

**Center for Advanced Multimodal Mobility** 

**Solutions and Education** 

Project ID: 2019 Project 10

#### Are Transportation Network Companies Synergistic with Other Shared Ride Mode Offerings? An Exploratory Analysis of Demand Data from NYC Utilizing High Resolution Spatiotemporal Models

#### **Final Report**

by

Nalini Ravishanker (ORCID ID: <u>https://orcid.org/0000-0002-2028-4771</u>) Professor, Department of Statistics University of Connecticut, Storrs CT 06269 Phone: 1-860-486-4760; Email: <u>nalini.ravishanker@uconn.edu</u>

Karthik Konduri (ORCID ID: <u>https://orcid.org/0000-0003-2788-9455</u>) Research Scientist University of Connecticut, Storrs CT 06269 Phone: 1-860-486-2992; Email: <u>karthik.konduri@uconn.edu</u>

for

Center for Advanced Multimodal Mobility Solutions and Education (CAMMSE @ UNC Charlotte) The University of North Carolina at Charlotte 9201 University City Blvd Charlotte, NC 28223

September 2019

#### ACKNOWLEDGEMENTS

This project was funded by the Center for Advanced Multimodal Mobility Solutions and Education (CAMMSE @ UNC Charlotte), one of the Tier I University Transportation Centers that were selected in this nationwide competition, by the Office of the Assistant Secretary for Research and Technology (OST-R), U.S. Department of Transportation (US DOT), under the FAST Act. The authors are also very grateful for all of the time and effort spent by DOT and industry professionals to provide project information that was critical for the successful completion of this study.

#### DISCLAIMER

The contents of this report reflect the views of the authors, who are solely responsible for the facts and the accuracy of the material and information presented herein. This document is disseminated under the sponsorship of the U.S. Department of Transportation University Transportation Centers Program in the interest of information exchange. The U.S. Government assumes no liability for the contents or use thereof. The contents do not necessarily reflect the official views of the U.S. Government. This report does not constitute a standard, specification, or regulation.

## **Table of Contents**

EXCUTIVE SUMMARY	7
Chapter 1. Introduction	8
1.1 Problem Statement	8
1.2 Objectives	8
1.3 Expected Contributions	9
1.4 Report Overview	9
Chapter 2. Literature Review	10
2.1 Introduction	10
2.2 Existing Research on Ridesourcing	10
2.3 Summary	11
Chapter 3. Dynamic Predictive Models for Ridesourcing Services Using Daily Compositional Data	
3.1 Introduction	
3.2 Data Description and Exploratory Analysis	
3.3 VARX modeling for the transformed compositions	14
3.4 Summary	15
Chapter 4. Spatio-Temporal Analysis of Ridesourcing Data by Taxi-zones	17
4.1 Introduction	<b>17</b>
<ul> <li>4.1 Introduction</li></ul>	<b>17</b> 17 17
<ul> <li>4.1 Introduction</li></ul>	<b>17</b> 17 17 18
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 19 21
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 19 21 ographic 29
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 19 21 ographic 29 29
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 19 21 ographic 29 29 29
<ul> <li>4.1 Introduction</li></ul>	17 17 18 19 19 19 19 21 ographic 29 29 29 29 29 29
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 21 ographic 29 29 29 29 29 21 
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 21 ographic 29 29 29 29 29 29 31 31 31
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 19 21 ographic 29 29 29 29 29 31 31 32 40
<ul> <li>4.1 Introduction</li></ul>	17 17 17 18 19 19 21 ographic 29 29 29 29 29 29 29 29 31 31 32 40 41

APPENDICES	
A. Brief Review of Statistical Methods	44
B. Additional Plots of Local Moran's I	45

# List of Figures - Content

Figure 3.1. Demand of Counts for Four Modes	13
Figure 3.2. Modal Demand Counts-TNC, Taxi, and Citi Bike	13
Figure 3.3. 85 Day Ahead Forecast for Total Daily Demand Counts	15
Figure 4.1. Weekly Trip Counts of TNC and Taxi at Allerton/Pelham Gardens, Bronx	18
Figure 4.2. Taxi Zones with Temporally Clean Residuals for Taxi and TNC	19
Figure 4.3 Local Moran's I of ARIMA/GARCH Residuals – Full Length	22
Figure 4.4 Local Moran's I of ARIMA/GARCH Residuals – Segment	23
Figure 4.5 Local Moran's I of ARIMA/GARCH Residuals – Season	24
Figure 4.6 Local Moran's I of ARIMA/GARCH Residuals – Month	
Figure 4.7 Local Moran's I on ARIMA/GARCH/MLR Residuals – Full Length	
Figure 4.8 Local Moran's I on ARIMA/GARCH/MLR Residuals – Segment	
Figure 4.9 Local Moran's I on ARIMA/GARCH/MLR Residuals – Season	
Figure 4.10 Local Moran's I on ARIMA/GARCH/MLR Residuals – Month	

## **List of Figures - Appendices**

Figure B. 1 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals - Full Length	45
Figure B. 2 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals - Segment	48
Figure B. 3 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals - Season	51
Figure B. 4 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals - Month	59
Figure B. 5 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals - Full Length	59
Figure B. 6 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals - Segment	62
Figure B. 7 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals - Season	65
Figure B. 8 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals - Month	73

## List of Tables

Table 3.1 Five Number Summary of Observed Modal Demand Counts	12
Table 3.2: Estimated Coefficients from the VARX(1) Model Fit	14
Table 4.1. Ljung-Box and McLeod Li Test Results	18
Table 4.2: Global Moran's I - Segment Level	20
Table 4.3: Global Moran's I -Season Level	20
Table 4.4: Global Moran's I -Monthly Level	21
Table 4.5 MLR Results of Taxi	30
Table 4.6 MLR Results of TNC	30
Table 4.7 Global Moran's I on on ARIMA/GARCH/MLR Residuals-Segment Level	31
Table 4.8 Global Moran's I on ARIMA/GARCH/MLR Residuals -Season Level	31
Table 4.9 Global Moran's I on ARIMA/GARCH/MLR Residuals -Monthly Level	31
•	

#### **EXCUTIVE SUMMARY**

Spurred by technological advances, transportation networks and the mobility offerings for moving people and goods are undergoing transformative and significant changes. A significant operator in the area of moving people is transportation network companies (TNC), they are also commonly referred to by the name of the offering as dynamic ridesharing or ridesourcing. A research need is to comprehensively understand the impacts of TNCs so that transportation systems can be planned and implemented, that effectively respond to changes it brings. A unique feature of TNCs is the ease, efficiency, and effectiveness with which such services can be accessed and consumed, leveraged by technology and innovation. It is important to understand the demand for each of these services individually and to explore the interplay between these services so that policies and planning actions can be implemented to best promote these services and alleviate any negative impacts.

Our research consisted of a comprehensive exploration of all shared modes (subway, taxi, TNC, bikeshare) in a multivariate framework over multiple years, including incorporating the long-term patterns and incorporating the effects of short term shocks. This exploration was done using dynamic compositional models for time series, the data being aggregated across all of NY City, and would enable informed planning and operations decisions that positively impact all offerings within the shared mode landscape. Details are presented in the manuscript Toman et al. (2019). The next step in our research consisted of exploring the presence of spatial associations at taxi zone level in NYC, for which a comprehensive statistical analysis is scant in the ridesourcing literature. Together, the setup and outcomes of our research will be informative for building and estimating fine-scale spatio-temporal models for characterizing the existing system, as well as for short-term and long-term demand forecasting purposes.

# **Chapter 1. Introduction**

## **1.1 Problem Statement**

The United States is undergoing massive transformations not only in terms of the transportation infrastructure but also the mobility offerings. One of the most prominent sets of disruptive technologies in the transportation market is the Transportation Network Companies (TNCs), otherwise known as ridesourcing companies. These companies operate by using mobile devices such as smartphones to directly link commuters actively seeking transportation and drivers who act as owners/operators. The ridesourcing service has been rapidly adopted and has impressively penetrated the market since first being introduced by Uber in 2009. According to the data collected from the National Household Travel Survey (NHTS), the for-hire vehicle market has doubled from 2009 to 2017 due to the rapid expansion of TNCs, and about 10% of all Americans used ridesourcing services in any given month in 2017 (Conway, et al., 2018). The growing demand of TNCs is substantial. According to a recently released report, the total number of passengers transported by TNCs increased 37 percent from 1.90 billion in 2016 to 2.61 billion in 2017 (Schaller, 2018). Most of the passengers are serviced by Uber and Lyft. According to market share data from October 2018, the industry leader, Uber, accounts for 69 percent of the ridesourcing service market. 29 percent of the market is taken by Lyft, the second largest TNC in the US. The remaining TNCs, such as Via, Juno, and Gett, account for 2 percent of the US ridesourcing service market (Gessner, 2019). Although the adoption of TNCs is continuing to increase, the impact of these services on transportation network and travel behavior is still ambiguous. On one hand, the convenience and efficiency of TNCs hold promise for reducing vehicle ownership and promoting transit usage in urban areas. On the other hand, there is some concern that TNCs may take passengers away from public transit, increase vehicle miles traveled (VMT), and attenuate congestions.

The primary objective of the first part of this study is to understand the relationship of demand for TNCs and other shared modal offerings, namely taxis, subways and bikeshares, using a *multivariate modeling framework* to incorporate temporal patterns and effects of other exogenous factors. We formulate a vector autoregressive model with exogenous predictors (VARX) to explore the "substitutional" and "complementary" effects between TNCs, Taxis, and Citi Bike in New York City over the time span of time between April 2015 and June 2017. The response vector for the VARX model consists of transformed compositional time series, which is a multivariate data structure that allows one to model the *daily* demand for each mode as a proportion of the total. In addition, we fit a univariate DLM to total daily counts. We use both models to calculate fitted/predicted daily counts for each mode.

Exploring the role of TNCs in the shared mobility landscape is a useful research project. We carry out this research by not only assessing the spatiotemporal patterns for TNCs but also exploring the interplay with the demand for other shared ride modes in a given region. The growth of TNC is irrefutable and the direct impact of TNCs on mode choice behaviors of consumers is very evident. The current body of research on TNC is growing, and the literature is beginning to shine light on how they impact the demand for existing shared modes (e.g. bikeshare, transit). However, a comprehensive investigation of all shared ride modes in a particular region, including the temporal and spatial patterns of overall shared demand and its relationship to other shared modes, is lacking.

## **1.2 Objectives**

The objectives are as outlined below:

- 1) Develop and apply alternative multivariate modeling methodologies for analyzing the spatiotemporal dependence patterns both within different shared ride mode offerings but also across shared ride modes, at high resolution.
- 2) Demonstrate the methods to analyze the spatiotemporal patterns within and across shared ride modes in greater New York City metropolitan area. In particular, the proposed research will focus

on the synergy (or lack thereof) between TNCs and other shared mode offerings including subway, bikeshare, and taxis.

3) Disseminate the approaches that have been developed to benefit planning.

## **1.3 Expected Contributions**

To accomplish these objectives, several tasks have been undertaken.

- 1) We have done an exploratory analysis of the large ridesourcing data in order to understand the patterns of behavior of the counts of each model over time, by aggregating the data over all the zones in NYC.
- 2) We have carried out a comprehensive dynamic compositional statistical data analysis of the extensive ridesourcing data in order to understand patterns in each mode over time, as well as to understand patterns in the complementary and substitutability behaviors between the models.
- 3) We have done extensive exploratory analysis of the large ridesourcing data by taxi zone in NYC in order to understand the patterns of behavior of the counts of each mode in each taxi zone over time, and to understand any spatial patterns between the zones.

# **1.4 Report Overview**

The remainder of this report is organized as follows: Chapter 2 presents a comprehensive review of the state-of-the-art and state-of-the-practice literature on the ridesourcing data and analysis. Chapter 3 provides a detailed model formulation for doing a dynamic compositional analysis of the multivariate time series data aggregated over the zones in NYC using R packages to analyze state space models. The results show interesting aspects relating the different ridesourcing modes. Chapter 4 describes the analysis of the spatio-temporal patterns in the ridesourcing data across different taxi zones in NYC. We analyzed both daily and weekly data using R packages. We first fit adequate time series (ARIMA/GARCH) models to the data in each zone and then studied the spatial correlation between the residuals after removing the temporal effects. We also carried out a spatial association analysis at taxi zone level by regressing the ARIMA/GARCH residuals on land use and demographic variables and computing Moran's I statistics on the residuals from the resulting ARIMA/GARCH/MLR model. Chapter 5 summarizes the R code that was used to carry out the analysis. Finally, Chapter 6 concludes this report with a summary and a discussion of our project.

# **Chapter 2.** Literature Review

## **2.1 Introduction**

This chapter provides a review and synthesis of the state-of-the-art and state-of-the-practice literature on the ridesourcing problem. The growth of TNC is irrefutable and the direct impact of TNCs on mode choice behaviors of consumers is very evident. The current body of research on TNC is growing, and the literature is beginning to shine light on how they impact the demand for existing shared modes (e.g. bikeshare, transit).

## 2.2 Existing Research on Ridesourcing

The literature on ridesourcing has been growing rapidly in recent years given that more and more TNCs have made their data publicly available. Ridesourcing has been widely compared with traditional taxis since it exhibits similar characteristics and provides similar services. In fact, some studies point out that the TNCs provide better services compared to traditional taxis with respect to shorter waiting and travel times, and lower costs (Rayle, et al., 2016). Given the appealing advantages of ridesourcing services, it is not surprising that a large portion of the market share of taxis has been taken by the TNCs in many metropolitan cities. DeMay (2018) found that Seattleites used ridesourcing services 3.5 times more often than taxis. In New York City, Brodeur and Nield (2018) found that the number of taxi rides, number of passengers and fare income all decreased after Uber entered the market in May 2011, while Warerkar (2017) found that Uber had already overtaken the ridership of yellow cabs in 2017. In Washington D.C., the ridesourcing market has exploded since late 2015, which has coincided with a 31% drop in taxi ridership (Siddiqui, 2018).

Many studies have found that TNCs have significant impacts on public transit ridership as well. However, unlike the evident competitive relationship between TNCs and taxis, the impacts of TNCs on public transit remains unclear. On the one hand, TNCs can service as an alternative mode that lures passengers away from public transit. Alternatively, Uber can be the solution to the first-last mile problem to help connect riders to public transportation options, which in turn could help increase transit ridership. Current studies have found both substitution and complementary impacts of TNCs on public transit demand. Contreras and Paz (2018) applied a multinomial linear regression to ridership data from Las Vegas after controlling for exogenous variables, TNCs showed a significant negative impact on taxicab ridership but a complementary impact on public transit ridership. Similarly, Hall et al. (2018) analyzed variations of Uber's impacts on public transit across US metropolitan areas and indicated that Uber complements the public transit and leads to an average of 5 percent increase in transit ridership after two years. On the contrary, Erhardt et al. (2019) conducted a longitudinal analysis to explore the reasons for the decline in public transit in major US cities from 2002 to 2018 which suggests that TNCs may be the main reason for the decrease of transit ridership. The ridership of heavy rail and buses is expected to decrease by 1.3 percent and 1.8 percent respectively for each year since TNCs entry into the market. Jin et al. (2019) analyzed Uber pickup data in New York City in 2014 and found that Uber both competes and complements with public transit; Uber competes with the ridership of public transit during most hours of the day in areas with good public transit coverage, while it complements the public transit services in areas with insufficient public transit service during the midnight hours.

The relationship of TNCs and bikeshare has not been extensively analyzed. Both Hoffman (2016) and Erhardt et al. (2019) noted the impacts of bikeshare on public transit demand, but did not mention the relationship between bikeshare and TNCs. To the best of our knowledge, the study by Gerte et al. (2019) is the only one exploring the influence of bikeshare on the demand of TNCs using data from New York City from 2015 to 2017. They found that bikeshare negatively influences the demand of TNCs, which could be because the both modes share the same user population. Depending on circumstances, such as weather, TNCs/bikeshare availability, and cost, the users may be switching back and forth. Gerte et al. (2019) explore the relationship between TNCs and other shared modes (subway, taxi, bikeshare), their univariate

analysis for each modal demand fails to incorporate the correlations between modes. In this article, we build a multivariate VARX model to time series of transformed compositions of daily modal demand in order to incorporate the relationship between demand patterns of TNCs and other shared modes (subway, taxi, and bikeshare) in New York City.

## 2.3 Summary

A comprehensive review and synthesis of the current and existing research and development of the ridesourcing problem has been discussed in the preceding section.

# Chapter 3. Dynamic Predictive Models for Ridesourcing Services Using Daily Compositional Data

## **3.1 Introduction**

The primary objective of this study was to understand the relationship of demand for TNCs and other shared modal offerings, namely taxis, subways and bikeshares, using a *multivariate modeling framework* to incorporate temporal patterns and effects of other exogenous factors. We formulated a vector autoregressive model with exogenous predictors (VARX) to explore the "substitutional" and "complementary" effects between TNCs, Taxis, and Citi Bike in New York City over the time span of time between April 2015 and June 2017. The response vector for the VARX model consisted of transformed compositional time series, which is a multivariate data structure that allows one to model the *daily* demand for each mode as a proportion of the total. In addition, we fit a univariate DLM to total daily counts. We used both models to calculate fitted/predicted daily counts for each mode.

The format of this section is as follows. Section 3.2 provides a description of the data as well as an exploratory analysis. Sections 3.3 presents the VARX modeling for the transformed compositions of daily modal demand. Section 3.4 shows the univariate DLM model for total daily counts. Section 3.5 describes forecasting of daily modal counts based on both models. Finally, Section 3.6 gives an overall summary and discussion of the results and conclusions that can be drawn from this analysis. Details have been presented in the manuscript Toman et al. (2019), which is under review in a peer reviewed journal.

## 3.2 Data Description and Exploratory Analysis

Our data follows the format of Gerte et al. (2019). Missing data and data quality issues related to Green Cabs, subway, or Citi Bike were rectified via imputation using local averaging or deleting observations. Verification of this data was done by cross referencing yearly totals used in this paper with MTA's reported subway ridership and other published records. Our analysis is restricted to the time period spanning from 04/01/2015-06/30/2017 because Via and Lyft had not yet started their services prior to April 1st, 2015. The seven transportation providers have been aggregated into four mode categories:

- 1. TNC (consolidating Uber, Lyft, and Via) (TLC, 2017)
- 2. Taxi (consolidating Yellow cabs and Green cabs) (MTA, 2017)
- 3. Citi Bike (Citi Bike, 2017)
- 4. Subway (MTA, 2017)

Table 3.1 provides a numerical description of daily observed counts for each mode as well as the total. Figures 3.1 and 3.2 show time series plots for all four modes and all modes except subway, respectively.

		•			
	TNC	Taxi	Citi Bike	Subway	Total
Min.	59075.00	106071.00	1997.00	1334767.00	156701.00
Q1	147538.00	363319.00	25920.00	3503973.00	4269713.00
Median	219908.00	401732.00	36224.00	5525581.00	6159584.00
Q3	295363.00	439449.00	47023.00	5870137.00	6566306.00
Max	539267.00	580465.00	69772.00	6233796.00	6975008.00

## Table 3.1 Five Number Summary of Observed Modal Demand Counts





Figure 3.2. Modal Demand Counts-TNC, Taxi, and Citi Bike

## **3.3 VARX modeling for the transformed compositions**

- We first defined proportions of daily demand for each transportation mode (Citi Bike, subway, taxi, and TNC).
- We used the Additive Log Ratio (ALR) transformation (Aitchison, 1986) to convert the G=4 proportions into compositions  $Y_t = (Y_{t,1}, Y_{t,2}, Y_{t,3})^T$ , defined on a 3-dimensional simplex. We use subway as the baseline component,  $X_{t,G}$ .
- We investigated cross-correlations between thee components of the ALR transformed counts.
- We fit a vector autoregressive model with exogenous predictors to the vector of ALR components. The exogenous predictors included a set of indicators functions corresponding to the day of the week, federal holidays, peak NYC travel season (Sep-Dec), and Peak Citi Bike Usage (May-Oct). In addition, covariates for the number of city-issued event permits on a particular day and daily precipitation measured in inches were included in the model. This model was fit using conditional least squares

implemented via the *vars* (Pfaff, 2008) package in R. Note that the model includes coefficients for all seven days and no intercept.

We fit VARX(p) models for 1 ≤ p ≤ 10 using the same set of exogenous predictors for every p. To select the best model, i.e., the best value of p, we used the Bayesian Information Criterion (BIC) and Mean Absolute Prediction Error (MAPE).

Table 5.2 Estimated Coefficients from the VARA(1) Model Fit					
TNC(t)	Taxi( <i>t</i> )	Citi( <i>t</i> )			
0.699***	-0.043*	-0.020			
-0.544***	0.299***	-0.189			
0.019*	-0.017**	0.432***			
0.0004***	-0.0002***	0.0003			
-2.509***	-2.029***	-3.675***			
-2.430***	-1.985***	-3.707***			
-2.381***	-1.943***	-3.796***			
-1.875***	-1.442***	-3.526***			
-1.900***	-1.474***	-3.297***			
-2.719***	-2.232***	-3.712***			
-2.529***	-2.046***	-3.710***			
0.115***	0.021**	-0.348***			
0.359***	0.342***	0.155***			
-0.014	-0.021***	0.099***			
-0.00004	-0.00004	0.001***			
-0.024**	-0.010	0.208***			
736	736	736			
0.999	0.999	0.997			
0.098	0.070	0.288			
50,027.28***	57,473.750 ***	13,835.260***			
	TNC(t)           0.699***           -0.544***           0.019*           0.0004***           -2.509***           -2.381***           -1.875***           -1.900***           -2.719***           -2.529***           0.115***           0.359***           -0.014           -0.00004           -0.024**           736           0.999           0.098           50,027.28***	TNC(t)Taxi(t) $0.699***$ $-0.043*$ $-0.544***$ $0.299***$ $0.019*$ $-0.017**$ $0.0004***$ $-0.0002***$ $-2.509***$ $-2.029***$ $-2.430***$ $-1.985***$ $-2.381***$ $-1.943***$ $-1.875***$ $-1.442***$ $-1.900***$ $-1.474***$ $-2.719***$ $-2.232***$ $-2.529***$ $-2.046***$ $0.115***$ $0.021**$ $0.359***$ $0.342***$ $-0.014$ $-0.021***$ $-0.00004$ $-0.00004$ $-0.024**$ $-0.010$ $736$ $736$ $0.999$ $0.999$ $0.098$ $0.070$ $50,027.28***$ $57,473.750***$			

We show results from a VARX(1) model fit in Table 3.2.

Table 3.2 Estimated Coefficients from the VARX(1) Model Fit

- We next fit a dynamic linear model (DLM) for the daily total count.
- We then predicted rider counts by modal type by combining the results from the compositional analysis with the model from total counts. The forecasts are shown in Figure 3.3.



Figure 3.3. 85 Day Ahead Forecast for Total Daily Demand Counts

## **3.4 Summary**

The primary goal of this analysis was to explore the dynamic relationships in demand patterns between four modal offerings, TNC, Taxi, Citi Bike, and Subway and discuss how the usage of different modes may be changing over time in New York City. A compositional time series approach was used to study the dynamic relationships between the ALR transformed compositions of TNC, Taxi, and Citi Bike, relative to the baseline mode, Subway. This model helps us to estimate temporal patterns present in the daily demand for TNC, Taxi, and Citi Bike and how they have changed over the time period from 04/01/2015 up until 04/06/2017.

The results show that over this time period, TNC's proportion relative to the subway system steadily increased, while taxi services saw a steady decrease. These results suggest that there is a substitutionary relationship between the two modes as TNC poaches many of the same customers who would utilize taxi services. The compositional analysis also reveals that all three modes have a strong weekly seasonality, with TNC and taxi services seeing a large increase in usage between Thursday and Sunday. Furthermore, exogenous predictors such as major holidays and peak travel season were all found to be statistically significant in predicting demand proportions. This model enables us to forecast several steps ahead. By contrast, the univariate DLM showed that total daily ridership counts remain constant over the same time period and that the exogenous predictors. This supports the conjecture of a strong substitutionary relationship between TNC and taxis. More explicitly, since the total count of ridership does not appear to be increasing, it seems plausible that the gains of TNC have come mostly at the expense of taxi services. The final step

of the analysis involves combining the predicted modal proportions from Section 4 and the predicted total counts from Section 5 to obtain forecasts for the modal counts over the holdout period. The count forecasts in the holdout period for subway and taxi are more accurate than forecasts for counts of TNC and Citi Bike.

While research is ongoing regarding the effects of TNCs in the ridesourcing marketplace, many questions about the substitutionary and complementary dynamics between TNCs and other shared ride modes remain unresolved. Recent research on this topic by Erhardt et al., 2019 used a longitudinal random-effects model to study the effects of TNCs and bikesharing on public transport. They examined monthly aggregated rideshares in 22 metropolitan areas in the US from January 2002 to April 2018 and concluded that the introduction of TNCs had a negative association with motor bus and heavy rail ridership. Their findings also indicated that bikeshare had a substitutionary impact on motor buses and a complementary impact on heavy and light rail ridership. Ostensibly, their research goals are like ours in terms of assessing substitutionary and complementarity relationships between ridesourcing modes over time. However, there are some differences between the two analyses.

- (i) First, our study focuses on the *dynamic* relationships between all forms of ridesourcing in a *joint framework* with an emphasis on modeling cross-correlations between the modes.
- (ii) Secondly, our analysis is performed on daily data which allows us to gain insights into dynamic relationships at a finer temporal resolution. As a result, we can use the dynamic compositional analysis to not only draw inferences about relationships between modal offerings but also use this framework to generate useful short and medium term forecasts for use in public policy settings in contrast to the analysis in Schaller (2018) and Erhardt (2019).

In summary, the results of our compositional analysis indicate that the overall usage of shared ride modes does not show any appreciable increase over the study time period. However, at the modal level, there does seem to be a significant substitutionary dynamic between TNC and taxi as they vie for the same user base, and we can quantify this effect over time.

# Chapter 4. Spatio-Temporal Analysis of Ridesourcing Data by Taxi-zones

## **4.1 Introduction**

The primary purpose of this section is to discuss temporal modeling of ridesourcing data using suitable time series models and subsequent spatial analysis of resulting residuals from these models to understand associations between taxi zones in NYC. In this study, we fit time series models to each of the taxi and TNC demand data using autoregressive integrated moving average/Generalized autoregressive conditionally heteroscedastic (ARIMA/GARCH) models to trip counts of TNC and Taxi in New York City from January 1, 2015 to June 30, 2017. The analysis was conducted at a daily level and weekly level of aggregation. We then analyzed the residuals from these time series models to investigate spatial associations after accounting for land use and demographic information at the taxi zone level. Specifically, we carried out the following tasks:

- Data Processing and EDA.
- ARIMA/GARCH model fitting.
- Spatial Association Analysis on ARIMA/GARCH residuals at the taxi zone level.
- Multiple Linear Regression (MLR) analysis of time series residuals on demographic and land use variables.
- Spatial Association Analysis on ARIMA/GARCH/MLR residuals at the taxi zone level.

The weekly level analysis is shown in this report. Both weekly and daily levels of analysis will be included/summarized in our manuscript to be submitted for publication.

## 4.2 Data Processing and EDA

There are total of 263 taxi zones in New York City, however, some of the taxi zones have very low trip counts (<10) of either TNC or Taxi. For example, the zone of Governor's Island/Ellis Island/Liberty Island and the zone of Central Park. Similar as daily level data processing, we first removed the time period where the minimum daily trip counts of either mode are equal to zero. Then we aggregate the daily trip counts to weekly trip counts. After aggregation, there are total of 129 complete weeks in our dataset. We further removed the zones with mean weekly trip count less than 10. Our final dataset includes TNC trip counts of 229 zones and Taxi trip counts of 212 zones for 129 weeks starting from 2015-01-11 to 2017-06-25. Besides of modal data, the values of three exogenous variables are also aggregated to weekly level namely, weekly average precipitation in inch, weekly count of city permitted events, and a dummy variable to indicate if any holiday is included in a week. In most of the zones, TNC trip counts show a continuous increase over time, while the taxi trip counts exhibit a decrease trend. Figure 1 shows the weekly trip counts of TNC and Taxi at Allerton/Pelham Gardens, Bronx.



Figure 4.1. Weekly Trip Counts of TNC and Taxi at Allerton/Pelham Gardens, Bronx

## 4.3 ARIMA/GARCH Model Fitting Result

The purpose of fitting ARIMA and GARCH model is to remove the temporal pattern from trip counts of TNC and Taxi. Similar as daily-level data modeling, we fit ARIMA models on weekly TNC and Taxi trip counts for each taxi zone by applying auto.arima function in R. A log-transformation is applied for both TNC and Taxi trip counts in order to stabilize the variance. Ljung-Box and McLeod Li tests are performed to evaluate if the residuals are temporally clean. For the zones that are failing McLeod Li test, a GARCH (1,1) model is fitted on the residuals of ARIMA model to further remove the temporal pattern. Table 4.1 shows the final results of Ljung-Box and McLeod Li tests. There are a total of 213 taxi zones with temporally clean residuals of TAX data and 189 taxi zones with temporally clean residuals of Taxi data. Figure 4.2 shows the map of these taxi zones for both modes.

	Ljung Dos un		itcourto		
Mode	If include	Number of Taxi	Number of Taxi	Total Number	Total Number of
	Exogenous	Zones Fail	Zones Fail	of Temporally	Taxi Zones
	Variables	Ljung-Box Test	McLeod Li Test	Clean Zones	
		(p<0.05 and Lag	(p<0.05 and Lag		
		=12)	=12)		
TNC	No	16	2	213	229
Taxi	No	14	2	189	212

Table 4.1. Ljung-Box and McLeod Li Test Results



Figure 4.2. Taxi Zones with Temporally Clean Residuals for Taxi and TNC

## 4.4 Spatial Analysis of ARIMA/GARCH Residuals

The residual data of both TNC and taxi counts after fitting and removing temporal dependence are used for spatial analysis. Moran's I is calculated to quantity the correlation of a zone with its neighborhood. Both global and local Moran's I values are calculated to investigate the overall and local spatial correlation. R package 'spdep' is used for Moran's I calculation (Bivand, 2019).

#### 4.4.1. Global Moran's I

Moran's I is a cross-product statistic between a variable and its spatial lag, with the variable expressed in deviations from its mean. Global Moran's I is calculated as the equation below (Gimond, 2019):

$$I = \frac{\sum_{i} \sum_{j} w_{ij} z_i * z_j / S_o}{\sum_{i} z_i^2 / n}$$

- $w_{ij}$ : is the spatial weights of location *i* and *j*
- $z_i$ : is the observation at location *i*
- $S_o = \sum_i \sum_j w_{ij}$  is the sum of all weights
- *n*: is the number of observations

Besides of Moran's I, a pseudo P value is also calculated to inform if the spatial correlation is statistically significant.

For our analysis, zones that share the same boundary are considered neighbors. All neighbors are weighted equally. Since Moran's I is often applied on cross-sectional data instead of time series, we aggregate the residuals at the following temporal resolutions (we do a similar aggregation for the as daily level data analysis as well):

- Full time series length
- 1/4 of the time series length
- Season Spring, Summer, Fall, Winter
- Month

The residuals of both TNC and taxi are segmented into four equal sized sequential segments of residuals of 32 weeks (the first week was removed to get an integer number of weeks for each segment). Also, we aggregate all the series over the full length of time as a reference value. The results in Table 4.2 indicate that for all four segments of both modes, Moran's I rejects the null in favor of the alternative hypothesis, indicating a significant degree of spatial correlation across the zones. Furthermore, it is worth noting that when we aggregate across the full length of the series, Moran's I fails to reject the null hypothesis for Taxi; it rejects the null hypothesis for TNC.

	TNC		Taxi	
	Moran I Statistic	p-value	Moran I Statistic	p-value
Segment 1	7.9680	< 0.001	4.9851	< 0.001
Segment 2	3.2541	< 0.001	4.1059	< 0.001
Segment 3	9.1424	< 0.001	6.4023	< 0.001
Segment 4	6.8790	< 0.001	2.5635	0.0052
Full Series	3.7491	< 0.001	1.5318	0.0628

 Table 4.2: Global Moran's I - Segment Level

Our next level of analysis is for the major seasons. Essentially, we take all the time points corresponding to spring, summer, fall, and winter, aggregate them for all the residual series and once again perform a global Moran's test. Indeed, all four seasons exhibit spatial clustering according to the results in Table 4.3 below.

 Table 4.3:
 Global Moran's I -Season Level

	TNC		Taxi	
	Moran I Statistic	p-value	Moran I Statistic	p-value
Spring	4.7672	< 0.001	6.7718	< 0.001
Summer	7.1486	< 0.001	3.7837	0.0001
Autumn	8.1210	< 0.001	5.8486	< 0.001
Winter	5.2768	< 0.001	0.4374	0.3309

All 12 months exhibit spatial clustering according to the results in Table 4.4 below.

	TNC		Taxi	
	Moran I Statistic	p-value	Moran I Statistic	p-value
January	4.9744	< 0.001	5.2250	< 0.001
February	9.7074	< 0.001	10.0815	< 0.001
March	9.9091	< 0.001	6.7233	< 0.001
April	2.1195	0.017	5.8554	< 0.001
May	7.3713	< 0.001	4.6212	< 0.001
June	7.5752	< 0.001	3.5595	< 0.001
July	5.7473	< 0.001	2.6634	0.004
August	4.0230	< 0.001	5.0354	< 0.001
September	10.0105	< 0.001	3.7446	< 0.001
October	6.1406	< 0.001	4.6914	< 0.001
November	7.3623	< 0.001	3.2865	< 0.001
December	4.4517	< 0.001	5.6918	< 0.001

Table 4.4: Global Moran's I -Monthly Level

#### 4.4.2 Local Moran's I

While the global Moran's I explains the overall spatial pattern of the 'clean' trip count of TNC and Taxi in NYC, the local Moran's I is a local indicator of spatial association of a zone with its neighborhoods. It is calculated by the following equations (Anselin, 1995):

$$I_{i} = \frac{z_{i} - \bar{Z}}{S_{i}^{2}} \sum_{j=1, j \neq i}^{n} w_{i,j}(z_{j} - \bar{Z})$$
$$S_{i}^{2} = \frac{\sum_{j=1, j \neq i}^{n} (z_{j} - \bar{Z})^{2}}{n - 1}$$

where

-  $w_{ij}$ : is the spatial weights of location *i* and *j* 

-  $z_i$ : is the observation at location *i* 

- *n*: is the number of observations

The plots below are local Moran's I maps of taxi zones. The first plot indicates the values of local Moran's I for each taxi zone. The second plot only shows local Moran's I value of zones that are significant correlated with its neighborhood (p value < 0.05). The third plot shows p-value of local Moran's I. Similar as the global Moran's I, local Moran's I are also calculated at the same four temporal levels including: full length, four segments, four seasons and twelve months



Figure 4.3 Local Moran's I of ARIMA/GARCH Residuals – Full Length













Figure 4.5 Local Moran's I of ARIMA/GARCH Residuals – Season









Figure 4.6 Local Moran's I of ARIMA/GARCH Residuals – Month

# 4.5 Multiple Linear Regression of ARIMA/GARCH Residuals on Land Use and Demographic Variables

After removing the temporal pattern from both TNC and taxi trip counts, the potential influence of other land use and demographic characteristics was removed by a multiple linear regression (MLR). This section presents a short description of census and land use data used for MLR and also the model estimation results.

#### 4.5.1 Census and Land Use Data

The U.S. Census Bureau collects variety demographic information about American population and economy at different geographical resolutions annually. For our analysis, we focus on total number of population, number of full time employees, median age and median earning in each taxi zone in New York City from 2015 to 2017. The data are available to download at the website of U.S. Census Bureau. One must be note that the data is reported at census track level which is smaller than taxi zones. An aggregation is required to get the data at the taxi zone level. Land use data of New York City is collected by the Department of City Planning (DCP) which is a primary land use agency in New York City. DCP collects detailed land use and geographic data at the tax lot level annually including residential area, commercial area, retail area etc. The dataset also provides the census track id for each tax lot. Therefore, a similar aggregation has been performed to obtain the land use data in each taxi zone from 2015 to 2017.

#### 4.5.2 Multiple Linear Regression on Time Series Residuals

Having established the presence of spatial auto-correlation between the aggregated residuals of the time series models, the residual series from each mode are pooled and then a multiple linear regression model is fit where we seek to account for variation in the residual series by land use and demographic covariates. We denote the model as such:

$$e = X\beta + \eta$$

where *e* is a vector of residuals that is created by pooling together the residual from each time series model, *X* is a design matrix consisting of all main effects for the demographic and land variables plus all secondorder interactions between the demographic and land use variables which yields a total of covariates,  $\beta$  is the vector of coefficients for each covariate and  $\eta \sim N(0, \sigma^2 I_n)$  where  $I_n$  denotes the nxn identity matrix. Stepwise model selection is then performed on these models using the MASS library in R (Ripley et al., 2019). The selection criterion is AIC and both forward and backwards selection are utilized.

For the land use covariates, the sum of lot area and building area is used to create an exposure variable. That yields a proportion for eight types of land use in a respective taxi zone. More specifically, we had the following 8 land use covariates:

- 1. (Residential Area)/(Total Area)
- 2. (Commercial Area)/(Total Area)
- 3. (Retail Area)/(Total Area)
- 4. (Factory Area)/(Total Area)
- 5. (Storage Area)/(Total Area)
- 6. (Garage Area)/(Total Area)
- 7. (Office Area)/(Total Area)
- 8. (Other Area)/(Total Area)

Furthermore, we used the following 4 demographic variables:

- 1. (Total Population)/(# of Buildings)
- 2. (Fulltime Employed)/( # of Buildings)
- 3. Median Age
- 4. Median Earnings

Two different regression analysis are built on each mode. The first model incorporates only main effects while the second includes all main effects plus second order interactions. For both analyses, I use stepwise model selection based off the AIC to find a parsimonious subset of the predictors in both sets of models. Regression outputs for these models are given below-Note that stepwise selection gave the same model for taxi in both cases.

## 4.5.2.1. Taxi Results

Stepwise model selection reveals that only the number of fulltime employed individuals has a statistically significant correlation with the residuals of taxi services at the 5% level. Results are detailed in the table below.

Tuble ne milit Rebuik				
Taxi-Best Model According to AIC				
	Term	Std. Error	<b>T-Statistic</b>	P-Value
Intercept	-0.003	0.001	-2.521	0.012
Fulltime Employment	-1.000e-08	4.336e-09	-2.307	0.022
Observations	25413			
Adjusted $R^2$	0.0002094			
Residual Std. Error	0.1491			
F-Stat (df=1;25411)	5.5322			

## Table 4.5 MLR Results of Taxi

## 4.5.2.2 TNC Results

Model selection revealed a larger subset of covariates that were statistically significant for the 0.05 level in explaining variation in the TNC residuals. For the main effects, full time employment, median earnings, and median age had statistically significant relationships to the TNC residuals. In addition, interaction effects between the residential land use percentage and median age, office land use percentage and median age, and commercial percentage and fulltime employment were all found to have a statistically significant correlation with the TNC residuals.

TNC-Best Model According to AIC				
	Term	Std. Error	T-Statistic	P-Value
Intercept	-0.005	0.004	-1.3405	0.180
ResidentialPct	0.024	0.013	1.778	0.075
FulltimeEmp	-2.311e-08	5.487e-09	-4.213	2.53e-05
Median Earnings	-2.151	8.391	-2.564	0.010
Median Age	0.001	0.0001	3.467	0.0005
ResidentialPct:Median Earnings	3.418e-07	1.900e-07	1.828	0.068
StoragePct:Median Earnings	1.022e-06	6.949e-07	1.472	0.141
ResidentialPct:Median Age	-0.0009	0.0004	-2.097	0.0360
OfficePct:MedianAge	0.0006	0.0002	2.950	0.0032
CommercialPct:FulltimeEmp	-9.396e-08	2.949e-08	-3.187	0.0014
Observations	27477			
Adjusted $R^2$	0.005			
Residual Std. Error	0.1234			
F-Stat (df=9;27467)	15.563			

#### Table 4.6 MLR Results of TNC

# 4.6 Spatial Analysis on ARIMA/GARCH/MLR Residuals

After removing the impact of demographic and land use effects by MLR, similar spatial analysis as shown in section 4.4 is repeated on the residuals from MLR.

## 4.6.1 Global Moran's I on ARIMA/GARCH/MLR Residuals

The results in Table 4.7 indicate that for all 4 segments of TNC, Moran's I reject the null in favor of the alternative hypothesis which is that there is a significant degree of spatial correlation across the zones. For taxi, Moran's I tests of the first 3 segments of taxi data also reject the null hypothesis, but it fails to reject the null for segment 4. Furthermore, it is worth noting that when we aggregate across the full length of the series, Moran's I fails to reject the null hypothesis for TAXi; it rejects the null hypothesis for TNC.

			8		
	TNC		Taxi		
	Moran I Statistic	P-value	Moran I Statistic	P-value	
Segment 1	7.1904	< 0.001	3.9660	< 0.001	
Segment 2	2.5985	0.0047	3.1412	< 0.001	
Segment 3	6.9465	< 0.001	5.8728	< 0.001	
Segment 4	1.8741	0.0305	1.2383	0.1078	
Full Series	1.7523	0.0399	1.1995	0.1152	

Table 4.7 Global Moran's I on on ARIMA/GARCH/MLR Residuals-Segment Level

All four seasons exhibit spatial clustering for TNC according to the results in Table 4.8 below. However, Winter season of taxi data does not exhibit spatial autocorrelation.

Table 4.8	<b>Global Moran's</b>	I on ARIMA/GARCH/MI	<b>LR Residuals -Season Level</b>
-----------	-----------------------	---------------------	-----------------------------------

	TNC		Taxi	
	Moran I Statistic	P-value	Moran I Statistic	P-value
Spring	4.3515	< 0.001	6.5305	< 0.001
Summer	7.0102	< 0.001	3.8943	< 0.001
Autumn	7.7366	< 0.001	5.8456	< 0.001
Winter	5.2898	< 0.001	0.4810	0.3152

All 12 months exhibit spatial clustering according to the results in Table 4.9 below.

Table 4.9 Global Moran's I on ARIMA/GARCH/MLR Residuals -Monthly Level

	TNC		Taxi	
	Moran I Statistic	P-value	Moran I Statistic	P-value
January	4.9848	< 0.001	5.1341	< 0.001
February	9.2391	< 0.001	9.9803	< 0.001
March	9.8670	< 0.001	6.6852	< 0.001
April	2.2448	0.0124	5.8475	< 0.001
May	6.9221	< 0.001	4.7753	< 0.001
June	8.1056	< 0.001	3.6554	< 0.001
July	5.4489	< 0.001	2.6596	0.0039
August	4.0695	< 0.001	5.0425	< 0.001
September	9.8920	< 0.001	3.7427	< 0.001
October	5.8578	< 0.001	4.6852	< 0.001
November	7.5311	< 0.001	3.2887	< 0.001
December	4.5969	< 0.001	5.6927	< 0.001

## 4.6.2 Local Moran's I on ARIMA/GARCH/MLR Residuals

The plots below show the local Moran's I values calculated using the residuals from MLR









Figure 4.8 Local Moran's I on ARIMA/GARCH/MLR Residuals – Segment





Figure 4.9 Local Moran's I on ARIMA/GARCH/MLR Residuals - Season










Figure 4.10 Local Moran's I on ARIMA/GARCH/MLR Residuals - Month

# **Chapter 5.** Summary of R Code used in this Project

All code for the analyses described in Chapter 3 and 4 of this report can be found on the Github repositories linked below. The first link corresponds to the models used in chapter 3 while the second corresponds to the analysis performed in chapter 4.

- 1. https://github.com/pato6664/ALR-Models
- 2. https://github.com/pato6664/ARIMA-GARCH\_SpatialAnalysis

## Chapter 6. Summary and Conclusions

The summary and conclusions of each analysis has been detailed the individual chapters. The research carried out in this project has both methodological and substantive contributions. Much more can be done to better understand these travel models with a goal towards using the information for planning purposes.

## **6.1 Directions for Future Research**

Many interesting lines of inquiry may be investigated in future research. First, Citi Bike's role in the marketplace of shared ride modes still seems unclear and needs closer scrutiny. While it does have weekly seasonal dynamics like the other modes, it has no appreciable increasing trend and it has no significant cross-correlation with the other modes on a daily level. Second, there are a significant number of outliers in the data set and a careful look into imputing them will be useful. Third, residuals from the models in Section 4 and Section 5 indicate some departure from normality and conditional homoscedasticity. Research into building more sophisticated models that can adequately incorporate time-varying volatility and heavy-tailed behavior will be attractive. Finally, disaggregating the data for NYC into areal units (boroughs or taxi zones) would enable us to study spatial and temporal dynamics in a richer modeling framework.

## References

- Aitchison, J., 1986. The Statistical Analysis of Compositional Data. London: Chapman and Hall.
- Anselin, L. Local Indicators of Spatial Association—LISA, Geographical Analysis 27(2): 93–115, 1995.
- Box, G. & Cox, D., 1964. An Analysis of Transformations. Journal of The Royal Statistical Society. Series B 26(2), pp. 211-252.
- Bivand. R. et al. 2019. Package 'spdep'. <u>https://cran.r-project.org/web/packages/spdep.pdf</u>
- Brodeur, A. & Nield, K., 2018. An empirical analysis of taxi, Lyft and Uber rides: Evidence from weather shocks in NYC. Journal of Economic Behavior & Organization, Volume 152, pp. 1-16.
- Citi Bike [Data File], 2017. Citi Bike Trip History Data. https://www.citibikenyc.com/system-data
- Contreras, S. D. & Paz, A., 2018. The effects of ride-hailing companies on the taxicab industry in Las Vegas, Nevada. Transportation Research Part A: Policy and Practice, Volume 115, pp. 63-70.
- Conway, M. W., Salon, D. & King, D. A., 2018. Trends in Taxi Use and the Advent of Ridehailing, 1995–2017: Evidence from the US National Household Travel Survey. Urban Science, p. 79.
- DeMay, D., 2018. Report: Goodbye taxis, Seattleites take Uber, Lyft 3.5 times more often. <u>https://www.seattlepi.com/local/transportation/article/Goodbye-taxis-Seattleites-take-Uber-way-more-12866867.php</u>
- Durbin, J. & Koopman, S., 2012. Time Series Analysis by State Space Methods. 2 ed. Oxford: Oxford Unviersity Press.
- Egozcue, J., Pawlowsky-Glahn, V. & Mateu-Figueras, G., 2003. Isometric Logratio Transformations for Compositional Data Analysis. Mathematical Geology., Vol. 35, pp. 279-300.
- Erhardt, G., Graehler, M. J. & Mucci, R. A., 2019. Understanding the Recent Transit Ridership Decline in Major US Cities: Service Cuts or Emerging Modes?. Washington D.C., 98th Annual Meeting of the Transportation Research Board.
- Gerte, R. et al., 2019. Understanding the Relationships Between Demand for Shared Ride Modes: A Case Study Using Open Data From New York City. Washington D.C., 98th Annual Meeting of Transportation Research Board.
- Gessner, K., 2019. Rideshare: With IPOs looming, Uber leads market share, but Lyft has gained ground. <u>https://blog.secondmeasure.com/datapoints/rideshare-industry-overview/</u>
- Gimond, M. 2019. Intro to GIS and Spatial Analysis. Retrieved March 11, 2019, from <a href="https://mgimond.github.io/Spatial/index.html">https://mgimond.github.io/Spatial/index.html</a>
- Hall, J. D., Palsson, C. & Price, J., 2018. Is Uber a substitute or complement for public transit?. Journal of Urban Economics, Volume 108, pp. 36-50.
- Hoffman, K., Sundararajan, A. & Ipeirotis, P. G., 2016. Ridesharing and the Use of Public Transportation. <u>https://pdfs.semanticscholar.org/1461/e4b58fc0a1ddce2d033bb0ebc99361df5de6.pdf</u>
- Jin, S. T., Kong, H. & Sui, D. Z., 2019. Uber, Public Transit, and Urban Transportation Equity: A Case Study in New York City. The Professional Geographer.
- Metropolitan Transit Authority (MTA) [Data File], 2017. Turnstile Data. http://web.mta.info/developers/turnstile.html
- NYC Taxi & Limousine Commission (TLC) [Data File], 2017. TLC Trip Data. http://www.nyc.gov/html/tlc/html/about/trip\_record\_data.shtml
- Pfaff, B., 2008. VAR, SVAR, and SVEC Models: Implementation Within R Package. Journal of Statistical Software, 27 (4).
- Ravishanker, N., Dey, D. & Iyengar, M., 2001. Compositional Time Series Analysis of Mortality Proportions. Communication in Statistics-Theory and Methods, pp. 2281-2291.
- Rayens, W. S. & Srinivasan, C., 1991. Estimation in Compositional Data Analysis. Journal of Chemometrics, 5(4), pp. 361-374.

- Rayle, L. et al., 2016. Just a better taxi? A survey-based comparison of taxis, transit, and ridesourcing services in San Francisco. Transportation Policy, Volume 45, pp. 168-178.
- Ripley. B., Venables. B., Bates. D. M., Hornik. K., Gebhardt. A., and Firth., D. 2019. Package "Mass". https://cran.r-project.org/web/packages/MASS/MASS.pdf
- Schaller, B., 2018. The New Automobility: Lyft, Uber and the Future of American Cities, New York City: Schaller Consulting.
- Serhiyenko, V., 2014. Dynamic Compositional Modeling of Pedestrian Crash Counts on Urban Roads in Connecticut. Accident Analysis & Prevention, Volume 64, pp. 78-85.
- Shumway, R. H. & Stoffer, D. S., 2017. Time Series Analysis and Its Applications. 4 ed. Cham: Springer.
- Siddiqui, F., 2018. As ride hailing booms in D.C., it's not just eating into the taxi market it's increasing vehicle trips. <u>https://www.washingtonpost.com/local/trafficandcommuting/as-ride-hailing-booms-in-dc-its-not-just-eating-into-the-taxi-market--its-increasing-vehicle-trips/2018/04/23/d1990fde-4707-11e8-827e-190efaf1f1ee\_story.html?noredirect=on&utm\_term=.a2e517ba5b86
  </u>
- Smith, T. & Brundson, T., 1989. The Time Series Analysis of Compositional Data. Proc. Amer. Statist. Assoc, pp. 26-32.
- Toman, P., Zhang, J., Ravishanker, N. & Konduri, K., 2019. Dynamic Predictive Models for Ridesourcing Services in New York City Using Daily Compositional Data (under review).
- Warerkar, T., 2017. Uber surpasses yellow cabs in average daily ridership in NYC: For the first time ever, Uber has topped the city's yellow cabs in daily ridership figures. https://ny.curbed.com/2017/10/13/16468716/uber-yellow-cab-nyc-surpass-ridership

## **APPENDICES**

## A. Brief Review of Statistical Methods

### A.1. Dynamic Linear Model (DLM)

Dynamic linear modeling refers to a broad class of models that are readily generalizable to all manner of time series phenomenon. Indeed, the dynamic linear model is itself a subset of the even broader class of modeling frameworks known as state-space models. Two key characteristics define the state space modeling paradigm which is that we have a latent process denoted  $\Theta_t$  which is commonly called the state process. A key assumption of the state space model is that the state process is assumed to be Markovian, thus, the future and past observation are independent of the present. In addition, the observations, denoted as  $Y_t$ , are independent given the state process  $\Theta_t$ . This second feature implies then that any sort of dependence amongst observations is transmitted over time through the underlying state. The field of State Space Modeling or Dynamic Linear Modeling is a rich one and interested readers can find further expositions in Shumway and Stoffer (2017), Durbin and Koopman (2012), and numerous other texts on the subject.

#### A.2. Compositional Data Analysis

Compositional data can be broadly defined as data where all elements are non-negative and the sum of all data elements is equal to one. One can readily extend this idea of compositional data analysis to time series analysis where at every time point *t*, the sum of all the component time series are positive and sum to one. More formally, the G-variate compositional time series of positive value components can be defined as,  $\vec{X} = (X_{t,1}, \dots, X_{t,G})$  for  $t = 1, \dots, T$ , where the structure is defined by the g = G - 1 components such that,  $X_t$  lies in the g-dimensional simplex:

$$S^{g} = \left[ (X_{t,1}, \dots, X_{t,g}) : X_{t,1} > 0, \dots, X_{t,g} > 0; X_{t,1} + \dots + X_{t,g} = 1 \right]$$

In order to cope with issues such as non-normality, compositional data analysis is often performed via some sort of suitable transformation of the g-dimensional simplex into the g-dimensional Euclidean space  $\mathbb{R}^{g}$ . One of the quintessential data transformation approaches of compositional data analysis was the Additive Log Ratio (ALR) transformation and the Centered Log Ratio transformation (CLR), see Aitchison (1986). Rayens and Srinivasan (1991) generalized the ideas of compositional data analysis to include the Box-Cox transformation (1964), and Egozcue et al. (2003) expanded the topic through the development of the Isometric Log Ratio (ILR) transformation. Aitchison (1986), Smith and Brunsdon (1989), Ravishanker et al. (2001), and Serhiyenko et al. (2014) all discuss the topic of applying compositional methods in the context of time series analysis, the last paper dealing with transportation safety. The primary topic of interest in these papers is the use of some form of the generalized Box-Cox transformation, including the ALR transformation for compositional time series and the subsequent use of standard time series methods to analyze real, vector-valued data.



# **B.** Additional Plots of Local Moran's I

Figure B. 1 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals – Full Length







Figure B. 2 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals – Segment









Figure B. 3 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals – Season



















Figure B. 4 Recoded Local Moran's I and P-value of ARIMA/GARCH Residuals – Month



Figure B. 5 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals – Full Length

















Figure B. 7 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals – Season


















Figure B. 8 Recoded Local Moran's I and P-Value on ARIMA/GARCH/MLR Residuals – Month