

Development and Demonstration of an In-Vehicle Lane Departure Warning System using Standard GPS Technology

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JUNE 2021

Research Project
Final Report 2021-17



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Technical Report Documentation Page

1. Report No. MN 2021-17		2.		3. Recipients Accession No.	
4. Title and Subtitle Development and Demonstration of an In-Vehicle Lane Departure Warning System using Standard GPS Technology				5. Report Date June 2021	
				6.	
7. Author(s) S. Chowdhury, Md T. Hossain, M. I. Hayee				8. Performing Organization Report No.	
9. Performing Organization Name and Address Electrical Engineering University of Minnesota Duluth 1049 University Drive Duluth, MN 55812				10. Project/Task/Work Unit No. CTS #2019014	
				11. Contract (C) or Grant (G) No. (c)1003325 (wo)75	
12. Sponsoring Organization Name and Address Minnesota Local Road Research Board Minnesota Department of Transportation Office of Research & Innovation 395 John Ireland Boulevard, MS 330 St. Paul, Minnesota 55155-1899				13. Type of Report and Period Covered Final Design Report	
				14. Sponsoring Agency Code	
15. Supplementary Notes https://www.mndot.gov/research/reports/2021/202117.pdf					
16. Abstract (Limit: 250 words) A lane departure warning system (LDWS) has significant potential to reduce crashes on roads. Most existing commercial LDWSs use some kind of image processing techniques with or without Global Positioning System (GPS) technology and/or high-resolution digital maps to detect unintentional lane departures. However, the performance of such systems is compromised in unfavorable weather or road conditions, e.g., fog, snow, or irregular road markings. Previously, we proposed and developed an LDWS using a standard GPS receiver without any high-resolution digital maps. The previously developed LDWS relies on a road reference heading (RRH) of a given road extracted from an open-source, low-resolution mapping database to detect an unintentional lane departure. This method can detect true lane departures accurately but occasionally gives false alarms, i.e., it can issue lane departure warnings even when a vehicle is within its lane. The false alarms occur due to the inaccuracy of how the RRH originated from an inherent lateral error in open-source, low-resolution maps. To overcome this problem, we proposed and developed a novel algorithm to generate an accurate RRH for a given road using a vehicle's past trajectories on that road. The newly developed algorithm that generates an accurate RRH for any given road has been integrated with the previously developed LDWS and extensively evaluated in the field for detection of unintentional lane departures. The field test results showed that the newly developed RRH Generation algorithm significantly improved the performance of the previously developed LDWS by accurately detecting all true lane departures while practically reducing the frequency of false alarms to zero.					
17. Document Analysis/Descriptors Lane lines, Driver support systems, Roadway guidance markers, Dedicated short range communications				18. Availability Statement No restrictions. Document available from: National Technical Information Services, Alexandria, Virginia 22312	
19. Security Class (this report) Unclassified		20. Security Class (this page) Unclassified		21. No. of Pages 46	22. Price

DEVELOPMENT AND DEMONSTRATION OF AN IN-VEHICLE LANE DEPARTURE WARNING SYSTEM USING STANDARD GPS TECHNOLOGY

FINAL REPORT

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June 2021

Published by:

Minnesota Department of Transportation
Office of Research & Innovation
395 John Ireland Boulevard, MS 330
St. Paul, Minnesota 55155-1899

This report represents the results of research conducted by the authors and does not necessarily represent the views or policies of the Minnesota Department of Transportation or University of Minnesota. This report does not contain a standard or specified technique.

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ACKNOWLEDGMENTS

The authors wish to acknowledge those who made this research possible. The study was funded by the Minnesota Department of Transportation (MnDOT) and Minnesota Local Road Research Board (LRRB).

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LIST OF ABBREVIATIONS

RRH	Road Reference Heading
PAH	Path Average Heading
PAS	Path Average Slope
PADH	Path Average Differential Heading
ALS	Accumulated Lateral Shift
ADAS	Advance Driver Assistance Systems

EXECUTIVE SUMMARY

A lane departure warning system (LDWS) is a critical element among several other advanced driver-assistance systems (ADAS) that has significant potential to reduce roadway departure crashes. The majority of these crashes include a single vehicle running off the road and crashing into the roadside as well as head-on crashes between two opposing vehicles. Generally, LDWSs use image-processing or optical-scanning techniques to detect an unintentional lane departure. Most of the camera-based systems use different image-processing techniques such as a linear parabolic lane model or the extended edge-linking algorithm, both of which extract the lane markings from consecutive picture frames to calculate lateral shift of a vehicle. Some of the LDWSs can also detect the lane markings under varying lighting conditions. Similarly, optical scanning systems, which are comprised of a linear array of infrared transmitting devices to scan the lateral area of the highway for lane marking, are inherently independent of the varying lighting conditions.

Although advanced camera and optical sensor-based systems can be somewhat immune to varying lightening conditions, they work as expected only in favorable weather and road conditions. Their performance deteriorates when road conditions are not favorable, such as extensively worn or missing pavement markings, or harsh weather conditions, e.g., snow or severe rain, resulting in an inaccurate lane departure detection. Moreover, some systems use Global Positioning System (GPS) receivers in conjunction with the lane-level resolution digital maps to improve efficiency of a camera-based system, thereby making the overall system more complex and expensive to implement. To alleviate this problem, previously, the project developed an LDWS that uses a standard GPS receiver and low-resolution maps obtained from a commonly available digital mapping database without using any camera-based image processing. The proposed system used the low-resolution digital maps to extract a road reference heading (RRH) for any given road so that the current trajectory of any given vehicle on that road could be compared to the RRH of that road to detect an unintentional lane departure. That system was developed and tested in the field to evaluate its effectiveness. The field tests proved this system was effective enough to detect any unintentional lane departure; however, occasionally it produced false alarms, i.e., it produced false warning even when a vehicle was within its lane.

To alleviate this problem, a second phase of the project (to be discussed in this report) was proposed to develop an enhanced LDWS for which the needed RRH was not extracted from a low-resolution digital map but from a vehicle's past trajectories on the same road. The enhanced LDWS extracts RRH of any given road from a vehicle's past trajectories on that road using a novel algorithm without the need of any digital maps of the given road. The newly proposed RRH Generation algorithm generates RRH for any given road using a vehicle's one or more past trajectories on that road acquired by a standard GPS receiver. Once a RRH for a given road is generated, it is used to detect any future unintentional lane departure of a vehicle using the previously developed lane departure detection algorithm. The novelty of the newly developed enhanced LDWS comes from the fact that an accurate RRH is generated from a vehicle's past trajectories on any given road instead of extracting it from digital road maps.

The process of converting a vehicle's trajectory into a useful RRH works in three stages. In the first stage, a vehicle's GPS trajectory on any given road segment is used to identify any straight, curved, and transition

sections present in that road segment. There could be multiple straight, curved and transition sections present in any segment of a road for which the GPS trajectory is available. In the second stage, each identified section is characterized by a set of optimized parameters defining a RRH value at each point on that road section. In the third stage, all individual road sections are combined to obtain a composite RRH for that road segment. Once a RRH for any given road segment is generated, it is stored in a vehicle's RRH database and can be used to detect any future unintentional lane departure using the previously developed lane departure detection algorithm.

While a vehicle is moving on a given road for which the RRH has been previously generated, its trajectory is acquired in real time by a GPS receiver. At any given time, the lane departure detection algorithm calculates the vehicle's current heading and compares it with a previously generated RRH of that road at that point in time to calculate an instantaneous lateral shift. The instantaneous lateral shift accumulates over time and if the accumulative lateral shift exceeds a certain threshold, an unintentional lane departure is detected and an audible warning is issued. The audible warning stops as soon as an unintentional lane departure is corrected, i.e., the vehicle's trajectory becomes parallel to the RRH of that road. The lane departure is also detected in case of intentional lane departure, e.g., in case of a lane change; however, the distinction between an unintentional and intentional lane departure can be made by using the trigger initiated by the lane-change signal. After successfully developing the RRH Generation algorithm, it was integrated in the previously developed LDWS and extensive field tests were performed to evaluate the system's efficiency by detection of a variety of lane-departure scenarios on both straight and curved road segments of I-35 near Duluth, MN. The test results showed that the newly proposed algorithm significantly improved the performance of the previously proposed lane departure detection method by accurately detecting all true lane departures while reducing the number of false alarms to zero.

One of the limitations of the newly developed LDWS is that when a vehicle is traveling on a road for the first time, it will not have the required RRH of that road to detect an unintentional lane departure. To overcome this problem, the authors also proposed adding a vehicle-to-vehicle (V2V) communication component to exchange RRH between two vehicles when needed. In this case, a first-time travelling vehicle can request a RRH for that road from a neighboring vehicle that has traveled on that road before and has previously generated and stored a RRH for that road. This exchange process can be implemented either using cellular vehicle-to-vehicle (C-V2V) communication or dedicated short-range communication (DSRC). Once a RRH is successfully received from a nearby vehicle, it can be stored in the receiving vehicle's memory/database for future use. The V2V communication approach can only be successful when the market penetration of V2V communication-enabled vehicles reaches a critical level, which has not yet occurred.

As an alternative to the V2V communication approach, the proposed LDWS can also be integrated into popular smartphone apps, e.g., Waze, Google Maps or Apple Maps, to take advantage of the vast database of multiple GPS trajectories of the wider road network, which can then be used to generate RRH for almost any road, making it available for a vehicle to detect its unintentional lane departure on any road even when the vehicle is being driven on that road for the first time. Please note that the authors have been approved for a new project to develop a smartphone app for the newly developed LDWS, using a vehicle's

past trajectories. The successful development of this project will pave the way for integration of the proposed algorithm into one of the popular smartphone apps.

CHAPTER 1: INTRODUCTION

1.1 BACKGROUND

A lane departure warning system (LDWS) has significant potential to reduce crashes. According to the American Association of State Highway and Transportation Officials (AASHTO), almost 60% of fatal accidents are caused by an unintentional lane drifting of a vehicle on major roads (1). Roadway departure crashes are the greatest contributor to traffic fatalities in the United States. A recent study that compared crashes with and without an LDWS found that an in-vehicle LDWS was helpful in reducing crashes of all severities by 18%, those with injuries by 24% and those with fatalities by 86% (2). Systems that predict the driver's attentive state and intent of lane change (3-5) and provide map-based route guidance and/or warning about unintentional lane departure (6-7) are also useful to reduce severe road crashes.

Most available LDWSs rely on image processing technology using a camera or an optical scanning device to estimate a vehicle's lateral shift within a lane to detect an unintentional lane departure (8-12). Although advanced image-processing techniques work well in diminished lighting scenarios (13-14), the performance of image processing-based LDWSs deteriorates in unfavorable weather and road conditions, e.g., fog and snow-covered or worn-out road marking signs. To overcome these problems and improve performance, Global Positioning System (GPS) technology is integrated within vision-based LDWSs. However, such systems use differential GPS technology and/or inertial navigation sensors as well as high-resolution digital maps to estimate a vehicle's lateral shift in its lane, making such systems more complex and expensive to implement (15).

Previously, we proposed a novel method to accurately detect an unintentional lane departure using a standard GPS receiver and commonly available open-source, low-resolution digital maps (16). The previously proposed method estimates a vehicle's lateral shift by comparing the vehicle's heading acquired by a standard GPS receiver and road-reference heading (RRH) extracted from an open-source, digital map. Although this method works well to successfully detect unintentional lane departure, occasionally, it generates false alarms, i.e., it wrongfully issues lane departure warnings even when the vehicle is within its lane (16). The false alarms occur due to inherent error in open-source, digital maps that result in an error in the corresponding RRH of the given road extracted from such maps. We now propose another method to generate an accurate RRH for any given road using a vehicle's past GPS trajectories on that road without relying on open-source, digital maps.

Previously, many techniques have been proposed to process GPS trajectories to generate a routable road network or create a complete digital road map using graph and structured learning theory and/or statistical analysis (17-22). In this report, a novel algorithm is proposed to generate an accurate RRH from a vehicle's past GPS trajectories to improve the performance of the previously proposed lane departure detection method (16). The test results show that the newly proposed algorithm significantly improves the performance of the previously proposed lane departure detection method by accurately detecting all true lane departures while practically reducing the frequency of false alarms to zero.

One of the limitations of the newly developed LDWS is it requires that the vehicle has traveled on a given road at least once in the past to successfully generate a RRH for that road from a past vehicle trajectory that can be stored in a vehicle's RRH database. This RRH of a given road can then be used for future unintentional lane departure detection on that road. However, if a vehicle travels on a given road for the first time, its database will not have the necessary RRH for unintentional lane departure detection. To overcome this problem, vehicle-to-vehicle (V2V) communication can be used for a vehicle traveling for the first time on a given road to obtain the needed RRH from a nearby vehicle that has travelled on that road in the past and has already generated and stored the RRH for that road in its memory. To achieve this purpose, this part of the proposed project included a provision to add a V2V communication component in the newly developed LDWS.

The V2V communication approach can only be successful when the market penetration of V2V communication enabled vehicles has reached a critical level, which has not yet occurred. Furthermore, the V2V communication approach won't be effective in the case of an isolated vehicle traveling on a new route for the very first time even when the market penetration of V2V communication technology has reached a critical level.

Our proposed LDWS relies on the past trajectories of a vehicle on any given road to generate a RRH for that road to detect a future unintentional lane departure. Once a vehicle travels on a road, its trajectory is acquired using a GPS receiver to generate a RRH for that road, which is then stored in the database for future use. However, while traveling on a road for the first time, a vehicle does not have the necessary RRH for that road in its database. In this case, the vehicle can request the RRH for that road from a neighboring vehicle that has traveled on that road before and has previously generated and stored the RRH for that road. This process can be facilitated either using cellular vehicle-to-vehicle (C-V2V) communication or via dedicated short-range communication (DSRC). Once a RRH is successfully received from a nearby vehicle, it can be stored in the receiving vehicle's memory/database for future use. Both RRH generation and RRH exchange via V2V communication are explained in great detail in future chapters.

As a better alternative to V2V communication, the proposed LDWS can also be integrated into popular smartphone apps e.g., Waze, Google Maps or Apple Maps, to take advantage of the vast database of multiple GPS trajectories that can be used to generate a RRH for almost all roads, making it available for a vehicle to detect its unintentional lane departure on any road even when the vehicle is being driven on that road for the first time. Please note that we have just been approved for a new project (third phase) to develop a smartphone app for our proposed LDWS, using a vehicle's past trajectories. The successful development of this project will pave the way for integration of the proposed algorithm into one of the popular smartphone apps.

1.2 OBJECTIVES

The primary objective of the current project is the design and development of a road reference generation algorithm that in conjunction with the previously developed lane departure detection method can accurately detect all unintentional lane departures without generating unnecessary false alarms while the vehicle is in its lane. In an earlier project, we developed and successfully demonstrated a lane departure

warning system using a standard GPS receiver and commonly available low-resolution mapping data. This system acquires the trajectory of a moving vehicle in real time using a standard GPS receiver and compares it with a RRH of the road to detect lane departure. In that project, the necessary RRH of the road is provided by a low-resolution mapping database commonly available in any navigation system. The goal of the current project is to design, develop and demonstrate an in-vehicle lane departure warning system that will use an accurate RRH generated from a vehicle's past trajectories instead of relying on any digital mapping database.

The secondary objective of the current project is to provide a V2V communication component in the newly developed LDWS to facilitate exchange of RRH from one vehicle to another when needed. The purpose of having this objective is to ensure that vehicles travelling on a given road for the first time would be able to obtain a RRH of that road from one of the neighboring vehicles when needed.

1.3 METHODOLOGY AND SYSTEM ARCHITECTURE

The newly proposed algorithm generates a RRH for any given road using a vehicle's one or more past trajectories on that road acquired by a standard GPS receiver. Once a RRH for a given road is generated, it can be used to detect any future unintentional lane departure of a vehicle as illustrated in Figure 1.1, where the dashed line represents a vehicle's past trajectory, which can be used to generate a RRH for the road to detect a future unintentional lane departure, e.g., as represented by a dotted line in Figure 1.1.

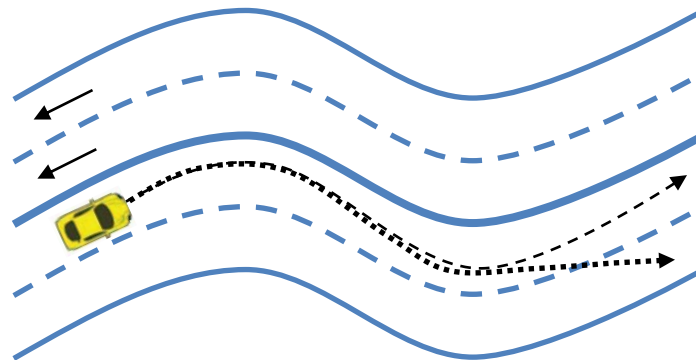


Figure 1.1 Conceptual diagram showing how recorded past trajectory (black dashed line) of a given vehicle can serve as reference direction of travel to detect its own unintentional lane departure in future (black dotted line).

The architecture of the proposed system, which combines the previously developed lane departure detection method and the newly proposed RRH Generation algorithm, is shown in Figure 1.2 where the GPS receiver acquires longitude and latitude of a moving vehicle's position in real-time to be used by both the RRH Generation algorithm and the LDWS. The RRH Generation algorithm uses a sufficient length of a GPS trajectory on a given road to generate a RRH for that road using the newly developed algorithm. On the other hand, LDWS works in real-time to detect unintentional lane departure, using the previously proposed lane departure detection method except that it uses the RRH generated by the RRH Generation algorithm, using one or more past GPS trajectories as opposed to the RRH extracted from an open-source,

low-resolution map used in the previous project. The LDWS can detect an unintentional lane departure of any vehicle on a given road if the vehicle has been driven on that road at least once before so that the necessary RRH for that road has already been generated by the RRH Generation algorithm. Please note that the proposed algorithm is suitable to be integrated into smartphone apps, e.g., Waze, Google Maps, or Apple Maps, to take advantage of the vast database of multiple GPS trajectories of a broader road network that could be used to generate a RRH for almost all roads using the proposed algorithm. This can enable any vehicle to detect an unintentional lane departure on any road even when the vehicle is being driven on that road for the first time.

Our proposed LDWS relies on the past trajectories of a vehicle on any given road to generate a RRH for that road to detect a future unintentional lane departure. Once a vehicle travels on a road, its trajectory is acquired using a GPS receiver to generate a RRH for that road, which is then stored in the database for future use (Figure 1.2). However, while traveling on a road for the first time, a vehicle does not have the necessary RRH for that road in its database. In this case, the vehicle can request the RRH for that road from a neighboring vehicle that has traveled on the road before and has previously generated and stored the RRH for that road. This process can be facilitated either using cellular vehicle-to-vehicle (C-V2V) communication or via dedicated short-range communication (DSRC). Once a RRH is successfully received from a nearby vehicle, it can be stored in the receiving vehicle’s memory/database for future use.

The system architecture of the proposed project as shown in Figure 1.2 also highlights the scope of the current project as opposed to the overall project. The small black-dashed rectangle (vertical) shows the scope of the previously developed LDWS project (Phase 1), which was successfully completed two years ago. The large, black-dashed rectangle (horizontal) represents the scope of the current project (Phase 2). The scope of the two main objectives of the current project are also marked separately in Figure 1.2. The blue-highlighted portion of Figure 1.2 enclosed in a blue-dashed boundary captures the scope of the primary objective, while the red-dashed rectangle represents the scope of the secondary objective of the current project. The details of the methodology and implementation of both of these objectives will be described in this report in the next two chapters followed by field tests and results in the last chapter.

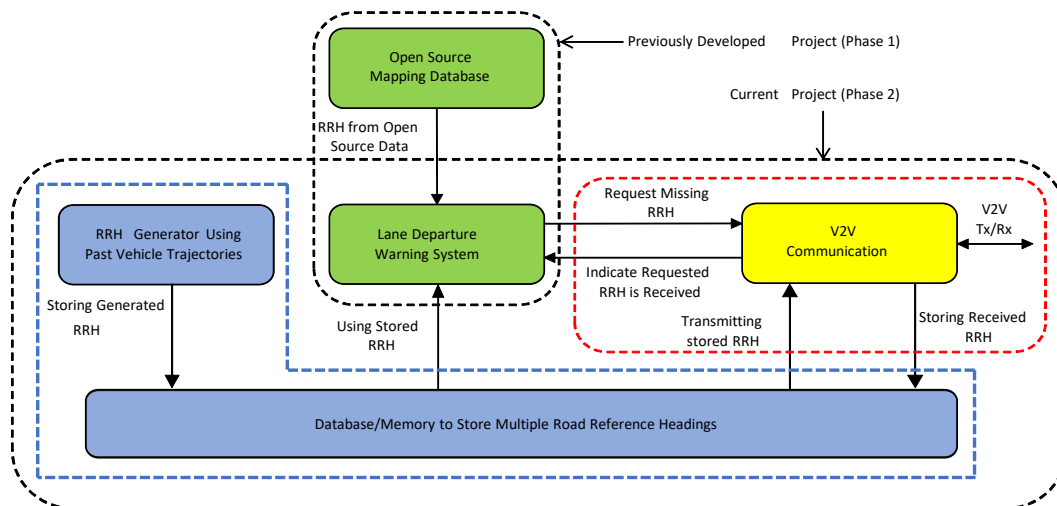


Figure 1.2 Architectural diagram of the proposed LDWS.

CHAPTER 2: ROAD REFERENCE HEADING GENERATION

This chapter will highlight the details of primary objective of the current project which is to develop an algorithm to generate a RRH for any given road using a vehicle's past trajectories on that road.

2.1 RRH GENERATION ALGORITHM

Any typical road segment may consist of combinations of many straight and curve road sections as shown in Figure 2.1 where a conceptual diagram of a road segment with a curve section sandwiched by two straight sections is shown. Usually, a road is not curved abruptly, therefore, a transition section – however, small - exists between a straight and a curve section of the road as illustrated in Figure 2.1(a). The heading at each point of the road is shown in Figure 2.1(b) and differential heading is shown in Figure 2.1(c). The heading for a straight section remains constant while it changes uniformly for a curve section (Figure 2.1b). Similarly, the differential heading for a straight section remains zero while it has a non-zero constant value for a curve section (Figure 2.1c). For sharper curves, the magnitude of non-zero value is larger. The vehicle trajectory obtained by a standard GPS receiver consists of a vehicle

location estimated by a GPS receiver every 100 msec and can be used to obtain heading and differential heading at any given point on a road. In reality, both heading and differential heading of a given road derived from a vehicle trajectory acquired by a standard GPS receiver exhibit some fluctuation for both straight and curve sections. The intensity of this fluctuation is contributed by both inherent GPS error and driver's ability to always keep the vehicle in the center of the lane. The dashed lines in Figure 2.1(b) and 2.1(c) indicate the magnitude of such fluctuation for both heading and differential heading.

Our designed algorithm to convert a previously recorded vehicle trajectory acquired by a standard GPS receiver into a useful road reference works in three stages. In the first stage, various straight, curve and transition sections present in the road are identified from the given trajectory. In the second stage, each identified section is characterized by a set of parameters so that it can be used as a RRH value at each point of the road. In the third and final stage, all individual sections are combined to obtain a composite RRH for the road. Our algorithm uses vehicle's differential heading to identify various sections present in a given road segment for which the trajectory is available. Before all three stages of the algorithm are described in more detail, it is important to statistically characterize the scale of the spurious fluctuation

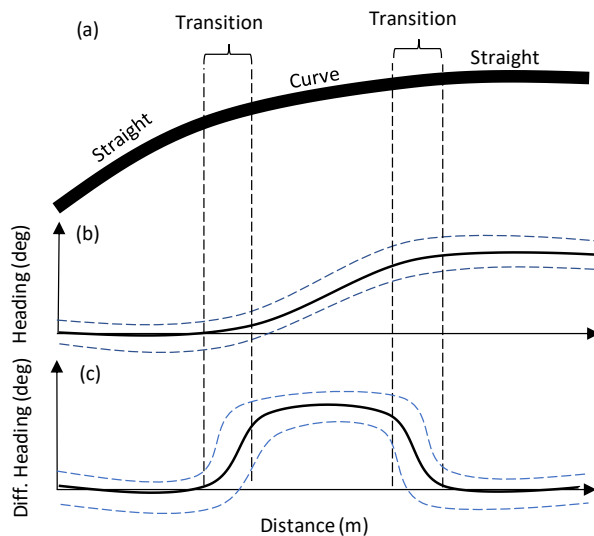


Figure 2.1 The conceptual diagram showing heading and differential heading of a road with two straight sections and a curve section including transition sections

in both heading and differential heading for a practical vehicle trajectory obtained from a standard GPS receiver.

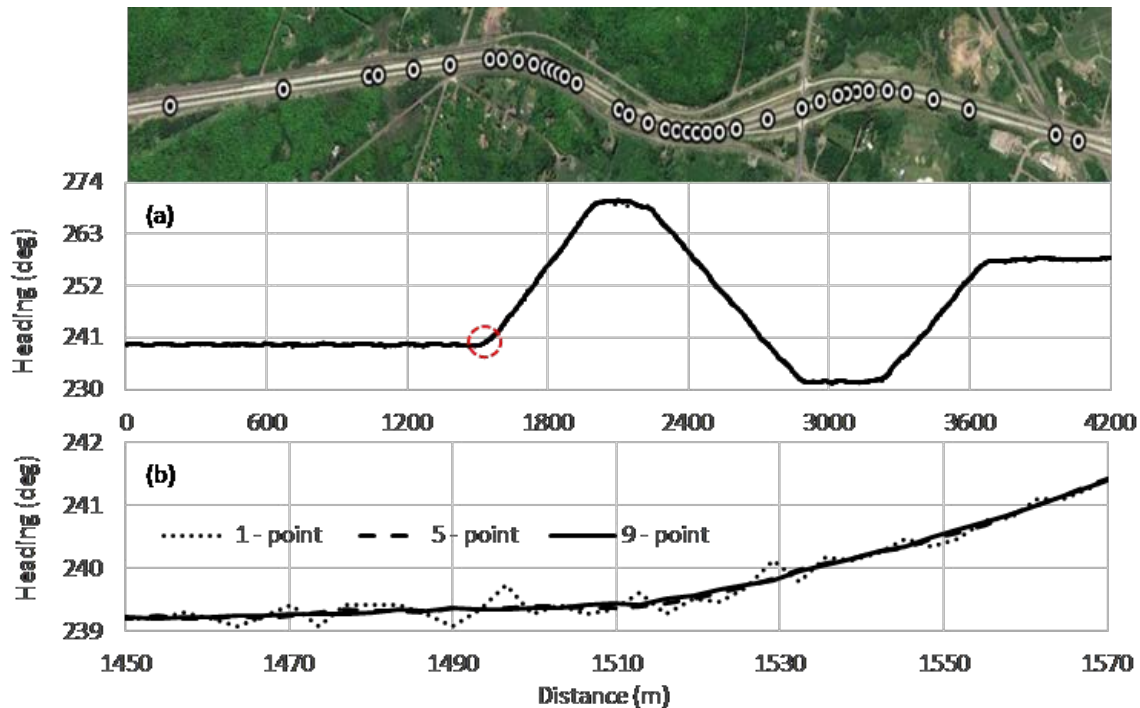


Figure 2.2 Vehicle heading vs. distance for (a) the complete road segment and (b) a small portion of the road segment highlighted by a dashed red circle. The picture of Google Map of the relevant portion of the road is shown on the top.

A typical vehicle trajectory acquired on the Interstate I-35 south bound (near Duluth, MN) for a ~4 km segment is given in Figure 2.2 where vehicle heading is plotted versus distance. There are three graphs shown in Figure 2.2a where heading is calculated using three different methods. The 1-point heading at any given point is calculated as the heading between that point and the previous point. The 5-point and 9-point heading at any given point are calculated as the path average heading using 5 and 9 points, respectively, including 2 and 4 neighboring points on each side. There are two types of fluctuation seen in any typical vehicle trajectory. The first type is a high frequency fluctuation which is caused by GPS inherent error which is commonly known as GPS noise. The second type is a low frequency fluctuation which is caused by vehicle's wandering within the lane. The magnitude of low frequency fluctuation remains almost same in all three methods of heading calculations while the GPS noise (high frequency fluctuation) reduces when more points are included in the heading calculation by taking a moving average. This can be seen in Figure 2.2b where a zoomed in portion of the Figure

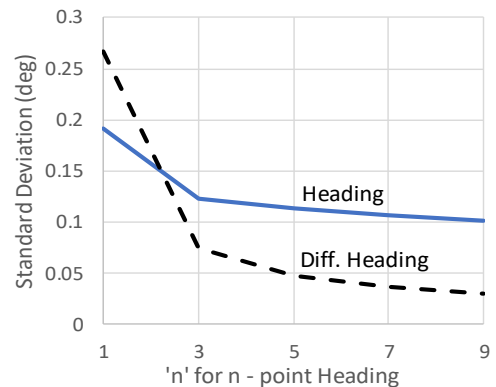


Figure 2.3 Standard deviation of heading and differential heading using n-point calculation method for varying values of n.

2.2a highlighted by a red dashed circle, is shown to illustrate the difference among heading values using 1-point, 5-point and 9-point methods.

The GPS noise (high frequency fluctuation) can be measured by the standard deviation of heading and differential heading obtained from a vehicle trajectory. The standard deviation of heading using n-point heading calculation method reduces when n increases as shown in Figure 2.3 where the standard deviation of n-point heading is plotted for a typical vehicle trajectory on a straight road section. Similarly, the GPS noise in differential heading significantly reduces with increasing n as shown in Figure 2.3 where standard deviation of differential heading for the corresponding portion of trajectory is also plotted. As can be seen from Figure 2.3 that GPS noise exhibiting in both heading and differential heading reduce with increasing n and the reduction trend saturates around $n = 9$. Therefore, our algorithm uses 9-point heading and differential heading calculation method to identify and characterize various road sections from a given vehicle trajectory. The standard deviation of heading and differential heading is 0.1° and 0.03° , respectively, using 9-point method. After statistically characterizing the scale of fluctuation in heading and differential heading, all three stages of our designed algorithm i.e., identifying, characterizing, and combining all characterized sections into a useful road reference are described below in detail.

2.1.1 Identification of Various Sections

The heading for a straight road section remains constant while it changes uniformly for a curve section. Similarly, the differential heading for a straight section is zero while it has a non-zero constant value for a curve section with larger values for sharper curves. A typical vehicle trajectory acquired by a standard GPS receiver consists of its position coordinates at fixed time intervals (typically every 100 msec). Any two

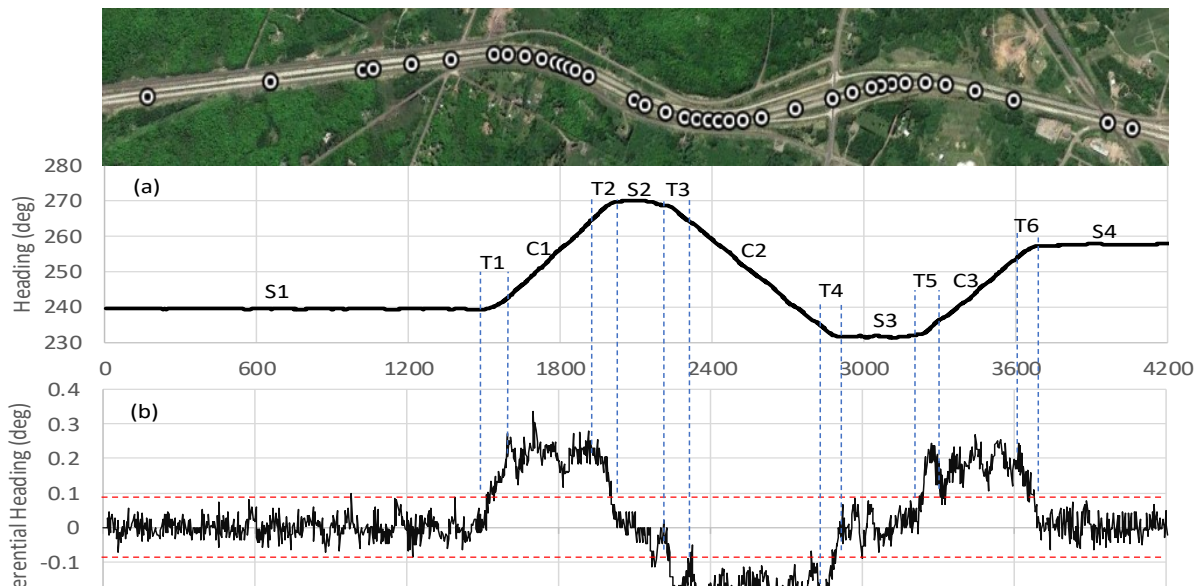


Figure 2.4 (a) Vehicle heading and (b) differential heading vs. distance for the entire trajectory. The picture of Google Map of the relevant portion of the road is shown on the top

consecutive position coordinates of a moving vehicle on a given road can be used to obtain heading and differential heading of the road at that point.

The proposed algorithm uses differential heading to identify various sections present in a given road by first identifying all straight sections where differential heading remains zero followed by curve sections where differential heading is a non-zero constant. The transition sections are identified at the end.

To illustrate the individual section identification process, heading and differential heading calculated from a typical GPS trajectory versus distance are shown in Figure 2.4a and 2.4b, respectively. The GPS trajectory was acquired using a standard GPS receiver with a UBlox LEA-6 chipset on a 4.2 km section of Interstate I-35 while driving at 70 MPH. The heading at each point of the given road, calculated from a vehicle's GPS trajectory, exhibits a high-frequency noise over distance caused by inherent GPS error which is further accentuated in differential heading values as shown in Figure 2b. This high-frequency noise can be reduced by moving average method using more than two consecutive GPS points for heading and differential heading calculation. For the proposed algorithm, a 9-point moving average was used to reduce the standard deviation of differential heading to 0.03° .

2.1.1.1 Identification of Straight Sections

Although the average differential heading of a straight section is zero, the instantaneous differential heading at any point of a straight section fluctuates around zero due to GPS noise. This fluctuation remains within the boundaries of $\pm 0.09^\circ$ or three times the standard deviation of differential heading as shown in Figure 2.4b. The proposed algorithm identifies straight sections by comparing the differential heading with a threshold of $\pm 0.09^\circ$ as shown by dashed red line in Figure 2.4b. Whenever the differential heading exceeds the threshold of $\pm 0.09^\circ$ in either direction, the crossing points are marked as the beginning and ending points of the straight sections of the road. All such points are shown by vertical blue dashed lines in Figure 2.4, identifying a total of four straight sections from the given trajectory which are marked as S1, S2, S3, and S4.

There is no lane change present in the trajectory of Figure 2.4. However, in reality, a vehicle may change lanes while traveling on a multiple lane road. The lane changes present in any given trajectory may wrongfully be considered as road curvature on that road. However, the differential heading during any typical lane change does not exceed the threshold of $\pm 0.09^\circ$. Therefore, the proposed algorithm can correctly identify all straight sections of the road even if lane changes are present in a given trajectory.

2.1.1.2 Identification of Curve Sections

To identify a curve section between any two consecutive straight sections, the proposed algorithm calculates a path average differential heading (PADH) between the ending point of the first and beginning point of the second of the two consecutive straight sections.

There is usually a curve and two transition sections present between any two consecutive straight sections. Therefore, the value of calculated PADH between two straight sections will be slightly smaller than the true PADH value of the curve section alone because its calculation includes the two adjoining

transition sections on each side of the curve as illustrated in Figure 2.5, where a zoomed-in portion of the trajectory of Figure 2.4 is reproduced showing only the first curve section surrounded by two straight sections (S1 and S2) and corresponding transition sections. To identify the beginning and ending points of a curve section alone, a set of two points between two consecutive straight sections (one on each side) are identified where the differential heading value is closest to the calculated PADH.

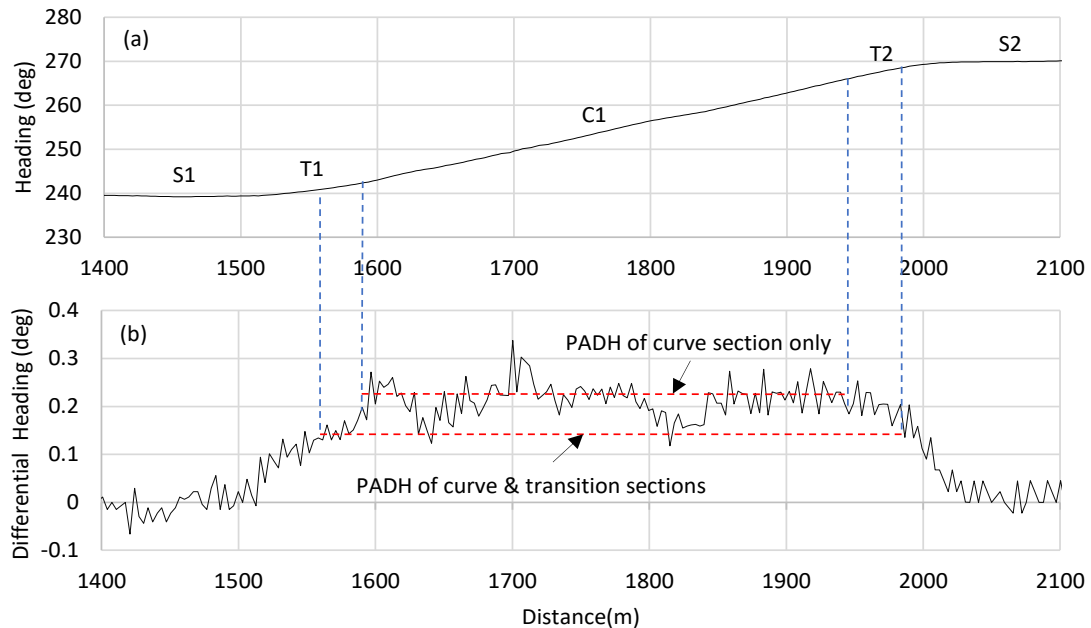


Figure 2.5 (a) Vehicle heading and (b) differential heading vs. distance for a small portion of the trajectory of Figure 2.4. This portion includes a part of first straight section, S1, T1, C1, T2, and a part of S2.

The beginning and ending points of a curve section identified this way will still not be the true beginning and ending points of the curve because PADH value used to identify these points was calculated for the curve section including the two transition sections. Therefore, a second iteration of the same routine is performed by calculating a new PADH value between the two points identified in the first iteration. The new PADH value calculated in the second iteration is more likely to be closer to the true PADH value of the curve section alone because it is calculated for the curve section including only the extreme ends of the transition sections on both sides. This process can be repeated, however, beyond two iterations, the beginning and ending points of a curve section do not change significantly. Using this method, all curve sections can be identified in any given GPS trajectory. A total of three curve sections (C1, C2, and C3) were identified in the given GPS trajectory of Figure 2.4. Please note that the proposed algorithm can correctly identify all curve sections in a given trajectory even when a lane change is present for the same reason as explained for a straight section.

2.1.1.3 Identification of Transition Sections

After identifying the beginning and ending points of all straight and curve sections, all remaining portions of the trajectory are marked as transition sections. The beginning and ending points of any transition

section will be the ending and beginning points of adjoining straight and curve sections as shown for the transition sections T1 and T2 in Figure 2.5. Similarly, all transition sections in any given trajectory are identified.

2.1.2 Characterization of Various Sections

After identifying all individual sections of the road from a given trajectory, each section is characterized separately with a proper set of parameters to define RRH at each point of the given road section. Each straight section is characterized with a path average heading (PAH) as heading remains the same for the entire length of a straight section. Similarly, heading of a curve section changes uniformly with distance, therefore, it is characterized with a path average heading slope (PAHS) and an initial heading (IH) i.e., the heading at the beginning point of the curve section to completely define RRH at each point of the curve section. For a transition section, heading neither remains the same as in a straight section nor does it change uniformly with distance as in a curve section suggesting that a transition section should be characterized as a second-order polynomial. However, the length of a typical transition section is usually too small to characterize it as a second-order polynomial. Furthermore, the incremental accuracy of RRH with a second-order characterization is negligibly small. Therefore, the proposed algorithm characterizes each transition section just like a curve section i.e., with IH and PAHS values. Please note that the PAHS value of a transition section is different from the PAHS value of the adjoining curve section.

2.1.2.1 Characterization of Straight Section

Each straight section is initially characterized with a PAH value, between the beginning and ending points of a straight section, calculated using **Equation 1**:

$$PAH = \frac{\sum d_n h_n}{\sum d_n} \quad (1)$$

Where h_n is the vehicle heading between any given point n and its previous point, and d_n is the distance between the two points. However, the initially assigned value of PAH for any given straight section may not be the optimal value. To find the optimal value of PAH for a straight section, the heading error between the vehicle heading and PAH should be minimized. The value of PAH is varied in small increments around its initially assigned value and root mean square of heading error (RMSHE) is calculated for each value of PAH using **Equation 2**:

$$RMSHE = \sqrt{\langle |h_n - h_{ref}|^2 \rangle} \quad (2)$$

Where h_{ref} is the RRH i.e., PAH for a straight section. The RMSHE for the first straight section (S1) of Figure 2.4 is shown in Figure 2.6a for varying values of PAH. The RMSHE remains almost flat for a wide range of PAH values suggesting that optimal value of PAH is not very sensitive to small changes. Although minimizing RMSHE would result in an optimized value of h_{ref} for a given straight section, the objective at hand is to minimize ALS for each section because ALS is to be used to detect unintentional lane departure.

Therefore, the absolute value of ALS ($|ALS|$) is also calculated by varying PAH value for each straight section using **Equation 3**:

$$|ALS| = \left| \sum_{k=1}^n d_k \sin(h_k - h_{ref,k}) \right| \quad (3)$$

Where $h_{ref,k}$ is the RRH value at the current point, k , of the road. The calculated value of $|ALS|$ for different PAH values around its initially assigned value for the section S1 is also shown in Figure 2.4a, along with RMSHE values, revealing a clear minimum. The optimal value of PAH (239.50°) not only minimizes $|ALS|$ but also falls within the flat minimum range of RMSHE. The same general trend was true for all straight sections of the trajectory. Using this method, any straight section can be characterized with an optimal value of PAH.

Please note that the heading can change significantly as opposed to differential heading during a lane change present in a trajectory. Therefore, the optimal value of PAH can be adversely affected for a straight

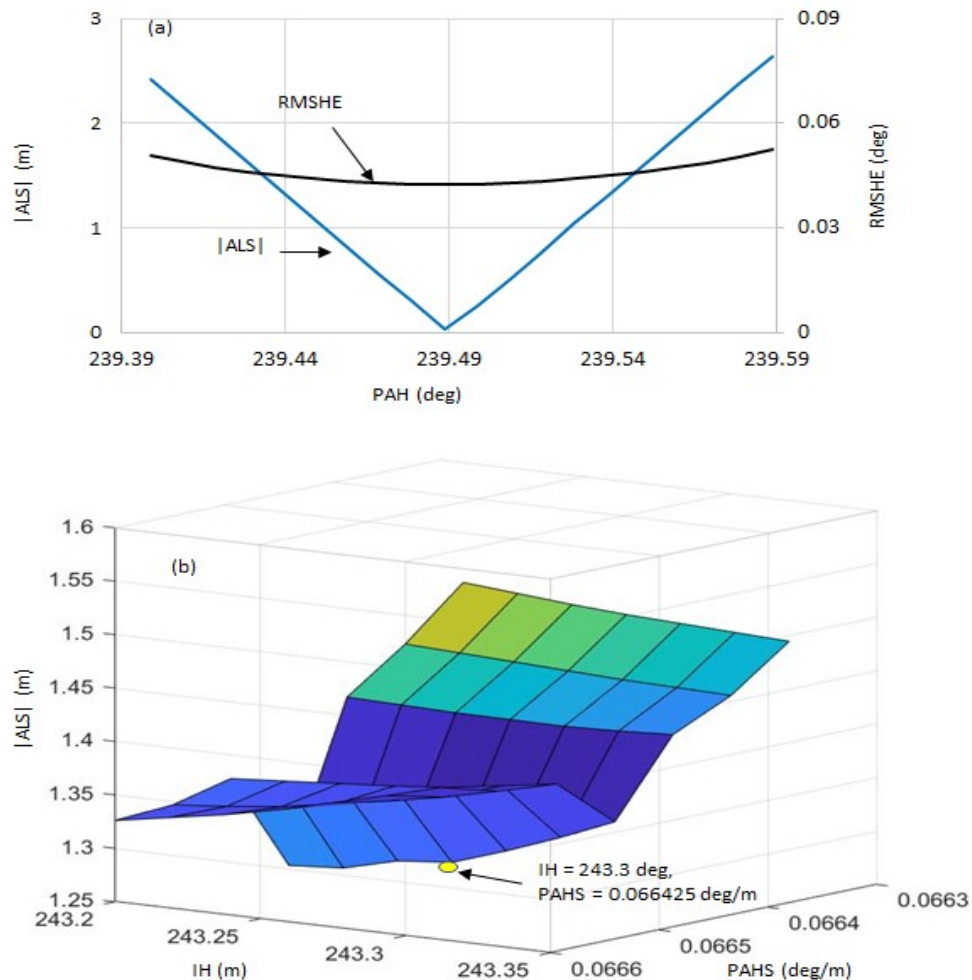


Figure 2.6 (a) RMSHE and $|ALS|$ vs. PAH for the straight section S1 showing optimal value of PAH, and (b) a surface plot of $|ALS|$ vs. IH and PAHS for the curve section C1 showing optimal combination of IH and PAHS values

section if a lane change is present. The proposed algorithm can detect the location and span length of such a lane change and optimize the PAH value excluding the lane change portion of the section.

2.1.2.2 Characterization of Curve Section

As described earlier, each curve section is characterized with two parameters, i.e., IH and PAHS. An initial value of IH is assigned as the heading at the beginning point of any curve section and the initial value of PAHS is assigned using **Equation 4**:

$$PAHS = \frac{(\sum d_n \times \frac{h_n - h_{n-1}}{d_n})}{\sum d_n} \quad (4)$$

Where h_n is the heading between any given point n and its previous point, and h_{n-1} is the heading between point $n-1$ and its previous point. After initial values are assigned to both IH and PAHS for a curve section, they are optimized by minimizing |ALS| by varying both IH and PAHS values in small increments around their initially assigned values. The optimization process is illustrated in Figure 2.6b, where |ALS| is plotted versus IH and PAHS as a surface plot for the curve section C1. Please note that the resulting optimal values of IH and PAHS are 243.30° and 0.066425 deg/m, respectively, and are noticeably different from their corresponding initially assigned values (243.26° and 0.066475 deg/m). Using the same method, all other curve sections are optimized. Please note that the optimization of a curve section in the presence of a lane change is performed the same way as described for straight section.

2.1.2.3 Characterization of Transition Section

As discussed earlier, each transition section is characterized as it is a curve section. Therefore, it should be initially assigned with two parameters, i.e., IH and PAHS, and their optimization process should be similar to that of a curve section. However, if both parameters are optimized independently, there is a possibility of an abrupt change of heading at corner points where transition section adjoins a straight or a curve section. This is because the end points of any transition section are the same as the beginning and/or ending points of adjoining straight and/or curve sections. Therefore, the characterization of transition section is more straightforward. The optimized heading at the ending point of the preceding straight or curve section is considered as the IH value of the transition section. Similarly, an optimal value of PAHS for a transition section is calculated using the optimized values of heading at the two end points of the transition section.

2.1.3 Combining All Sections to Generate a Composite RRH

After identifying and characterizing each section with an optimal set of parameters, all sections are combined to generate a composite RRH for that road. The typical output file generated by the algorithm is shown in Figure 2.7, where each row represents an individual section of the road defined by its beginning and ending points (in terms of latitude and longitude), the optimized parameter values, and the section type. Please note that an “N” indicates that the corresponding parameter is not applicable to that section. This file has the necessary information to completely define the RRH at any point along the road

and can be used to detect an unintentional lane departure in real-time using previously proposed lane departure detection method.

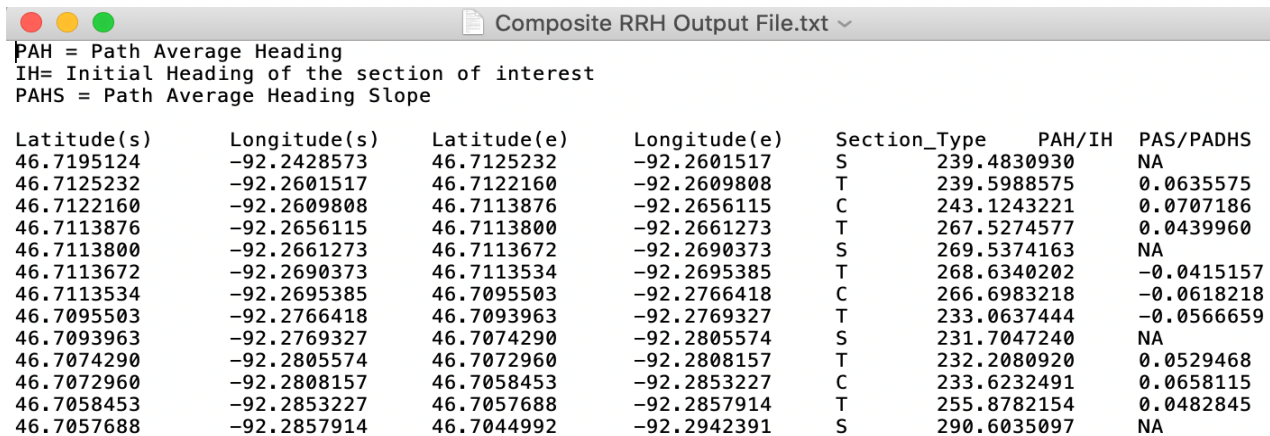


Figure 2.7 Screenshot of a typical output file containing optimized parameters of each section in a composite RRH

A composite RRH generated from a single trajectory may not be accurate for all future trajectories because usually, a vehicle will take a slightly different trajectory in each new trip on the same road. However, multiple composite RRHs obtained from different vehicle trajectories for a given road can be combined to obtain an average composite RRH. The combination of two or more composite RRHs generated from different individual GPS trajectories is achieved in two steps. First, every optimized parameter of each straight and curve section is combined using a simple average method. Second, the beginning and ending points of each straight and curve section are combined by averaging the latitude and longitude values of the beginning and ending points, separately.

After combining all straight and curve sections, transition sections are automatically combined because the beginning and ending points of all transition sections are the same as the beginning and ending points of adjoining straight and/or curve sections as described earlier. Using the same averaging method, each additional composite RRH generated from a future vehicle trajectory can be added to an already existing average composite RRH to improve its accuracy over time.

The proposed algorithm was applied to many vehicle trajectories on the same road segment of Interstate I-35 and a composite RRH was generated from each trajectory. Three such composite RRHs generated from three different trajectories on the same road and the average composite RRH are shown in Figure 2.8a where heading versus distance is plotted across the entire 4.2 km length.

The difference in heading values of multiple composite RRH is not visible in Figure 2.8a because of the large variation of heading over the span of the road segment. To highlight the difference in different composite RRH values, a zoomed-in portion of Figure 2.8a marked by a red dashed circle is shown in Figure 2.8b. The zoomed-in portion includes the right-side portion of S2, entire T2, and the left side portion of C2 sections of the road where the difference in heading values of each composite RRH is more pronounced showing the averaging effect.

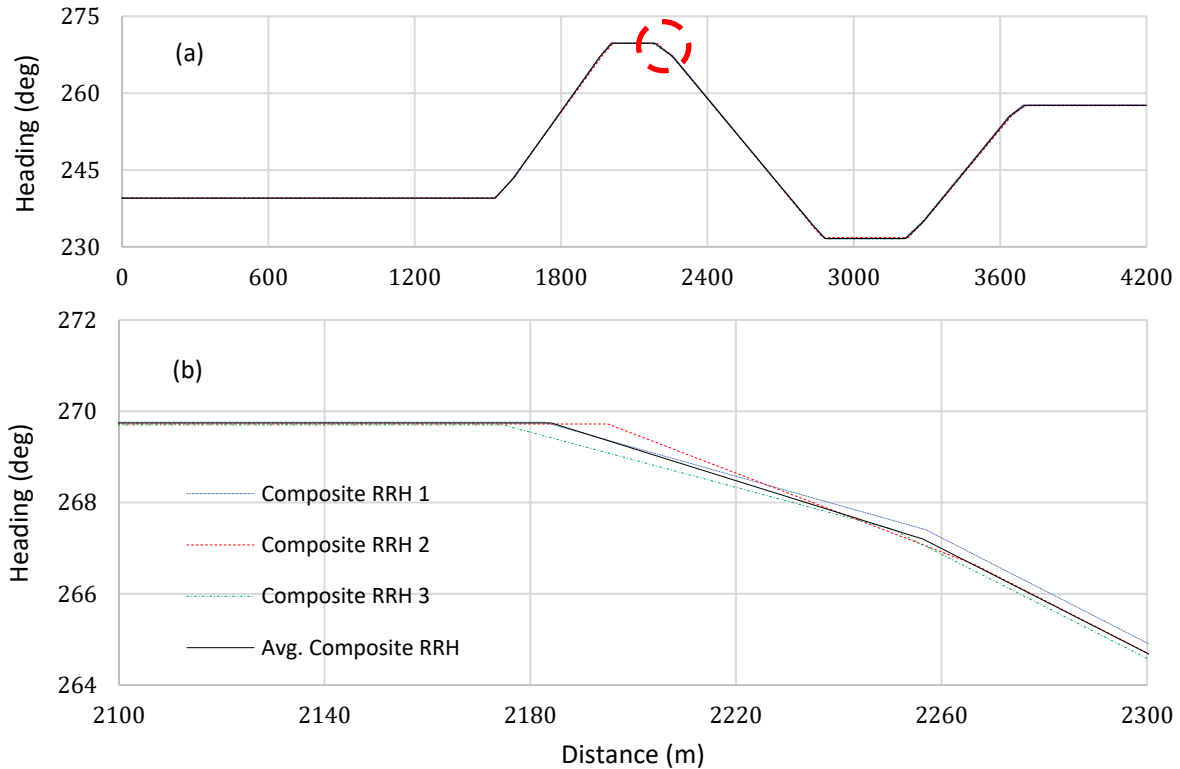


Figure 2.8 (a) Heading of average composite RRH and three individual composite RRH obtained from three different vehicle trajectories of 4.2 km segment of Interstate I-35, and (b) zoomed portion of (a) highlighted by red dashed circle

2.2 EFFECT OF NON-STANDARD TRAJECTORIES ON RRH

So far, we have used vehicle trajectories where a vehicle travelled in the same lane for the entire length of the trajectory without making any lane change during the travel. This may not be true for all practical vehicle trajectories. Therefore, it is important to see the effect of a lane change present in a given trajectory on both identification and characterization of various sections. The scenario of lane change in case of a straight and a curve section is illustrated in Figure 2.9a and 2.9b, respectively. The top row of Figure 2.9a and 2.9b shows a vehicle trajectory with a lane change from right-to-left in the middle of the trajectory on a two-lane road for a straight section and a curve section, respectively. The relative heading and differential heading of the two trajectories are also shown in Figures 2.9a and 2.9b, respectively, for both straight and curve section. Whenever a lane change is made from right to left side on a straight or a curve road section, vehicle heading deviates from its normal value and first increases (or decreases for case of a lane change from left-to-right) and then changes back to its normal trend as can be seen from Figure 2.9. Similarly, the differential heading deviates around zero for a straight section and around a non-zero constant value for a curve section during the span of the lane change. However, the differential

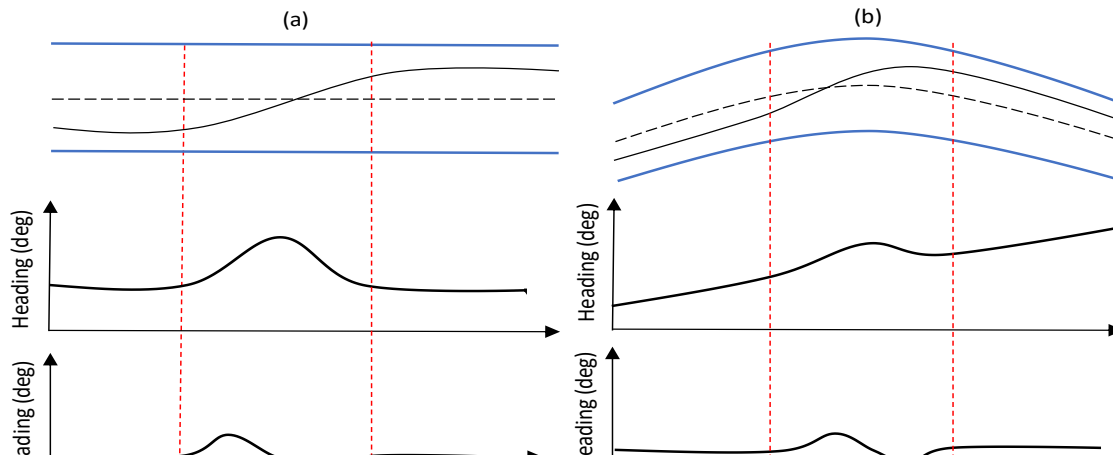


Figure 2.9 A conceptual diagram showing a lane change and resulting deviation in heading and differential heading for (a) a straight section, and (b) a curve section

heading is inherently much noisier than the heading of the vehicle as seen in Figure 2.10 in which both heading and differential heading of an actual trajectory on a straight section are plotted vs. distance, respectively in a and b. In this part of the trajectory, there are two lane changes present which can be seen from Figure 2.10a (i.e. from the heading) but the corresponding back and forth deviation in differential heading is buried in noise (Figure 2.10b). The back and forth deviation in differential heading, during a typical lane change, is usually smaller than 3 times the standard deviation of the differential heading ($\pm 0.09^\circ$), which is used by our algorithm as a threshold to identify various sections in any given trajectory. Therefore, a lane change present in any given trajectory on either a straight or a curve section will not adversely affect the identification process of any section present in that trajectory.

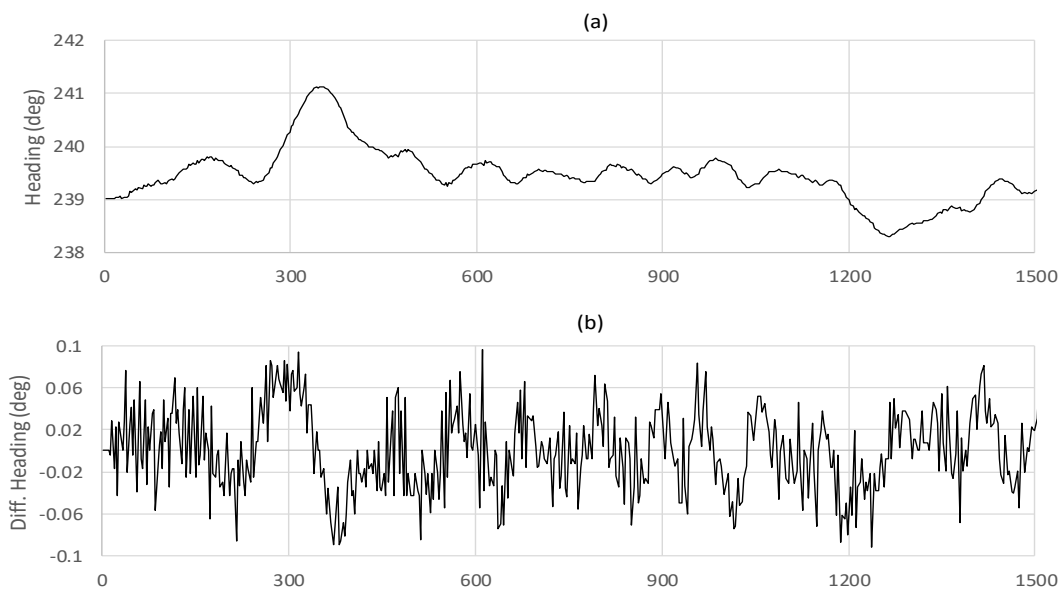


Figure 2.10 (a) Heading, and (b) differential heading vs. distance for a straight section with two lane changes.

After identifying various sections, our algorithm uses heading of a trajectory to characterize each section separately. Therefore, the characterization of each section may be negatively affected due to deviation in heading during the span of the lane change in any given section. To explore the potential negative impact of a lane change present in a given trajectory on the characterization of various sections, we processed a vehicle trajectory with multiple lane changes using our algorithm. As expected, our algorithm correctly identified all sections of the given trajectory. After identifying each section, our algorithm characterized each of the straight and curve sections separately to obtain a road reference. The adverse effect due to lane change on characterization of both straight and curve sections is discussed below.

2.2.1 Effect of Lane Change on Characterization of a Straight Section

We used the first straight section (S1) of a trajectory which is the longest straight section in this trajectory (~1,500 m). There was a total of three lane-changes present in this trajectory in the first 1000 m. Our algorithm assigned this section an optimized value of PAH at first to characterize it which becomes h_{ref} at any given point on this straight section.

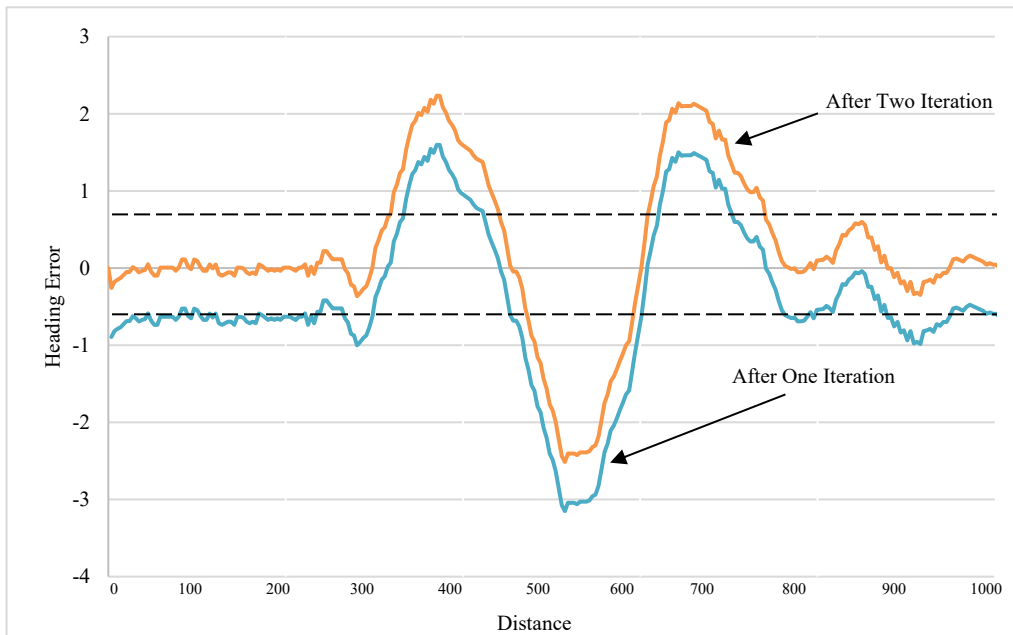


Figure 2.11 Heading error vs. distance for a straight section with three lane changes

In this case, the RMSHE ($\sim 0.87215^\circ$) for the optimized PAH value was almost seventeen times larger as compared to the usual range of RMSHE ($< 0.05^\circ$) for the optimized PAH values for a typical straight section extracted from a trajectory without any lane change. This implies that either the curve fitting (or characterization) for this straight section was totally off by the presence of a lane change(s) in the trajectory or alternatively the curve fitting was appropriate and the large value of RMSHE is due to the deviation in heading caused by lane change(s) present in the trajectory. To illustrate this point, the curve fitting error $h_e = h_n - h_{ref}$ vs. distance is plotted in Figure 2.11 as blue line. In reality, h_e should be around zero throughout the length of the section.

The blue line in Figure 2.11 indicates that the characterization of this straight section i.e., h_{ref} cannot provide the true reference for this straight section because h_e is not close to zero for most of the trajectory in spite of having an average value of zero. This implies that there are at least one or more but odd number lane changes present in this trajectory.

This is further bolstered by the large value (0.87215°) of RMSHE (or standard deviation) of h_e . The two dashed lines highlight the standard deviation threshold which can be used to detect the span of the lane change. Because there are three lane changes in this trajectory, a second iteration is needed to characterize this straight section to obtain a true reference.

After detecting the location and span of any lane changes, a second iteration is performed excluding the lane change portions of the trajectory. The second iteration results in a new PAH characterizing the straight section with a new RRH. Using this new RRH, h_e is re-calculated and shown in the same graph of Figure 2.11.

As can be seen from the yellow line of this figure, h_e for the new reference is zero at most of the points on the trajectory except during the lane change portion implying a valid characterization for the straight section. This second iteration method is needed to truly characterize any straight section with one or more odd number of lane changes.

2.2.2 Effect of Lane Change on Characterization of a Curve Section:

To explore the negative impact of a lane change on the characterization of a curve section, we used the first curve section of the trajectory (C1) which is $\sim 400\text{m}$ long. There was only one lane change (right-to-left) present in the middle of the trajectory on this curve section.

In the first iteration (normal characterization routine), our algorithm assigned this curve section an optimized value IH and PAHS to characterize it i.e., to completely define RRH at any given point of the curve section. The $h_e = h_n - h_{ref}$ is plotted vs. distance for this curve section in Figure 2.12.

The average value of h_e is almost zero but its RMSHE (or standard deviation) is 0.75° highlighted by two dashed lines on either side of the average in Figure 2.12. As can be seen from the Figure that h_e crosses

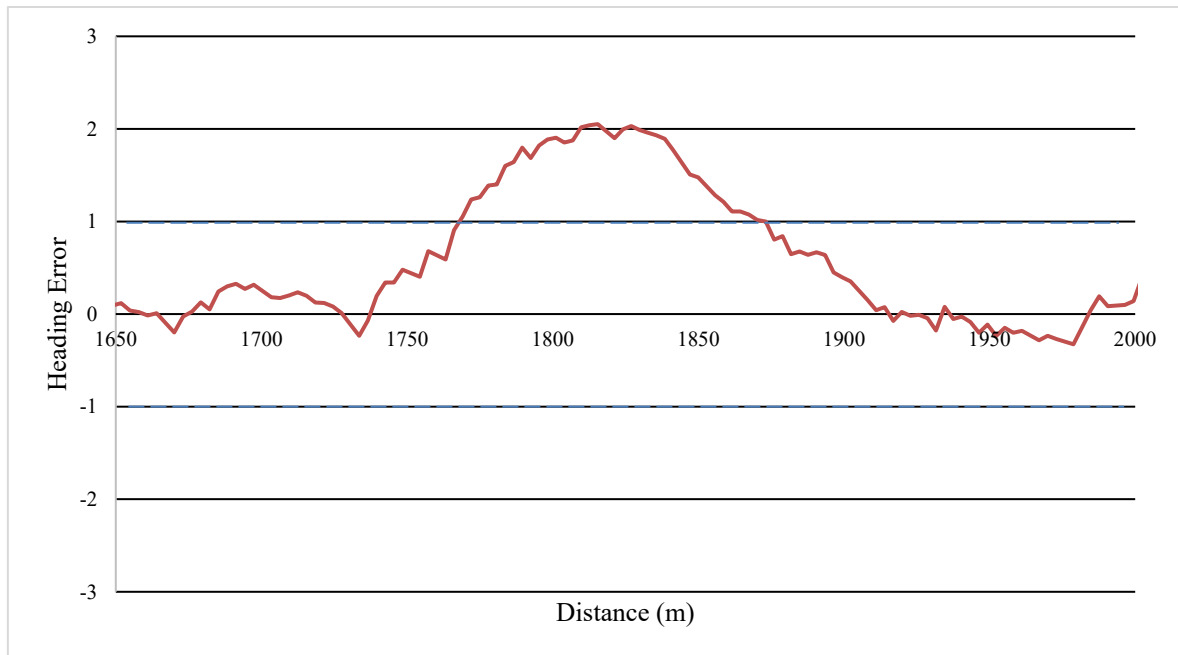


Figure 2.12 Heading error vs. Distance for a curve section with one lane changes present in the middle of the section.

RMSHE threshold for a span of $\sim 110\text{m}$ in the middle of the curve section. This is the exact location where the lane change was present in the trajectory implying that the lane change span can be detected by h_e .

This lane-change present in this trajectory are responsible for the large value of RMSHE of h_e (0.72135). However, the instantaneous values of h_e are still close to zero for those portions of the trajectory where there is no lane change, implying that the characterization (assigned optimal value of PAHS and IH) of the curve section is not negatively impacted by a lane change present in the trajectory.

It is evident that presence of any number of lane changes does not affect the characterization of a curve section. This is due to the fact that curve sections are characterized by PAHS and any number of lane change can not affect PAHS as differential heading for a single lane first increases and then decreases or vice versa as shown in Figure 2.9b. So, changes in differential heading cancel out each other and thus have no negative impact on PAHS.

In summary, lane changes do not affect identification or characterization of a curve or a transition section of a trajectory. However, odd number of lane changes has negative impact on characterization of a straight section. The initially value of PAH assigned to a straight section, when lane change portions exists, is not the true PAH of that straight section. So, our algorithm can detect and exclude those lane change portions by monitoring the heading error to calculate the true PAH of a straight section. After excluding those lane change portions, our algorithm continues to follow its normal routine to generate RRH for that trajectory.

2.2.3 Altered Road Segment

Sometimes, an existing straight or a curve section of any road can be altered from its standard design for any portion for a number of reasons after it has been designed and constructed.

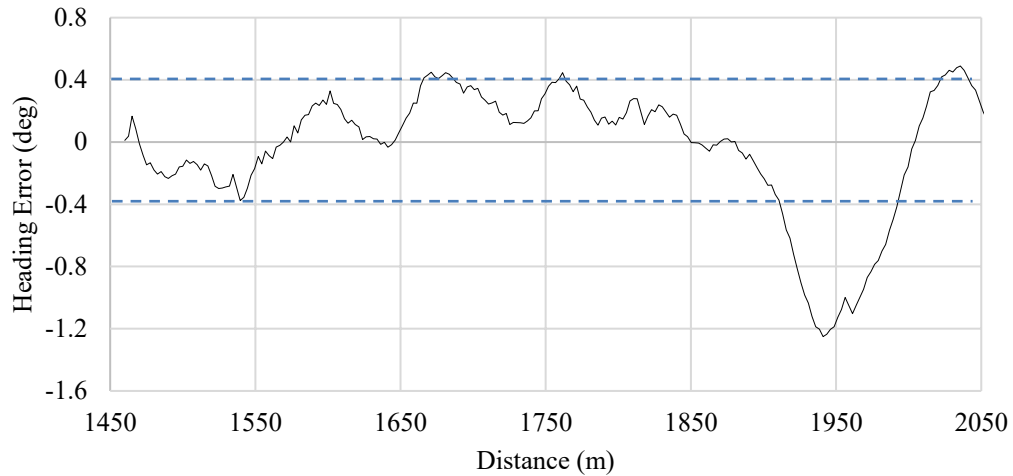


Figure 2.13 Heading error vs. distance for a curve section of Rice Lake Rd., without any lane change

Our algorithm can confuse it with a lane change in any trajectory obtained on that altered section. For example, we noticed such a scenario in the curve section of the Rice Lake Rd in Duluth, MN. The curve section of the Rice Lake Rd. was recently altered to accommodate a turn signal intersection. This effectively altered the curvature of the curve section for a span of about 100m adding one more lane on that portion to accommodate intersection light. We observed a lane change in all trajectories obtained on that section even when there was a no lane change present. This is illustrated in Figure 2.13 where heading error, h_e , between a vehicle trajectory and the extracted road reference is plotted versus distance.

The standard deviation of h_e is 0.4° which is large enough to indicate that there is a lane change present in this section. Using the standard deviation threshold, a lane change span of 100 m can be detected as seen in Figure 2.13. This is detected as a lane change because the differential heading change is not significantly large to be detected as a small curvature. However, it is not a real lane change but an altered curvature of an existing curve section of the road. If a lane change is detected in multiple trajectories at the same location having a similar span length, it is not likely to be a real lane change. Instead, it is more likely to be an altered curvature of an existing road. This can happen on a straight road section as well. We can detect such alterations of the existing road sections and mark its location in our road reference to avoid false alarms in lane departure detection in future trajectories on that road section. Alternatively, we can also characterize the altered section as a separate section to avoid false alarms.

CHAPTER 3: V2V COMMUNICATION FOR TRANSFERRING RRH

This chapter will capture the details of the second objective of the project which is to facilitate transfer of RRH from one vehicle to another using V2V communication. The chapter is divided into three sections. The first section describes the necessity of V2V communication to transfer RRH. The second section describes the V2V handshake protocol for RRH transfer followed by the third section describing the implementation details of the V2V handshake protocol and software development.

3.1 WHY V2V COMMUNICATION

To successfully generate the RRH for a given road from a vehicle's past trajectories on that road, it is necessary for the vehicle to have traveled on that road for at least once in the past. However, if a vehicle travels on a given road for the first time, it will not have the necessary RRH for unintentional lane departure detection. To overcome this problem, V2V communication can be used for a vehicle traveling for the first time on a given road to obtain the needed RRH from a nearby vehicle which has travelled on that road in the past and have already generated the RRH for it. To achieve this purpose, we proposed to add V2V communication provision to the proposed project. This chapter will highlight the work accomplished to design and develop the V2V communication process needed to exchange RRH between two vehicles upon need.

The V2V communication approach can only be successful if the market penetration of V2V communication enabled vehicles reaches a critical level which is not there as of now. As an alternative to V2V communication, the proposed LDWS can also be integrated into popular smartphone apps e.g., Waze, Google Maps or Apple Maps, to take advantage of the vast database of multiple GPS trajectories which can be used to generate RRH for almost all roads making it available for a vehicle to detect its unintentional lane departure on any road even if the vehicle is driven on that road for the first time. Please note that we have just been approved for a new project (third phase) to develop a smartphone app for our proposed LDWS using a vehicle's past trajectories. The successful development of this project will pave the way for integration of the proposed algorithm into one of the popular smartphone apps.

Our proposed LDWS relies on the past trajectories of a vehicle on any given road to generate a RRH for that road to detect a future unintentional lane departure. Once a vehicle travels on a road, its trajectory is acquired using GPS receiver to generate a RRH for that road which is stored in the database for future use. However, while traveling on a road for the first time, a vehicle does not have the necessary RRH for that road in its database. In this case, the vehicle can request the RRH for that road from a neighboring vehicle which has traveled on that road before and have previously generated and stored the RRH for that road. This process can be facilitated either using cellular vehicle to vehicle (C-V2V) communication or via dedicated short-range communication (DSRC). Once a RRH is successfully received from a nearby vehicle, it can be stored in the receiving vehicle's memory/database for future use.

3.2 V2V HANDSHAKE PROTOCOL

For successful transfer of a RRH from one vehicle to another, proper V2V handshake protocol is required to identify the most suitable neighboring vehicle to transfer RRH to the vehicle in need. A vehicle will request a RRH from neighboring vehicles only when it is traveling on a road for the very first time or does not have the RRH for that road. One such scenario showing a vehicle V_R traveling on a 4-lane road for the first time while not having the RRH for that road is illustrated in Figure 3a. A total of 12 neighboring vehicles (V_1 to V_{12}) are also traveling on the same road (Figure 3a). The vehicle V_R will need the RRH for that road to detect any unintentional lane departure. Therefore, it broadcasts a request for the RRH by transmitting a message called *REQUEST*. The *REQUEST* reaches all nearby vehicles within its communication range as shown by dashed arrows in Figure 3a. The data of *REQUEST* includes the direction of travel of the requesting vehicle (V_R) and its location coordinates. The direction of travel is needed to eliminate those vehicles which are traveling in the opposite direction of the requesting vehicle (V_R) because those vehicles will not stay within the communication range of the requesting vehicle long enough to complete the handshake protocol to transfer RRH.

All neighboring vehicles receiving the *REQUEST* will assess if they are traveling in the direction of the requesting vehicle and if they have the requested RRH to pass on. Any vehicle not having the requested RRH or traveling in the opposite direction of the requesting vehicle will ignore the *REQUEST*. Any vehicle having the requested RRH and traveling in the same direction as the requesting vehicle becomes a potential candidate vehicle to transfer RRH to the requesting vehicle (V_R). There are 4 such potential candidate vehicles (V_1 , V_3 , V_4 , and V_5) shown in green color in the scenario of Figure 3a. The rest of the vehicles (shown in grey color) are either traveling in the opposite direction or do not have the requested RRH. There is always a possibility to have more than one potential candidate vehicles to transmit RRH as in the scenario of Figure 3a. In case of more than one potential candidate vehicles having the needed RRH, it is important that only one of those vehicles is selected to transfer RRH to avoid broadcast congestion. Usually, a vehicle which is the nearest to the requesting vehicle should transfer the requested RRH for most reliable communication. To accomplish this, each potential candidate vehicle calculates its distance from the requesting vehicle (V_R) and transmits a message called *REPLY* back to the requesting vehicle as shown by dashed arrows in Figure 3b where the same scenario of Figure 3a is repeated showing communication paths of *REPLY* messages from all potential candidate vehicles. The data of each *REPLY* message from a potential candidate vehicle includes its distance from the requesting vehicles as well as a unique identifier (ID) so that the requesting vehicle can distinguish among all potential candidate vehicles.

After receiving the *REPLY* messages from all potential candidate vehicles, the requesting vehicle, V_R selects one potential candidate vehicle at the shortest distance. Please note that if two or more vehicles are at the same distance, then the requesting vehicle can randomly select any one of them. After selecting one of the potential candidate vehicles, the requesting vehicle (V_R) sends a message called *SELECT* back to all potential candidate vehicles as shown in Figure 3c where the same scenario is repeated showing the multiple communication paths of the *SELECT* message to all potential candidate vehicles. The data of the

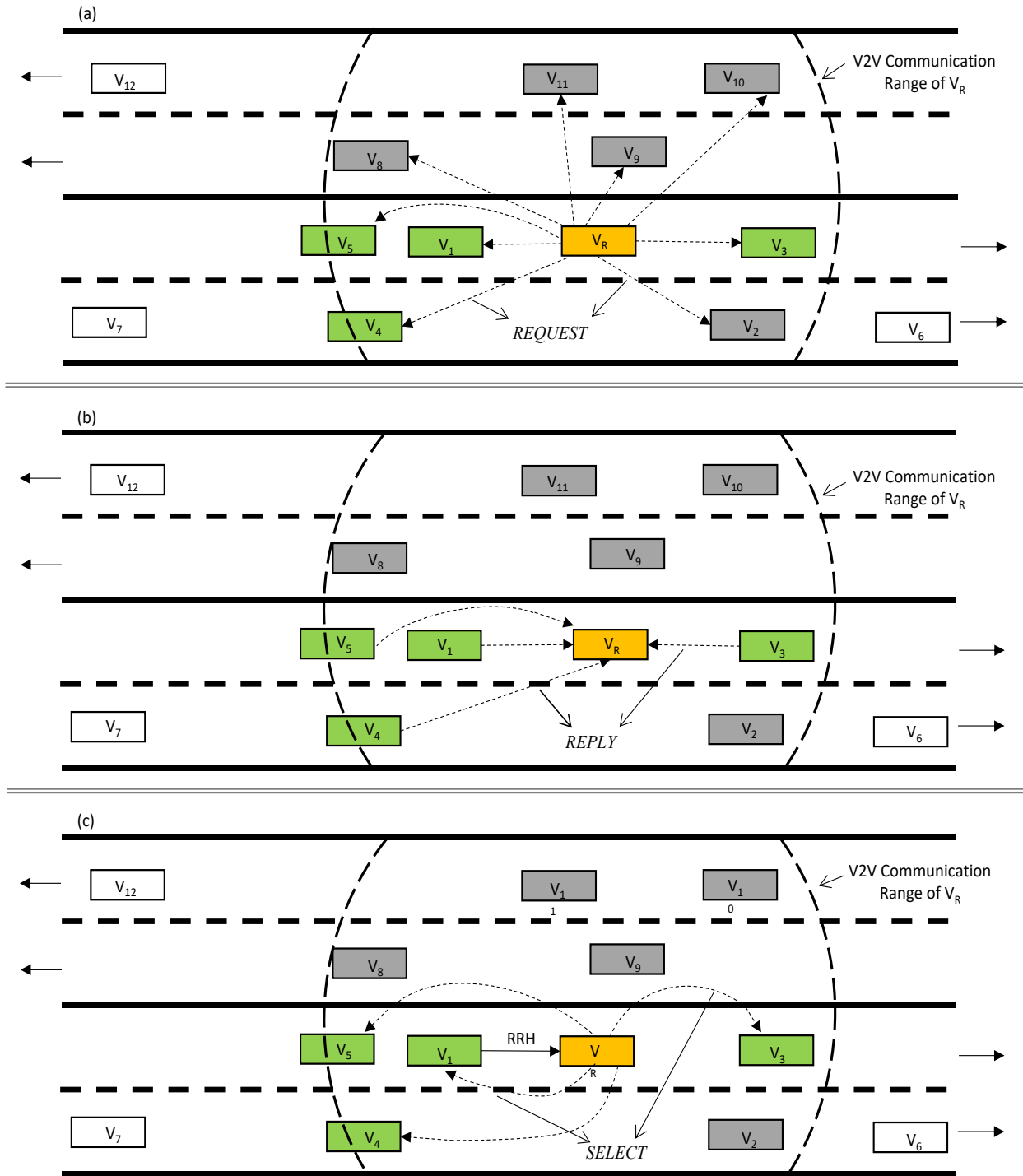


Figure 3.1 A scenario illustrating V2V handshake protocol where (a) a vehicle V_R in need of road reference heading (RRH) broadcasts a *REQUEST* to all neighboring vehicles within its V2V communication range, (b) all potential candidate vehicle (colored in green) send a *REPLY* message back to the requesting vehicle and (c) the requesting vehicle V_R sends a *SELECT* message to receive RRH from the most suitable potential candidate vehicle (V_1)

SELECT message includes the unique ID of only one potential candidate vehicle which is at the shortest distance from the requesting vehicle so that all other potential candidate vehicles can ignore this message except the one whose unique ID is carried in this message. This will complete the V2V handshake protocol by successfully selecting the most suitable vehicle to transfer RRH to the requesting vehicle. The potential candidate vehicle with matched unique ID (V_1 in case of the given scenario of Figure 3c) can now start transferring the requested RRH to the requesting vehicle (V_R) as shown by a solid arrow from V_1 to V_R in Figure 3c. The implementation details of the V2V handshake protocol and transfer of RRH are given in the next section.

3.2.1 Implementation of V2V Handshake Protocol

After developing the V2V handshake protocol to identify the most suitable vehicle to transfer RRH to a vehicle in need, we implemented this protocol in our LDWS and did the necessary programming to successfully demonstrate its functionality. The flowchart of the developed software to implement the developed V2V handshake protocol is shown in Figure 4. Please note that the software of flowchart given in Figure 4 will be running in each vehicle in addition to two other software i.e., RRH generation software as developed under Task 1 of the current project (Phase 2) and the lane departure detection software as developed in a previous project (Phase 1). The implementation platform of all the developed software is a DSRC based device which has a built in GPS receiver and necessary processing power to run the developed software. The software of the flowchart given in Figure 4 to implement the V2V handshake protocol to transfer RRH from the most suitable neighboring vehicle to the requesting vehicle is explained below.

1. The vehicle in need of RRH, after receiving a trigger from the LDWS software, broadcasts a *REQUEST* message to all nearby vehicles within its DSRC range. The data of the *REQUEST* consists of requesting vehicle's location and direction of travel.
2. All nearby vehicles receiving the *REQUEST* process its data to check if they have the needed RRH and traveling in the same direction as the requesting vehicle.
3. Each vehicle having the needed RRH and traveling in the same direction as the requesting vehicle (potential candidate vehicle) calculates its distance from the requesting vehicle and sends a *REPLY* message back to the requesting vehicle. The data of each *REPLY* message consists of the calculated distance and a unique identifier (ID) of the corresponding potential candidate vehicle. At this point, each potential candidate vehicle keeps waiting for the response back from the requesting vehicle to decide if it will need to transfer RRH to the requesting vehicle.

4. The requesting vehicle in need of RRH receives the *REPLY* messages from all the potential candidate vehicles and process all messages to select the closest potential candidate vehicle. If two or more vehicles are at same distance, then the requesting vehicle can randomly select any one of them.
5. The requesting vehicle in need of RRH now broadcasts a *SELECT* message containing the unique ID of the selected potential candidate vehicle.
6. All potential candidate vehicles process the received unique ID in the *SELECT* message to see if it matches with their unique ID. Any potential candidate vehicle not having a match with the unique ID will come out of the waiting routine and resume the normal operation by starting over. Please note that for some reason, if a potential candidate vehicle does not receive the *SELECT* message, it will assume that it is now out of communication range of the requesting vehicle and will resume normal operation after waiting for 300 ms (3 DSRC communication cycles).
7. The potential candidate vehicle with matched unique ID will now start transferring RRH data to the requesting vehicle. The process of actual transfer of RRH data takes place in next several cycles of DSRC communication (100 ms each) depending upon the length of data in RRH. The complete process of RRH data transfer is described later below.
8. The requesting vehicle receives the RRH data and checks received data periodically after every DSRC communication cycle (100 ms) to evaluate if it has received enough length of RRH data. For some reason, if the connection between the requesting vehicle in need of RRH and the selected potential candidate vehicle is lost/interrupted before receiving enough data (e.g., 1 mile), then the requesting vehicle sends the *SELECT* message again but with the unique ID of the next closest potential candidate vehicle. However, if the connection between the two vehicles is lost after enough RRH data has been received by the requesting vehicle, then it will initiate another *REQUEST* at a later time upon need to start the whole process again.

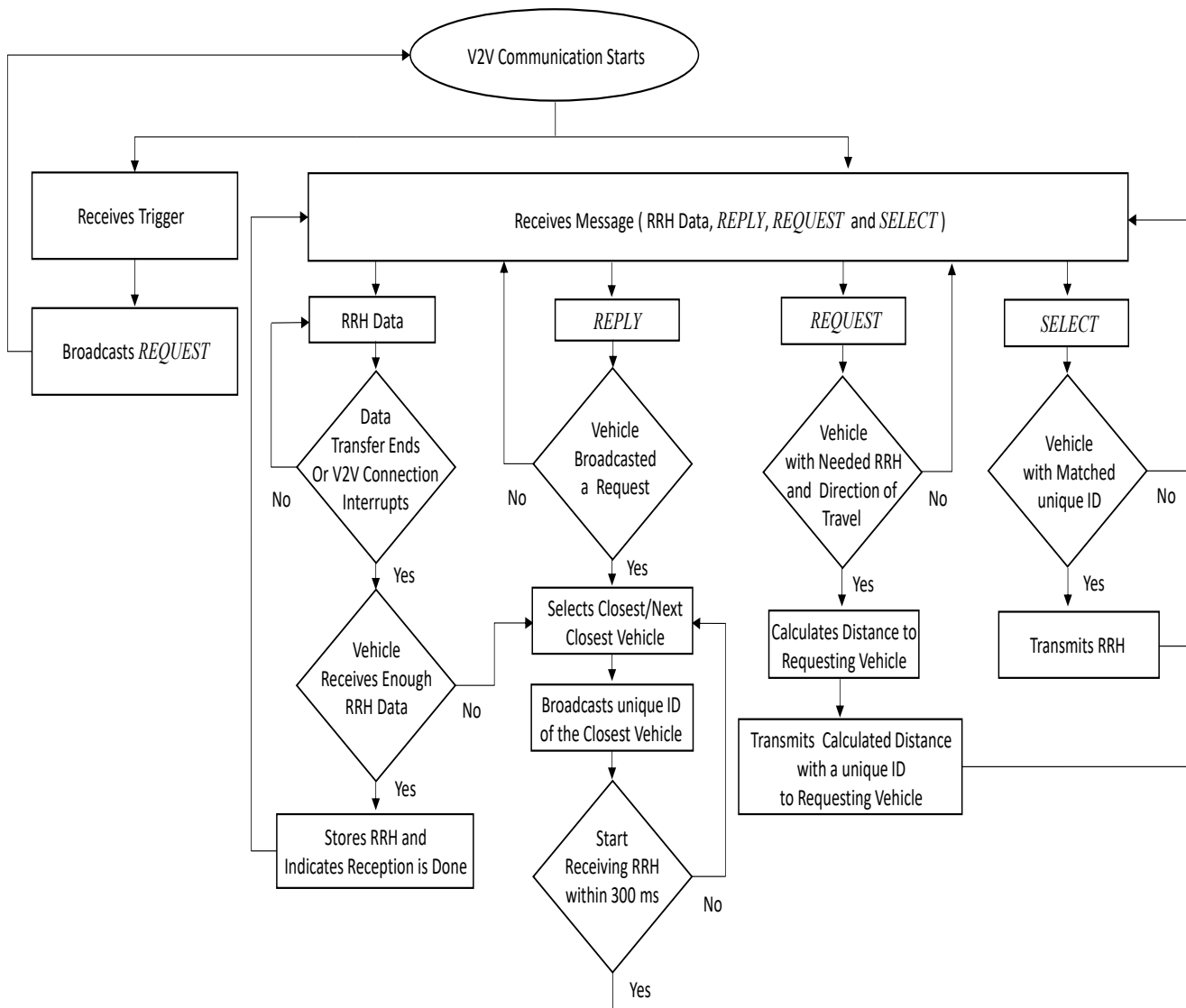


Figure 3.2 Flow chart of the V2V handshake protocol for a vehicle in need to receive RRH data of a given road from the most suitable neighboring vehicle on that road

3.3 TRANSFER OF RRH DATA USING V2V COMMUNICATION

The handshake protocol to select the most suitable vehicle to transfer RRH to the vehicle in need is described above. After the most suitable vehicle is identified and selected, the process to transfer RRH takes place slowly over next several cycles of DSRC communication depending upon the amount of RRH data. The data of RRH generated from past vehicle trajectories using our proposed algorithm is included in a text file containing many rows as shown in Figure 3.3 where a screenshot of a typical RRH data file for a 4.2 km road segment of the Interstate I-35 is shown. Each row describes an individual section (straight, curve or transition) of the road and there are 13 sections (rows) in the given text file. Each section is

defined by its beginning and ending points (in terms of latitude and longitude), the optimized values of relevant parameters, and the section type. Please note that an “N” indicates that the corresponding parameter is not applicable to that section. This text file has the necessary information to completely define the road reference heading at any point along the road and can be used by LDWS to detect any unintentional lane departure in real-time. Although each section of the road in RRH data file contains seven parameters to fully characterize the given section, one of the 7 parameters (Section Type) is not necessarily needed as it can be deduced from the other parameters. Therefore, in our developed system, each section is transmitted using only six parameters.

In DSRC based V2V communication, each data transfer cycle is 100 ms and any data transfer can take place during this cycle. We have implemented RRH data transfer process section by section but in such a way that only two parameters can be transferred in one communication cycle (100 ms). As there are six useful parameters in each section of RRH data for any given road, we need three cycles (300 ms or 0.3 s) to completely transfer one section. Depending upon the number of sections of the road in a RRH text file, it can take up to a few seconds to complete the RRH transfer process. For example, there are 13 sections in the RRH text file of Figure 3.4, therefore, it will take 3.9 seconds (13 x 0.3 s) to completely transfer all the sections of this RRH. After successfully completing the transfer of all the sections present in the RRH data file, a final message is sent to the receiving vehicle to indicate that all the data has been sent. Please note that an additional communication cycle (0.1 s) will be needed for the final message indicating the data transfer completion. For some reason, if the connection is lost before the transfer of RRH data is completed or before enough RRH data is transferred, our developed software can manage the situation by restarting the process as described above in the V2V handshake protocol.

PAH= Path Averaged Heading
 IH= Initial Heading of the Section of interest
 PAHS= Path Averaged Slope

Latitude(s).	Longitude(s)	Latitude(e)	Longitude(e)	Section_Type	PAH/IH	PAHS
46.719700	-92.240000	46.712520	-92.260181	S	239.478679	N
46.712520	-92.260181	46.712210	-92.261108	T	239.478679	0.04800
46.712210	-92.261108	46.7113795	-92.265950	C	243.350113	0.06680
46.7113795	-92.265950	46.711377	-92.266125	T	267.625114	0.03120
46.711377	-92.266125	46.711373	-92.268585	S	269.795181	N
46.711373	-92.268585	46.711358	-92.269322	T	269.795181	-0.02600
46.711358	-92.269322	46.709410	-92.276968	C	267.480130	-0.05750
46.709410	-92.276968	46.709200	-92.277564	T	234.324152	-0.03550
46.709200	-92.277564	46.707590	-92.280056	S	231.612356	N
46.707590	-92.280056	46.707210	-92.280957	T	231.612356	0.04320
46.707210	-92.280957	46.705865	-92.285124	C	234.555494	0.05800
46.705865	-92.285124	46.705750	-92.286159	T	255.341927	0.04475
46.705750	-92.286159	46.704300	-92.300000	S	257.677107	N

Figure 3.3 Screenshot of a typical RRH data file

After developing the software for V2V handshake protocol and RRH data transfer, we evaluated this in the lab by using two DSRC devices to simulate two vehicles, one vehicle without the RRH and the other with the RRH. One such lab evaluation scenario is illustrated in Figure 3.4 where the vehicle shown as yellow needs a RRH for a given road and the vehicle shown as green has that RRH. Once the V2V handshake protocol establishes the connection between the two vehicles (transmitting and receiving), the transfer of RRH data takes place section by section. The transfer of the RRH data is also illustrated in Figure 3.4 where the screenshots of the consoles of the two DSRC devices of the two corresponding vehicles are also shown. The left side console is for the transmitting vehicle's device and shows the actual RRH data which is being transmitted to the other vehicle. The right side console is for the device of the receiving vehicle and shows the actual received RRH data by the receiving vehicle's device. There are 11 sections in the RRH of the text file used in this lab evaluation which was successfully transmitted in a total of 3.4 seconds. The transmission of each of the 11 sections in the RRH data file took 0.3 seconds so all 11 sections were successfully transmitted in 3.3 seconds (11 x 0.3 s). The final message (in the form of two consecutive zeros) took another 0.1 second indicating that the transfer was complete.

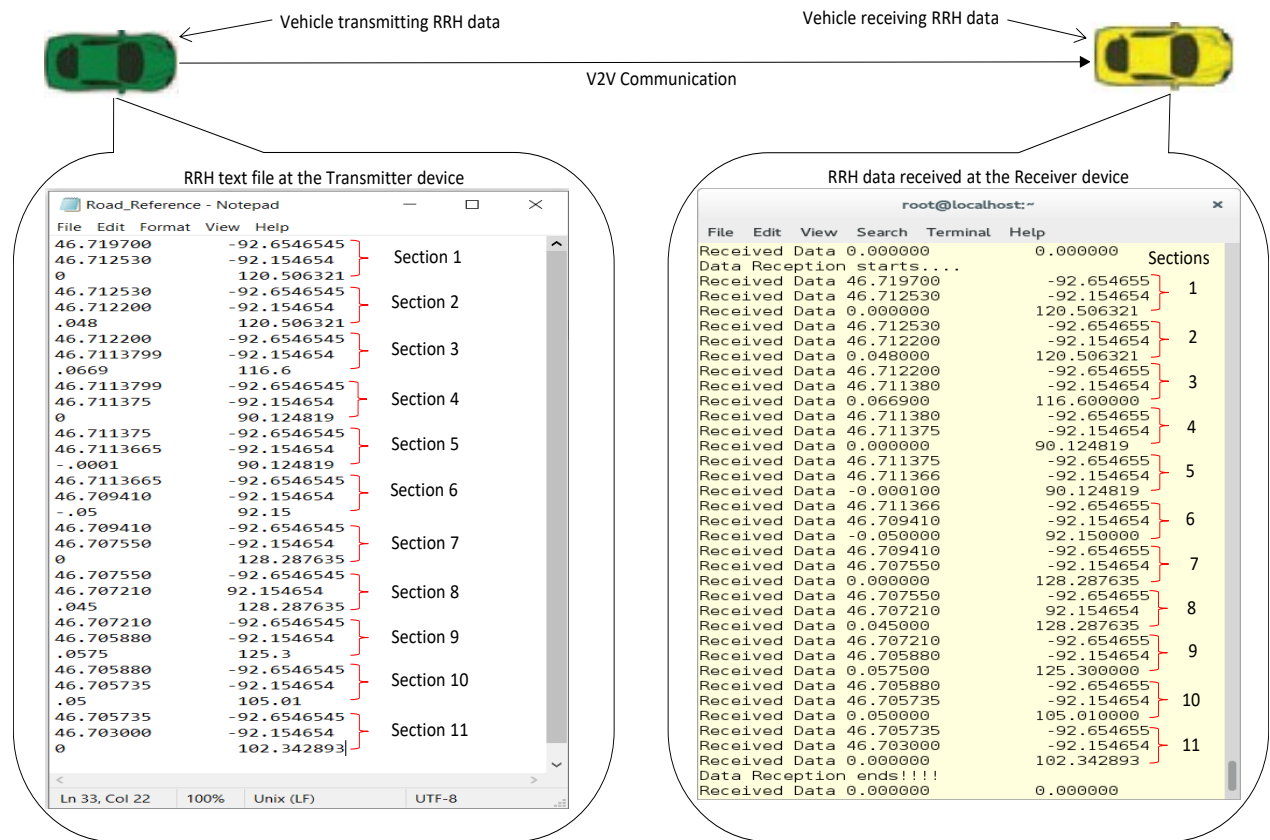


Figure 3.4 Screenshot of the console of the DSRC device in the transmitter vehicle (left bubble box) showing a text file of RRH data stored in the device and screenshot of the console of the DSRC device in the receiving vehicle (right bubble box) when the RRH data is received via DSRC based V2V communication.

CHAPTER 4: FIELD TESTS, RESULTS, AND CONCLUSIONS

This chapter will highlight the field test results of the LDWS using a newly developed algorithm to generate RRH for any given road from a vehicle's past trajectories on that road for accurate detection of unintentional lane departure while minimizing the frequency of false alarms.

4.1 FIELD TESTS AND RESULTS

The accuracy of the lane departure detection method depends upon the accuracy of the composite RRH for that road. To evaluate its accuracy, field tests were performed by driving a test vehicle multiple times on the same 4.2 km segment of Interstate I-35 for which an average composite RRH was already generated using the newly proposed algorithm. When a vehicle unintentionally drifts away from its lane, ALS starts to increase in value (positive or negative), and once its value increases/decreases beyond a certain threshold ($\pm 1\text{m}$), an unintentional lane departure is detected initiating a warning for the driver. Please note that ALS will also increase in value if a vehicle intentionally changes its lane. An intentional lane change can be distinguished from an unintentional lane departure by the presence or absence of turn signal. In case of an intentional lane change, the increase in ALS begins to saturate upon completion of lane change because the vehicle starts to travel again in parallel to the RRH of the road. As a result of normal driving behavior, this phenomenon i.e., the saturation of ALS can also occur in case of an unintentional wandering within a lane while ALS values remain within the $\pm 1\text{m}$ threshold. This phenomenon is used to reset the value of ALS to zero whenever its value begins to saturate either after completion of a lane change or during normal driving within the lane to detect a future lane change or a potential unintentional lane departure.

During the field tests, the test vehicle was driven at about speed limit (70 MPH) on this 4-lane freeway (2-lanes each way) and many back-and-forth lane changes were made intentionally during the field tests. For safety reasons, intentional lane changes were made to test the accuracy of lane departure detection using the composite RRH generated by the newly proposed algorithm.

The test vehicle was driven on the same road segment multiple times making many lane changes in each trip and ALS was calculated in real-time to detect any lane departure. The vehicle heading for one such test trip vs. distance is plotted along with the RRH of the road segment in Figure 4.1a showing that vehicle heading deviates from the RRH during each lane change as expected. The corresponding ALS vs. distance is plotted in Figure 4.1b showing that ALS exceeds $\pm 1\text{m}$ threshold during each lane change. A total of ten right and left lane changes were made in this trip and all lane changes were detected accurately and in a timely manner. A digital mask for lane departure detection warning signal is plotted as a dashed red line showing the start and end of each lane change in Figure 4.1b. Lane departure warning signal becomes active when ALS exceeds the $\pm 1\text{m}$ threshold and is deactivated when the vehicle heading becomes parallel to RRH of the road. In multiple field tests, more than 100 lane changes were made, and each lane change or lane departure was accurately and timely detected.

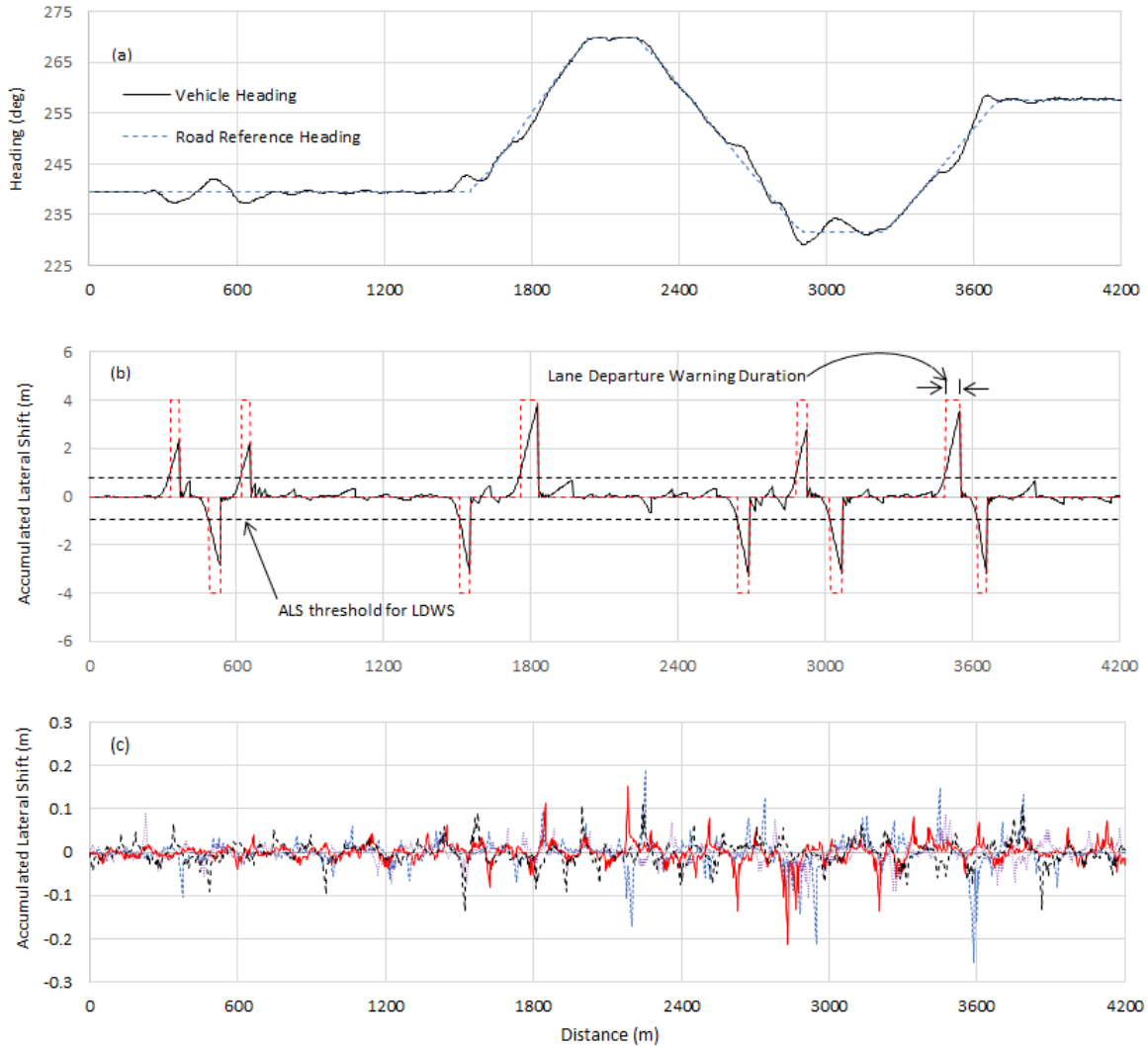


Figure 4.1 (a) Vehicle heading and RRH vs traveled distance for one test trial, (b) ALS versus traveled distance of the corresponding test trial trajectory, and (c) ALS versus distance on the same 4.2 km segment of Interstate I-35 for four typical trial trajectories with no lane change

Furthermore, nowhere else along the trajectory, ALS exceeded the threshold i.e., no false alarm was observed. To evaluate the frequency of the false alarms, the test vehicle was also driven multiple times on the same road segment without making any lane changes. In more than 10 trips on the 4.2 km long route, no false alarm was observed as indicated in Figure 4.1c, where ALS is plotted vs. distance for four such test trips.

It is also important to observe that ALS value along any point on the road remained below $\pm 0.3\text{m}$ which is well below the $\pm 1\text{m}$ threshold, even on the curve sections of the road showing that the composite RRH generated from past vehicle trajectories significantly improves the accuracy of previously proposed lane departure detection method by practically reducing the frequency of false alarms to zero with a lot of margins to spare.

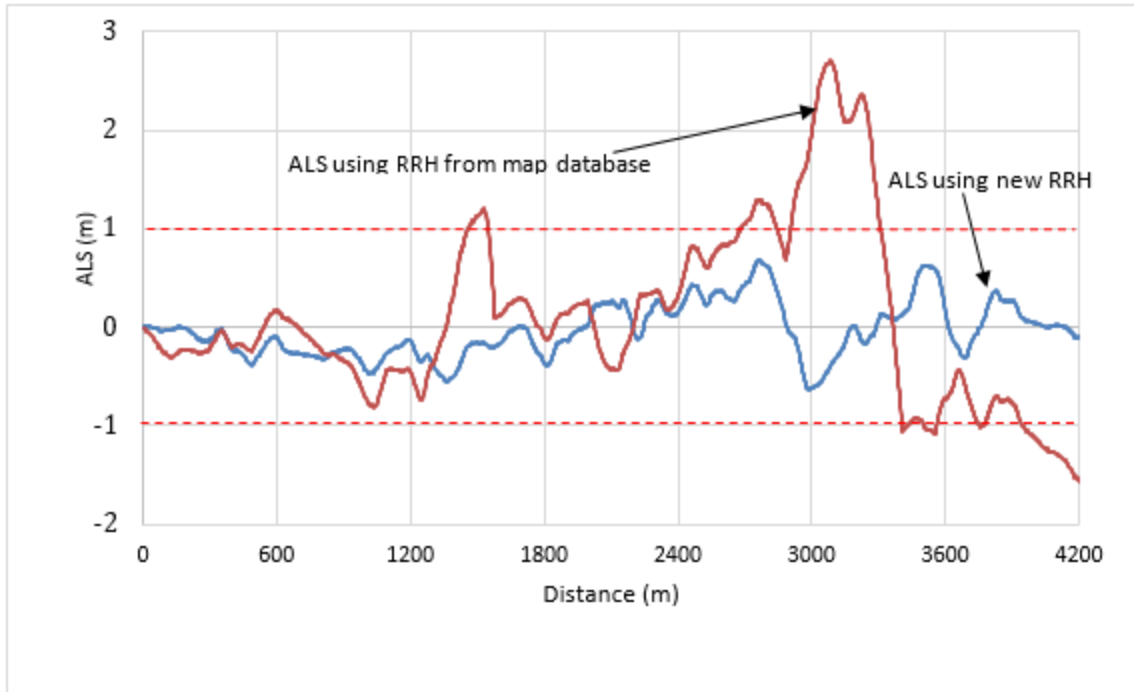


Figure 4.2 A comparison between two LDWSs using a selected trajectory where the previous LDWS issues false alarm (the red trajectory crosses the threshold line three times in absence of any lane changes, indicating three false alarms). The blue trajectory does not cross the threshold line using the new RRH and no false alarm is issued

It is also crucial to make a comparative analysis between the previous LDWS and the new LDWS. To make this comparison, we selected a particular trajectory with no lane changes, from our previously developed LDWS, where false warnings were issued for that trajectory. We re-evaluated that particular trajectory using our newly developed LDWS and observed no false alarm. This comparative analysis is shown in Figure 4.2 where the horizontal red lines indicates the threshold of $\pm 1\text{m}$. The figure shows that we did not experience any false alarm but also the stark comparison of the ALS from the two methods (old vs. new improved method) shows that ALS remains well below the threshold, thus minimizing the probability of false alarms drastically.

Additionally, after successfully developing and testing V2V handshake protocol and RRH data transfer software in the lab, we wanted to evaluate both in the field to detect unintentional lane departures. We used the same road segment to test the V2V handshake protocol and RRH data transfer software. The complete field test involves driving at least two test vehicles, one of these two vehicles without having the RRH data file in its DSRC device and running only lane departure warning software while the other vehicle having the required RRH data file in its DSRC device. The two vehicles should be driven within the DSRC communication range of each other on the same road.

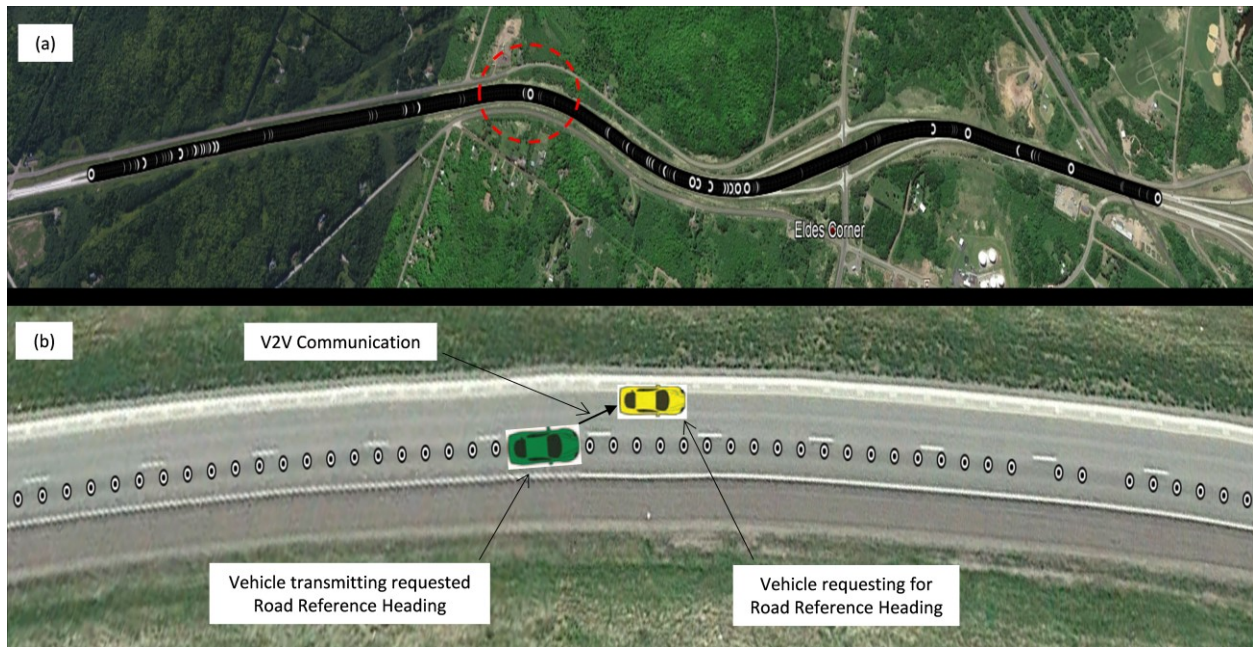


Figure 4.3 (a) Google Earth view of a travel trajectory of a 4.2 km road segment on the interstate I-35 and (b) Zoomed portion of (a) highlighted by red dashed circle illustrating a typical V2V communication scenario for transferring RRH data of that road segment

We wanted to drive two test vehicles in close proximity on our test road segment as shown in Figure 4.2b which is a zoomed-in view of the portion of the I-35 of Figure 4.3a highlighted by the red dashed circle. However, because of the Covid-19, we were not able to go to the field as it required at least two people in each of the two vehicles for a prolonged period of time. Instead, we used an innovative method to test the full operation of all the pieces of our developed software including V2V handshake protocol, RRH data transfer, and lane departure detection. We had previously acquired and stored multiple GPS trajectories of a test vehicle on our test road segment. We used two such separate trajectories of two vehicles driven in close proximity of each other on the test road segment and stored them in two separate DSRC devices. The two DSRC devices represented two test vehicles traveling on the actual road. Each of the two DSRC devices was operated normally in the lab except that every new GPS point acquired by the GPS receiver of the corresponding DSRC device was replaced with one of the GPS points in stored trajectory. By doing this, each DSRC device appeared to be as it was being driven on the actual road. The DSRC device of one of the two vehicles (shown as yellow in Figure 4.3b) was running the lane departure detection software but did not have the corresponding RRH of that road segment so it needed to request RRH from a neighboring vehicle to detect lane departure and issue an audible warning. The other vehicle (shown as green in Figure 4.3b) acted as a neighboring vehicle having the necessary RRH data file in its DSRC device. In this test, only one of the two vehicles (yellow) without the needed RRH data file was tested for lane departure detection algorithm after successfully receiving the RRH data file from the neighboring vehicle (green). The results are similar and consistent with our first field test results as shown in Figure 4.1 and Figure 4.2.

4.2 CONCLUSIONS AND FUTURE WORK

We have successfully developed an in-vehicle lane departure warning system (LDWS) using GPS technology and DSRC based V2V communication to transfer RRH from one vehicle to another. Our newly designed algorithm can be easily applied to large tracts of vehicle trajectories. Our algorithm first partitions various sections of the road from the trajectory and then characterizes each section separately with an optimized set of parameters completely defining heading value at any point on the road. This road reference when used for our previously designed lane departure detection algorithm, works efficiently to detect unintentional lane departures while minimizing the number of false alarms to almost zero, which was the prime goal of the algorithm design. Field tests were performed on two road segments – one on a highway and the other on a freeway – containing a variety of curves and straight road sections to evaluate the performance of the newly designed algorithm. The results of the field tests showed that the system can detect the true lane departures on a straight or a curved road with an accuracy of almost 100%. While doing the tests, no false alarms or spurious lane departures were detected even on sharp curved sections of the freeway.

Additionally, to enable proper communication among vehicles to transfer RRH from one vehicle to another, we have developed the V2V handshake protocol using DSRC devices. According to our developed V2V handshake protocol, a vehicle in need of RRH can initiate a request to receive a RRH from its neighboring vehicles and receive from the most suitable neighboring vehicle on the road. Upon receiving the requested RRH, the vehicle in need can use the received RRH for unintentional lane departure detection and warning as well as store it in its memory/database for future use. We have used two DSRC devices simulating the two vehicles in the lab to test the developed V2V handshake protocol and RRH data transfer software. After developing and extensively testing our software, we have performed field tests to successfully detect lane departures using the RRH received via DSRC-based V2V communication.

A better alternative to V2V communication is to integrate the developed LDWS into popular smartphone apps, e.g., Waze, Google Maps or Apple Maps, to take advantage of the vast database of multiple GPS trajectories that can be used to generate RRH for almost all roads, making it available for a vehicle to detect its unintentional lane departure on any road even if the vehicle is being driven on that road for the first time. We have already begun work to develop a smartphone app for our proposed LDWS using a vehicle's past trajectories. The successful development of this project will pave the way for integration of the proposed algorithm into one of the popular smartphone apps.

REFERENCES

1. American Association of State Highway and Transportation Officials (2008). Driving down lane-departure crashes: A national priority, 11-12.
2. Cicchino, J. (2018). Effects of lane departure warning on police-reported crash rates, *Journal of Safety Research*, 66, 61-70.
3. Salvucci, D. D. (2008). Inferring driver intent: A case study in lane-change detection. *Proceeding of Human Factors Ergonomics Society 48th Annual Meeting*, 2228–2231.
4. Kuge, N., T. Yamamura & O. Shimoyama (2000). A driver behavior recognition method based on a driver model framework, *Society of Automotive Engineering*, 109, 6, 469-476.
5. McCall, J. & M. M. Trivedi (2004). Visual context capture and analysis for driver attention monitoring. *IEEE Conference on Intelligent Transportation Systems*, 332–337.
6. Heimes, F. & H. H. Nagel (2002). Towards active machine-vision-based driver assistance for urban areas. *International Journal of Computer Vision*, 50, 1, 5–34.
7. Kwon, W. & S. Lee (2002). Performance evaluation of decision making strategies for an embedded lane departure warning system. *Journal of Robotics Systems*, 19, 10, 499–509.
8. An, X., M. Wu & H. He (2006). A novel approach to provide lane departure warning using only one forward-looking camera. *International Symposium on Collaborative Technologies and Systems*, 356-362.
9. Hsiao, P. & Chun-Wei Yeh (2006). A portable real-time lane departure warning system based on embedded calculating technique. *IEEE 63rd Vehicular Technology Conference*, 2982-2986.
10. Yu, B., W. Zhang & Y. Cai (2008). A lane departure warning system based on machine vision. *IEEE Pacific-Asia Workshop on Computational Intelligence and Industrial Application*, 197-201.
11. Leng, Y. C. & C. L. Chen (2010). Vision-based lane departure detection system in urban traffic scenes. *11th International Conference on Control Automation Robotics & Vision*, 1875-1880.
12. Lindner, P., E. Richter, G. Wanielik, K. Takagi & A. Isogai (2009). Multi-channel lidar processing for lane detection and estimation. *12th International IEEE Conference on Intelligent Transportation Systems*, 1-6.
13. McCall, J. C., and M. M. Trivedi (2006). Video-based lane estimation and tracking for driver assistance: survey, system, and evaluation. *IEEE Transactions on Intelligent Transportation Systems*, 7, 1, 20-37.

14. Dobler, G., S. Rothe, P. Betzitza & M. Hartleib (2018). Vehicle with optical scanning device for a lateral road area. US Patent: 6,038,496.
15. Clanton, J. M., D. M. Bevly & A. S. Hodel (2009). A low-cost solution for an integrated multisensor lane departure warning system. *IEEE Transactions on Intelligent Transportation Systems*, 10, 1, 47-59.
16. Hussain S., M. Faizan & M.I. Hayee (2018). Real-time relative lane and position identification of surrounding vehicles using GPS and DSRC based vehicle-to-vehicle communication. *Proceedings of IEEE Conference on Communications*, 1-7
17. Cao, L. & J. Krumm (2009). From GPS traces to a routable road map. *GIS: Proceedings of the 17th ACM Sigspatial International Conference on Advances in Geographic Information Systems*, 3–12.
18. Guo,T., K. Iwamura & M. Koga (2007). Towards high accuracy road maps generation from massive GPS Traces data. *IEEE International Geoscience and Remote Sensing Symposium*, 667-670.
19. Chen, C. & Y. Cheng (2008). Roads digital map generation with multi-track GPS data. *International Workshop on Education Technology and Training & International Workshop on Geoscience and Remote Sensing*, 1, 508-511.
20. Guo, D., S. Liu & H. Jin (2010). A graph-based approach to vehicle trajectory analysis. *Journal of Location Based Services*. 4, 183-199.
21. Shi, W., S. Shen & Y. Liu (2009). Automatic generation of road network map from massive GPS, vehicle trajectories. *12th International IEEE Conference on Intelligent Transportation Systems*, 1-6.
22. Huang, J., M. Deng, J. Tang, S. Hu, H. Liu, S. Wariyo & J. He (2018). Automatic generation of road maps from low quality GPS trajectory data via structure learning. *IEEE Access*, 6, 71965 – 71975.