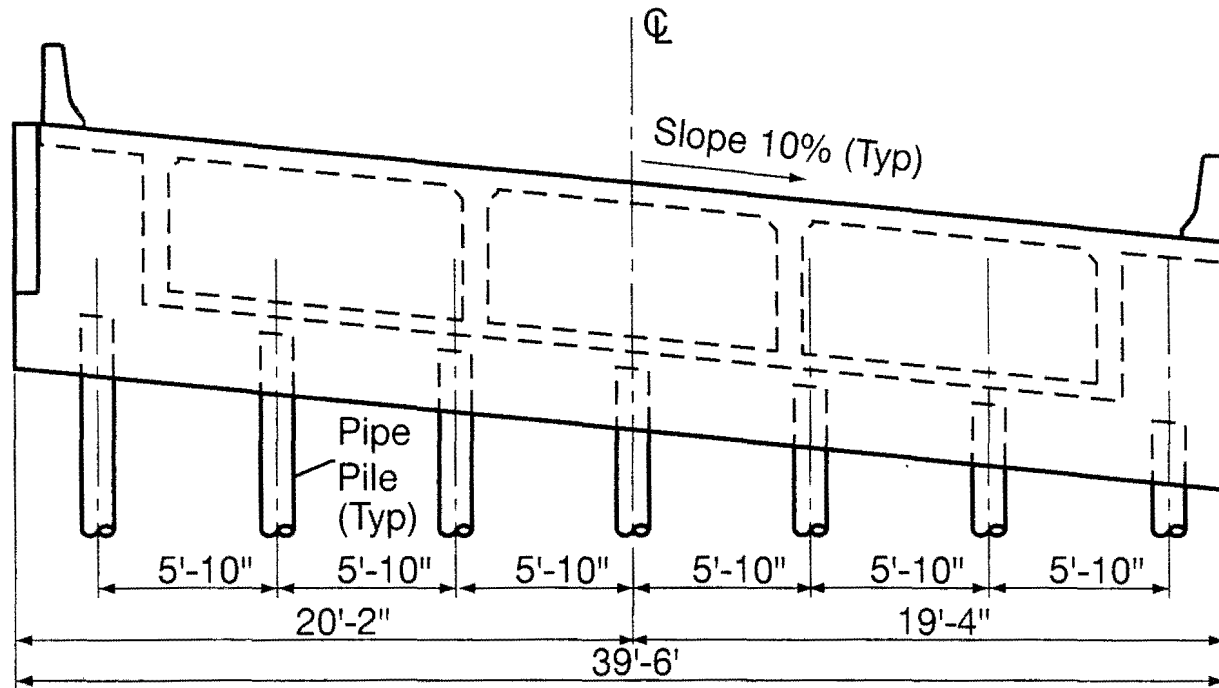


# Concrete Curved Box Girder Bridge / Abutment



② Section

# Concrete Curved Box Girder Bridge / Abutment



③ Elevation



# **Session 5**

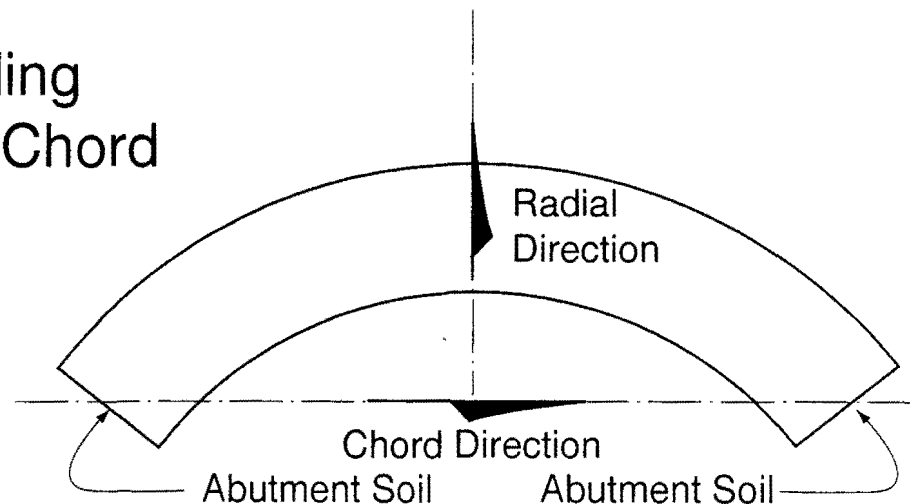
## **Curved Structure Issues**

---

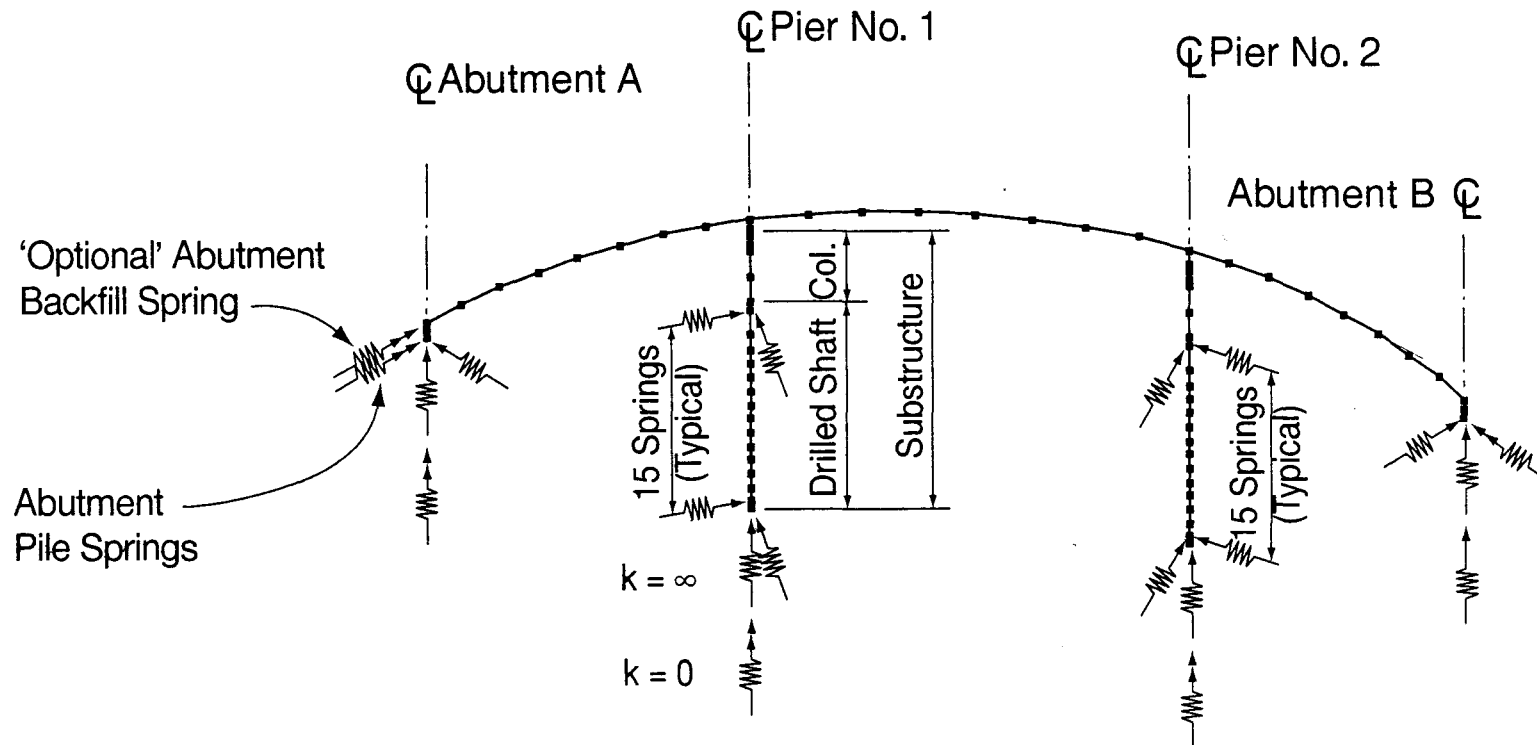
- **Loading Directions**
- **Conceptual Behavior**
- **Bounding Response**

# AASHTO Loading Directions

- If Modal Analysis Is Used (Required if 'Not Regular')
  1. Earthquake Loading Along Chord
  2. Earthquake Loading Perpendicular to Chord
- Suggest the Same Loading Directions for Other Analysis Methods

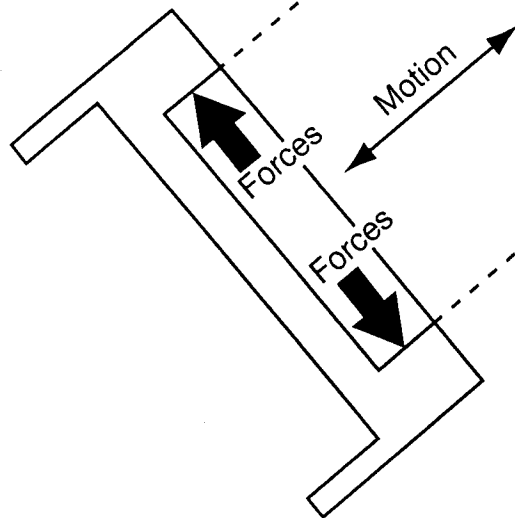


# Seismic Analysis Model / Example Bridge



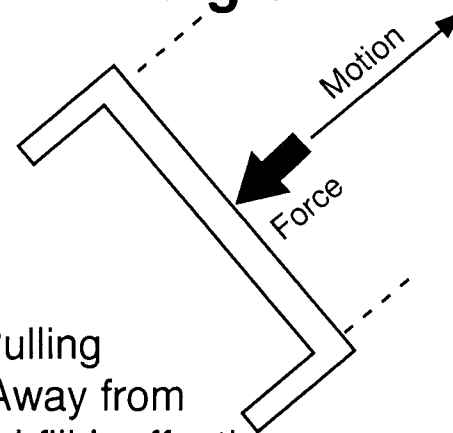
# Effects of Abutment Restraint

## Seat-Type with Shear Blocks



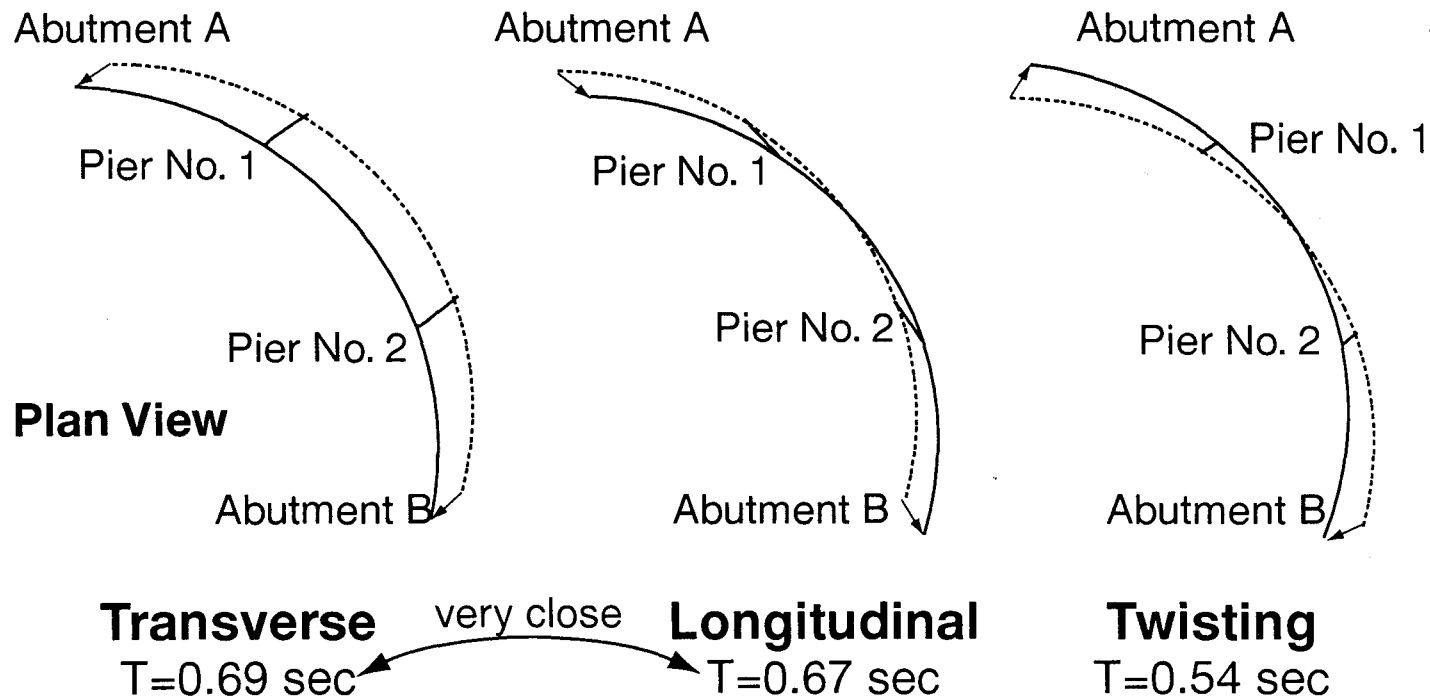
- Movement Will Heavily Load Shear Blocks

## Integral

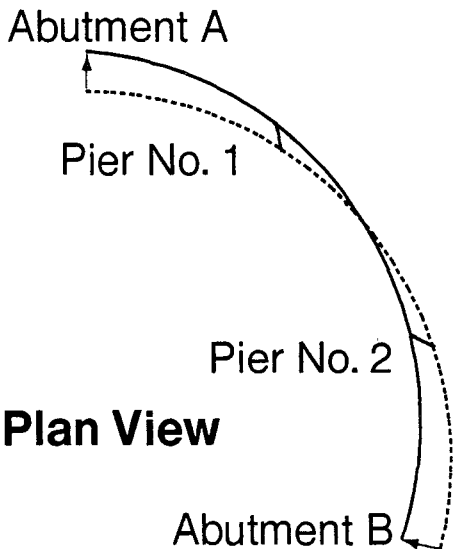


- Movement Pulling Diaphragm Away from Soil ~ Backfill Ineffective
- Movement Toward Soil Backfill Effective
- Use Bounding Analyses

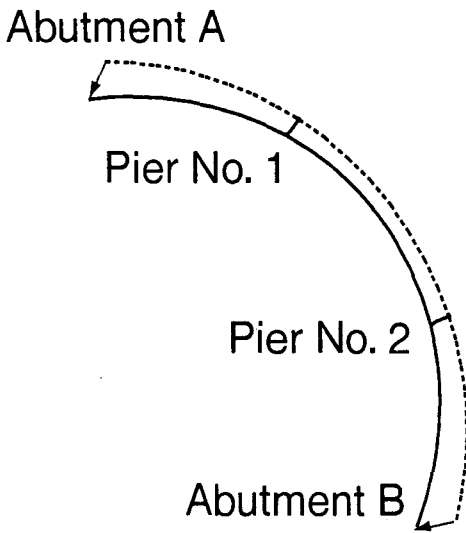
# Modal Behavior / No Backfill Considered



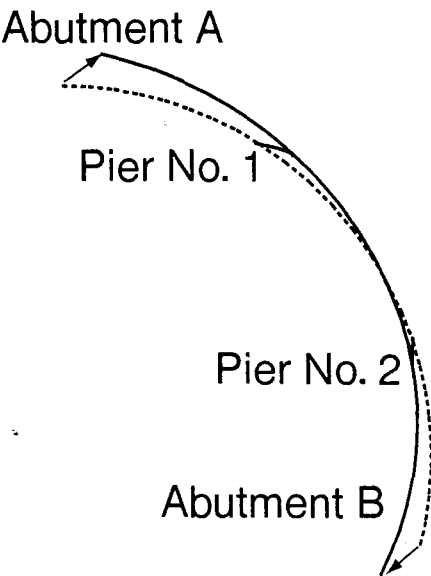
# Modal Behavior / Including Backfill



**Twisting**  
T=0.61 sec



**Transverse**  
T=0.29 sec



**Longitudinal**  
T=0.26 sec

# Effects of Curve for Example Bridge

---

- Both Abutment Backfills Are Effective or Not Effective at the Same Time (Do Not Put 1/2 K to Each)
- No Backfill Case Controls
  - Piers / Drilled Shafts
  - Piles
- Backfill Included Controls
  - End Diaphragm
  - Backfill Soil
- Torsional Stiffness of Superstructure Is More Influential in Forces Developed

# **Session 5**

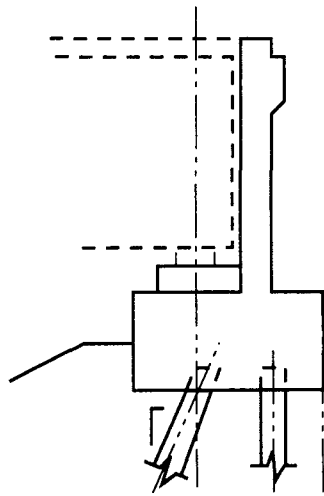
## **Piles**

---

- **Configuration and Behavior**
- **Including Flexibility in Analysis**
- **Coupling Effects**
- **Nonlinear Effects**
- **Multiple Pile Groups/Axial Stiffness**
- **Design and Detailing**

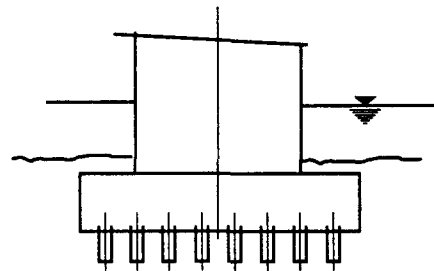


# Typical Configurations

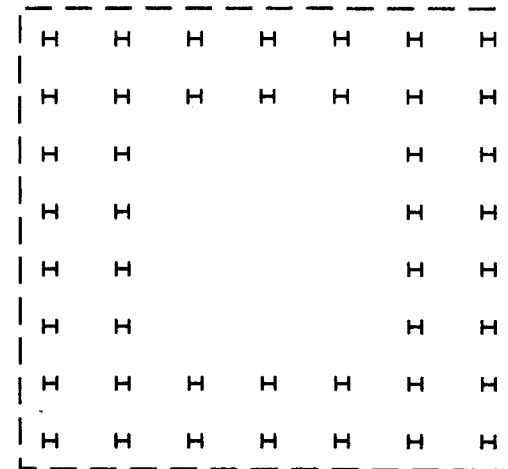


Piles Either Steel,  
Concrete, or Timber

**Abutment**

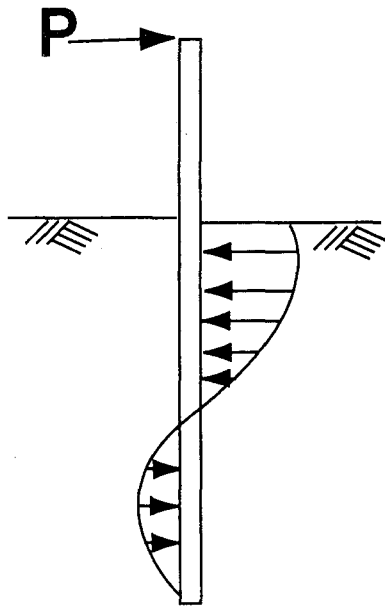


**Pier Section**

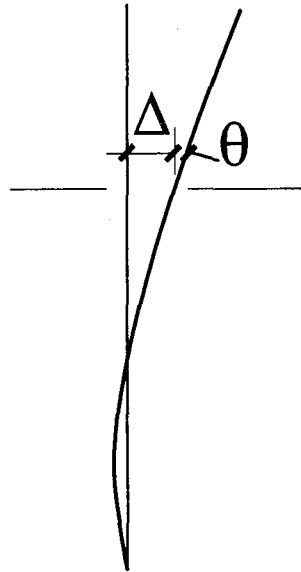


**Pier Plan**

# Behavior Under Lateral Loading

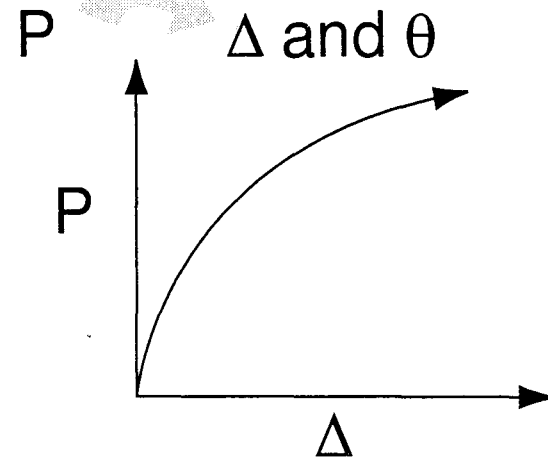


**Forces on Pile**

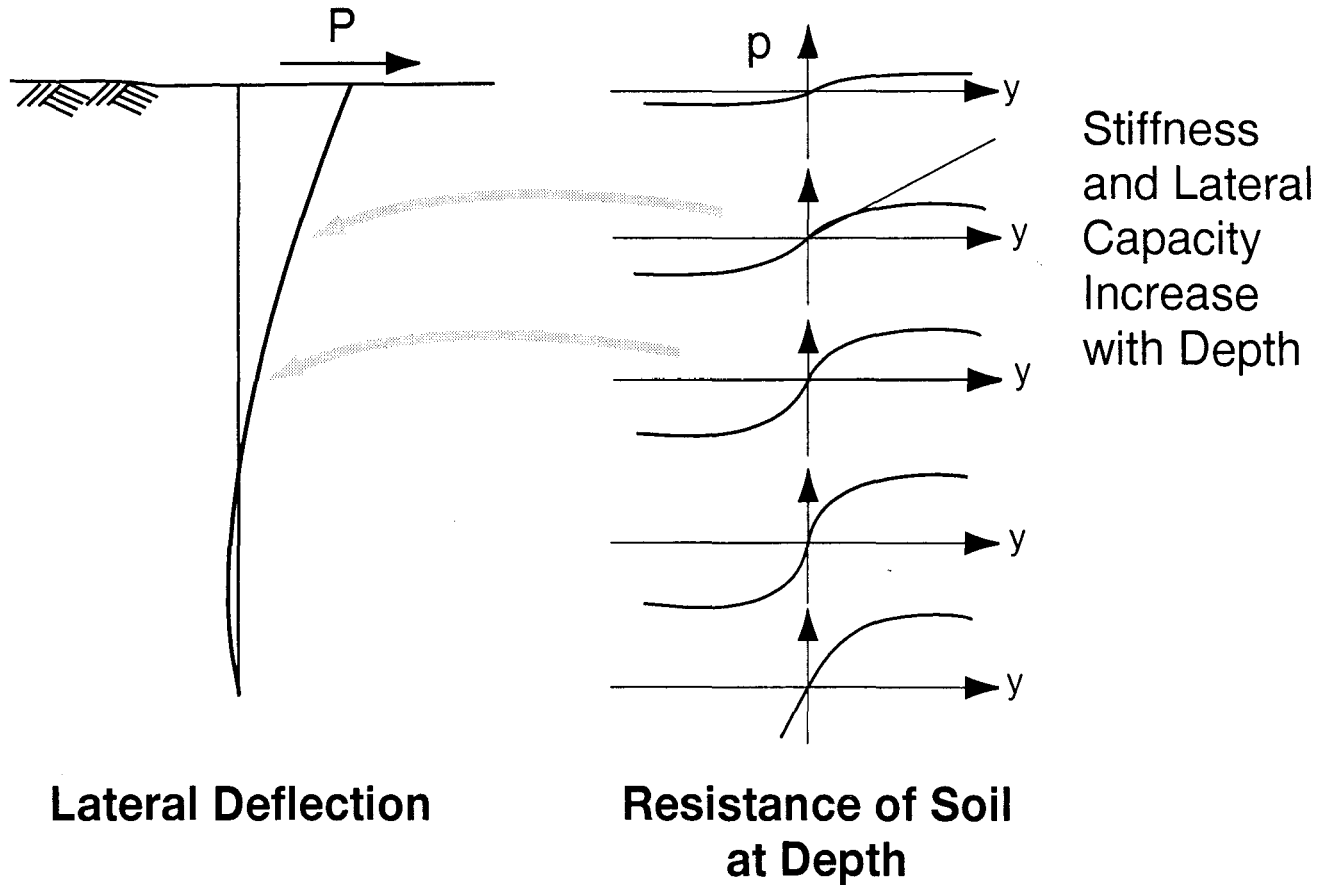


**Pile Lateral Deflection**

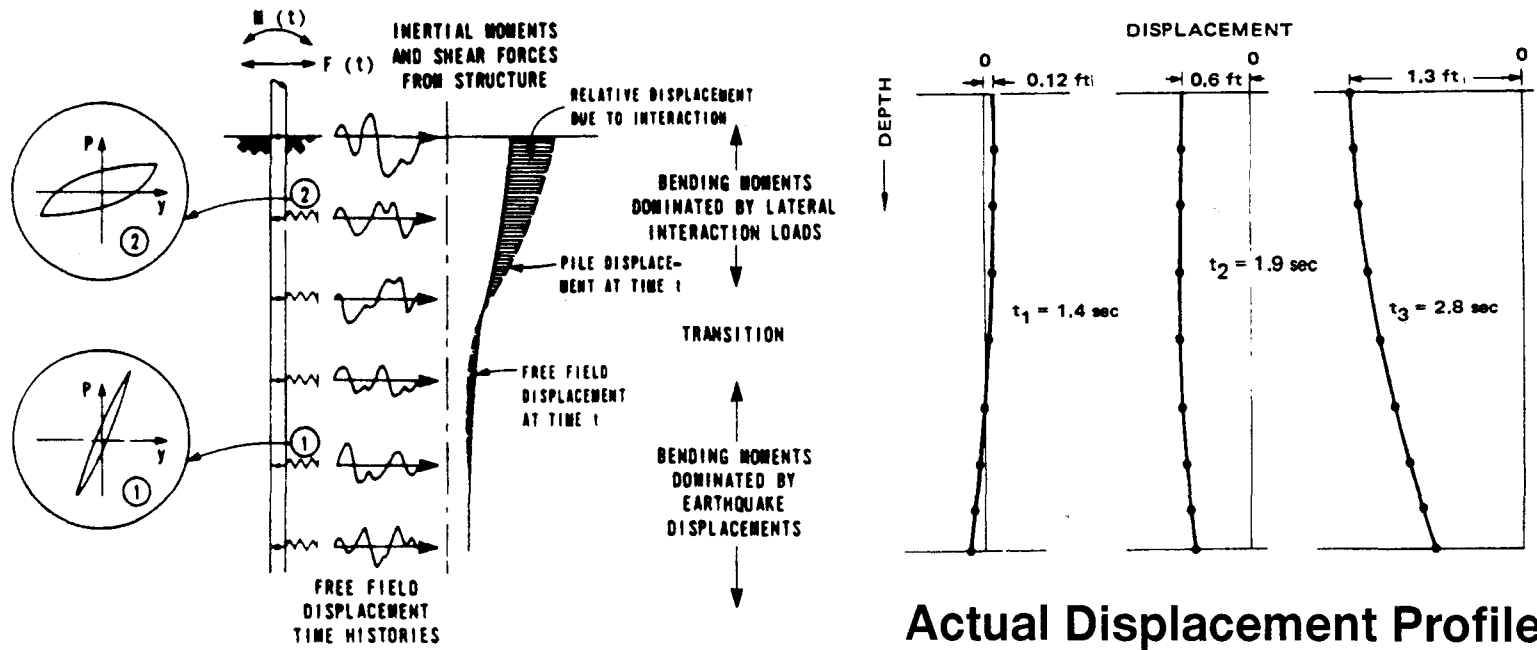
- $\Delta$  and  $\theta$  Are “Coupled”



# 'p-y' Relations (Curves) for Piles

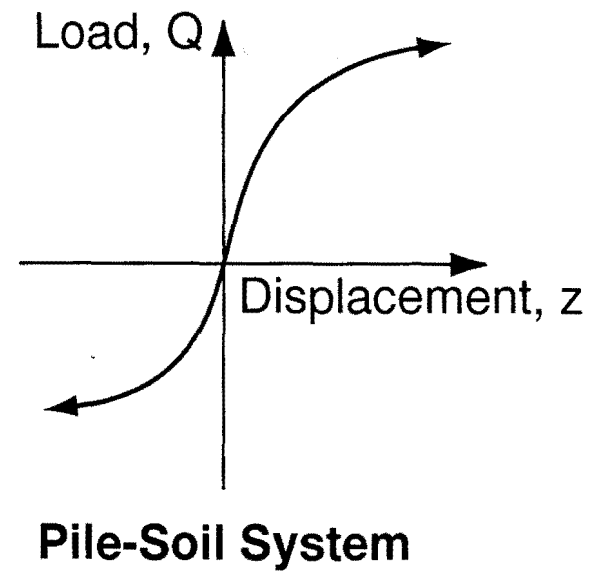
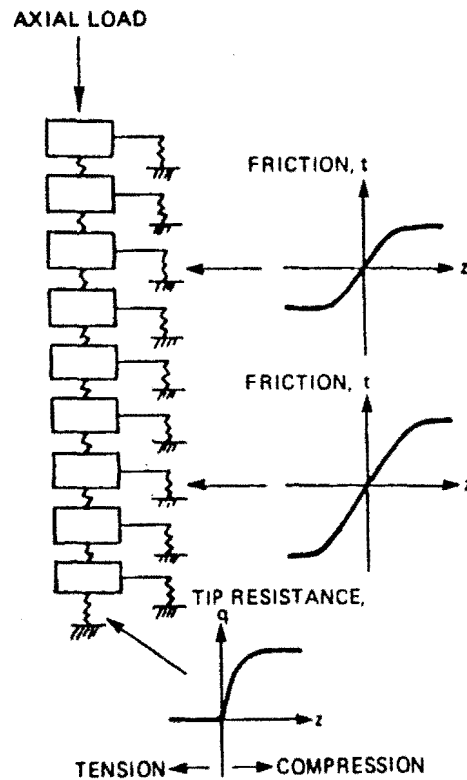
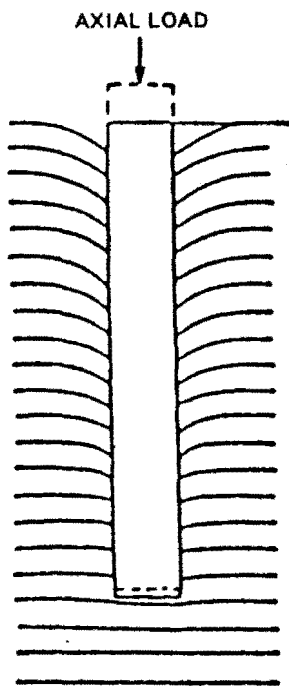


# Consideration of the Free-Field Ground Motion



AASHTO (1995)

# Behavior Under Vertical Loading



FHWA (1987)

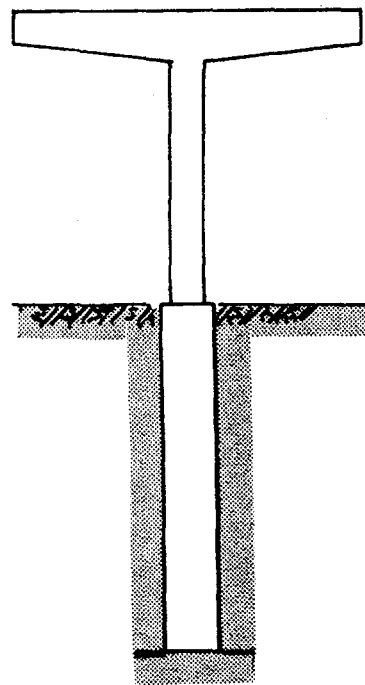
# Session 5

## Piles

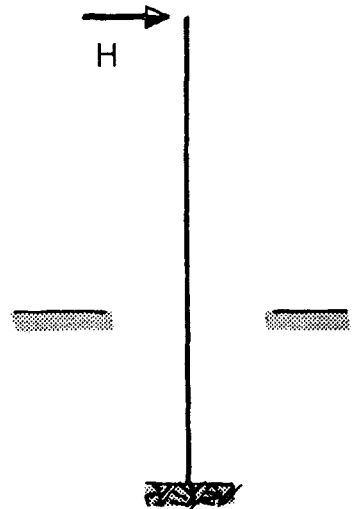
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- Configuration and Behavior
- **Including Flexibility in Analysis**
- Coupling Effects
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

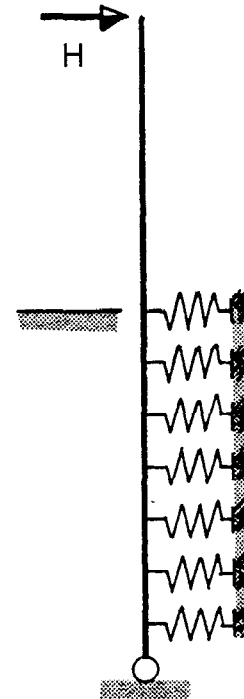
# Analytical Models of Pile Foundations



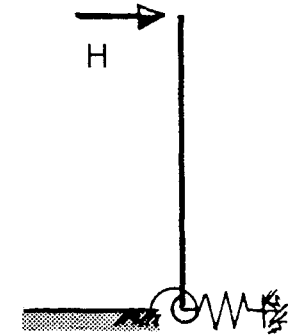
**Bridge Pile System**



**Equivalent  
Cantilever Model**



**Equivalent  
Soil Spring Model**



**Equivalent Base  
Spring Model**

FHWA (1987)

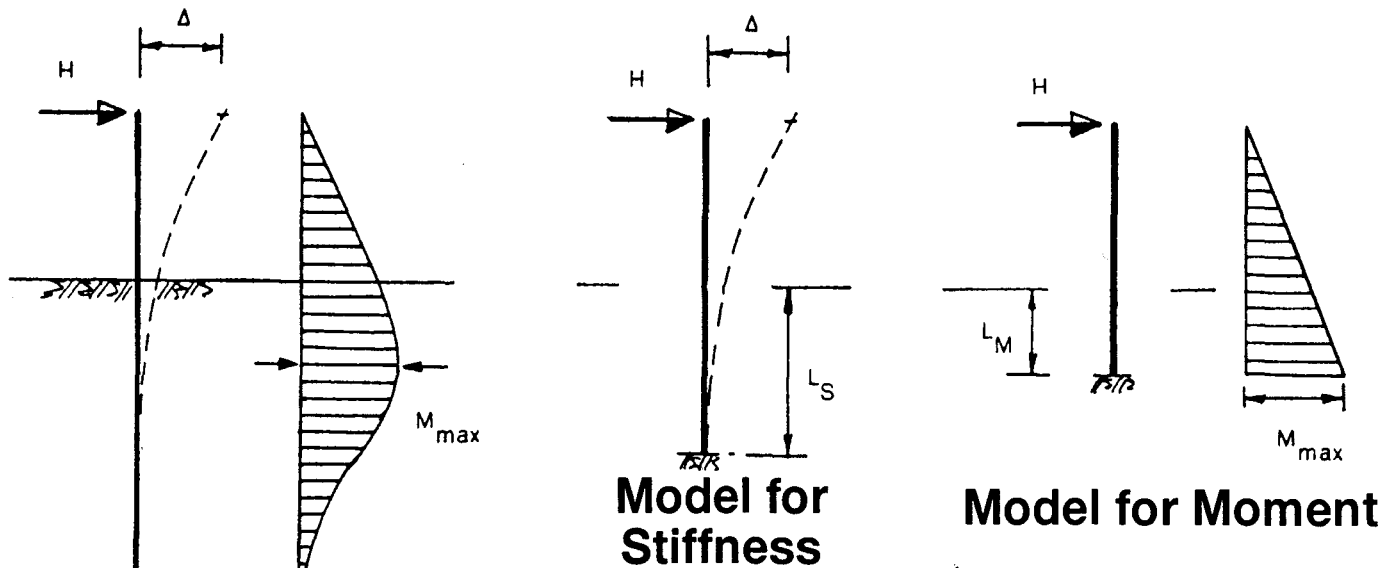
Session 5 Page 21 of 58

UMD-ITV

Seismic Bridge Design Applications

25 July 1996, NHI Course Code No. 13063

# Equivalent Cantilever Method



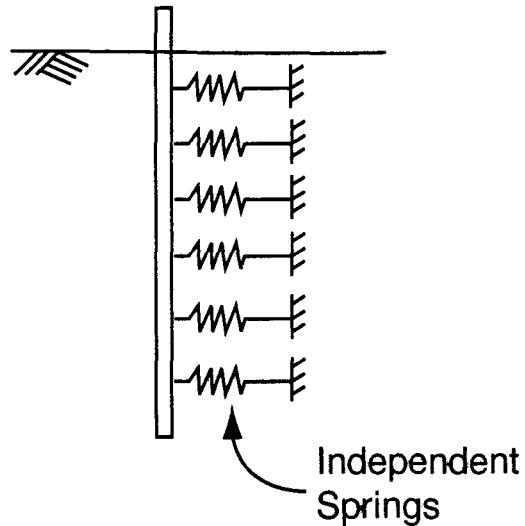
	$L_s$	$L_M$
Cohesive Soil Constant $K_h$	$1.4 \sqrt[4]{\frac{EI}{K_h}}$	$0.44 \sqrt[4]{\frac{EI}{K_h}}$
Cohesionless Soil Constant $n_h$	$1.8 \sqrt[5]{\frac{EI}{n_h}}$	$0.78 \sqrt[5]{\frac{EI}{n_h}}$

FHWA (1987)

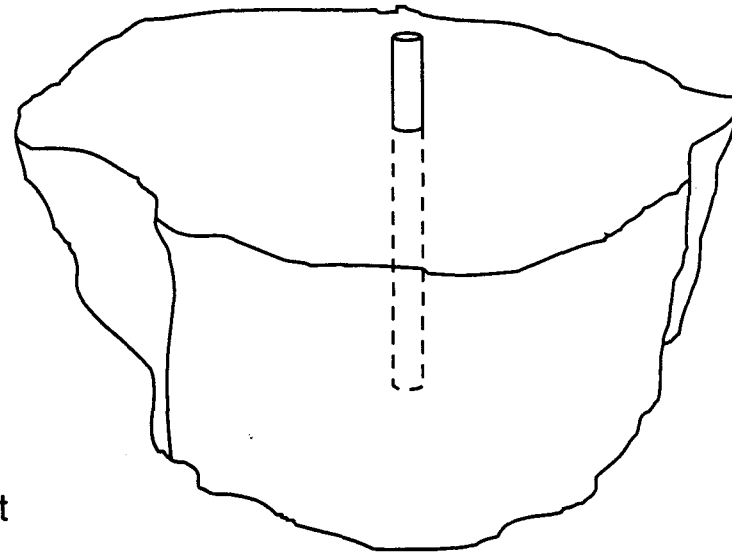


# Determining Piles-Soil Stiffness

Most  
Common



**Subgrade Reaction Method**



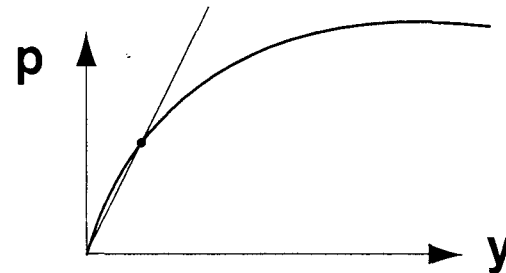
**Elastic Continuum  
(Half-Space)**

# Subgrade-Reaction Method (Linear Elastic)

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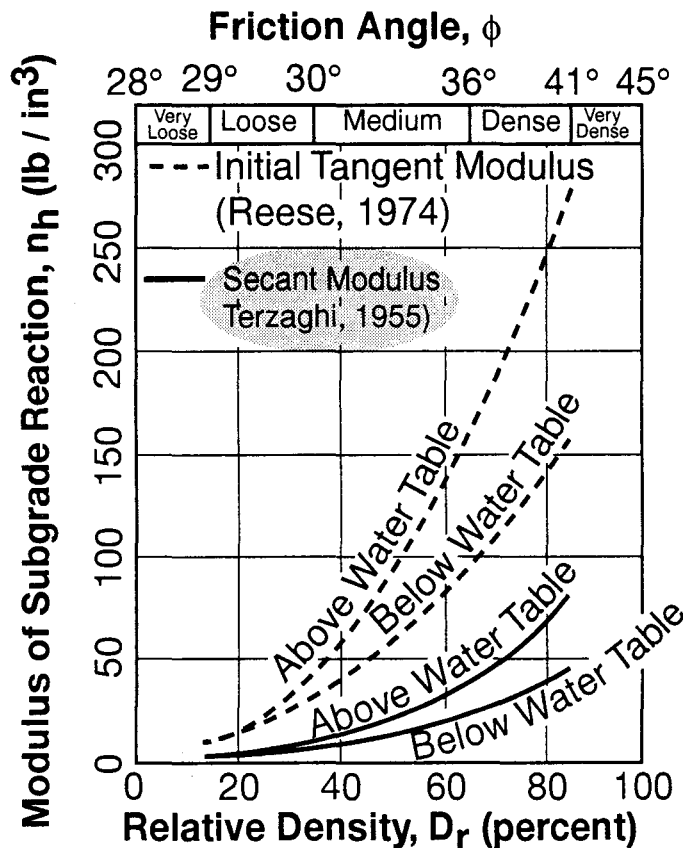
- **Basis** (Assumptions)

- Known Modulus of Subgrade Reaction,  $n_h$
- Modulus, Function of Depth and Lateral Stiffness Is Independent of the Pile Diameter (Cohesionless and Cohesive)
- Stiffness Typically Is Secant and Applies for About 1/3 of Ultimate Capacity



References: FHWA/RD-86/102 (1986)  
NAVFAC DM7.02 (1986)  
Poulos and Davis (1980)

# Modulus of Subgrade Reaction / Cohesionless



- **Modulus at Depth z:**  

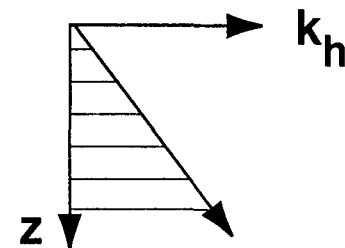
$$k_h = n_h \frac{z}{D} \quad (\text{kip/ft}^3)$$

D = Diameter

- **Spring Stiffness:**  

$$K_h = k_h DH$$

H = Tributary Height



FHWA (1986)

# Modulus of Subgrade Reaction / Cohesive

- Modulus at Depth

$$k_h = k_0 + k_1 z$$

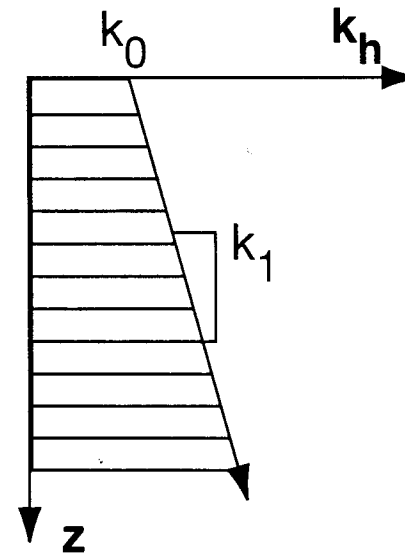
$$k_0 = 0.6 c / \epsilon_c$$

$$k_1 = \frac{0.2}{\epsilon_c} \left( \gamma + \frac{0.25 c}{D} \right)$$

$c$  = Undrained Shear Strength

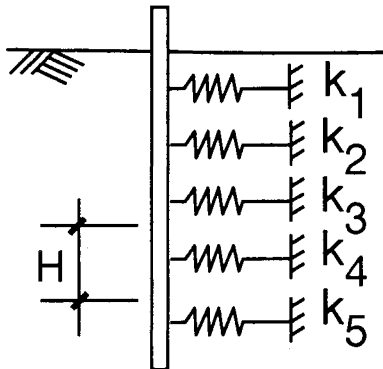
$\gamma$  = Effective Unit Weight

$\epsilon_c$  = Strain Amplitude at 1/2  
Peak Deviatoric Stress



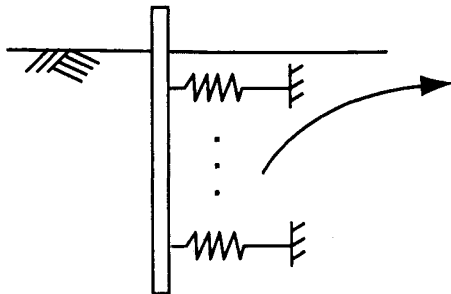
FHWA (1986)

# Including Stiffness



## DIRECT

- Use Equations for Subgrade Method and Calculate  $K_1, \dots$  etc.
- Include  $K$ 's in Model Along with Pile



## INDIRECT

- Use Existing (Linear Elastic) Solutions that Give Spring Stiffness at Ground Surface

# Example of 'Indirect' Method

---

- **Use Influence Charts (NAVFAC DM7.02, for Example)**

1. Find  $n_h$  for Soil Type

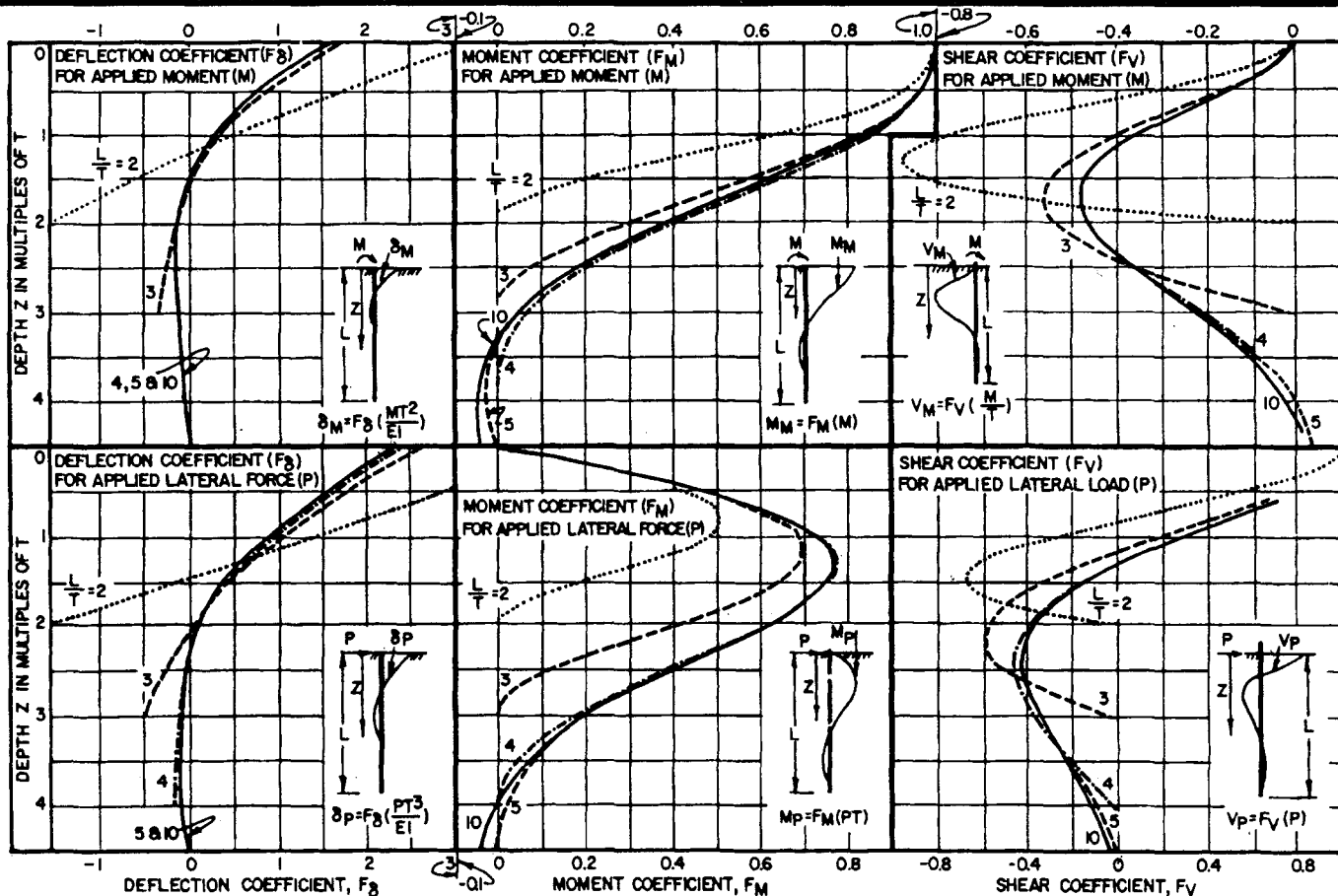
2. Determine Characteristic Length,  $T = \left( \frac{EI}{n_h} \right)^{1/5}$

3. Calculate  $L / T$  ( $L$ =Pile Length)

4. Use Charts to Calculate Stiffness, Moment, and Shear — Free or Fixed Head Piles

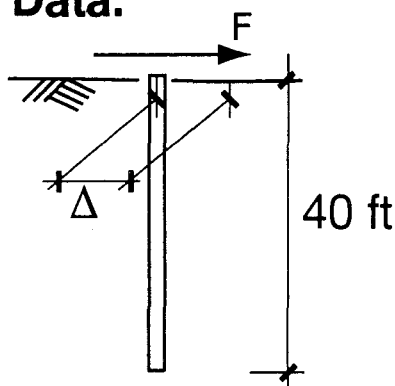
(Use Superposition — Treat Forces and Moments Applied to Pile Separately)

# NAVFAC DM7.02 Coefficients / Free Head



## Example / 'DM7' Method (1 of 3)

**Data:**



**12 in. Concrete-Filled Pipe Pile / Free Head /**

$I = 406 \text{ in}^4$  (Pipe + Concrete - Upper Bound)

$E_s = 29000 \text{ ksi}$

**Soil (Cohesionless)  $\phi \approx 33^\circ$  ( $n_h = 23 \text{ pci}$ )**

**Required:** Lateral Translational Stiffness

$$\text{Characteristic Length, } T = \left( \frac{EI}{n_h} \right)^{1/5} = \left( \frac{29000(406)}{0.023} \right)^{1/5} = 55.1 \text{ in.}$$



## Example / 'DM7' Method (2 of 3)

$$\frac{L}{T} = \frac{40(12)}{55.1} = 8.7$$

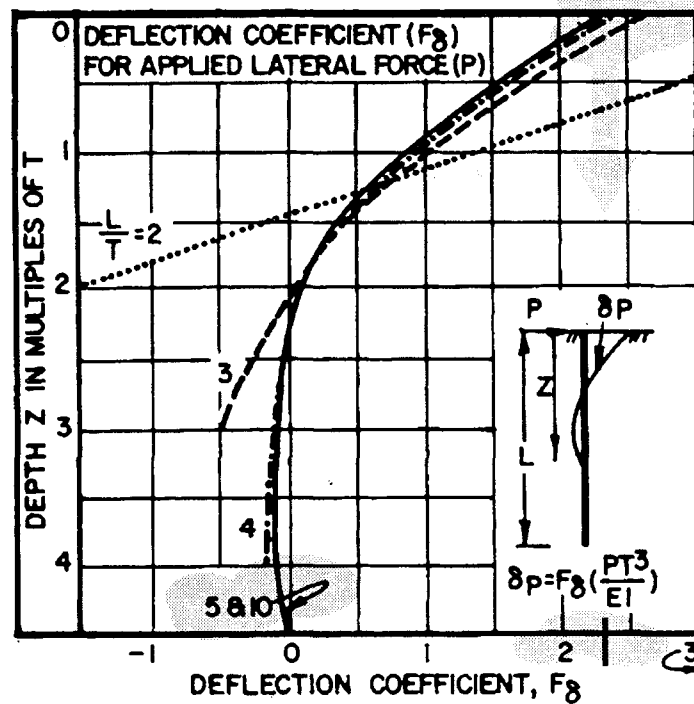
For Stiffness, Use:

$$z=0 \text{ ft} \rightarrow F_{\delta} = 2.3$$

$$K = \frac{P}{\delta_P} = \frac{EI}{F_{\delta} T^3}$$

$$K = \frac{(29000) 406 (12)}{2.3 (55.1)^3}$$

$$K = 367 \text{ kip / ft}$$



# Example / Check Using 'Equivalent Cantilever' (3 of 3)

---

• **Cantilever Length**

$$L_s = 1.8 \sqrt[5]{\frac{EI}{n_h}} = 1.8 \sqrt[5]{\frac{29000(406)}{0.023}}$$

$$L_s = 99.3 \text{ in.}$$

• **Stiffness**

$$K = \frac{3EI}{L_s^3} = \frac{3(29000)406(12)}{(99.3)^3} = 433 \text{ kip / ft}$$

vs. 367 kip / ft

# Session 5

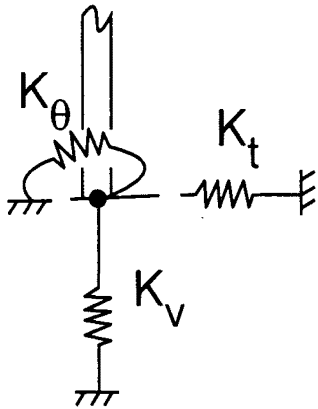
## Piles

---

- Configuration and Behavior
- Including Flexibility in Analysis
- **Coupling Effects**
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

# Coupling Effects / Overview

## No Coupling



- Individual Springs

$$P = K_t \Delta_t$$

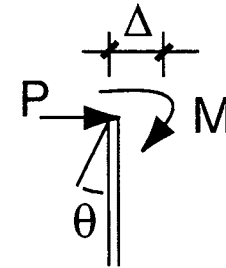
$$M = K_\theta \theta$$

$$V = K_v \Delta_v$$

## Coupling (P and M)

$$P = K_{tt} \Delta + K_{t\theta} \theta$$

$$M = K_{\theta t} \Delta + K_{\theta\theta} \theta$$



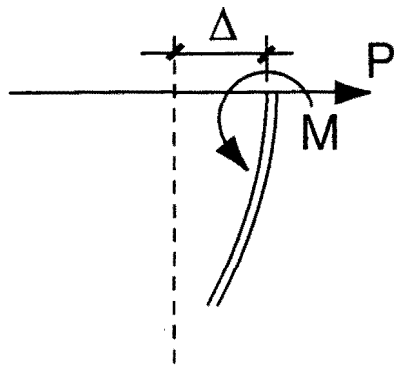
- Apply P Alone  $\rightarrow$   $\Delta$  and  $\theta$
- Apply M Alone  $\rightarrow$   $\Delta$  and  $\theta$
- Include in Model with Either Stiffness or Flexibility Matrix for Foundation Node

# Calculating Coupled Stiffnesses (1 of 3)

- **Desired**  $K_{tt}, K_{t\theta}, K_{\theta t}, K_{\theta\theta}$   
Coupling Terms

- **Obtain These By**

1. Hold  $\theta = 0$  / Apply  $\Delta = 1$  / Calculate  $P$  and  $M^*$



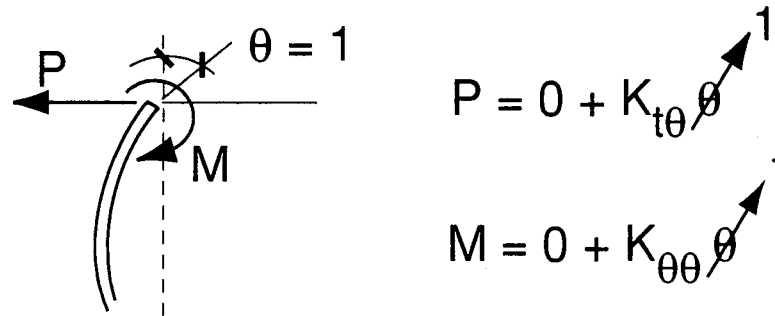
$$P = K_{tt}\overset{1}{\Delta} + K_{t\theta}\overset{0}{\theta} = K_{tt}$$

$$M = K_{\theta t}\overset{1}{\Delta} + K_{\theta\theta}\overset{0}{\theta} = K_{\theta t}$$

\*Use Fixed-Head Charts Provided at End of Section

## Calculating Coupled Stiffnesses (2 of 3)

2. Hold  $\Delta = 0$  / Apply  $\theta = 1$  / Calculate P and M



(See Outline of Method on Next Page)

3. Check / If Linear Elastic  $\rightarrow K_{t\theta} = K_{\theta t}$

- **Analysis Programs Use These Coefficients**  
(These Are Terms of "6 x 6 Matrix")

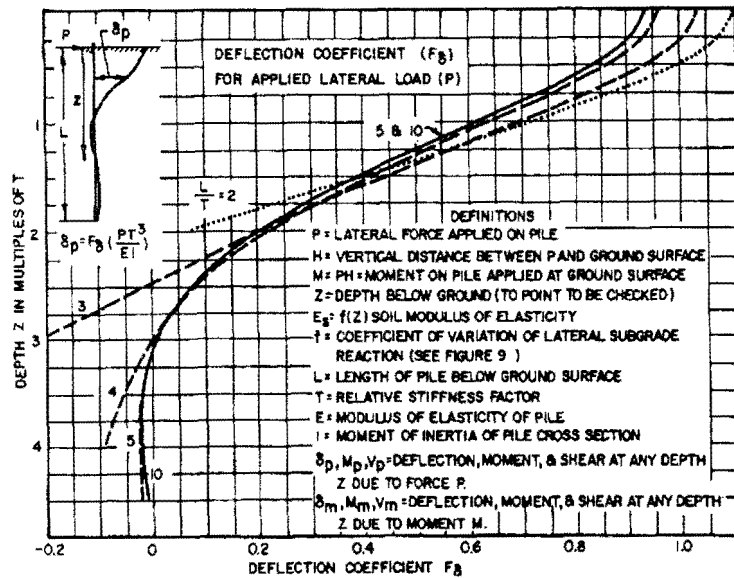
# Calculating Coupled Stiffnesses (3 of 3)

---

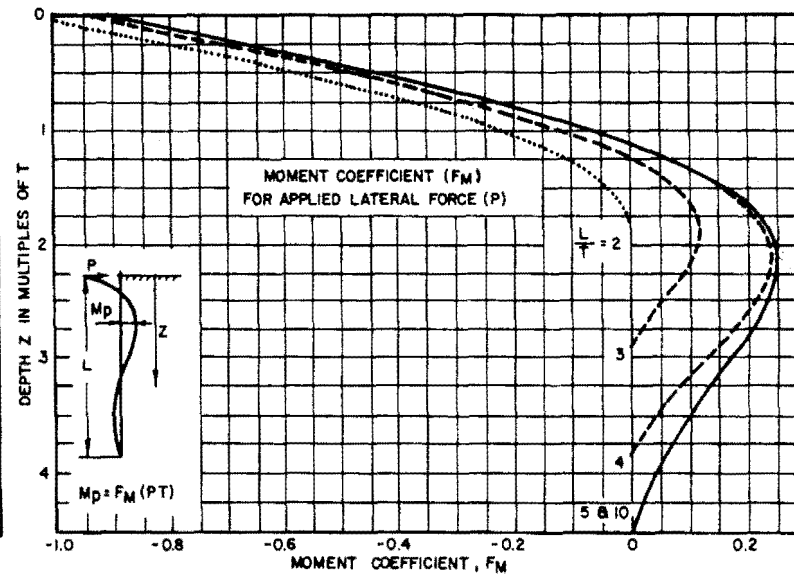
## Outline for Calculating $K_{t\theta}$ and $K_{\theta\theta}$

1. Apply Only P (Free Head)
  - Calculate  $\Delta$  and  $\theta$  (Slope) at Surface  
(Charts for Slope Given at End of Section)
2. Apply Only M (Free Head)
  - Calculate  $\Delta$  and  $\theta$  at Surface
3. Form Superposition of Scaled P & M to Give  $\theta = 1$  and  $\Delta = 0$

# Influence Coefficient / Fixed Head NAVFAC DM7.02 (1986)



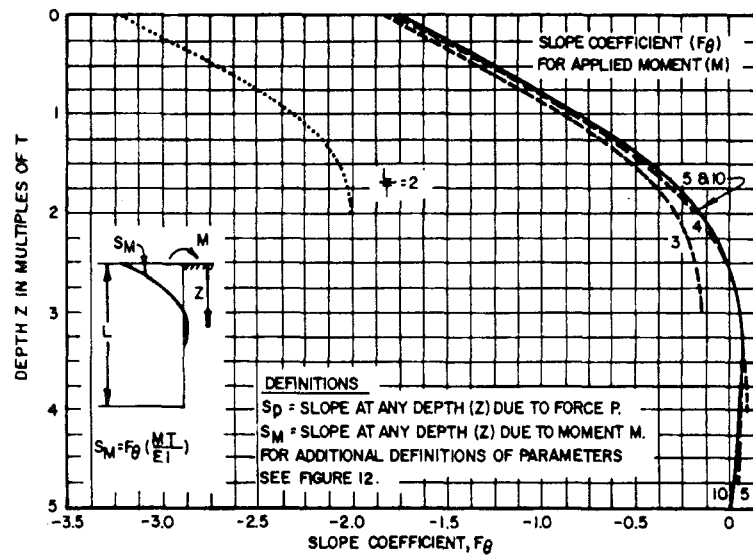
**Deflection for Applied Load**



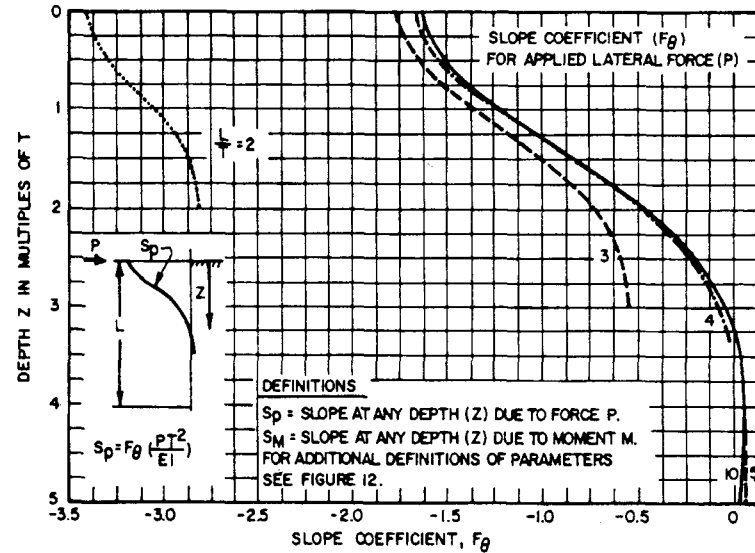
**Moment for Applied Load**



# Slope (Rotation) of Piles / NAVFAC DM7.02



**Slope for Applied Moment**



**Slope for Applied Load**

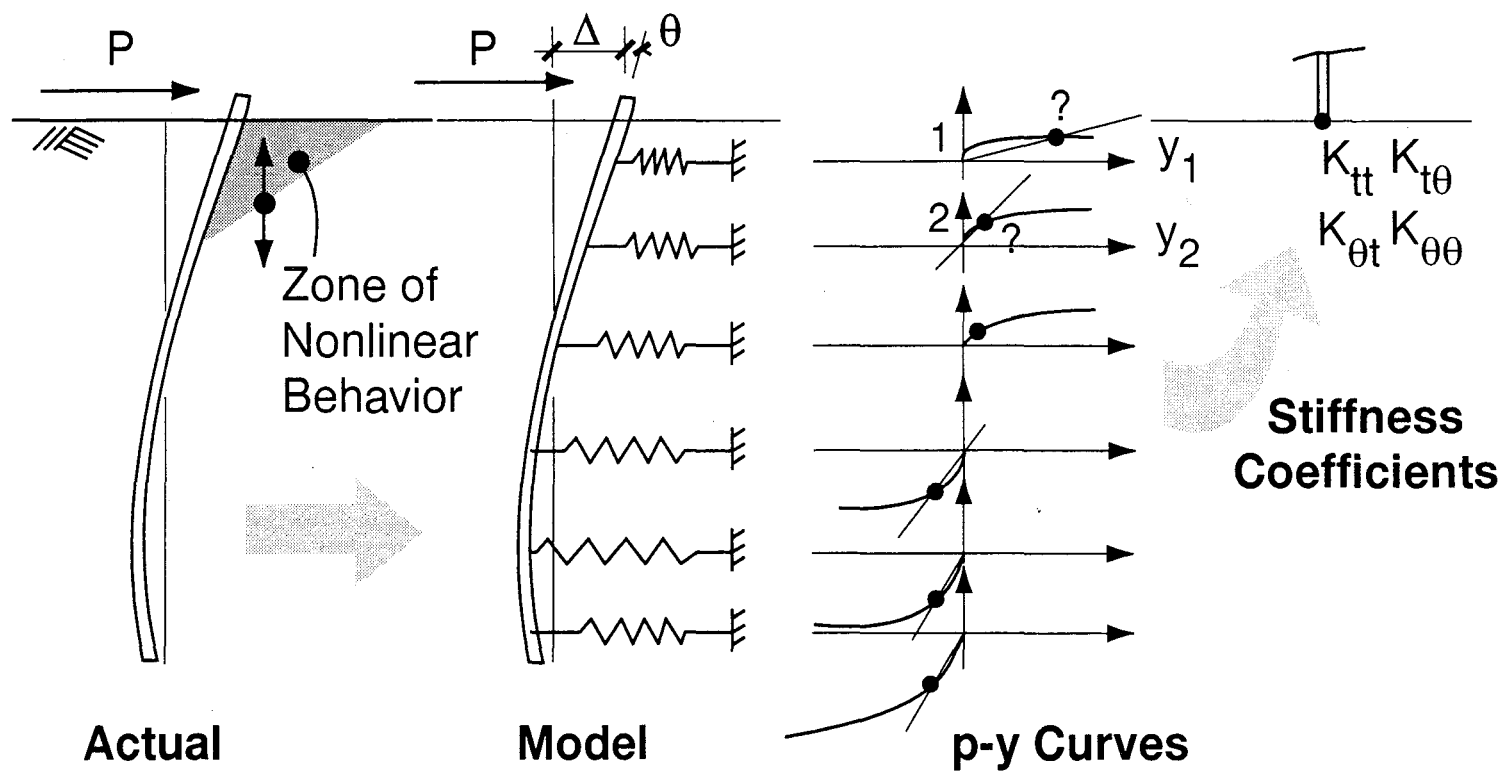
# Session 5

## Piles

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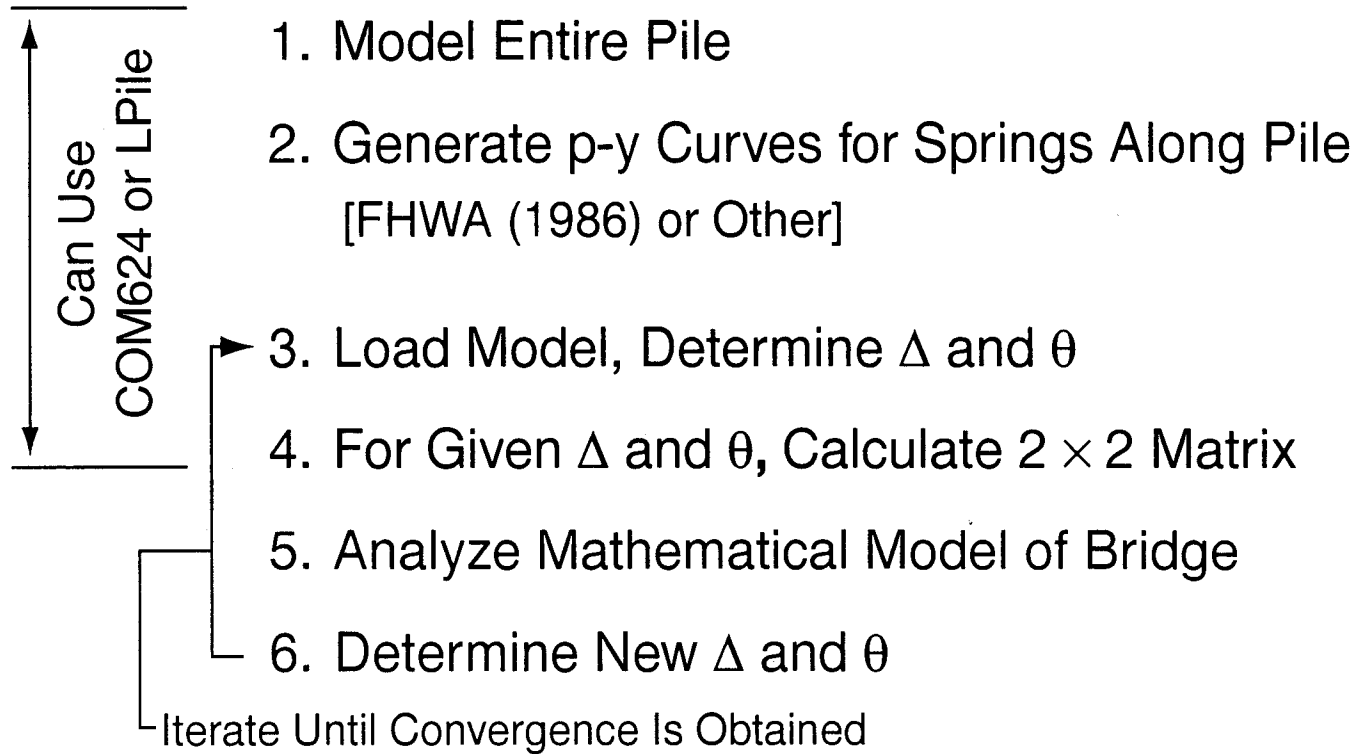
- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- **Nonlinear Effects**
- Multiple Pile Groups / Axial Stiffness
- Design and Detailing

# Nonlinear Effects of Soil



# Developing Stiffness for Nonlinear Case

---



# Session 5

## Piles

---

- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- Nonlinear Effects
- **Multiple Pile Groups / Axial Stiffness**
- Design and Detailing

# Effects of Closely Spaced Piles

---

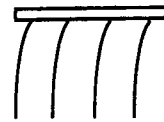
- **Group Effects**

<u>Pile Spacing in Direction of Loading</u>	<u>Reduction for Subgrade Modulus, <math>n_h</math></u>
8D .....	1.00
6D .....	0.70
4D .....	0.40
3D .....	0.25

D = Pile Diameter

# Stiffness for Pile Groups / Rigid Cap

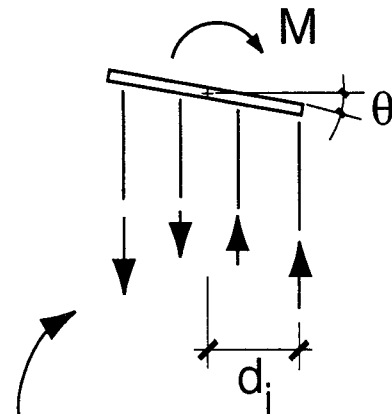
- Translation



$$K = nK_t$$

n Piles

- Rotation

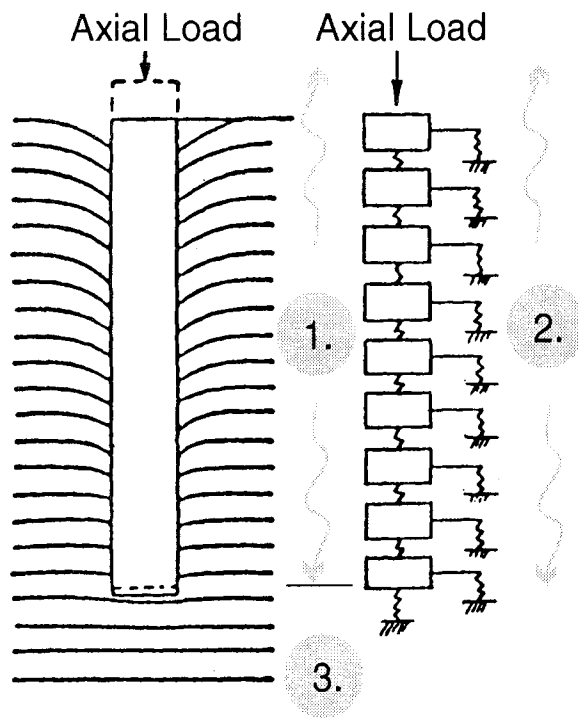


$$K_{\theta \text{ group}} \approx \sum_{i=1}^n K_{\text{axial}} d_i^2 = \frac{M}{\theta}$$

↻ Axial K Most Important

# Axial Stiffness Components

## Vertical Loading Behavior



FHWA (1986)

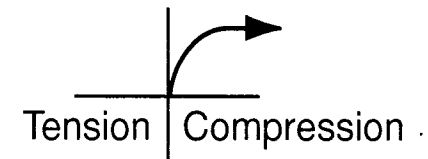
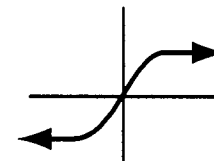
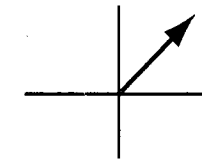
### Components of Flexibility

1. Pile Stiffness

2. Side Friction

3. End Bearing

### Force / Deformation





# Axial Stiffness of Piles

**1. Pile Stiffness** —  $\frac{AE}{L}$

**2. Side Friction** —  $f = f_{\max} \left( 2\sqrt{\frac{z}{z_c}} - \frac{z}{z_c} \right)$

(No Universal Agreement,  
'a Way to Do It')

$f_{\max}$  = Maximum  
Unit Friction

$z$  = Slip

$z_c$  = Critical Slip (0.2 in)

**3. End Bearing** —  $q = \left( \frac{z}{z_c} \right)^{1/3} q_{\max}$

(No Universal Agreement,  
'a Way to Do It')

$q_{\max}$  = Maximum  
Tip Resistance

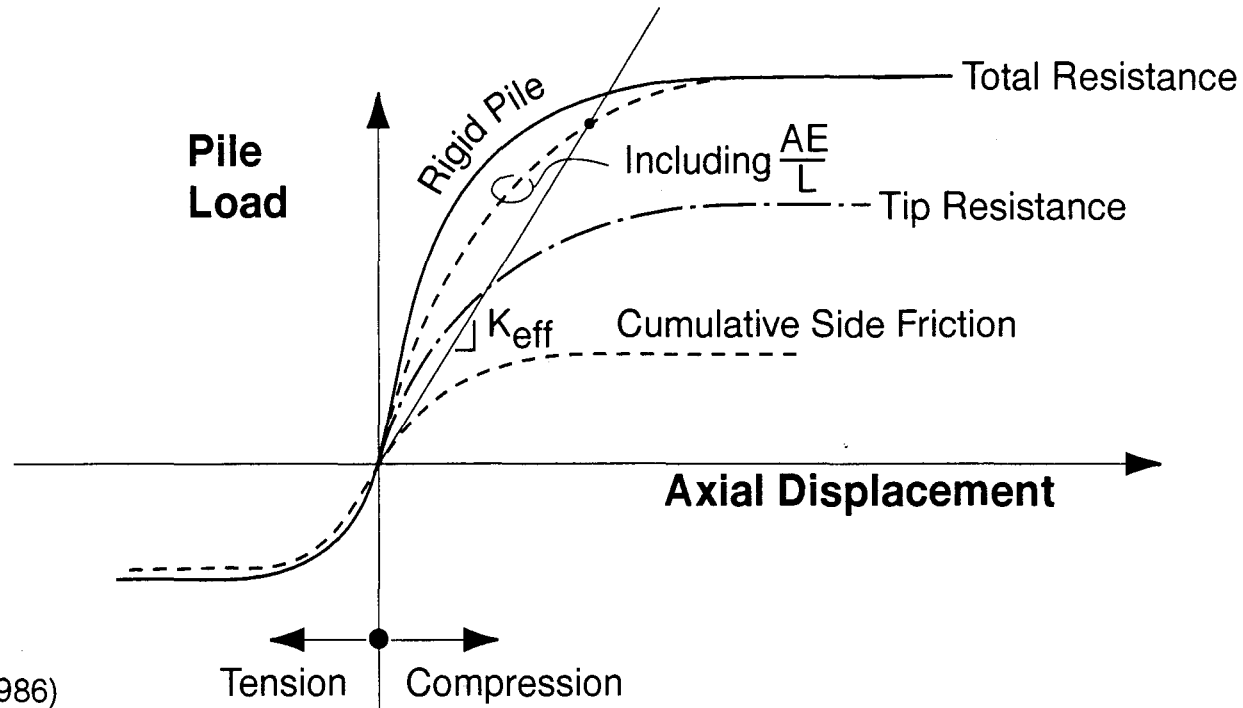
$z$  = Deflection at Tip

$z_c$  = Critical Displacement  
at  $q_{\max} \sim 0.05$  Diameter

FHWA (1986)

# Axial Stiffness of Piles (continued)

Sum (Integrate) Expressions to Obtain:



FHWA (1986)

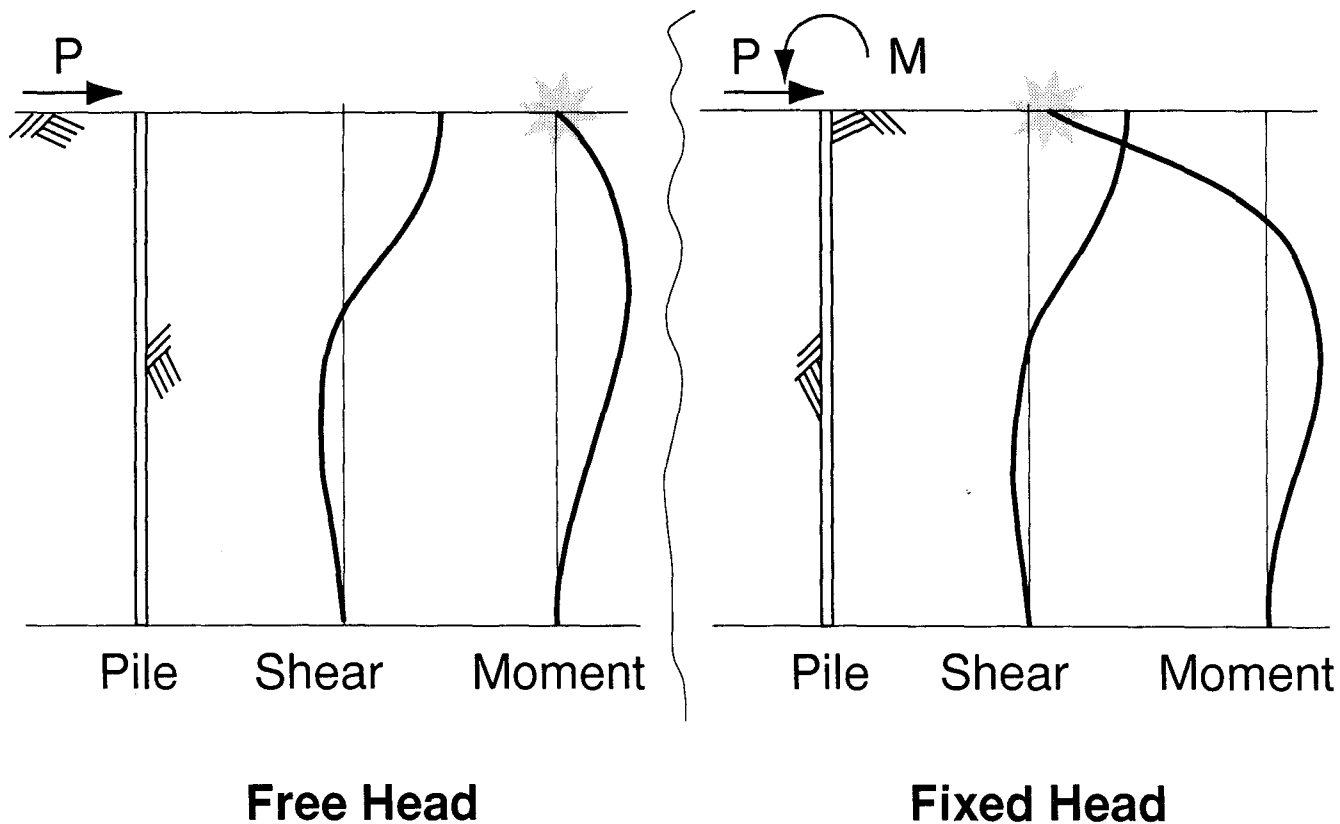
# Session 5

## Piles

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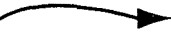
- Configuration and Behavior
- Including Flexibility in Analysis
- Coupling Effects
- Nonlinear Effects
- Multiple Pile Groups / Axial Stiffness
- **Design and Detailing**

# Internal Force Distributions (Elastic)



# Effect of Head Condition

---

- **Performance Objective**  Damage Should Be Detectable  
∴ Not in Foundation
- **Design**  Elastic or Plastic Hinging Forces

Fixed Head — Large Moment / Concentrated Near  
Top of Pile  
∴ Potential for Plastic Hinging

Free Head — Largest Moment at Depth /  
Distributed Curvatures

# Division I-A Requirements (1 of 6)

---

## Overview

- Capacity Protect /  $R = 1.0$  or Hinging Forces
  - Tie Piles and Cap Together
  - Provide Ductility at Top of Pile
- 

## SPC B / 6.4.2 (C)

- Design to Carry All Forces

Plus

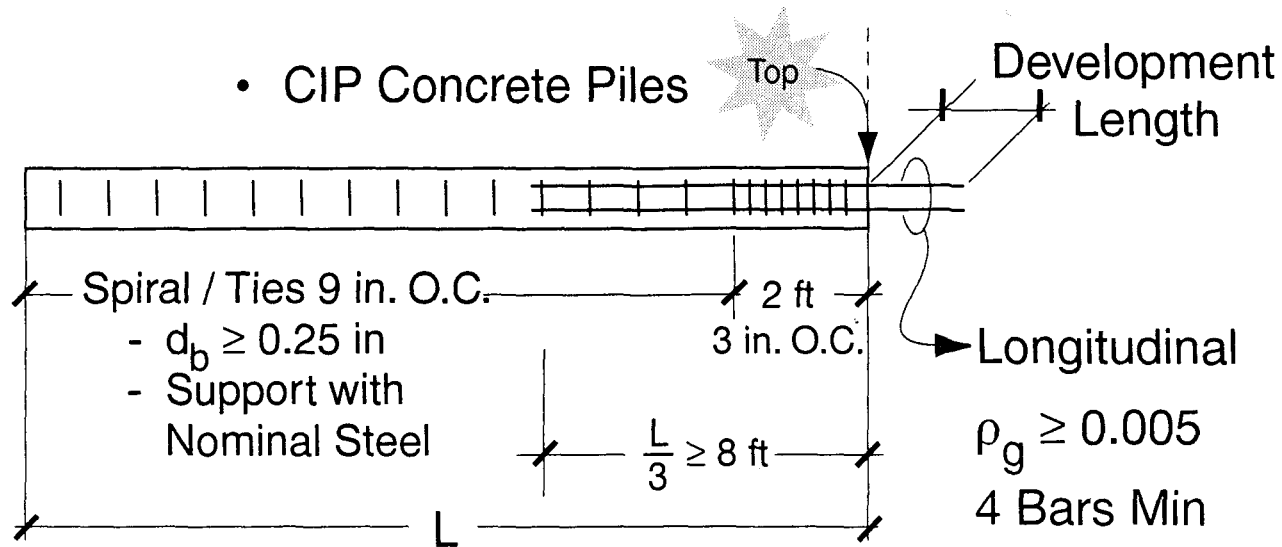
- Timber and Steel — Uplift Capacity  $\geq 10\%$  of Allowable Pile Load

# Division I-A Requirements (2 of 6)

## SPC B / 6.4.2 (C) (continued)

- Concrete-Filled Pipe Pile — 4 Dowels /  $\rho = 0.01$   
(Note: Completely Free Head Not Realistic)

- CIP Concrete Piles



# Division I-A Requirements (3 of 6)

---

## SPC B / 6.4.2 (C) (continued)

- Precast Piles
  - $\rho_g \geq 0.01$  (4 Bars Min) Over Entire Length
  - Spiral / Ties  $\geq \#3$
  - Spacing as for CIP Piles
- Precast — Prestressed Piles
  - Same Ties as for Precast Piles



# Division I-A Requirements (4 of 6)

---

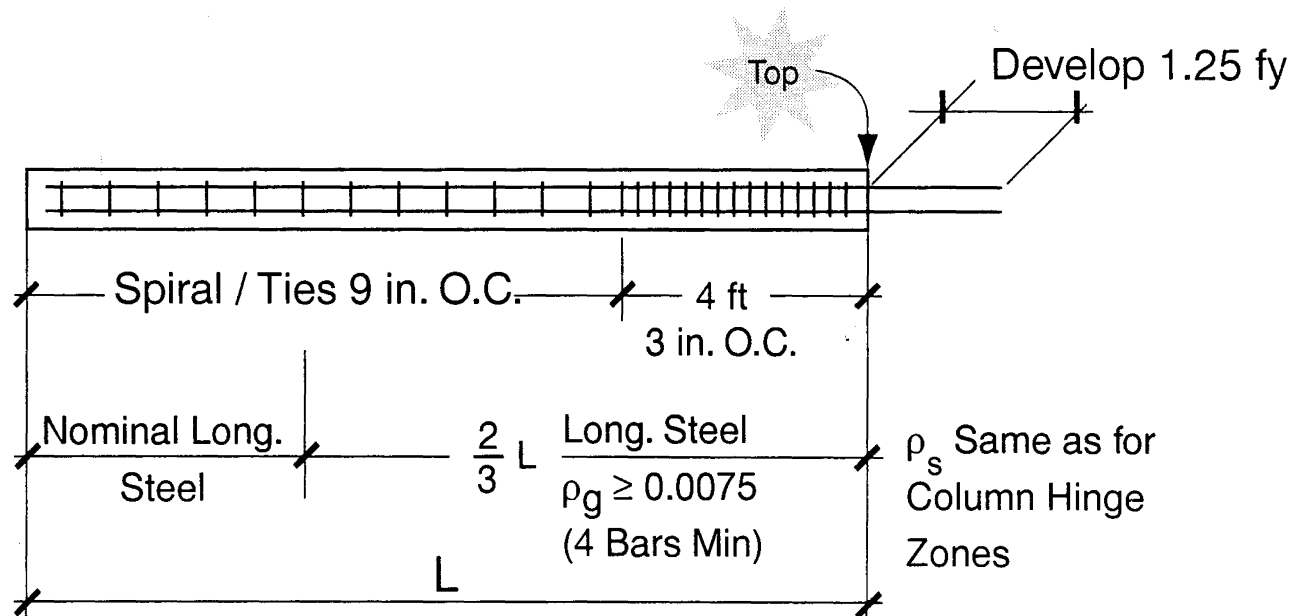
## SPC C and D / 7.4.2 (C)

- Same as SPC B
- Concrete Piles
  - Anchor to Cap to Develop  $1.25 f_y$  of Pile Longitudinal Bars
- Potential Plastic Hinge Zones
  - Same Confinement as for Columns!
  - $2D_{pile}$  or 24 in. at Top or Other Possible Hinge Zones

# Division I-A Requirements (5 of 6)

## SPC C and D / 7.4.2 (C) (continued)

- CIP Concrete Piles



# Division I-A Requirements (6 of 6)

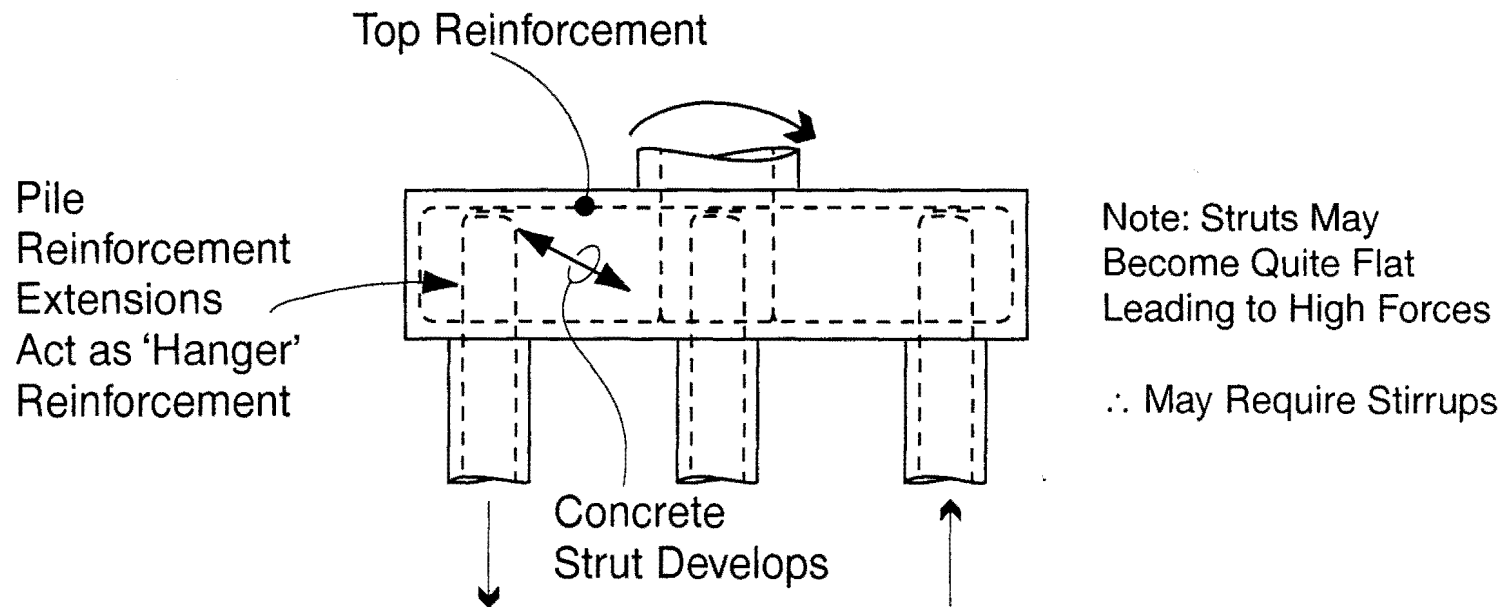
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## SPC C and D / 7.4.2 (C)

- Precast Piles
  - $\rho_g \geq 0.01$  (4 Bars Min) Over Entire Length
  - Spiral / Ties  $\geq \#3$
  - Spacing as for CIP Piles
- Precast — Prestressed Piles
  - Same Ties as for Precast Piles

# Pile Cap Considerations for Uplift Forces

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# **Session 6**

## **Curved Box Girder Bridge Example**

### **Drilled Shaft\***

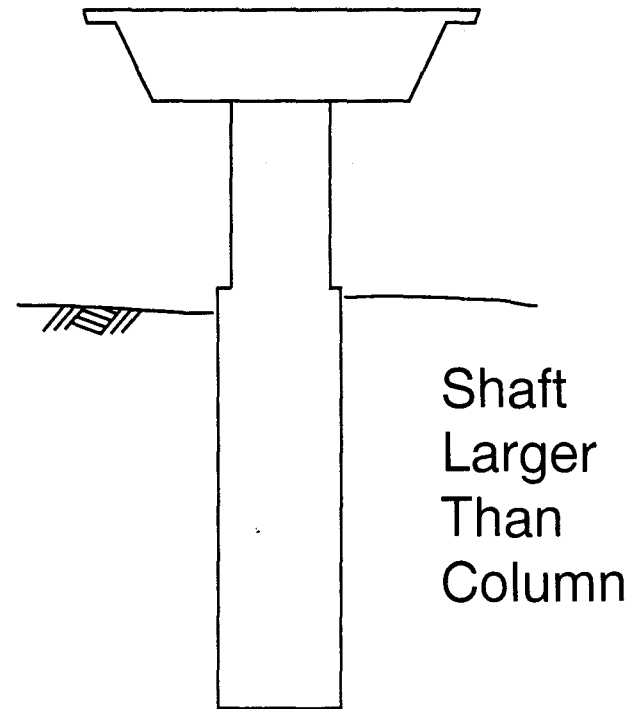
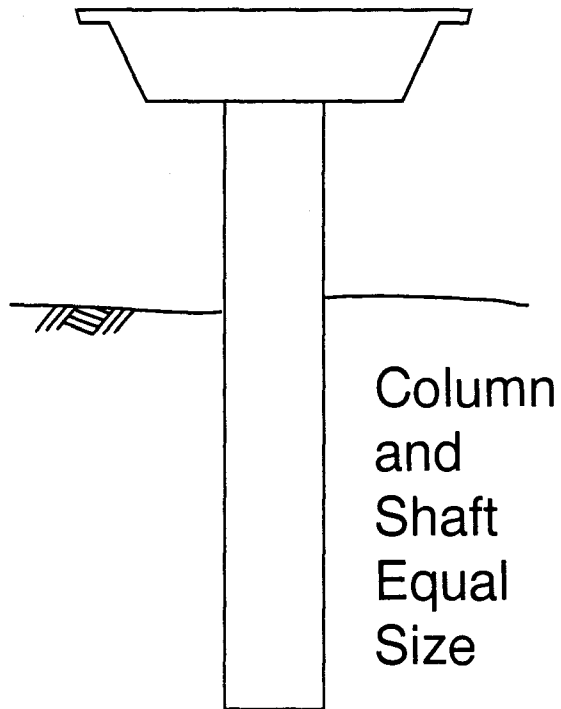
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- **Behavior and Stiffness**
- **Design and Detailing**

\* Also Called Pile Shafts, etc.

# Configurations

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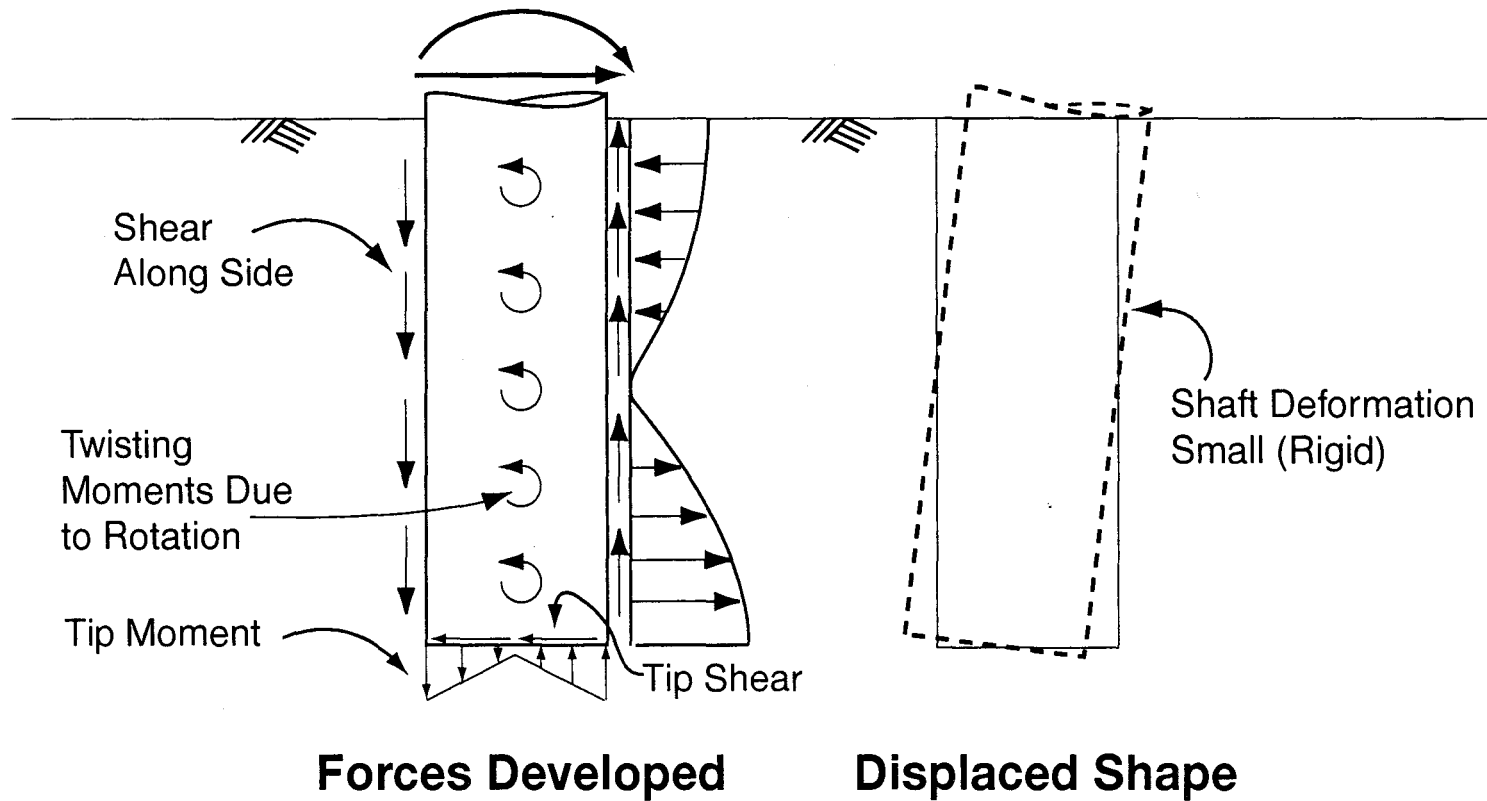


# Drilled Shaft Behavior

---

- Lateral Behavior Similar to Piles
- Length / Diameter (or  $L / T$ ) Smaller Than Piles
  - Stiffness Less Than Longer Elements of Same Diameter
  - Lateral Stiffness More Sensitive to ( $L / T$ )
  - Coupling Between Displacement and Rotation More Important
- Larger Diameters Lead to Additional Mechanisms for Resistance

# Mechanisms of Lateral Resistance



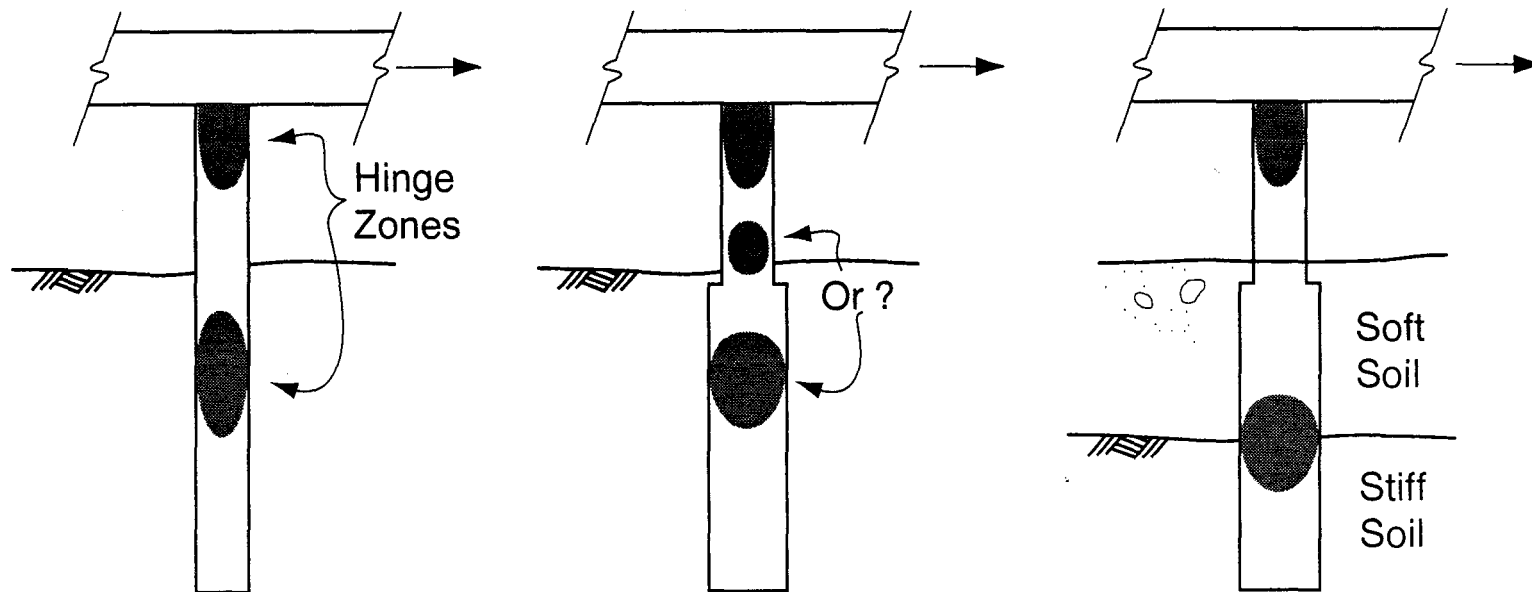


# Developing Stiffness of Drilled Shafts

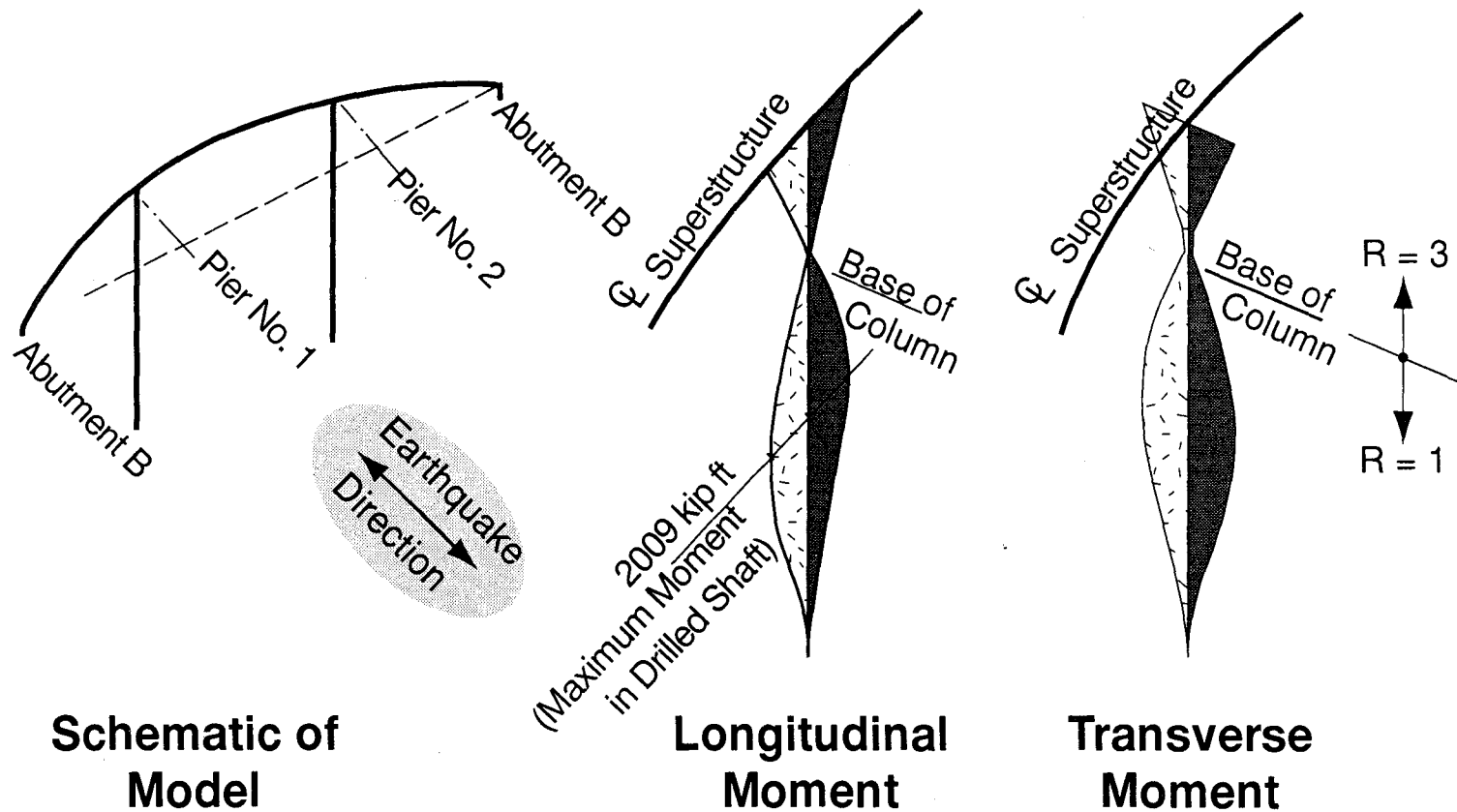
---

- Use Same Approach as for Piles
- Neglect Additional Resistance Mechanisms  
(May Underpredict Strength)
- Include Coupling Effects (More Critical Than with Piles)
- Some Methods Are Under Development for Including  
All Resistance Mechanisms  
(Approaches May Change in the Future)

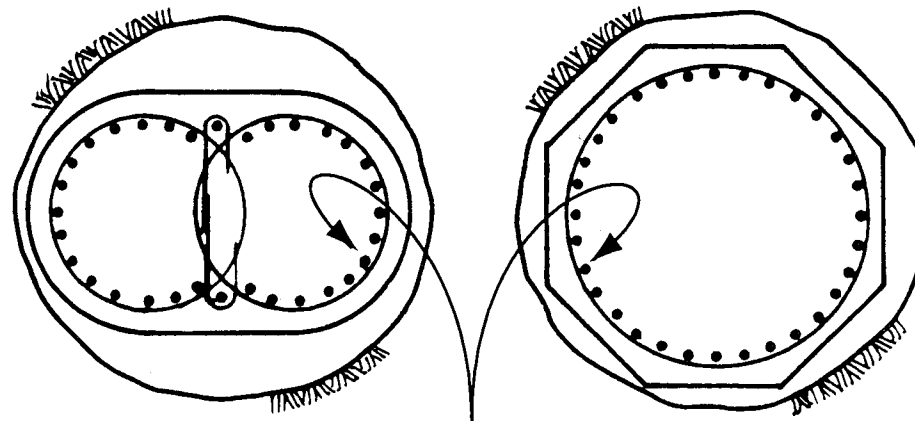
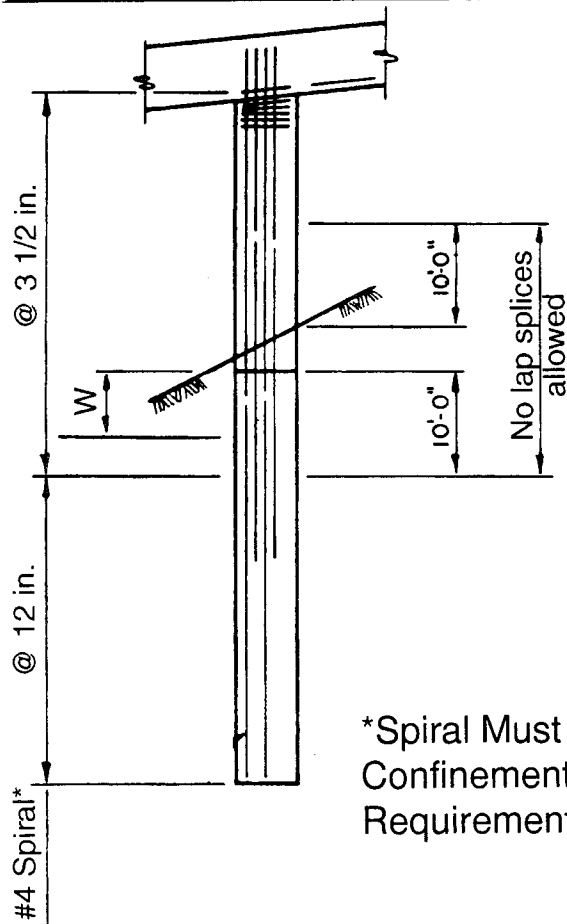
# Plastic Hinging Behavior



# Example / Distribution of Elastic Moments



# Detailing Issues/ 'Same Size' Columns and Shafts

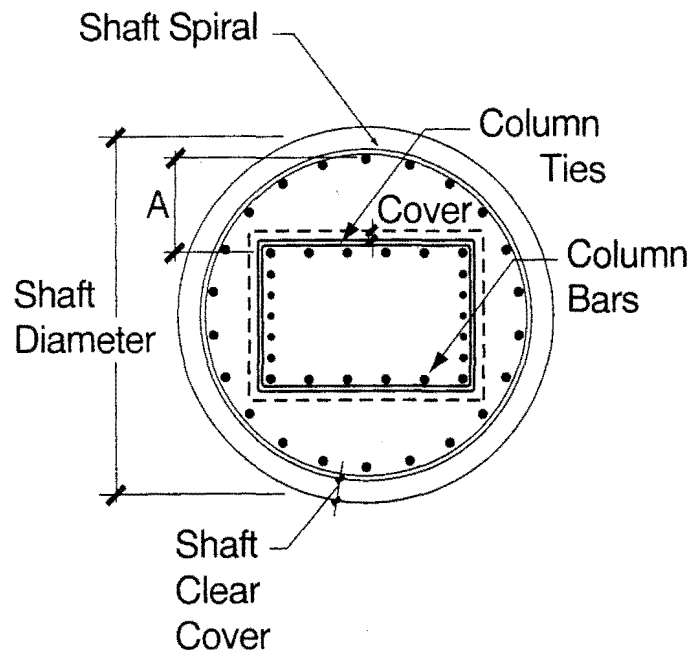


Reinforcement Pattern Extending into  
CIDH Pile to Be the Same as in Column

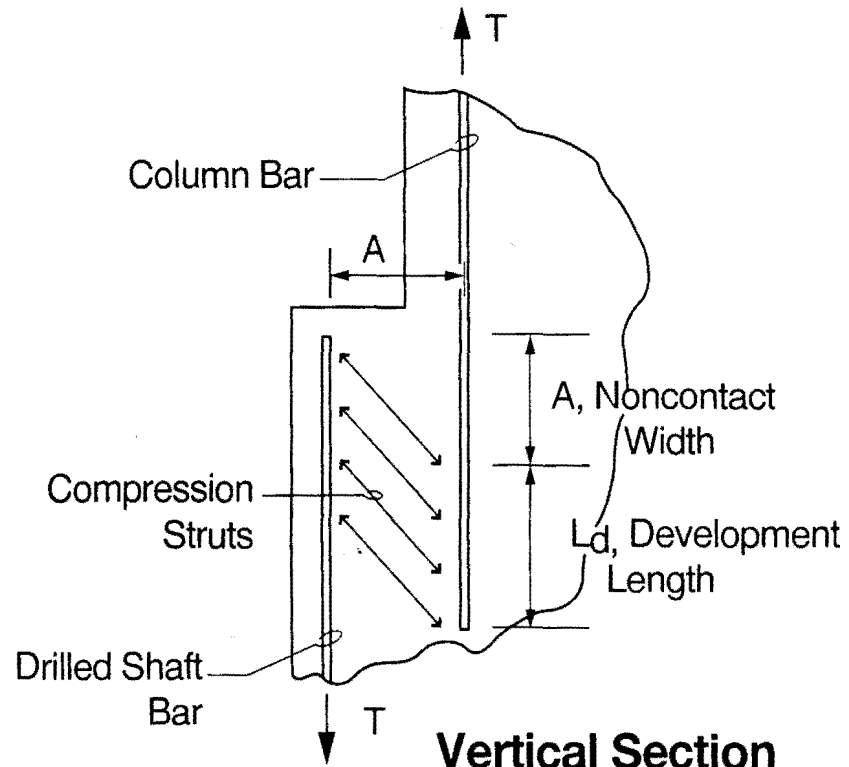
\*Spiral Must Comply with  
Confinement and Shear  
Requirements

Caltrans (1995)

# Detailing Issues/ Shafts Larger Than Columns

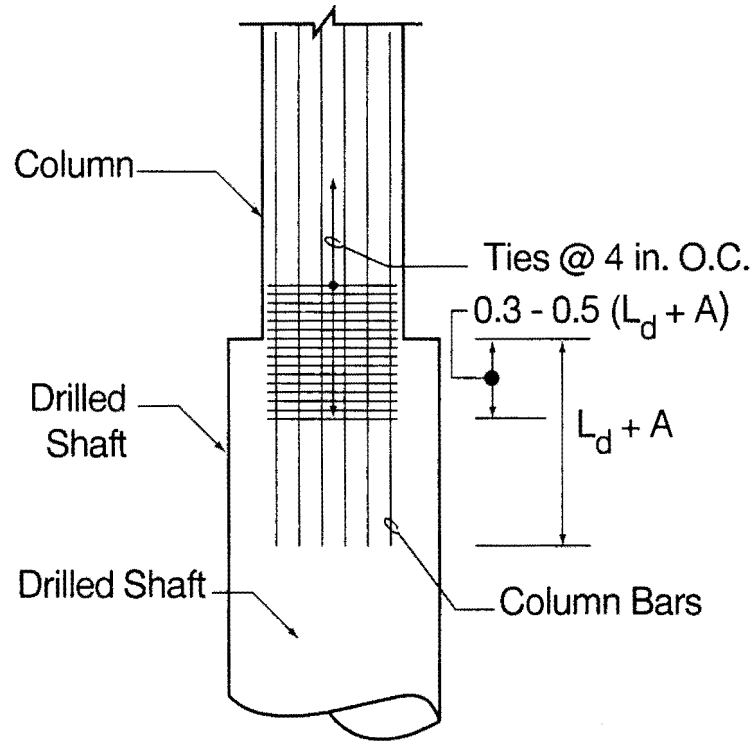


**Horizontal Section**

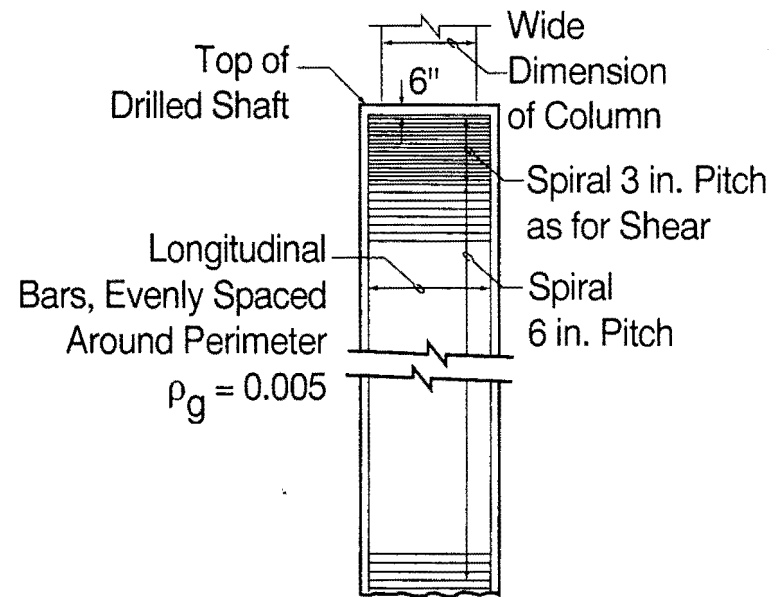


**Vertical Section**

# Detailing Issues/ Shafts Larger Than Columns



**Section at Connection**



**Shaft Reinforcement**

# **Session 6**

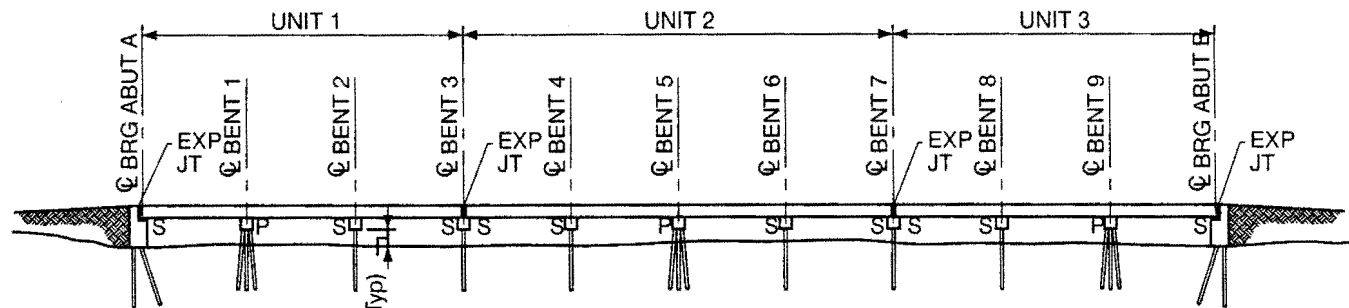
## **Pile Bent Bridge Example**

### **Pile Bent Issues**

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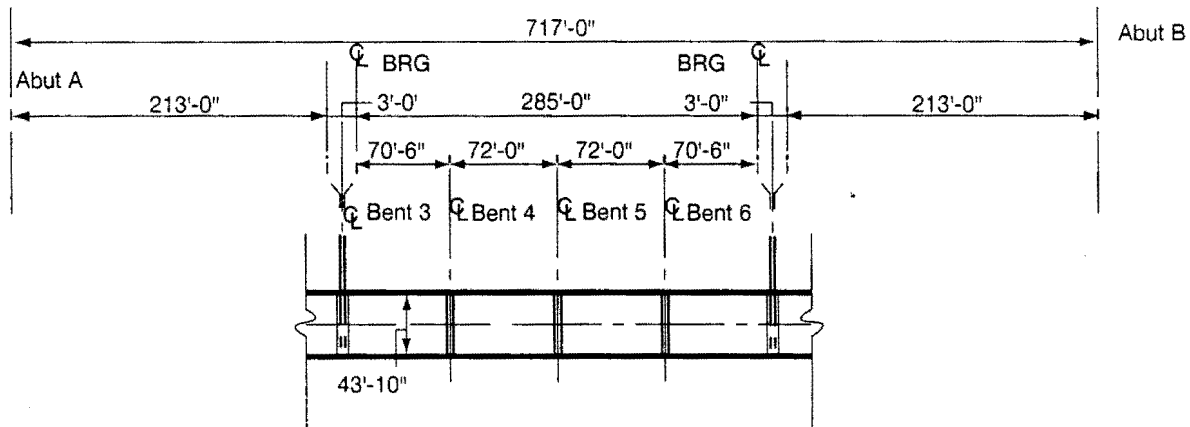
- **Description**
- **Behavior**
- **Stiffness Considerations**
- **Design Considerations**

# Pile Bent Bridge / Layout and Elevation



S = SLIDING  
P = PINNED

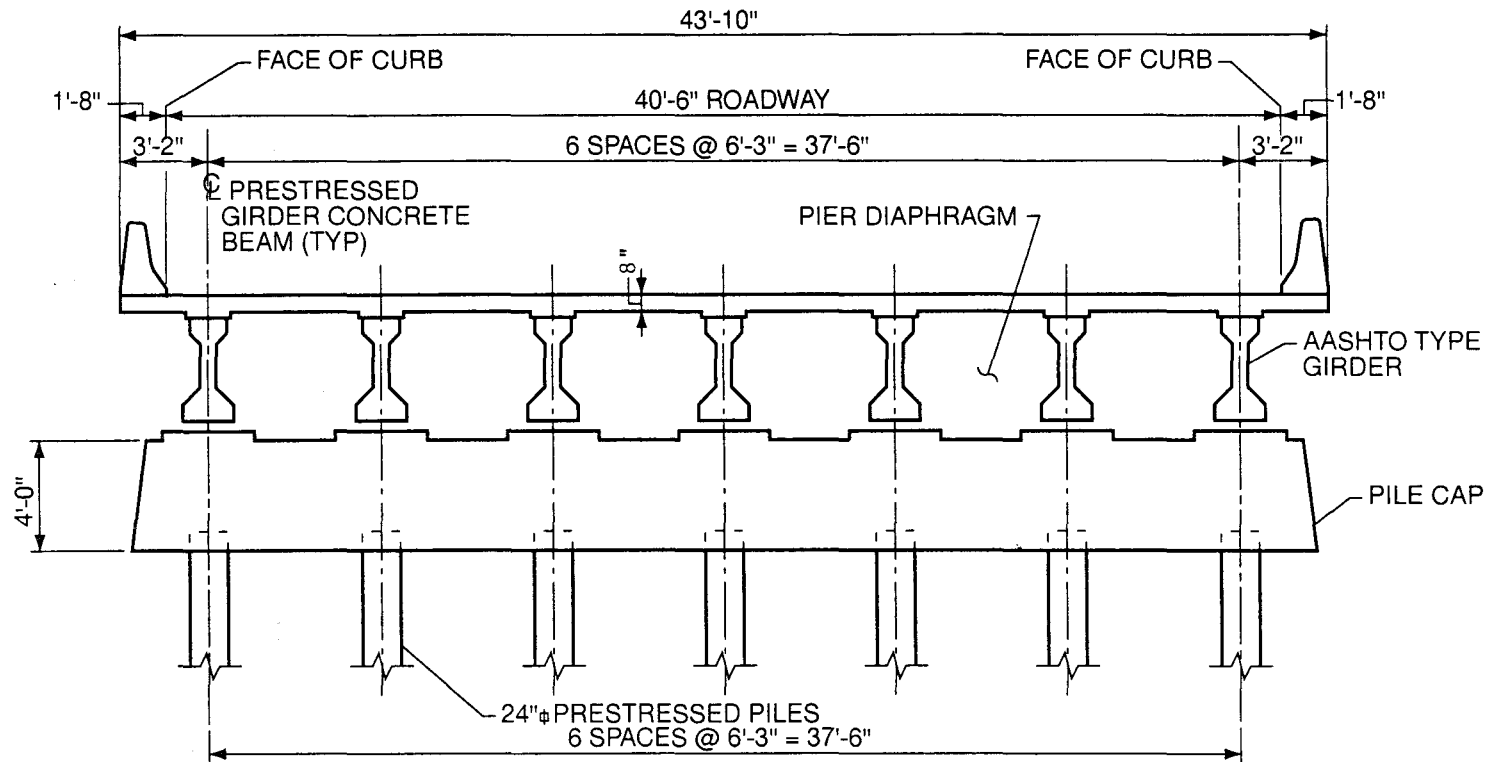
**Elevation**



**Plan of Center Unit**

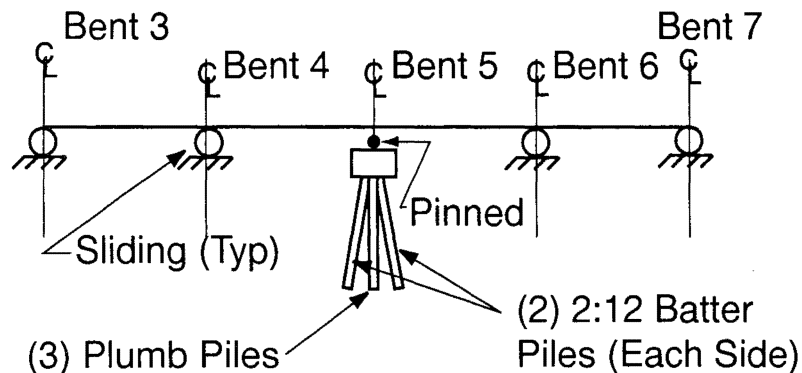


# Pile Bent Bridge / Bent Elevation



Section

# Typical Configuration / Lateral Load Transfer



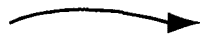
## Longitudinal Structural Model

- All Longitudinal Inertial Loads Taken by Bent No. 5
- All Other Bents Assumed to Have Sufficient Seat Widths
- Stiffness of and the Load Taken by Bent No. 5 Very Dependent on Number and Slope of Batter Piles

# Developing the Stiffness of Pile Bents

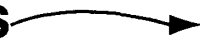
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## Plumb Piles



- Methods for Piles (Previously Discussed) May Be Used
- Account for Clear Height Above Mudline

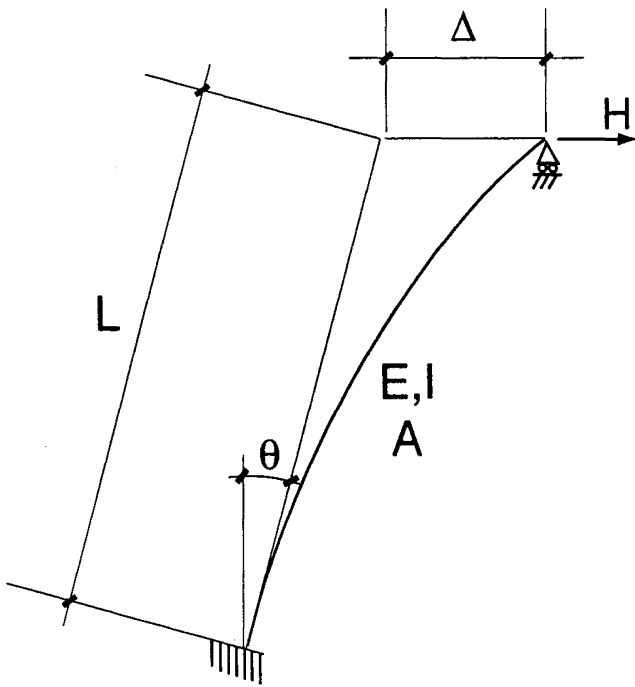
## Battered Piles



- Separate Flexural and Axial Effects
- Standard Pile Methods for Flexure
- Axial Stiffness and Capacity Much More Important

# Lateral Stiffness of Battered Pile

Consider One Pile of a Two Battered Pile Pair



$$K = \frac{H}{\Delta} = \frac{3EI}{L^3} \cos^2 \theta + \frac{AE}{L} \sin^2 \theta$$

- No Rotational Restraint at Cap
- If Cap Fixed  $3 \rightarrow 12 \frac{EI}{L^3}$
- No Axial (Soil) Deformation Below Pile
- If Add Flexibility Beneath Pile

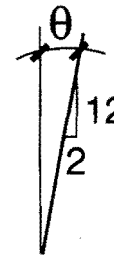
$$\frac{AE}{L} = K_{\text{eff}} = \frac{1}{1/(AE/L) + 1/K_{\text{soil}}}$$

## Example / Lateral Stiffness of 2:12 Batter Piles (1 of 3)

---

- 24 in. Square Prestressed Concrete Pile

$$\begin{array}{lll} E = 4030 \text{ ksi} & L = 60 \text{ ft} & \theta = 9.46^\circ \\ A = 40 \text{ ft}^2 & I = 1.33 \text{ ft}^4 & \end{array}$$



- Use Different Effective Length to Fixity for Flexure and Axial Contributions

$L_f = 25 \text{ ft}$   Based on Equivalent Cantilever for Plumb Pile

$L_a = 41.7 \text{ ft}$   Based on Skin Friction and No Tip Displacement

## Example / Lateral Stiffness of 2:12 Batter Piles (2 of 3)

---

- Flexural Contribution to Lateral Stiffness

$$K_f = \frac{3EI}{L_f^3} \cos^2 \theta + \frac{3(4030)144}{(25)^3} \cos^2 (9.46^\circ) = 144 \frac{\text{kip}}{\text{ft}}$$

- Axial Contribution to Lateral Stiffness

$$K_a = \frac{AE}{L_a} \sin^2 \theta = \frac{4.0(4030)144}{41.7} \sin^2 (9.46^\circ) = 1504 \frac{\text{kip}}{\text{ft}}$$


Even @ 2:12  $K_a \sim 10 K_f$

## Example / Lateral Stiffness of 2:12 Batter Piles (3 of 3)

---

- Include (Approximately) the Surrounding Soil Flexibility  
From Geotech: Soil  $\Delta \sim 0.25$  in at 600 kip maximum load

$$K_{\text{soil}} = \frac{600}{0.25} = 2400 \text{ kip/in}$$

- Assume  $\longrightarrow$  

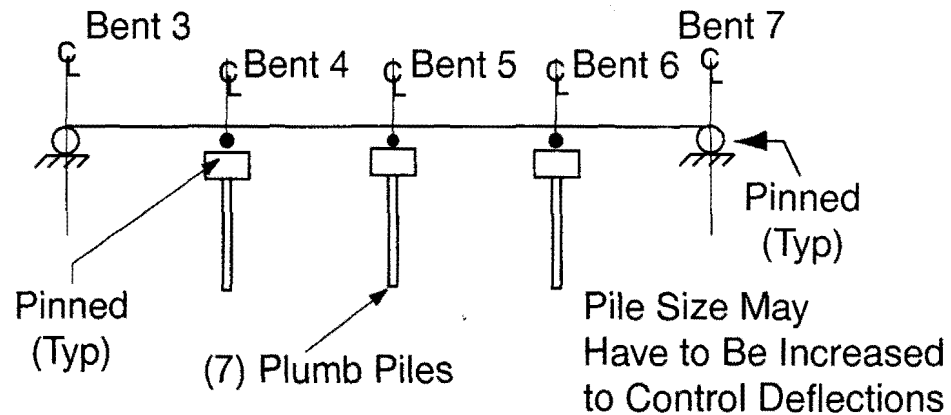
$$K_a = \frac{1}{\frac{1}{\frac{4.0(4030)144}{41.7}} + \frac{1}{2400(12)}} \sin^2(9.46^\circ) = 513 \frac{\text{kip}}{\text{ft}}$$

$K_a \sim 3.6 K_f$

# Considerations for Batter Pile Designs (1 of 3)

- High Axial Stiffness Will Attract Large Seismic Forces
- In Some Cases, May Consider Using All Plumb Piles

For Instance:



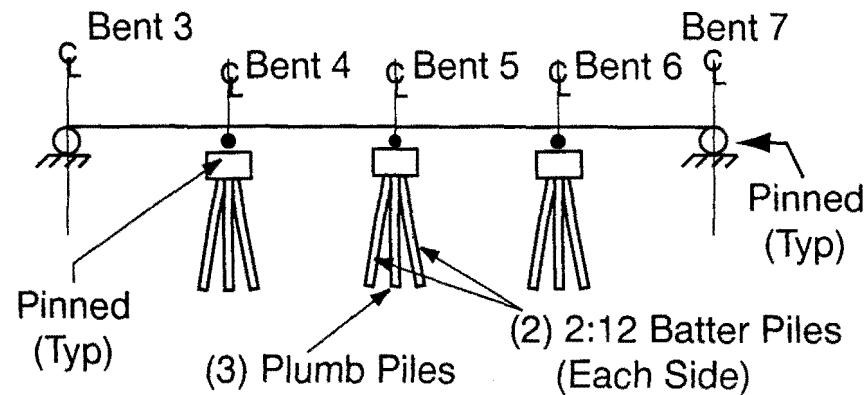


# Considerations for Batter Pile Designs (2 of 3)

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- More Than One 'Braced' Bent Per Frame May Be Required

**For Instance:**



# R Factors for Pile Bents

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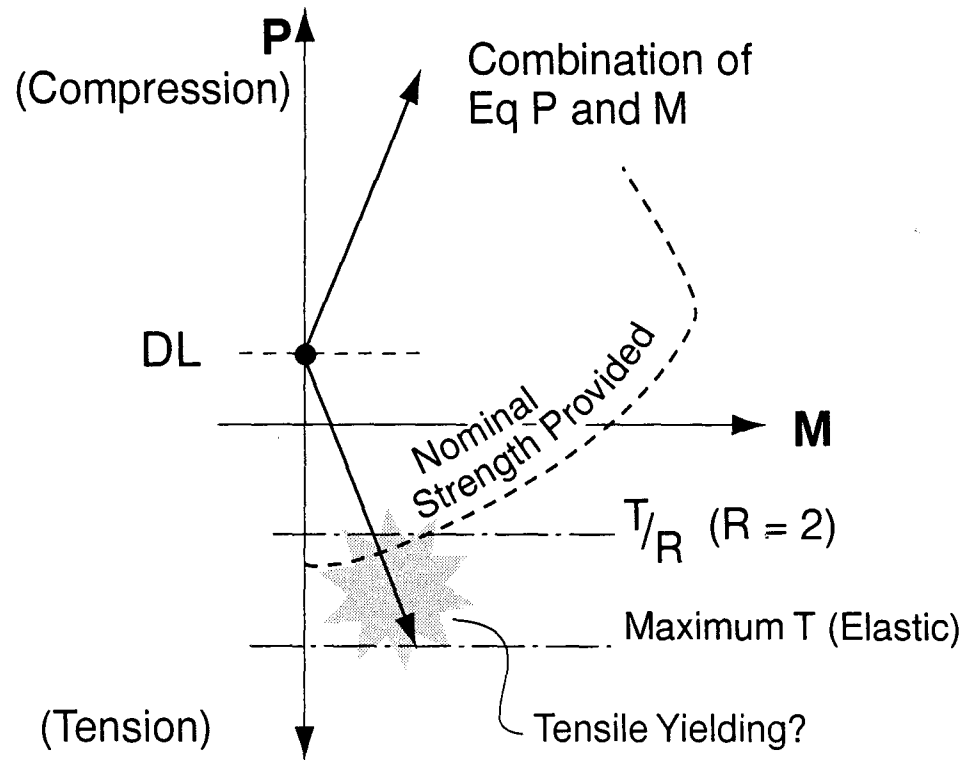
## AASHTO Division IA, Table 3

	Concrete Piles	Steel Piles
All Piles Vertical (Plumb)	3	5
Some Piles Battered	2	3

**SPC B:** Do Not Divide Above Factors by 2 for “Foundations”

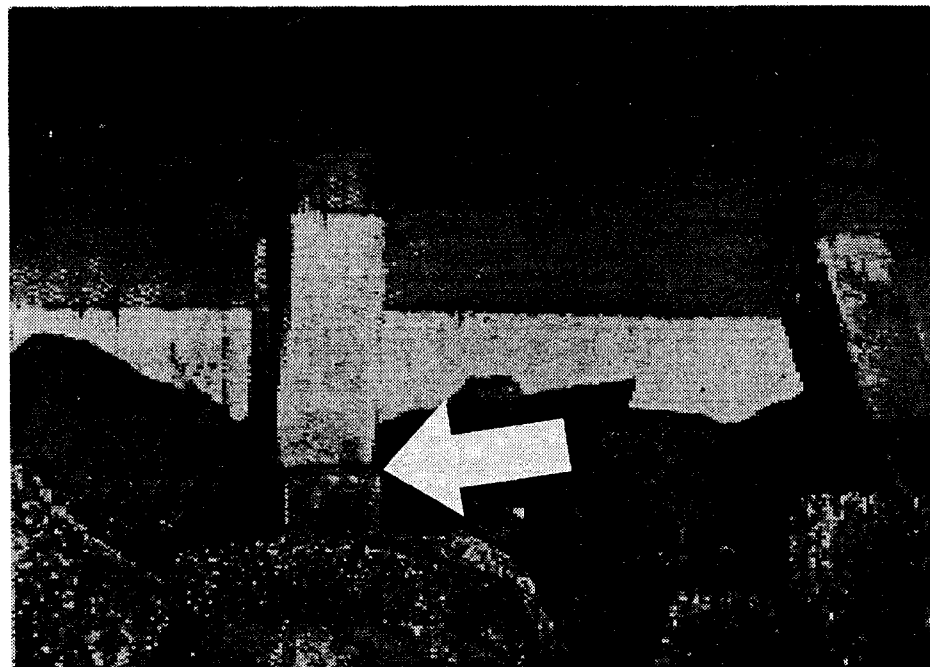
**SPC C and D:** Use  $R = 1$

# Axial Force Issues



# Consequences of Inadequate Tensile Strength / Batter Piles

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Loma Prieta, 1989

EERI (1990)

# Consequences of Inadequate Confinement / Plumb Piles

---



Loma Prieta, 1989

EERI (1990)

# Considerations for Batter Pile Designs (3 of 3)

---

- Ductile Performance Is Associated with Plastic Hinging
- Axial Yielding Not Considered a Viable Ductile Mechanism
- Consider Designing with Elastic Forces?  
(At Least For Axial Forces in Pile)
- Large Axial Forces Transferred to Soil May Result in Residual Displacements
- Does Bridge Collapse? — Probably Not
- Is Bridge Serviceable After Earthquake? — Probably Not

# Examples / Results for Center Frame of Bridge

## Options:

1. One Bent with Batter Piles
2. All Plumb Piles
3. All Bents Have Battered Piles

Concrete Pile Options	Units	Longitudinal Direction			Transverse Direction
		Option 1	Option 2	Option 3	
Total Stiffness, K	kip/in.	587	258	1761	583
Period, T	sec	0.74	1.17	0.45	0.40
Total Seismic Shear, V	kip	550	447	845	225
Elastic Deflection, $\Delta$	in	0.94	1.73	0.48	0.39
Max. Pile Tension	kip	-590		-238	
Max. Pile Compression	kip	846		494	
Max. Pile Moment, with R = 3	kip ft		340		192
Pile Tension Strength	kip	-213		-213	
Pile Compressive Strength	kip	767		767	
Pile Moment Strength	kip ft		370		370

# Summary

---

- **Option No. 2**      All Plumb Piles, Works Well
- **Option No. 3**      Batter Piles in All Bents, Is Workable
- **Option No. 1**      Batter Piles in One Bent, Does Not Work,  
too Much Load Is Attracted to too Few Batter Piles



# Conclusions

---

- Batter Piles Tend to Attract High Seismic Loads
- An All-Plumb Pile Solution May Be Better, Even if Pile Size Needs to Be Increased to Provide Adequate Stiffness
- If Batter Piles Are Used, Many Batter Piles May Be Necessary to Resist Seismic Loads

# **Session 6**

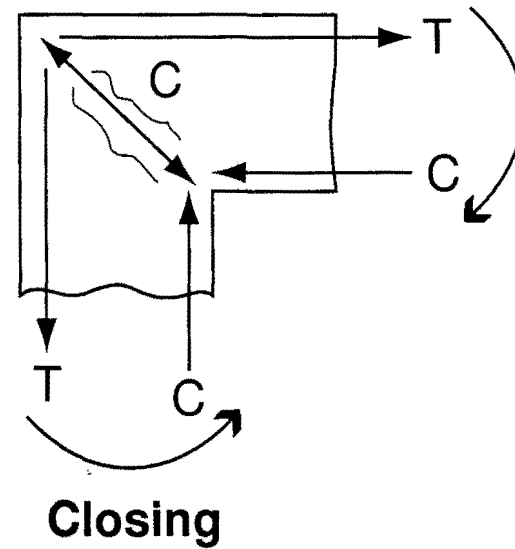
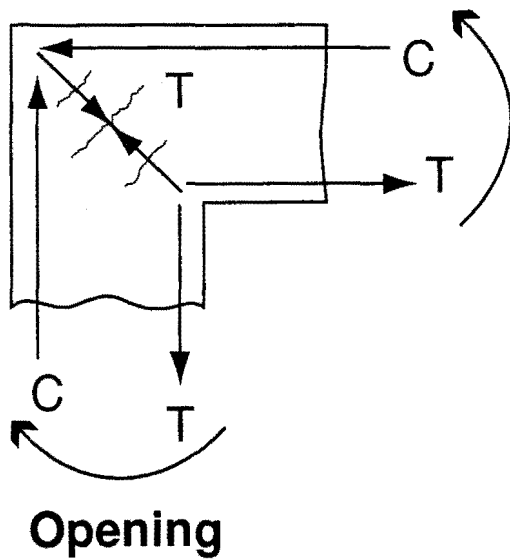
## **Other Topics**

### **Joint Design**

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- **Behavior**
- **Design Forces**
- **Shear Forces**

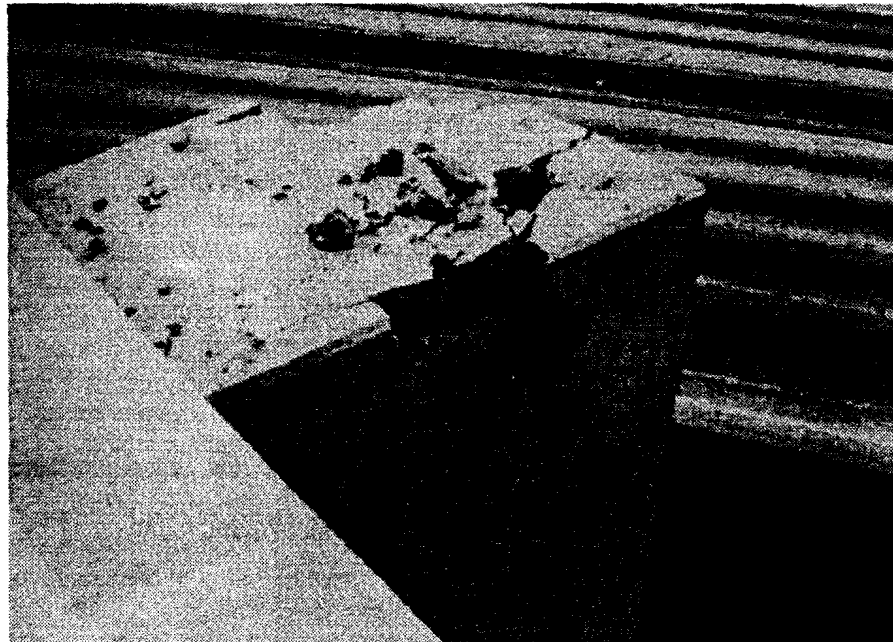
# Behavior of Joints / Knee Joints



T = Tension  
C = Compression

# Knee Joint Damage

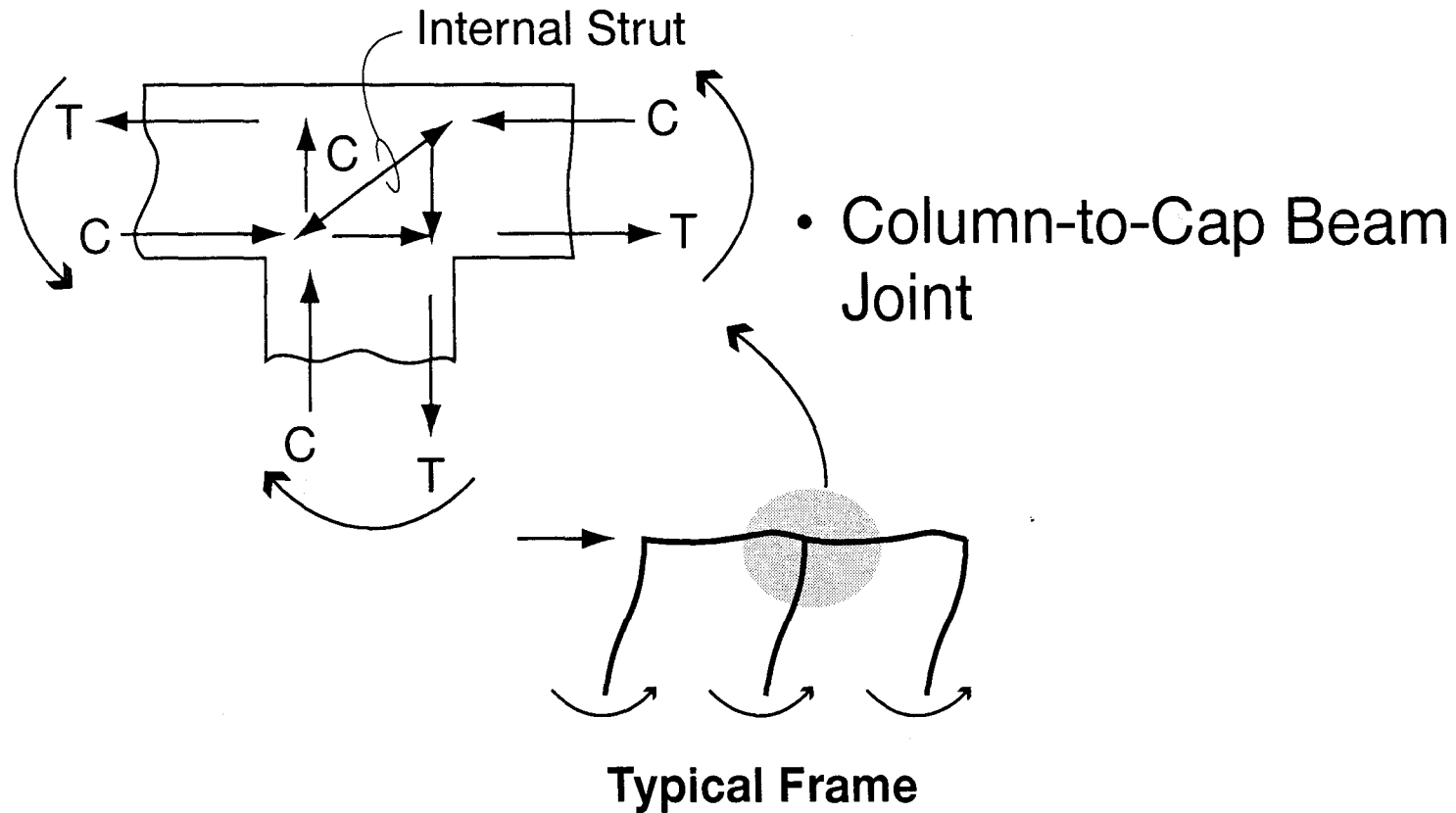
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Loma Prieta, 1989

EERI (1990)

# Behavior of Tee-Joints



• Column-to-Cap Beam Joint

Typical Frame

# Design Practice

---

## Empirical Joint Design Procedure

- Limit Magnitude of Average Joint Shear Stress  
(Limit Based on Experimental Data)
- Provide 'Minimum' Joint Confinement  
Steel Hoops to Preserve Integrity

# Calculating Shear Forces

---

- **Option 1 Use Approximations**

$$V_j = \frac{M_p}{b_e h_b h_c}$$

Where

$b_e$  = Effective Joint Width

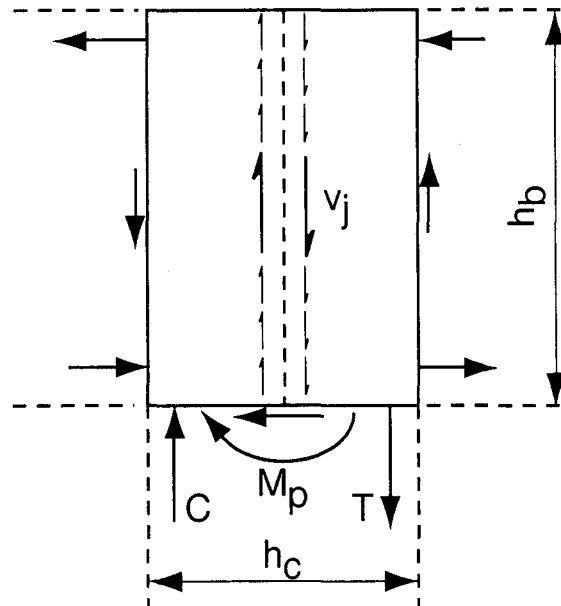
$h_b$  = Beam Depth

$h_c$  = Column Width

- **Option 2 Use Free Body Diagram with All Forces**

See Priestley, Seible, Calvi (1996)

# Free Body of Joint



## Approximations

$$T \cong C \cong M_p/h_c$$

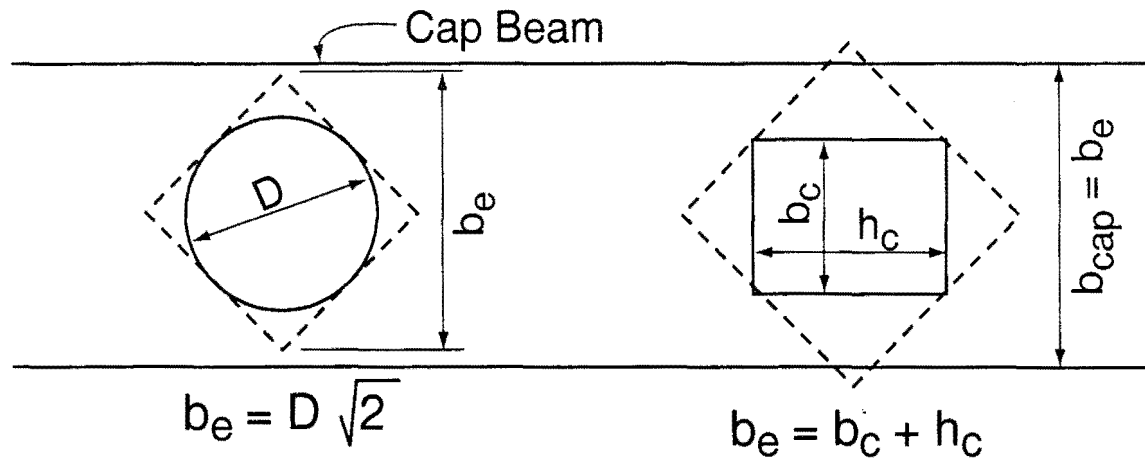
$$v_j \cong T/(b_e \cdot h_b)$$

$$v_j \cong \frac{M_p}{b_e h_b h_c}$$



# Effective Joint Width

Circumscribe a Square About the Column



$$b_e = D \sqrt{2}$$

$$b_e = b_c + h_c$$

But:  $b_e$  not  $>$   $b_{cap}$

**Plan View**

# Limiting Joint Shear Stress / Division I-A

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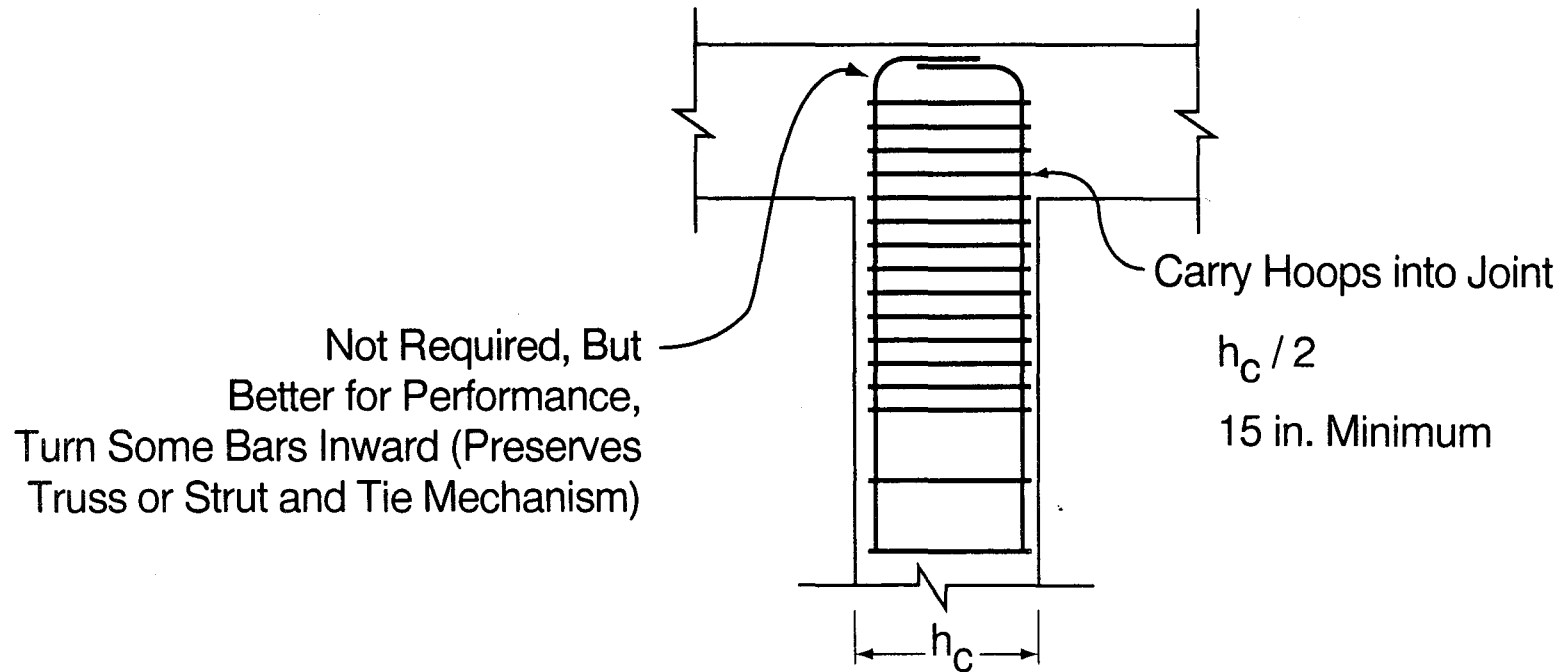
- **SPC C and D**  $v_j \leq 12 \sqrt{f'_c}$  Normal Weight Concrete
- $v_j \leq 9 \sqrt{f'_c}$  Light Weight Concrete

# General Comments

---

- Current Method Provides No Increase Based on Amount of Confinement Steel, Which Is the Plastic-Hinge Confinement Steel Carried One-Half of Column Dimension into Adjoining Member, Not Less Than 15 in.
- If Stress Limit Not Met, Increase Cap Beam Size
- Other Methods in Development
  - Truss Models
  - Limiting Principal Tension in Joint

# Detailing Considerations



# **Session 7**

## **Other Topics**

### **Existing Bridge Assessment and Retrofit**

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- **Expected Performance**
- **Actual Behavior**
- **Assessment Methodologies**
- **Comparison of New Design and Retrofit Practice**

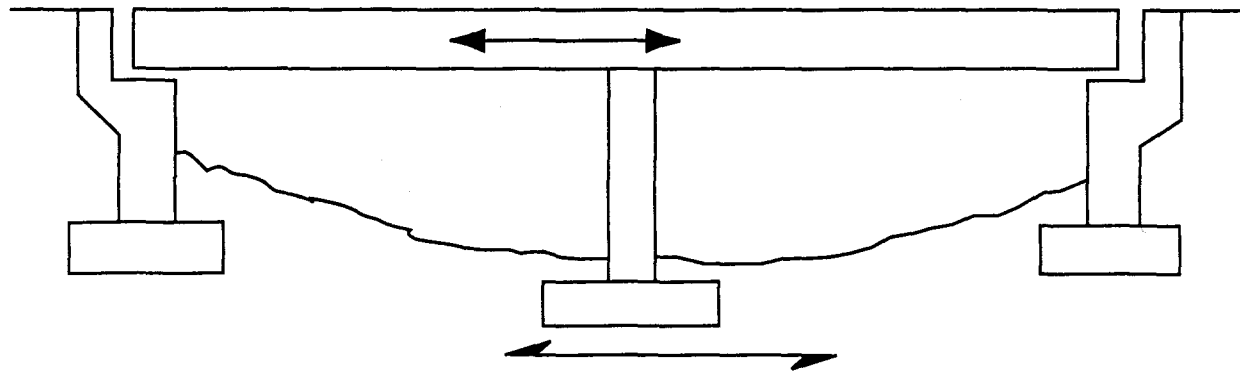
# Performance Objectives

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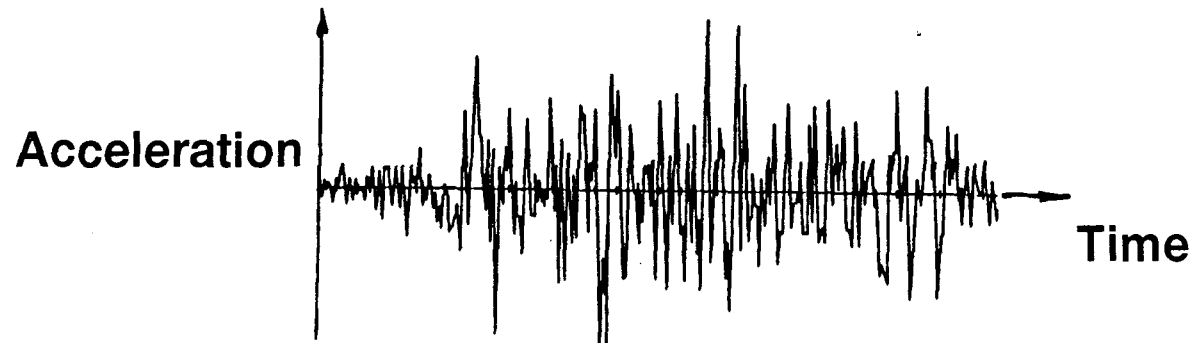
## What Do We Expect from Our Bridges?

- Small to Moderate Earthquakes  $\curvearrowright$  Elastic Response  
No Significant Damage
- Large, Infrequent Earthquakes  $\curvearrowright$  Inelastic Response  
Damage Occurs, Detectable  
No Collapse

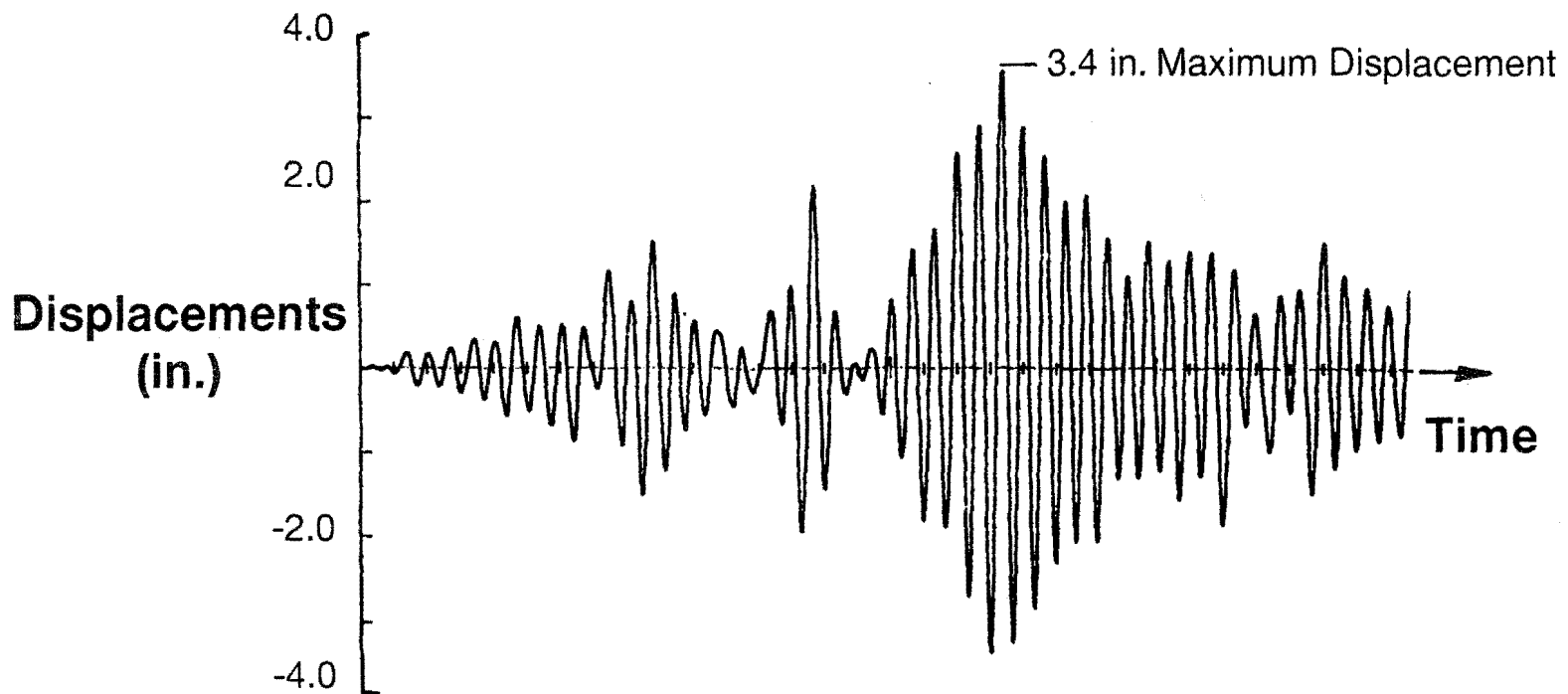
# Conceptual Example



Longitudinal Earthquake Loading

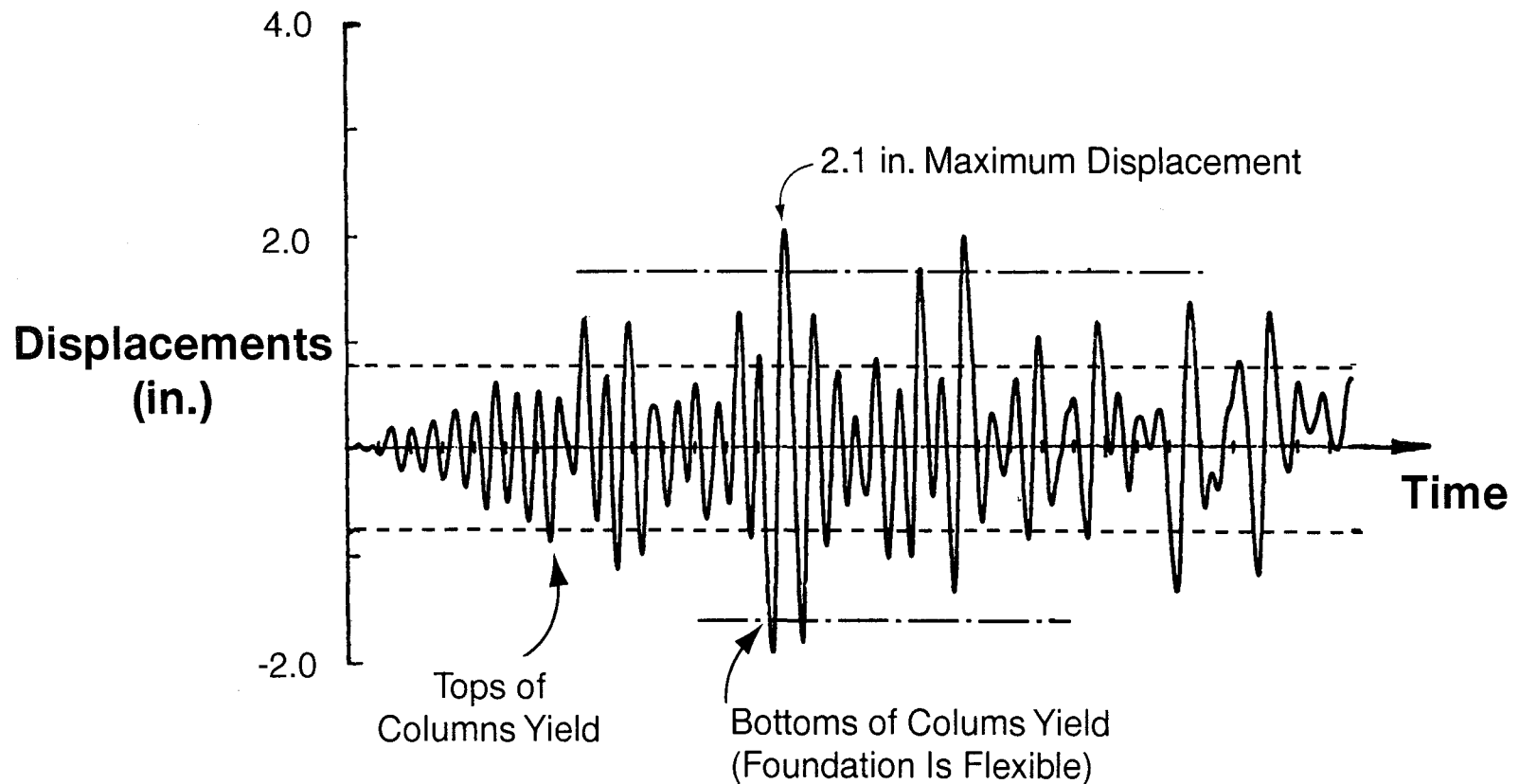


# Response if Structure Remains Elastic

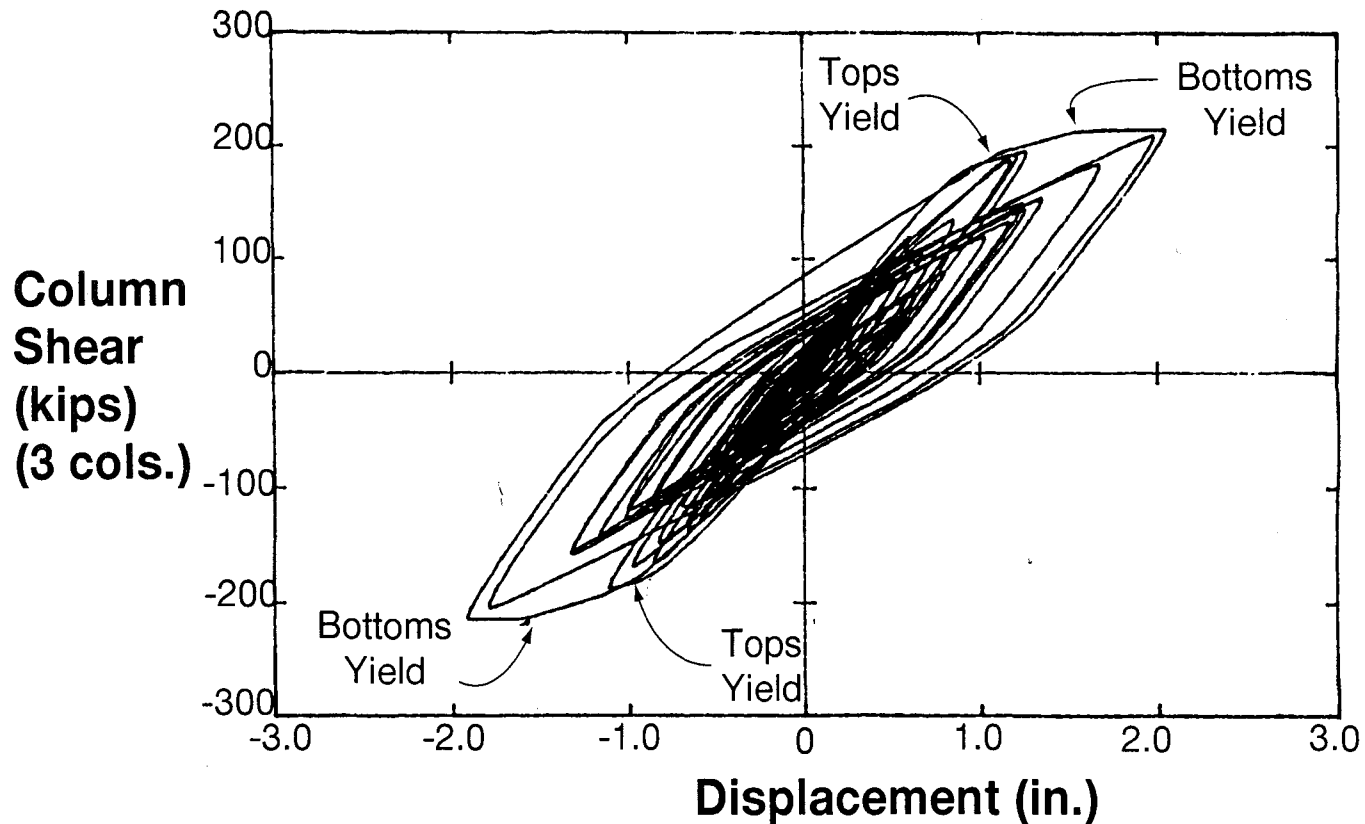




# Response with Column Yielding

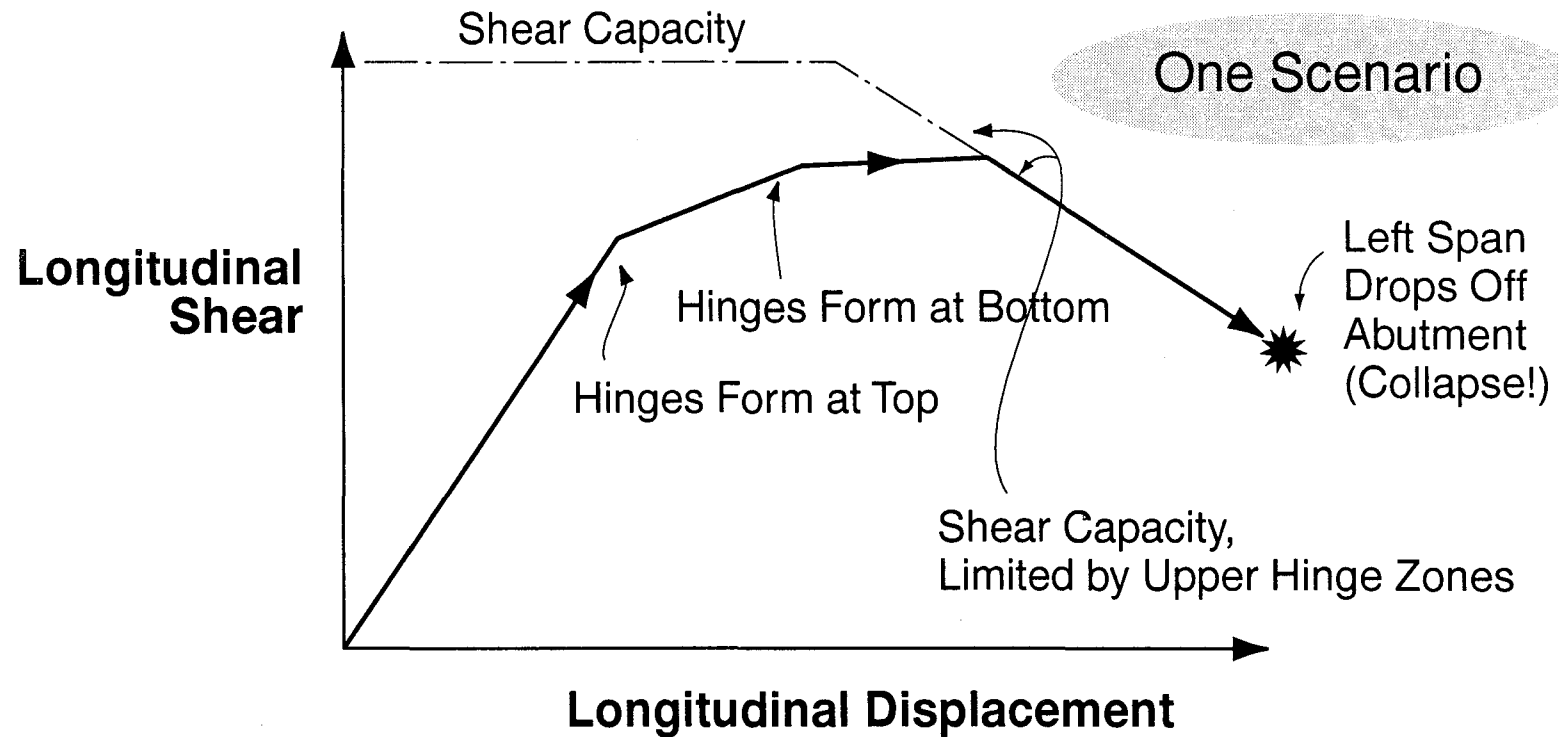


# Shear in Column vs. Displacement





# Quasi-Static Look at Behavior (Envelope)



# Issues and Failure Modes to Consider

---

- Displacements at Abutments
- Displacements at Interior Expansion Joints
- Forces in Restrainers (If Present)
- Column Hinge Confinement (Plastic Hinge Rotation Capacity)
- Shear Strengths — Columns, Hinges, Footings, Joints, etc.
- Anchorage and Development / Splices
- Footing, Yielding, Overturning, Sliding
- Foundation Strength / Liquefaction

# Assessment Methodologies

---

- Capacity / Demand Ratio Method
- Lateral Strength Method (FHWA)

Plastic Collapse Mechanism  
Pushover

# Capacity / Demand Ratio Method (1 of 3)

---

- Analyze Bridge Elastically to Obtain Demands
- Calculate Member / Item Capacities

( $\phi = 1.0$ , Nominal Ultimate Values)

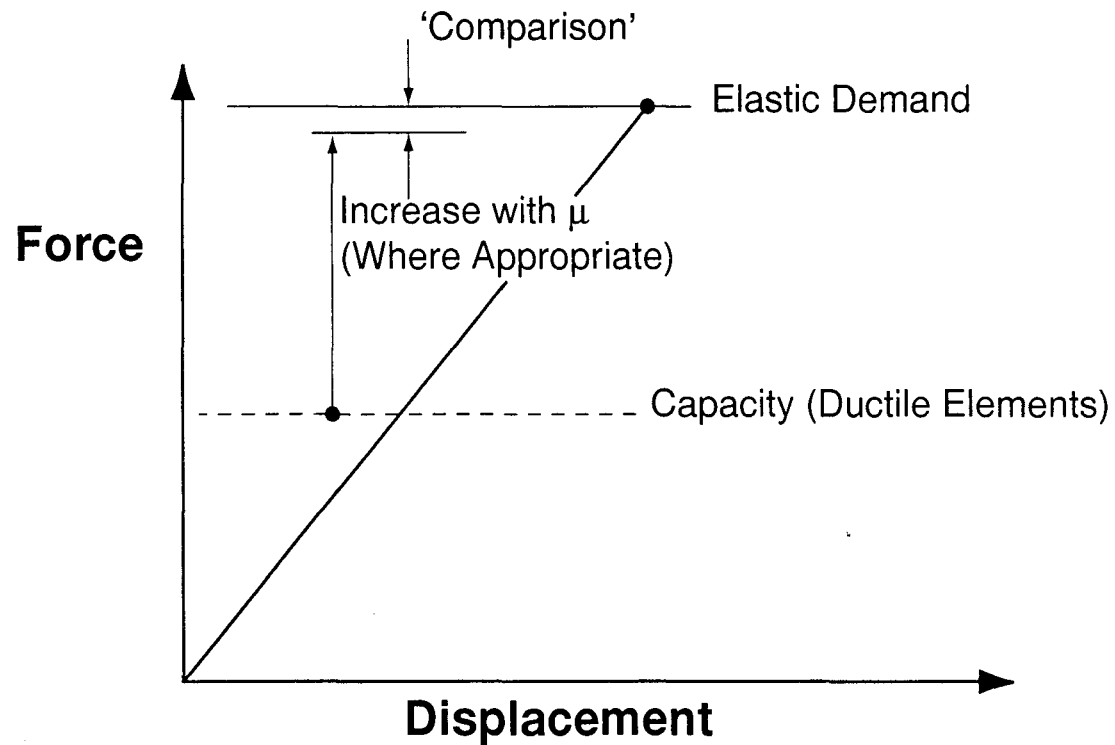
- Form C/D Ratio
- Increase Ratios for Ductile Elements

Using Ductility Indicator,  $\mu$


$$\frac{C}{D} < 1.0 \rightarrow \text{Failure}$$

- Estimate Damage / Failure Likelihoods  
(Lowest C/D First, etc.)

# Capacity / Demand Ratio Method (2 of 3)





# Capacity / Demand Ratio Method (3 of 3)

---

## **Advantages**

- Simple Analysis
- Quick Ranking of Element Performance
- Relatively Comprehensive Comparisons Developed

## **Disadvantages**

- Focus Is Entirely on Element Performance
- Cannot Account for Force Redistribution
- Does Not Account for Capacity Protection of Elements

# Lateral Strength (Pushover) Method (1 of 4)

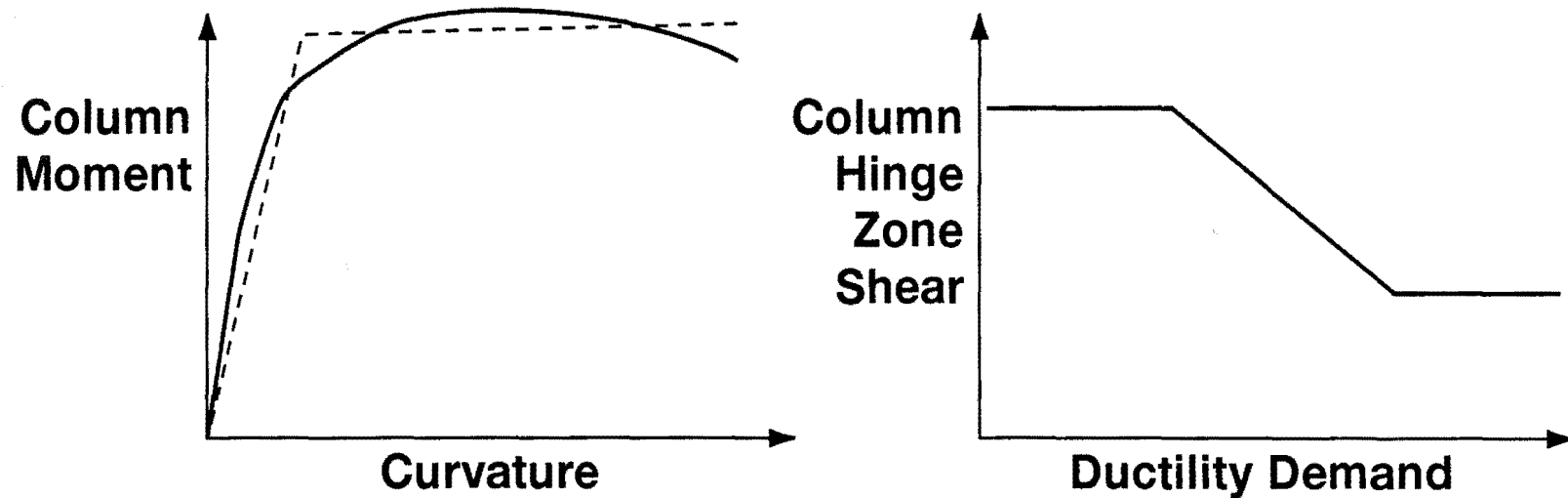
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- Analyze Bridge Elastically to Obtain Target Displacements
- Develop Member Yield / Deformation / Failure Relations
- Develop Static Force / Resistance Curves (Pushover)
  - Entire Structure
  - Individual Frames
- Evaluate Behavior Up to Target Displacement

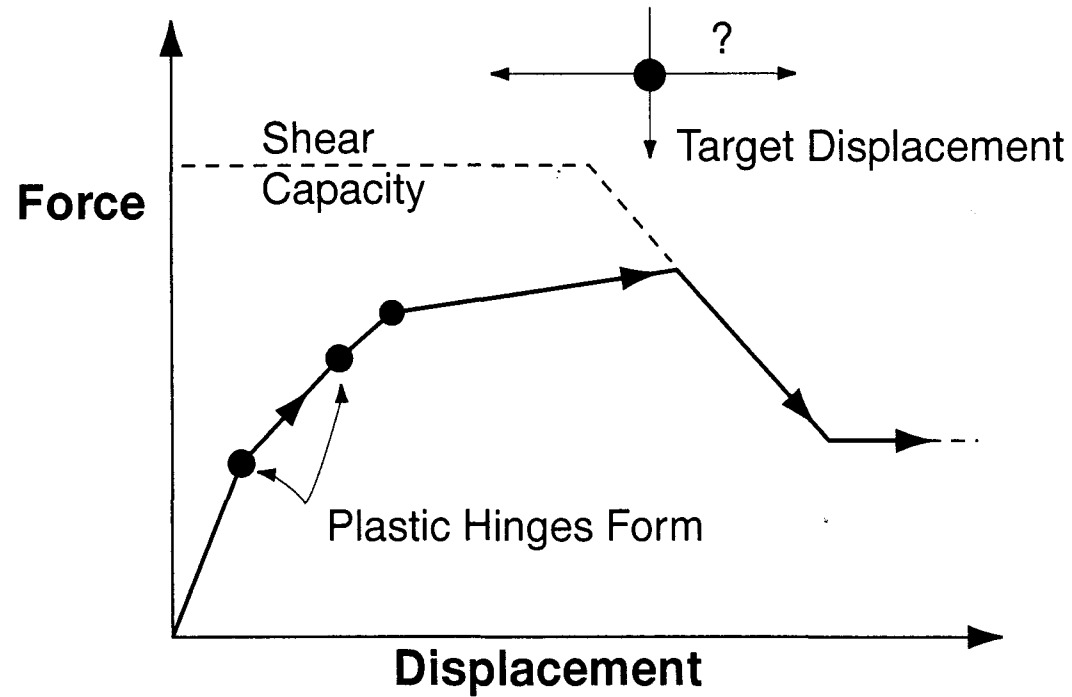
**Can Elements Endure Entire Displacement Sequence?**

# Lateral Strength (Pushover) Method (2 of 4)

---



# Lateral Strength (Pushover) Method (3 of 4)



# Lateral Strength (Pushover) Method (4 of 4)

---

## Advantages

- Tracks Sequence of Events (Yielding, Degradation, etc.) in Structure
- Indicates Structure (Sub-Structure) Overall Response — **System Focus**

## Disadvantages

- More Effort Required (Development of Basic Member Data)
- Does Not Address Cyclic Effects Directly

# New Design vs. Assessment / Retrofit

---

<b>Item</b>	<b>New Design Provisions</b>	<b>Existing Bridges</b>
• <b>Plastic Hinging</b>	Prescriptive Confinement	Assess Rotation Capacity Add Jacketing
• <b>Member Shear</b>	Design for Plastic Hinging Forces	Assess Shear Capacity and Ductility Demand Add Jacketing
• <b>Structure Displacements</b>	Provide Wide Seats	Probable Displacements Extend Seats Add Restrainers

# New Design vs. Assessment / Retrofit

---

<b>Item</b>	<b>New Design Provisions</b>	<b>Existing Bridges</b>
<ul style="list-style-type: none"><li>• <b>Reinforcement Splices</b></li></ul>	No Splices in High Moment Zone	Assess Ductility Demand Add Jacketing
<ul style="list-style-type: none"><li>• <b>Footing Yielding Footing Shear</b></li></ul>	Design for Plastic  Add Overlay Enlarge Footing	Assess Probable Forces Hinging Forces
<ul style="list-style-type: none"><li>• <b>Joint Shear</b></li></ul>	Limit Average Shear Stress Protect from Force	Enlarge Joint Add Jacketing

# Seismic Bridge Design Applications Concluding Considerations



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- In the Wake of the **1994 Northridge Earthquake:**

The Seismic Advisory Board Appointed to Evaluate  
Caltrans' Efforts Concluded:

7 Collapses  
~ 4823 Total Bridges in LA Co.

**“Caltrans’ design procedures and  
retrofit procedures are ‘technically sound.’”**

- Caltrans' efforts  AASHTO  
Division I-A  
 Other's  
Experience  
(NZ, Japan, etc.)

**Long Way  
from  
1971!**



# Seismic Bridge Design Applications

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## Questions and Answers



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