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7. Author(s)  Vasileios Papadopoulos and P. Benson Shing				8. Performing Organization Report No.  UCSD/SSRP-15/07	
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16. Abstract For the construction of cast-in-drilled-hole (CIDH) piles in the presence of ground water, slurry is used before and during concrete placement to stabilize the drilled hole. When concrete is placed under slurry, defects may occur, affecting the structural integrity of the pile. In this situation, non-destructive testing, such as gamma-gamma testing, is to be conducted to detect potential anomalies in the concrete. These tests require the placement of inspection (PVC) tubes inside the pile. To accommodate the inspection tubes, the center-to-center spacing of the adjacent longitudinal bars in the pile has to be larger than the 8-in. maximum permitted by the Caltrans Bridge Design Specifications and the AASHTO LRFD Bridge Design Specifications.  This report presents a numerical investigation to study the effect of the spacing of the longitudinal reinforcement in CIDH piles on their structural performance. It is aimed to confirm and generalize the experimental data obtained in this project, which has been reported elsewhere. To this end, three-dimensional nonlinear finite element (FE) models have been developed for RC pile shafts, and used for a numerical parametric study. The modeling method has been validated by experimental data. The parametric study considers piles of different diameters, with different lineal and angular spacings of the longitudinal bars, and with different levels of the axial load. To capture the strength degradation of piles under lateral loading, a phenomenological stress-strain law for steel that accounts for the low-cycle fatigue of bars under large-amplitude cyclic strain reversals has been developed in this study. To model the nonlinear behavior of concrete, a damaged-plasticity model has been used. In addition, a microplane model for concrete has been implemented as an alternative. The latter has been found to be superior in that it does not require artificial remedies to capture the tensile unloading and reloading behavior of concrete and the compressive behavior of confined concrete. The bond-slip behavior between the longitudinal bars and the surrounding concrete is modeled with a phenomenological bond-slip law.  The numerical study has shown that the spacing of the longitudinal bars in circular RC members can be larger than 8 in. without jeopardizing their structural performance. Similar to the experimental findings, the numerical parametric study has shown that the lineal spacing of the longitudinal bars does not have any impact on the ductility of an RC pile. However, the size of the longitudinal bars can affect the ductility of a pile. The load degradation in a pile is often associated with the spalling of the cover concrete, and the buckling and the fracture of the longitudinal bars in the plastic-hinge region of the pile. Larger-diameter bars are more resistant to buckling for the same spacing of the lateral reinforcement and therefore result in a more ductile behavior. The parametric study has also confirmed that a smaller lineal spacing with smaller-size longitudinal bars can lead to more closely spaced flexural cracks with smaller widths. These observations are true for piles of different diameters and subjected to different levels of axial loads.					
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Report No.  
SSRP-15/07

**Influence of the Spacing of Longitudinal  
Reinforcement on the Performance of Laterally  
Loaded CIDH Piles – Analytical Investigation**

by

**Vasileios Papadopoulos  
P. Benson Shing**

Report Submitted to the California Department of Transportation  
under Contract No. 65A0369

December 2015

Department of Structural Engineering  
University of California, San Diego  
La Jolla, California 92093-0085



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**Vasileios Papadopoulos**  
*Graduate Student Researcher*

**P. Benson Shing**  
*Professor of Structural Engineering*

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University of California, San Diego  
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The authors would also like to thank Dr. Juan Murcia Delso for his contributions and advice in the finite element modeling of RC members, and Dr. Ioannis Koutromanos for his contributions in the implementation of the microplane model used in this study.



## **ABSTRACT**

For the construction of cast-in-drilled-hole (CIDH) piles in the presence of ground water, slurry is used before and during concrete placement to stabilize the drilled hole. When concrete is placed under slurry, defects may occur, affecting the structural integrity of the pile. In this situation, non-destructive testing, such as gamma-gamma testing, is to be conducted to detect potential anomalies in the concrete. These tests require the placement of inspection (PVC) tubes inside the pile. To accommodate the inspection tubes, the center-to-center spacing of the adjacent longitudinal bars in the pile has to be larger than the 8-in. maximum permitted by the Caltrans Bridge Design Specifications and the AASHTO LRFD Bridge Design Specifications.

This report presents a numerical investigation to study the effect of the spacing of the longitudinal reinforcement in CIDH piles on their structural performance. It is aimed to confirm and generalize the experimental data obtained in this project, which has been reported elsewhere. To this end, three-dimensional nonlinear finite element (FE) models have been developed for RC pile shafts, and used for a numerical parametric study. The modeling method has been validated by experimental data. The parametric study considers piles of different diameters, with different lineal and angular spacings of the longitudinal bars, and with different levels of the axial load. To capture the strength degradation of piles under lateral loading, a phenomenological stress-strain law for steel that accounts for the low-cycle fatigue of bars under large-amplitude cyclic strain reversals has been developed in this study. To model the nonlinear behavior of concrete, a damaged-plasticity model has been used. In addition, a microplane model for concrete has been implemented as an alternative. The latter has been found to be superior in that it does not require artificial remedies to capture the tensile unloading and reloading behavior of concrete and the compressive behavior of confined concrete. The bond-slip behavior between the longitudinal bars and the surrounding concrete is modeled with a phenomenological bond-slip law.

The numerical study has shown that the spacing of the longitudinal bars in circular RC members can be larger than 8 in. without jeopardizing their structural performance. Similar to the experimental findings, the numerical parametric study has shown that the lineal spacing of the longitudinal bars does not have any impact on the ductility of an RC pile. However, the size of the longitudinal bars can affect the ductility of a pile. The load degradation in a pile is often associated with the spalling of the cover concrete, and the buckling and the fracture of the longitudinal bars in the plastic-hinge region of the pile. Larger-diameter bars are more resistant to buckling for the same spacing of the lateral reinforcement and therefore result in a more ductile behavior. The parametric study has also confirmed that a smaller lineal spacing with smaller-size longitudinal bars can lead to more closely spaced flexural cracks with smaller widths. These observations are true for piles of different diameters and subjected to different levels of axial loads.

# CHAPTER 1

## INTRODUCTION

### 1.1 Background and Motivation of the Study

For the construction of cast-in-drilled-hole (CIDH) piles in the presence of ground water, slurry is used before and during concrete placement to stabilize the drilled hole. When concrete is placed under slurry, defects may occur, affecting the structural integrity of the pile. Hence, the construction of CIDH piles larger than 2 ft. in diameter under wet conditions requires the installation of inspection (PVC) tubes for non-destructive detection of potential anomalies in the concrete, as shown in Figure 1.1. Normally, one inspection tube is required per foot of pile diameter. The inspection tubes are placed around the pile reinforcement cage in contact with the inside of the outer most hoop reinforcement and must be at least three (3) inches clear of the vertical reinforcement, as shown in Figure 1.1. This will require that the clear spacing between the longitudinal reinforcing bars in the reinforcement cage immediately adjacent to a tube be at least 8.5 in. so that the clear spacing between a tube and an adjacent bar will be at least 3 in. to allow a good flow of concrete. For Type I shafts, the spacing of longitudinal bars in both the column and the shaft is the same. Hence, the placement of inspection tubes will necessitate the violation of the maximum allowable center-to-center spacing of 8 in. for longitudinal bars, as specified in both the Caltrans Bridge Design Specifications (2004) and the AASHTO LRFD Bridge Design Specifications (2014).

Because of the lack of research data on the influence of the spacing of longitudinal reinforcement on the structural performance of reinforced concrete piles and circular columns, a research program was carried out to investigate this influence, especially the impact of a spacing exceeding the current Caltrans and AASHTO limits of 8 in. The research consisted of both experimental and numerical investigations.

Results and findings of the experimental investigation can be found in Papadopoulos and Shing (2014). This report presents details of the nonlinear finite element models used in the numerical investigation, the model calibration, and the findings of a numerical parametric study extrapolating the experimental results.

## **1.2 Past Research**

The influence of the quantity and spacing of transverse reinforcement on the ductility and structural performance of RC members subjected to axial loads and flexure has been well studied and understood. However, there is only limited information on the influence of the spacing of longitudinal reinforcement on the structural performance of RC members. It has been perceived that a larger spacing could negatively affect the efficiency of confinement on concrete and, thereby, reduce the flexural ductility of the member (Pauley and Priestley 1992). While this can be understood for members with rectangular sections, in which the spacing of the cross-ties is normally related to the spacing of the longitudinal bars, it is less so for circular members. Both Caltrans (2004) and AASHTO (2014) have specified a spacing limit of 8 in. for compression members regardless of the cross-sectional shape. Nevertheless, from the structural performance standpoint, the spacing limit for the longitudinal bars in a circular member should depend on the diameter of the member, and it is reasonable to expect that a member with a larger diameter can have a larger circumferential spacing of the longitudinal bars without affecting its structural performance. Limited experimental data obtained by Mander et al. (1988b) have shown that the influence of the spacing of longitudinal bars on the behavior of circular RC columns under compression is almost negligible, as shown in Figure 1.2. However, the maximum center-to-center spacing of longitudinal bars considered in their study was less than 6.5 in. Furthermore, there is no data on the influence of the bar spacing on the behavior of a circular member under simultaneous axial load and flexure. For rectangular columns, a closer spacing of longitudinal bars has a clear benefit of enhancing the compressive strength and ductility of the member, as shown in Figure 1.3. This is because a closer spacing of longitudinal bars



in rectangular columns requires a closer spacing of cross-ties, which results in a better arching action and a more effectively confined core as shown in Figure 1.4.

To investigate the impact of the spacing of longitudinal bars on the performance of a circular-sectioned member subjected to simultaneous axial and fully reversed cyclic lateral loading, two pile specimens were tested in the Powell Structural Engineering Laboratory of the University of California at San Diego. The two specimens had the same dimensions. One specimen was designed according to the Caltrans Bridge Design Specifications (2004) and the AASHTO LRFD Bridge Design Specifications (2014). The other had the same design except that its longitudinal reinforcement had spacing greater than 8 in., violating current design requirements. The test results show that the spacing of the longitudinal bars had no influence on the ductility of the pile specimens. Details of the experimental study and findings have been documented in a separate report (Papadopoulos and Shing 2014).

### **1.3 Scope of this Study and Organization of the Report**

The experimental study reported by Papadopoulos and Shing (2014) provided only one comparison of two pile specimens with the longitudinal bar spacing and bar size being the only variables. To have more data to confirm the experimental observation, numerical parametric studies using detailed nonlinear finite element models have been carried out, considering piles of different diameters and varying the lineal as well as the angular spacing of the longitudinal bars and the level of the axial load. The nonlinear finite element modeling methods used in the study have been first validated with the aforementioned experimental results. The finite element analyses have been performed with the commercial program Abaqus (Simulia 2012). This report documents the numerical study, including the constitutive models used and their calibration, the finite element models developed for the pile analyses, and the findings of the numerical parametric study. It has the following organization.

Chapter 2 of this report presents the constitutive models used to describe the behavior of concrete and reinforcing steel under cyclic stress reversals. A damaged-plasticity model provided in Abaqus (Lubliner et al., 1989, Lee and Fenves, 1998) is used to model concrete. It has been validated and calibrated with uniaxial and tri-axial test data from other studies. A phenomenological steel model developed in this study to account for the low-cycle fatigue of reinforcing bars under large cyclic strain reversals is thoroughly presented. A method to account for the large localized strains induced by the buckling of a bar is also described. Finally, this chapter presents the phenomenological bond-slip law, proposed by Murcia-Delso and Shing (2015), which is used to model bond slip between longitudinal bars and the surrounding concrete in the FE analyses.

Chapter 3 describes the finite element models developed to simulate the behavior of the two RC pile specimens tested in the laboratory as reported by Papadopoulos and Shing (2014). The finite element models have been validated with the test results. With this finite element modeling method, a parametric study, considering piles of different diameters and varying the lineal spacing of the longitudinal bars and the level of the axial load, is presented.

Chapter 4 presents the microplane model by Caner and Bazant (2013a), an alternative constitutive model for concrete which has been implemented in Abaqus to overcome the deficiencies of the damaged-plasticity model. The microplane model has been used in the finite element models of the pile specimens tested in this study. The results of the finite element analyses are compared to the test data of the pile specimens. Finally, a summary and the conclusions of this study are provided in Chapter 5.



Figure 1.1 – Typical drilled shaft reinforcement cage with PVC inspection tubes (Caltrans)

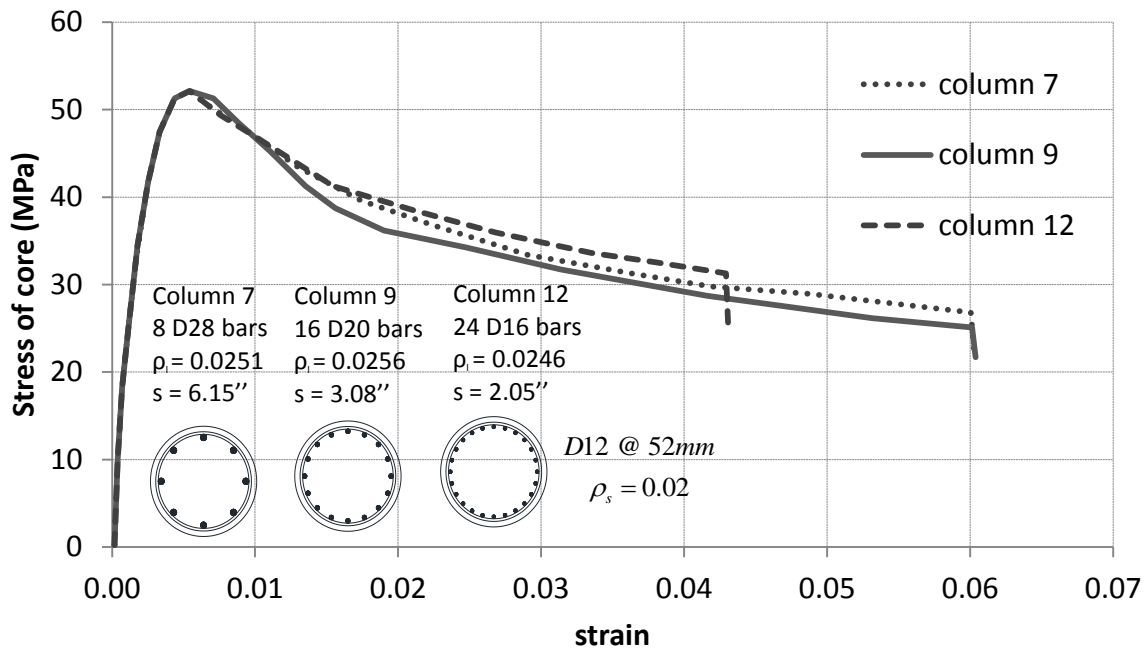


Figure 1.2 – Effect of spacing of longitudinal bars on circular columns (Mander et al. 1988)

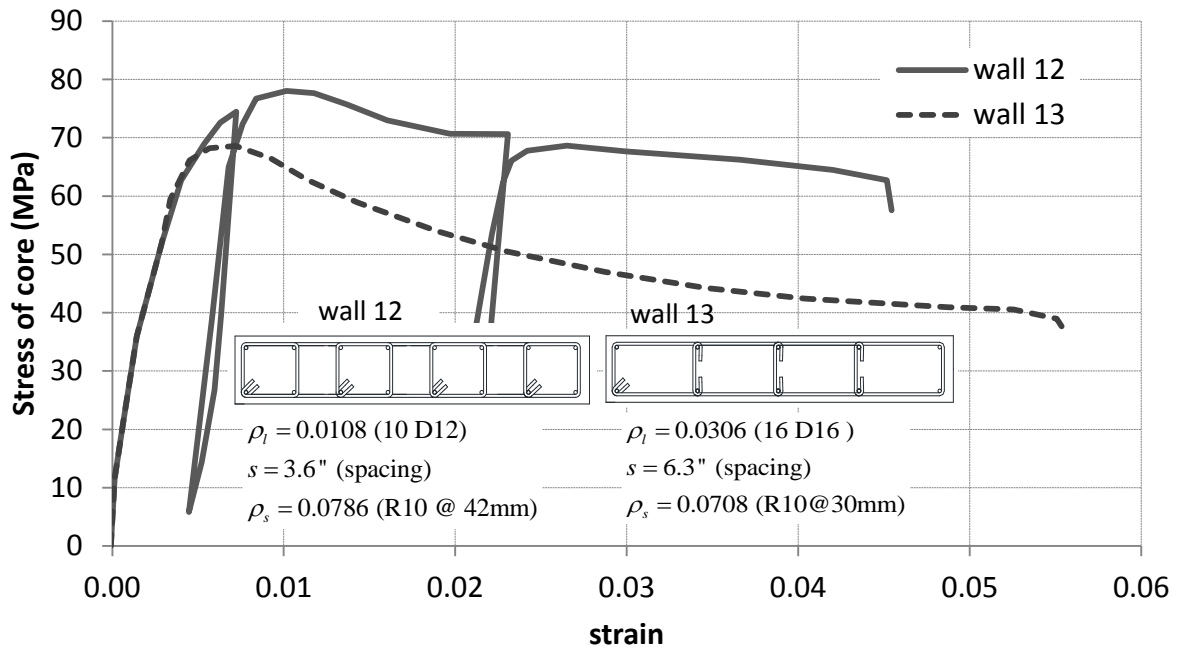


Figure 1.3 – Effect of spacing of longitudinal bars on rectangular sections (Mander et al. 1988b)

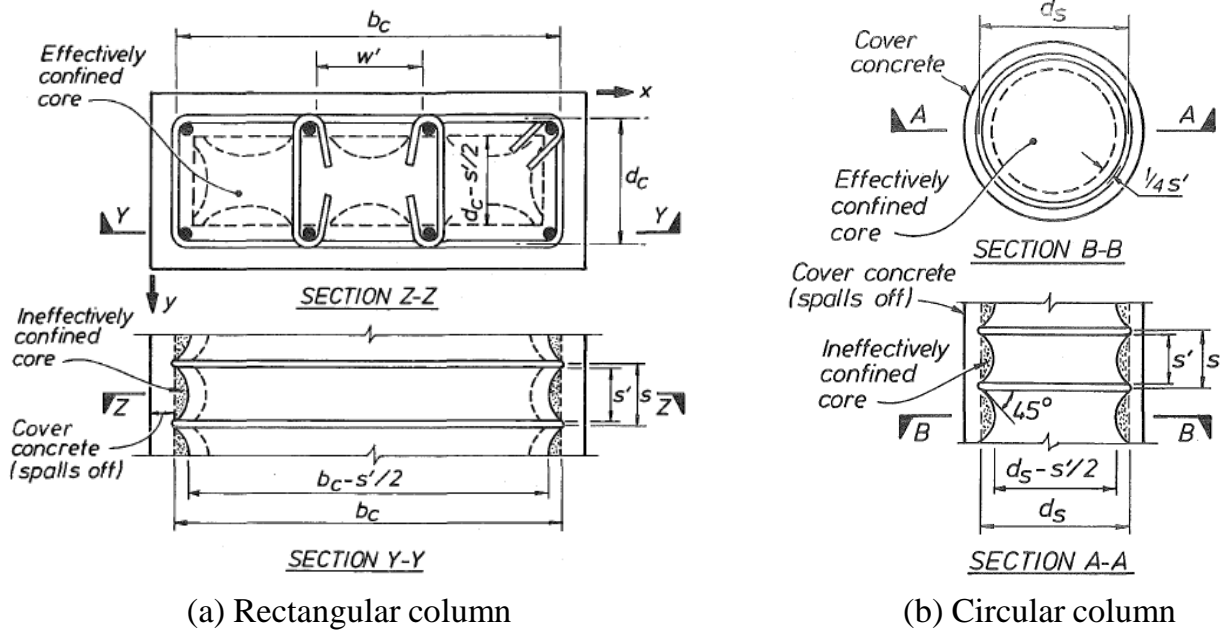


Figure 1.4 – Arching action introduced by confining reinforcement (Mander et al. 1988a)

## **CHAPTER 2**

### **CONSTITUTIVE MODELS**

The commercial program Abaqus (Simulia, 2012) has been used for the pile analyses conducted in this study. This chapter presents the constitutive models used to describe the nonlinear behaviors of concrete and reinforcing steel, and the bond-slip behavior between a reinforcing bar and the surrounding concrete in the analyses. Concrete is modeled as a continuum using the 3-D damaged-plasticity constitutive law that is available in Abaqus. Longitudinal reinforcement is modeled with beam elements using a phenomenological stress-strain law developed in this study to account for the low-cycle fatigue of bars under large-amplitude cyclic strain reversals. The finite element models also account for the slip of the longitudinal reinforcing bars in concrete, which has a profound influence on the plastic strain localization and subsequent fracture of bars. This behavior is simulated with a bond-slip law developed by Murcia-Delso and Shing (2015).

#### **2.1 Damaged-Plasticity Model for Concrete**

Models combining plasticity and damage mechanics theories are attractive for simulating the behavior of concrete in that they can account for both plastic deformation and stiffness degradation in concrete under severe multi-axial stress reversals. The concrete damaged-plasticity model available in Abaqus is based on the formulations proposed by Lubliner et al. (1989) and Lee and Fenves (1998). This section summarizes the basic formulation for this model, and describes how the model has been calibrated and validated in this study with the experimental data of Hurlbut (1985) and Mander et al. (1988b).

### 2.1.1 Damaged-Plasticity Model Formulation

The model complies with the classical theory of plasticity in that the strain tensor is decomposed into an elastic part and a plastic part, and the stress tensor is obtained as the double contraction of the elastic stiffness tensor and the elastic strain tensor.

$$\boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}^e + \boldsymbol{\varepsilon}^p \quad (2.1)$$

$$\boldsymbol{\sigma} = \mathbf{E} : \boldsymbol{\varepsilon}^e = \mathbf{E} : (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}^p) \quad (2.2)$$

To account for stiffness degradation using the damage mechanics theory, the elastic stiffness tensor is related to the initial stiffness tensor as:

$$\mathbf{E} = (1 - d)\mathbf{E}_0 \quad (2.3)$$

where  $d$  is a scalar damage parameter that assumes a value between 0 and 1, with 0 representing the state of no damage. For a uniaxial stress state,  $d$  can be interpreted as the ratio of the damaged cross-sectional area, which cannot carry any load, to the total cross-sectional area under consideration. The actual stress developed in the undamaged material is called the effective stress and is defined as:

$$\bar{\boldsymbol{\sigma}} = \mathbf{E}_0 : \boldsymbol{\varepsilon}^e = \mathbf{E}_0 : (\boldsymbol{\varepsilon} - \boldsymbol{\varepsilon}^p) \quad (2.4)$$

The damage parameter  $d$  is a function of the damage parameter in tension,  $d_t(\tilde{\boldsymbol{\varepsilon}}_t^p)$ , and the damage parameter in compression,  $d_c(\tilde{\boldsymbol{\varepsilon}}_c^p)$ , as follows:

$$(1 - d) = (1 - s_t d_t)(1 - s_c d_c) \quad (2.5)$$

The damage parameters,  $d_t = d_t(\tilde{\varepsilon}_t^p)$  and  $d_c = d_c(\tilde{\varepsilon}_c^p)$ , are calibrated from cyclic uniaxial tension and compression tests and are functions of the plastic tensile and compressive strain, respectively.

Variables  $s_t$  and  $s_c$  are defined as:

$$s_t = 1 - w_t r(\hat{\boldsymbol{\sigma}}) \quad (2.6)$$

$$s_c = 1 - w_c (1 - r(\hat{\boldsymbol{\sigma}})) \quad (2.7)$$

In Eq. (2.6) and (2.7),  $w_t$  and  $w_c$  are constants that control the recovery of stiffness upon stress reversal from compression to tension and from tension to compression, respectively. The values of  $w_t$  and  $w_c$  can be between 0, where no stiffness recovery is assigned, and 1, where total stiffness recovery is assigned.

$r(\hat{\boldsymbol{\sigma}})$  is a weight factor, with a value between 0 and 1, defined as:

$$r(\hat{\boldsymbol{\sigma}}) = \begin{cases} 0 & \text{if } \hat{\boldsymbol{\sigma}} = \mathbf{0} \\ \frac{\sum_{i=1}^3 \langle \hat{\sigma}_i \rangle}{\sum_{i=1}^3 |\hat{\sigma}_i|} & \text{otherwise} \end{cases} ; 0 \leq r(\hat{\boldsymbol{\sigma}}) \leq 1 \quad (2.8)$$

where  $\hat{\sigma}_i$ 's are the principal effective stresses.

The solid line in Figure 2.1 shows the stress-strain response of the concrete model under uniaxial loading, with total stiffness recovery ( $w_c = 1$ ) upon stress reversal from tension to compression, and no stiffness recovery ( $w_t = 0$ ) from compression to tension.

The equivalent plastic strains,  $\tilde{\epsilon}_c^p$  and  $\tilde{\epsilon}_t^p$ , are calculated from the equivalent plastic strain rates,  $\dot{\tilde{\epsilon}}_c^p$  and  $\dot{\tilde{\epsilon}}_t^p$ , as follows:

$$\tilde{\epsilon}_t^p = \int_0^t \dot{\tilde{\epsilon}}_t^p dt \quad (2.9)$$

$$\tilde{\epsilon}_c^p = \int_0^t \dot{\tilde{\epsilon}}_c^p dt \quad (2.10)$$

The equivalent plastic strain rates,  $\dot{\tilde{\epsilon}}_c^p$  and  $\dot{\tilde{\epsilon}}_t^p$ , are evaluated with the following expressions:

$$\dot{\tilde{\epsilon}}_t^p = r(\hat{\sigma}) \hat{\epsilon}_{\max}^p \quad (2.11)$$

$$\dot{\tilde{\epsilon}}_c^p = (1 - r(\hat{\sigma})) \hat{\epsilon}_{\min}^p \quad (2.12)$$

in which  $\hat{\epsilon}_{\max}^p$  and  $\hat{\epsilon}_{\min}^p$  are obtained from the principal plastic strain rates ( $\dot{\epsilon}_1^p, \dot{\epsilon}_2^p, \dot{\epsilon}_3^p$ ) in that  $\hat{\epsilon}_{\max}^p = \dot{\epsilon}_1^p$  and  $\hat{\epsilon}_{\min}^p = \dot{\epsilon}_3^p$  with  $\dot{\epsilon}_1^p > \dot{\epsilon}_2^p > \dot{\epsilon}_3^p$ .

The yield surface of the damaged-plasticity model is based on that proposed by Lubliner et al. (1989) with the modifications introduced by Lee and Fenves (1998) to account for the different behaviors of concrete in tension and compression. The initial shape of the yield surface in the principal stress plane for the plane-stress condition is shown in Figure 2.2. The yield function is defined in terms of the first stress invariant  $I_1$ , the second deviatoric stress invariant  $J_2$ , and the maximum principal stress as  $\hat{\sigma}_{\max}$ :

$$F = \frac{1}{1-a} \left( aI_1 + \sqrt{3J_2} + \beta(\tilde{\epsilon}_c^p, \tilde{\epsilon}_t^p) \langle \hat{\sigma}_{\max} \rangle - \gamma \langle -\hat{\sigma}_{\max} \rangle \right) - \bar{\sigma}_c(\tilde{\epsilon}_c^p) \quad (2.13)$$



in which  $\langle - \rangle$  denotes the Macauley brackets. Variable  $\bar{\sigma}_c$ , along with  $\bar{\sigma}_t$ , which is used to calculate variable  $\beta$ , defined in Eq. (2.19), are the effective compressive and tensile cohesion strengths, and are defined as:

$$\bar{\sigma}_c = \frac{\sigma_c}{(1-d_c)} \quad (2.14)$$

$$\bar{\sigma}_t = \frac{\sigma_t}{(1-d_t)} \quad (2.15)$$

in which the functions  $\sigma_t(\tilde{\varepsilon}_t^p)$  and  $\sigma_c(\tilde{\varepsilon}_c^p)$  represent the stress-vs.-plastic strain curves for uniaxial tension and compression, and are calibrated from uniaxial tension and compression test data.

Constant  $a$  in Eq. (2.13) is defined as:

$$a = \frac{(\sigma_{b0} / \sigma_{c0}) - 1}{2(\sigma_{b0} / \sigma_{c0}) - 1} \quad (2.16)$$

in which  $(\sigma_{b0} / \sigma_{c0})$  is the ratio of the initial equibiaxial compressive yield stress to the initial uniaxial compressive yield stress. In this study, the default value of 1.16 is used for  $(\sigma_{b0} / \sigma_{c0})$ . Constant  $\gamma$  is defined as:

$$\gamma = \frac{3(1-K_c)}{2K_c - 1} \quad (2.17)$$

in which  $K_c$ , as defined in Eq. (2.18), is the ratio of the second deviatoric stress invariant for a stress state on the tensile meridian to that on the compressive meridian at the initial yield, for any given value of the pressure invariant such that the maximum principal stress is negative,  $\hat{\sigma}_{\max} < 0$ .

$$K_c = \frac{(J_2)_{TM}}{(J_2)_{CM}} \quad (2.18)$$

The value of  $K_c$  must satisfy the condition that  $0.5 < K_c \leq 1.0$ . As shown in Figure 2.3, the shape of the deviatoric plane depends on the value of  $K_c$ . The value of  $K_c$  also affects the slopes of the tensile and compressive meridians in the meridian plane as it is shown in Figure 2.4. For low hydrostatic pressure states,  $K_c = 2/3$  provides a good fit of experimental data, while a higher value of  $K_c$  is more appropriate for high hydrostatic pressure states, as pointed out by Ottosen (1977).

The variable  $\beta$  is defined as:

$$\beta = \frac{\bar{\sigma}_c(\tilde{\varepsilon}_c^p)}{\bar{\sigma}_t(\tilde{\varepsilon}_t^p)}(1-a) - (1+a) \quad (2.19)$$

For the yield surface originally proposed by Lubliner et al. (1989),  $\beta$  is a constant, dependent only on the initial ratio of  $\bar{\sigma}_c / \bar{\sigma}_t$ . According to Lee and Fenves (1998), this gives good results for monotonic loading, but to model the cyclic behavior of concrete,  $\beta$  has to be dependent on the evolution of the compressive strength and tensile strength.

A non-associated flow rule has been adopted with the plastic strain rate is defined as  $\dot{\boldsymbol{\varepsilon}}^p = \dot{\lambda} \frac{\partial G}{\partial \boldsymbol{\sigma}}$ , where

$\dot{\lambda}$  is the plastic multiplier. The plastic potential  $G$  is defined as:

$$G = \sqrt{(\varepsilon \sigma_{t0} \tan \psi)^2 + 3J_2} + \frac{I_1}{3} \tan \psi \quad (2.20)$$

where  $\sigma_{t0}$  is the uniaxial tensile strength, which can be obtained from uniaxial tension test data,  $\psi$  is the dilation angle and  $\varepsilon$  is a parameter, referred to as the eccentricity that defines the rate at which the

function approaches the asymptote. Figure 2.5 shows the shape of the plastic potential for different values of  $\varepsilon$ . The plastic potential tends to a straight line as  $\varepsilon$  approaches zero as shown in the figure. For  $\varepsilon = 0$ , the plastic potential takes the form of the Drucker-Prager (1952) criterion. The default value for  $\varepsilon$  is 0.1.

### **2.1.2 Validation and Calibration of the Damaged-Plasticity Model**

Lee and Fenves (1998) validated the model for monotonic uniaxial and biaxial compression and tension loading. The model available in Abaqus (Simulia 2012) has been calibrated and further validated here for cyclic uniaxial compression-tension behavior and compression under lateral confinement. The calibration of the model in Abaqus requires the specification of the uniaxial compressive stress- inelastic strain curve and the uniaxial tensile stress-cracking displacement curve. Given the value of the compressive strength of concrete, the uniaxial compressive stress-plastic strain curve has been defined in this study based on the model proposed by Karthik and Mander (2011) for unconfined concrete. For tension, the tensile strength is assumed to decay linearly with the cracking displacement, reflecting the fracture energy released.

In cyclic loading, the damaged-plasticity model has stiffness degradation during unloading and reloading in tension to simulate the closing and opening of a crack. However, when the inelastic tensile strain is large, the complete closure of a crack would require a very large stiffness degradation (with the value of the damage parameter,  $d_t$ , very close to one), which leads to numerical problems. Hence, the model cannot be appropriately calibrated to simulate the complete closure of a crack with a small residual crack opening upon unloading. To circumvent this problem, contact conditions in Abaqus are used in this study to represent major flexural cracks in a discrete manner. Figure 2.6 shows a simple assembly of a finite element (FE) model which demonstrates how contact conditions can improve the behavior of concrete in simulation under uniaxial cyclic loading. In Figure 2.7, the dashed curve is the result from the model without contact conditions, and the solid curve is the result when contact conditions are introduced as shown in Figure 2.6.

The parameters affecting the yield surface have been calibrated with experimental data obtained by Hurlbut (1985) and Mander et al. (1988b) to capture the behavior of confined concrete in compression. The values of the parameters determined for the damaged-plasticity model are shown in Table 2.1.

Figure 2.8 shows a FE model to simulate the compressive behavior of concrete under equal bilateral compressive stresses. The assembly, whose mesh has 100 elements is simply supported at its base, and hydrostatic pressure is applied first. Then, additional compression is applied in one direction by controlling the displacement of the top face. As shown in Figure 2.9, the model is capable of reproducing the effect of the lateral confining stress on the compressive strength and lateral expansion of concrete observed in the tests of Hurlbut (1985). However, the increase of ductility in compression (i.e., a less steep declining slope in the stress-strain curve) due to increasing confining pressure is not captured by the model. This is due to the fact that the softening rule used in this damaged-plasticity model is defined only in terms of the uniaxial compressive stress-strain curve, which is embedded in the term  $\bar{c}_c(\tilde{\epsilon}_c^p)$ , as shown in the expression for the yield surface in Eq. (2.13), without taking into account the effect of the confining pressure. For the model to match the experimental results, the slope of the decaying branch of the input uniaxial compressive stress-strain curve has to be modified a priori based on the level of the confining pressure or the amount of the confining steel, as shown in Figure 2.10. In this figure,  $f_c$  is the uniaxial compressive strength of unconfined concrete, while  $f_{cc}$  is the uniaxial compressive strength of confined concrete. In this study, the post-peak slope of the input uniaxial compressive stress-strain curve is determined according to the confinement level based on the work of Karthik and Mander (2011). With this modification, the model is capable of capturing the increase of ductility with the increase of the confining pressure, which was observed in the tests of Hurlbut (1985) as shown in Figure 2.11.

The damaged-plasticity model was further validated by replicating the experimental results of Mander et al. (1988b) on the compression tests of circular-sectioned RC columns with different amounts of confining steel. Figure 2.12 shows a FE model of one of the RC columns tested by Mander et al. (1988b).

The longitudinal bars are modeled with beam elements and the hoops are modeled with truss elements. An elasto-plastic constitutive law with linear kinematic hardening is assigned to the steel reinforcement.

As shown in Figure 2.13, the FE model can adequately describe the effect of the lateral confining stress on the compressive strength and ductility of the RC columns, as shown in the experimental tests of Mander et al. (1988b).

## **2.2 Modeling of Steel Reinforcement**

For the purpose of this study, the stress-strain relation for steel reinforcing bars under cyclic loading has to be accurately described and efficient to calculate. However, Abaqus (Simulia 2012) only provides an elasto-plastic constitutive law with linear kinematic hardening. For this reason, a more realistic uniaxial stress-strain model has been implemented in Abaqus. In this model, the stress-strain relation for cyclic loading is based on the Menegotto-Pinto model (1973), and the low-cycle fatigue (LCF) law proposed by Manson (1953) and Coffin (1954) is incorporated. This steel model has been used in beam and truss elements.

A number of phenomenological steel models have been proposed in various studies to simulate the behavior of steel reinforcement under cyclic loading. Filippou et al. (1983) have adopted the Menegotto-Pinto model (1973), and added isotropic hardening to it. Dodd and Restrepo (1995) have proposed an analytical model that differentiates tensile behavior from compressive behavior by formulating the basic stress-strain relation in terms of the natural strain and true stress, and then converting it to a relation in terms of the engineering stress and strain based on an assumption that the volume of the reinforcing bar remains constant. Monti and Nutti (1992) have proposed a phenomenological stress-strain law that indirectly accounts for the drop of compressive resistance due to bar buckling. Kunnath et al. (2009a) have proposed a phenomenological steel model accounting for the LCF of a reinforcing bar based on the law developed by Manson (1953) and Coffin (1954). The model has been calibrated with experimental

data from LCF tests of bar specimens with specific slenderness ratios and a range of bar diameters. For the basic uniaxial stress-strain relation, Kunnath et al. (2009a) have adopted the Menegotto-Pinto model (1973) with modifications. They have also adopted the work of Dhakal and Maekawa (2002) to describe the drop of compressive strength due to bar buckling in the material model.

In this study, the Menegotto-Pinto model (1973) has been adopted, due to its simple formulation, and improved to better capture the stress-strain behavior of reinforcing bars when they are subjected to partial unloading and reloading, for which the original formulation has an issue. Similar to Kunnath et al.'s model (2009a), the LCF law proposed by Manson (1953) and Coffin (1954) has been incorporated. This law has been calibrated with experimental data obtained from LCF tests conducted on reinforcing bars. To account for bar buckling occurring in these tests, a calibration method is proposed here to extract the LCF properties of steel at the material level.

### **2.2.1 Cyclic Stress-Strain Relation**

The model adopted here is formulated in terms of the engineering stress and strain. For a reinforcing bar made of mild steel and subjected to monotonically increasing strain, the model represents the stress-strain relation in tension or compression with four segments: (a) a linearly elastic segment, (b) a plateau at the yield stress,  $f_y$ , (c) a strain hardening segment described by the Menegotto-Pinto relation, and (d) a plateau at the ultimate stress,  $f_u$ . As shown in Figure 2.14, the aforementioned idealized stress-strain relation matches the tensile test result for a No. 11 well. The ultimate strain at which bar fracture occurs is determined by a LCF law, which will be described later.

Upon strain reversal after the yield strain,  $\varepsilon_y$ , has been reached in tension or compression, the Menegotto-Pinto model (1973) is used to describe the cyclic stress-strain relation, as shown in Figure 2.15. The Menegotto-Pinto model (1973) has the following formulation:

$$\sigma^* = b\varepsilon^* + \frac{(1-b)\varepsilon^*}{(1+\varepsilon^{*R})^{\frac{1}{R}}} \quad (2.21)$$

where

$$\varepsilon^* = \frac{\varepsilon - \varepsilon_r}{\varepsilon_o - \varepsilon_r} \quad (2.22)$$

$$\sigma^* = \frac{\sigma - \sigma_r}{\sigma_o - \sigma_r} \quad (2.23)$$

Eq. (2.21) relates the normalized stress,  $\sigma^*$ , to the normalized strain,  $\varepsilon^*$ , representing the stress-strain curve for unloading from the strain reversal point  $(\varepsilon_r, \sigma_r)$  and reloading in the other direction. This curve has two asymptotes. One has a slope corresponding to the modulus of elasticity of steel and the other has a slope governing kinematic hardening. Figure 2.15 shows the stress-strain relation without normalization. In this figure,  $\sigma_o$  and  $\varepsilon_o$  are the stress and strain at which the two asymptotes meet. The second asymptote intersects with the straight line representing the linearly elastic behavior of steel under monotonic loading at  $(\varepsilon_{y,m}, f_{y,m})$  or  $(-\varepsilon_{y,m}, -f_{y,m})$  depending on whether it is on the tension or the compression side. Parameters  $\varepsilon_{y,m}$  and  $f_{y,m}$  assume positive values that are determined by calibration. Parameter  $b$  in Eq. (2.21) governs kinematic hardening in that  $b = E_1 / E_0$ , where  $E_0$  is the modulus of elasticity and  $E_1$  is the slope of the second asymptote, as shown in Figure 2.15, and  $R$  is a parameter which controls the stress-strain curvature of the curve simulating the Bauschinger effect. A smaller value of  $R$  corresponds to a larger radius of curvature. The values of  $(\varepsilon_o, \sigma_o)$ , and  $(\varepsilon_r, \sigma_r)$  are updated after each strain reversal. In the original Menegotto-Pinto model,  $R$  is calculated with the following equation:

$$R = R_0 - \frac{a_1 \xi}{a_2 + \xi} \quad (2.24)$$

where the variable  $\xi$  is defined as:

$$\xi = \begin{cases} \frac{|\varepsilon_{\max} - \varepsilon_o|}{\varepsilon_{y,m}} & \text{for reloading from compression to tension} \\ \frac{|\varepsilon_{\min} - \varepsilon_o|}{\varepsilon_{y,m}} & \text{for reloading from tension to compression} \end{cases} \quad (2.25)$$

in which  $\varepsilon_{\max}$  and  $\varepsilon_{\min}$  are the maximum and minimum strains attained in previous cycles. The constants,  $R_0$ ,  $a_1$ , and  $a_2$ , are determined by calibration.

One issue with the original Menegotto-Pinto model is that it is not able to accurately reproduce the stress-strain response during reloading right after partial unloading, showing stress overshoot, as noted by Filippou et al. (1983) and Kunnath et al. (2009a). This is illustrated in Figure 2.16, in which the curve with the original  $R$ , calculated with Eq. (2.24), shows a significant stress overshoot during reloading on the compression side. Besides the inaccuracy, this can also cause convergence problems in finite element analysis. In this study, this problem is corrected by introducing a modification to the expression for  $R$  in Eq. (2.24) so that the value of  $R$  also depends on the stress difference between the intersection point of the asymptotes,  $(\varepsilon_o, \sigma_o)$ , and the previous load reversal point,  $(\varepsilon_r, \sigma_r)$ , as shown in the following equation.

$$R = \left( R_0 - \frac{a_1 \xi}{a_2 + \xi} \right) \left| \frac{\sigma_o - \sigma_r}{2f_{y,m}} \right|^{1 - \left| \frac{\sigma}{2\sigma_o} \right|} \quad (2.26)$$

in which  $\sigma$  is the stress at the previous step. The curve with the modified  $R$  in Figure 2.16 shows that this change corrects the stress overshoot problem.



The steel model has been validated with experimental data. Figure 2.17 through Figure 2.19 compare stress-strain curves from the steel model and the tests conducted by Dodd and Restrepo (1995), Aktan et al. (1973), and Kent and Park (2973). The values of the model parameters used in the analyses are summarized in Table 2.2.

### 2.2.2 Low-Cycle Fatigue

Under severe earthquake loading, flexural reinforcement in plastic-hinge regions of RC members can be subjected to large-amplitude cyclic plastic strain reversals, due to direct tension or bending once the reinforcing bars have buckled. Hence, bar fracture is highly influenced by low-cycle fatigue (LCF).

The LCF of steel under cyclic loading with constant strain amplitude can be described with the following expression by Manson (1953) and Coffin (1954), as adopted in this study:

$$N_f = \left( \frac{\Delta\varepsilon}{2\varepsilon'_f} \right)^{-\frac{1}{c}} \quad (2.27)$$

in which  $N_f$  is the number of half cycles to failure and  $\Delta\varepsilon$  is the strain range, defined as  $\Delta\varepsilon = \varepsilon_{\max} - \varepsilon_{\min}$ , attained in the cyclic loading, as shown in Figure 2.20; and  $\varepsilon'_f$  and  $c$  are coefficients representing the LCF properties of the material. Parameters  $\varepsilon'_f$  and  $c$  have to be calibrated with experimental data.

To account for the random strain history during an earthquake event, the range counting method is adopted, and damage due to LCF is linearly accumulated according to Miner's rule (1945). During any strain reversal  $i$ , the strain range  $\Delta\varepsilon_i = \varepsilon_{\max,i} - \varepsilon_{\min,i}$  is computed in terms of the maximum and minimum strains attained in that half cycle no matter it is completed or not, as shown in Figure 2.21, and damage in that half cycle is defined as:

$$D_i = \frac{1}{(N_f)_i} \quad (2.28)$$

in which  $(N_f)_i$  is the number of half cycles to failure if the strain range were constant at  $\Delta\varepsilon_i$  according to Eq. (2.27). Total damage due to LCF during or right after the completion of the  $n^{\text{th}}$  half cycle is then calculated as follows:

$$D = \sum_{i=1}^n D_i \quad (2.29)$$

When the damage accumulated reaches or exceeds one, it is assumed that the steel will fracture and the stress will drop to zero following a steep descending curve in the stress-strain relation. However, in order to ensure the robustness of the finite element analyses (FEA), fracture is not sudden and the stress drop follows a descending curve that has a slope equal to  $-0.034E_0$  till it reaches a residual stress of  $0.1f_y$ .

The effects of the mean strain,  $\varepsilon_{\text{mean}}$ , and mean stress,  $\sigma_{\text{mean}}$ , which are defined in Figure 2.22 and Figure 2.23, are not taken into consideration in the LCF law adopted here. The strain amplitudes, defined as  $\Delta\varepsilon/2$ , of interest in this study are above 0.01. According to Koh and Stephens (1991), the effects of the mean strain and mean stress on the LCF of steel can be neglected for strain amplitudes above that level, as shown in Figure 2.24.

### 2.2.3 Calibration of Low-cycle Fatigue Law

In LCF tests, reinforcing bars were normally subjected to severe tensile and compressive load cycles, and would eventually buckle. Bar buckling exacerbated LCF because of large localized strains introduced by bar bending. In RC columns, flexural reinforcement in the plastic-hinge region may buckle after the cover concrete spalls, accelerating the LCF of these bars. The tendency of a bar to buckle depends on its slenderness ratio, which depends on the bar diameter and its unsupported length as determined by the

spacing of the lateral reinforcement in the RC member. Therefore, LCF laws directly calibrated with tests conducted on bars with specific slenderness ratios may not reflect the true material behavior and introduce an issue in modeling. If the computational model explicitly captures bar buckling, the model so calibrated will double count the effect of bar buckling on LCF. If the model does not explicitly consider bar buckling, then the calibrated model, in the strict sense, will only be appropriate for bars that have a similar slenderness ratio as the specimens that provided the data. To address this issue, a calibration strategy is proposed here.

The proposed strategy uses a nonlinear beam element model that captures bar buckling to extract the LCF properties of the steel material from the LCF tests of the bars. The bar is modeled with beam elements in Abaqus considering material and geometric nonlinearities. For material nonlinearity, the Menegotto-Pinto model with the LCF law of Manson and Coffin [Eq. (2.28)] as presented in the previous sections is used. To calibrate the material model, the LCF tests conducted by Brown and Kunnath (2004) and Kunnath et al. (2009b) are considered. Figure 2.25a shows the test apparatus used by Kunnath et al. (2009b) including a buckled bar specimen, while Figure 2.25b shows the FE model for the bar specimen. The bar is modeled with 2-node beam elements with one integration point at their middle length. The bending moment and axial force at the sampled section of a beam element are calculated with the trapezoidal rule based on stresses determined at the cross-sectional sampling points shown in Figure 2.26. The axial strains of the bars reported for these tests are the average values based on the axial deformation measured over the entire unsupported length of the bar specimen. The bar is modeled with 10 beam elements with an initial imperfection (initial offset at mid-span) of  $L/1000$ . The FE model is subjected to the same average-axial strain history (or more exactly the relative end displacement) experienced by the bar during the test. The values of  $\varepsilon'_f$  and  $c$  for the LCF law are so determined that the model exhibits bar fracture in the same cycle as in the test of the bar specimen. The stress-average axial strain curves obtained by the FE model and the tests by Kunnath et al. (2009b) are compared in Figure 2.27. The decrease of the compressive resistance due to the buckling of the bars is adequately described by the FE model. The

element size has been determined with a mesh sensitivity analysis. Figure 2.28 shows the stress-strain curves for FE models with different element sizes.

The LCF law has been calibrated with tests conducted on No. 9, 11, and 14 bars obtained by Brown and Kunnath (2004) and Kunnath et al. (2009b). The values of  $\varepsilon'_f$  and  $c$  have been determined to be 0.382 and 0.455, respectively. Table 2.3 compares the number of cycles to failure,  $(N_f / 2)$ , obtained by the FE analyses with this calibration and the tests. Figure 2.29 compares the LCF law calibrated here for the steel material to the LCF law calibrated by Brown and Kunnath (2004) directly with the average strain data for a No. 9 bar that had clear length of 6 times the bar diameter. As expected, the LCF law calibrated for the material gives a much larger number of cycles to failure for a given strain amplitude.

The use of nonlinear beam elements to model the buckling and LCF of reinforcing bars in RC members requires very refined FE meshes, at least for the plastic-hinge regions, and thus significant computational resources. Very often, geometric nonlinearity is ignored in the modeling of reinforcing bars and a mesh that is coarser than what is needed to simulate bar buckling is used to improve computational efficiency. It is even more common to represent reinforcing bars with truss elements, which only simulate the uniaxial stress-strain behavior of bars. With these simplified models, the LCF law calibrated for steel material will not be appropriate because the effect of bar buckling is not accounted for. On the other hand, a LCF law calibrated directly with bar test data may not be appropriate for bars that have a slenderness ratio different from that of the bar specimen that provided the data. The slenderness ratio will affect the tendency of the bar to buckle and the resulting bending deformation. In an RC member, the slenderness of a longitudinal reinforcing bar after the cover concrete spalls is governed by the spacing of the lateral reinforcement.

To address the aforementioned issue, the following procedure is used to calibrate the steel model when bar buckling is not explicitly accounted for in the FE analysis of an RC member or structure. First, a single bar is modeled with a refined mesh using nonlinear beam elements which account for bar buckling.

The LCF law calibrated for the steel material is used. The clear length of the bar is set to be equal to the center-to-center spacing of the lateral reinforcement in the member. Finite element analyses are conducted with the model to simulate LCF tests with varying average-strain ranges. For each strain range,  $\Delta\varepsilon$ , the number of cycles to fracture is obtained. A plot of  $N_f$  versus  $\Delta\varepsilon$  is then generated with the numerical data. From this plot, the values of  $\varepsilon'_f$  and  $c$  are determined to obtain a LCF law that accounts for the effect of bar buckling and can therefore be used for simplified bar models used in the structural analysis. This has to be repeated for every bar size and every lateral steel spacing. Figure 2.30 shows results obtained for No. 9 bars with different slenderness.

## **2.3 Modeling of Bond-Slip**

The bond-slip behavior between the longitudinal bars and the concrete in an RC member is simulated in the finite element analyses (FEA) with a bond-slip model developed by Murcia-Delso and Shing (2015). The model adopts a semi-empirical law, based on concepts originally proposed by Eligehausen et al. (1983) and further extended by others (Pochanart and Harmon 1989; Yankelevsky et al. 1992 and Lowes et al. 2004), accounting for bond deterioration caused by cyclic slip reversals, the tensile yielding of the bars, and the opening of radial splitting cracks in concrete. The bond-slip model has been implemented in interface elements in Abaqus, which can be used to connect steel to concrete in the three-dimensional FEA of RC members.

### **2.3.1 Bond-Slip Interface Model**

The relative displacements and stresses in the normal and tangential directions of the interface between a reinforcing bar and the surrounding concrete are defined in Figure 2.31. The bar slip and bond stress are denoted by  $s_2$  and  $\tau_2$ , respectively.

### 2.3.2 Bond Stress-Slip Law

In the bond-slip law of Murcia-Delso and Shing (2015), the total bond resistance consists of the bearing resistance and the friction resistance. Figure 2.32(a) shows the monotonic bond stress-slip curves with the contributions of these two mechanisms. The model has three parameters, namely, the peak bond strength for an elastic bar,  $\tau_{\max}$ , the slip at which the peak strength is attained,  $s_{peak}$ , and the clear spacing between the ribs,  $s_R$ , to calibrate.  $s_R$  is a known geometric property of the bar and is usually between 40% and 60% of the bar diameter.  $\tau_{\max}$  and  $s_{peak}$  depend on many factors and no theoretical formulas are available to accurately predict their values. Thus, they should be determined experimentally for each case, if possible. When no experimental data are available, the following empirical formulas can be used to estimate the values as suggested by Murcia-Delso and Shing (2015).

$$\tau_{\max} = 0.72f_c^{3/4} \text{ (in ksi)} \quad (2.30)$$

$$s_{peak} = 0.07d_b \quad (2.31)$$

in which  $f_c'$  is the compressive strength of concrete and  $d_b$  is the bar diameter.

The bond-slip model accounts for the deterioration of both the bearing and the friction resistances as a function of the maximum and cumulative slips, the yielding of the bar in tension, and the opening of the steel-concrete interface with respect to the rib height. Figure 2.32(b) shows the bond stress-vs.-slip relations for cyclic loading. As shown in the figure, when the bar slips between previously attained slip levels, the bond stress is bounded by the friction resistance,  $\tau_{rev}$ . This is because part of the concrete in contact with the ribs of the bar on the bearing side has been crushed, and a gap has been created on the other side of the ribs. This gap needs to be closed before the bearing resistance of the ribs in the opposite

direction can be activated. Once contact is resumed, the bond resistance increases, but up to a lower peak due to the deterioration of the bearing resistance.

### 2.3.3 Normal and Transverse Tangential Stresses

To simulate the wedging action of the bar ribs, the resultant force exerted by the bar on the surrounding concrete is assumed to have a fixed angle of inclination,  $\theta$ , with respect to the longitudinal axis of the bar. The normal component of the interface stress, as shown in Eq.(2.32), is proportional to the bond stress with the proportionality constant determined by the angle,  $\theta$ , while a penalty stiffness  $K_{pen,1}$  is added, which is active only in compression to minimize the interpenetration of the steel and concrete.

$$\sigma_1 = -|\tau_2| \tan \theta + K_{pen,1} \min(s_1, 0) \quad (2.32)$$

The rotation of the bar around its longitudinal axis is restrained by a penalty stiffness  $K_{pen,3}$ , as presented in the following equation.

$$\tau_3 = K_{pen,3} s_3 \quad (2.33)$$

### 2.3.4 Interface Element Implementation

The bond-slip law serves as a constitutive model for the interface element that connects truss or beam elements representing reinforcing bars to the surrounding concrete, as shown in Figure 2.33. To evaluate the stress for a given relative displacement, the value of the axial strain in the bar may be calculated inside the interface element from the displacements parallel to the bar axis at the nodes connected to the bar (nodes A and B in Figure 2.33) and the length of the element  $L_e$ , as

$$\varepsilon_s = \frac{u_{2B} - u_{2A}}{L_e} \quad (2.34)$$

An interface element that allows the computation of  $\varepsilon_s$  with Eq. (2.34) has been implemented in Abaqus in a user-defined subroutine. The interface element has four nodes (with two nodes connected to the bar and two connected to the concrete), linear shape functions, and two integration points at its ends, as shown in Figure 2.33.



Table 2.1 – Damaged-plasticity model calibration

Parameter	Description	Value
$\sigma_{b0}/\sigma_{c0}$	Controls biaxial compressive strength	0.12
$\psi$	Dilation angle	20°
$\varepsilon$	eccentricity	0
$K_c$	Controls shape of yield surface	2/3
$w_c$	Compression recovery factor	0
$w_t$	Tension recovery factor	1

Table 2.2 – Calibration of the Menegotto-Pinto Model

$f_{y,m}$	$1.25 f_y$
$\varepsilon_{y,m}$	$1.25 \varepsilon_y$
$f_u$	$1.45 f_y$
$b$	0.01
$R_o$	0.03
$a_1$	0.15
$a_2$	0.02

Table 2.3 – Comparison of number of cycles to failure in the FEA and tests

Bar size	Strain amplitude, $\varepsilon_a = \Delta\varepsilon / 2$	$N_f/2$	
		FEA	Test
#9	0.015	54	63-67
#9	0.02	25	27-31
#9	0.03	9	7-9
#11	0.02/0.04	8/3	8/3
#11	0.05	4	3
#14	0.01	53	41-45
#14	0.02	17	14-16
#14	0.04	2	4

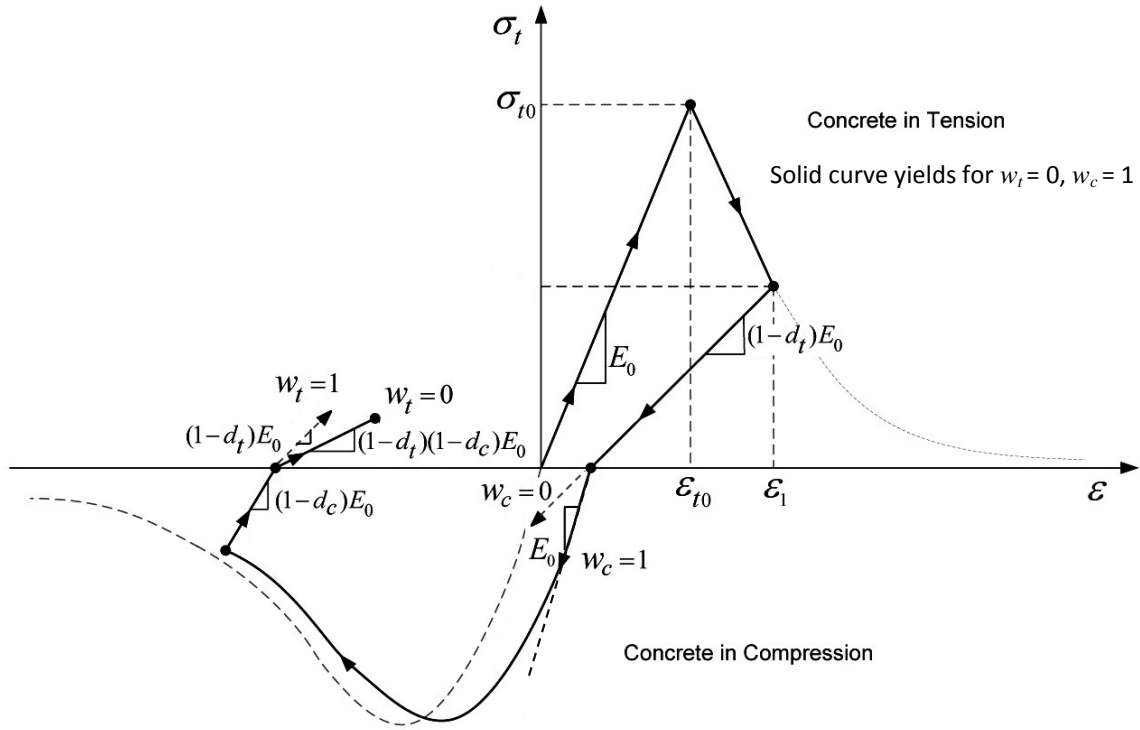


Figure 2.1 – Stiffness recovery under uniaxial load cycle for damaged-plasticity model

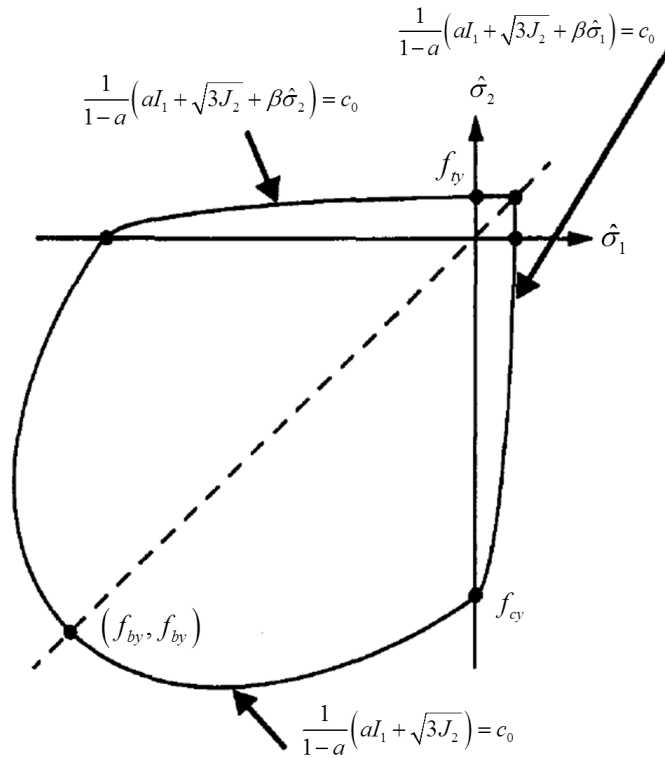


Figure 2.2 – Initial yield function in principal stress space under plane-stress condition (Lee and Fenves 1998)

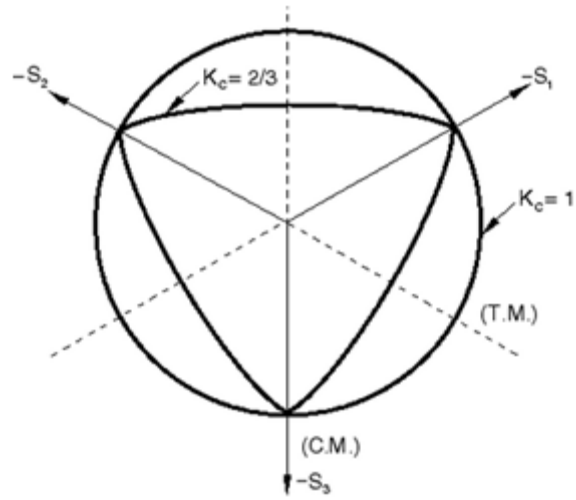


Figure 2.3 – Deviatoric plane for different values of  $K_c$

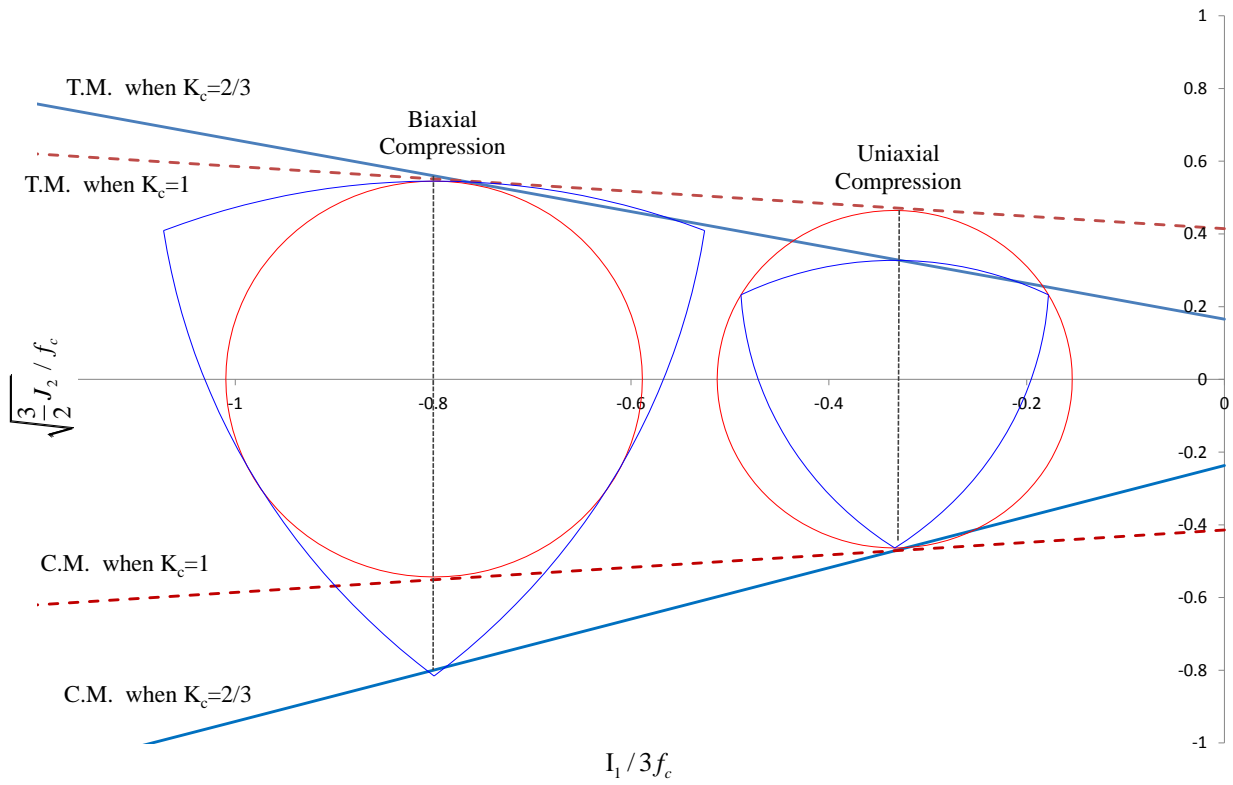


Figure 2.4 – Meridian plane of yield surface for different values of  $K_c$

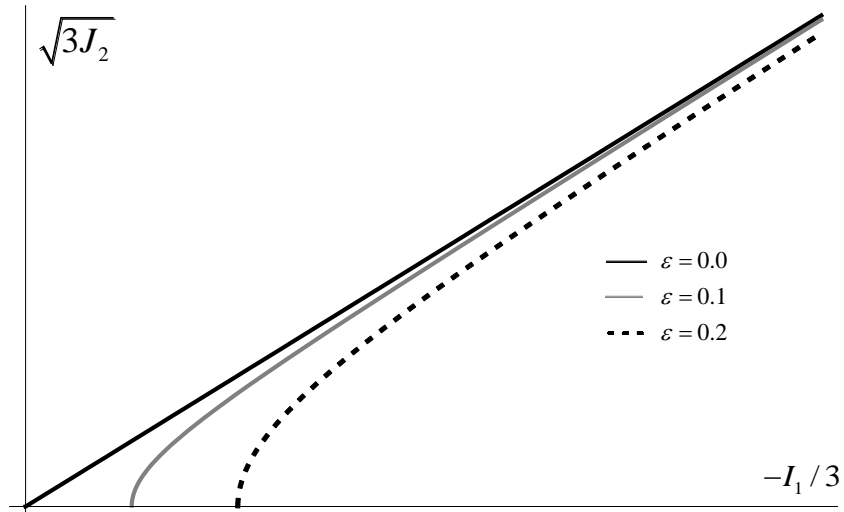


Figure 2.5 – Plastic potential for different values of  $\epsilon$

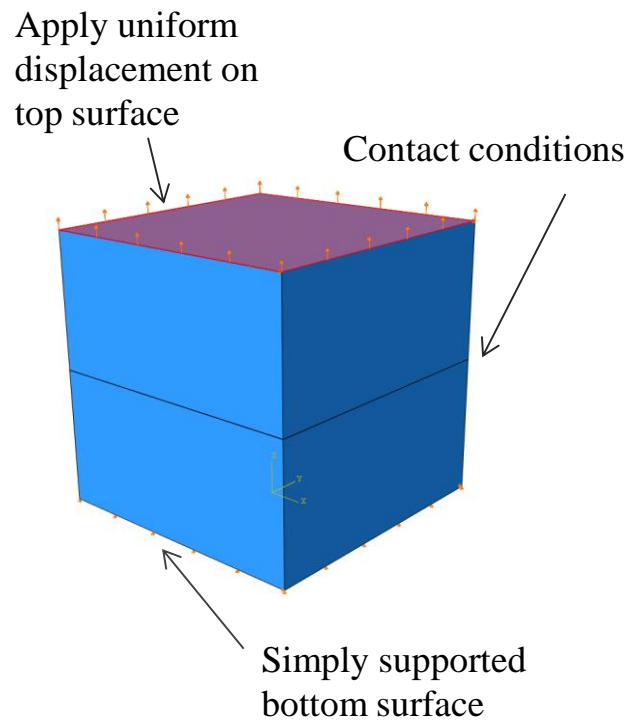


Figure 2.6 – Model for uniaxial loading with contact conditions

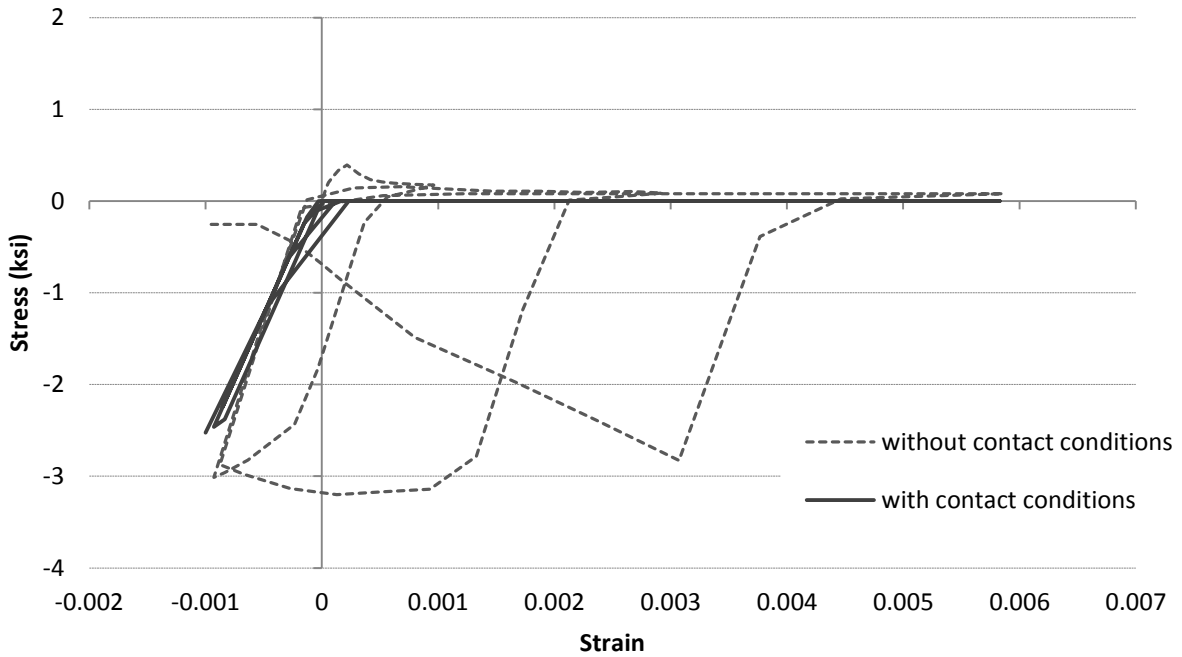


Figure 2.7 – Uniaxial loading test of models with and without contact conditions

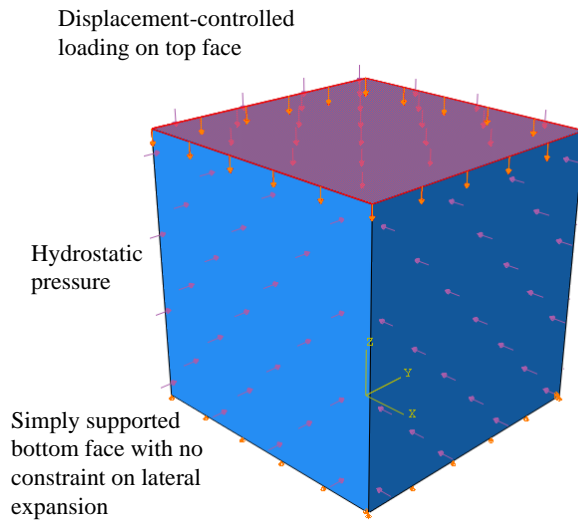


Figure 2.8 – FE model of hydrostatic pressure tests by Hurlbut (1985)

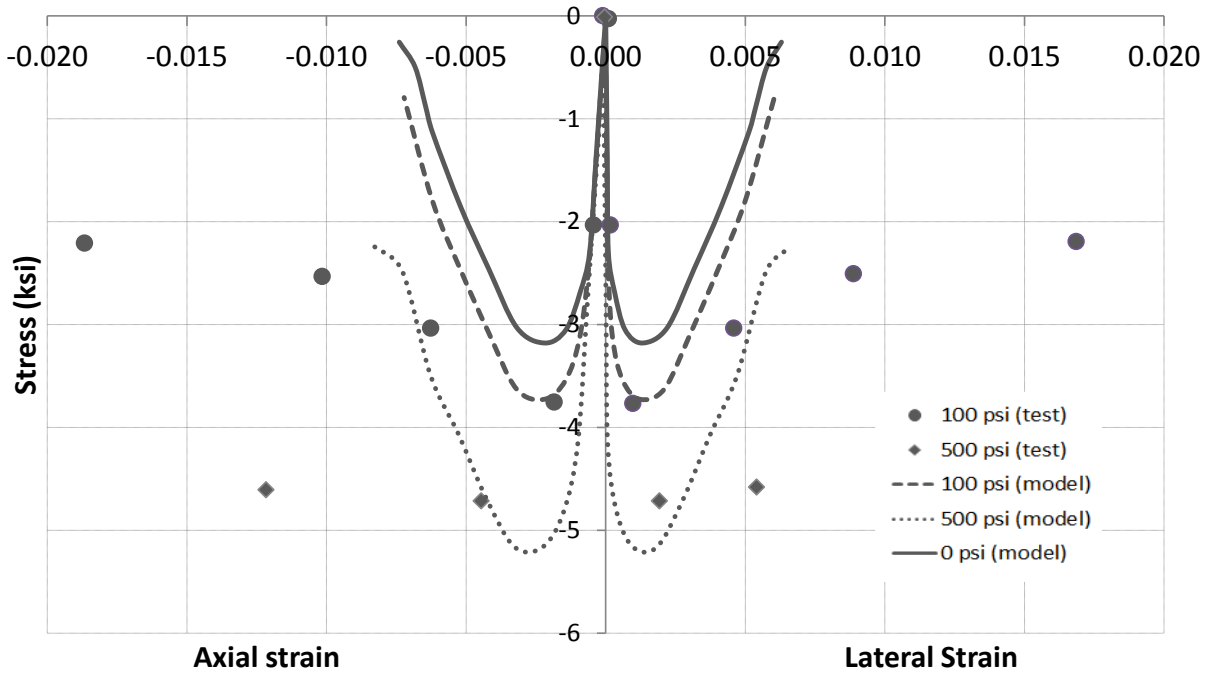


Figure 2.9 – Confined compression tests by Hurlbut (1985)

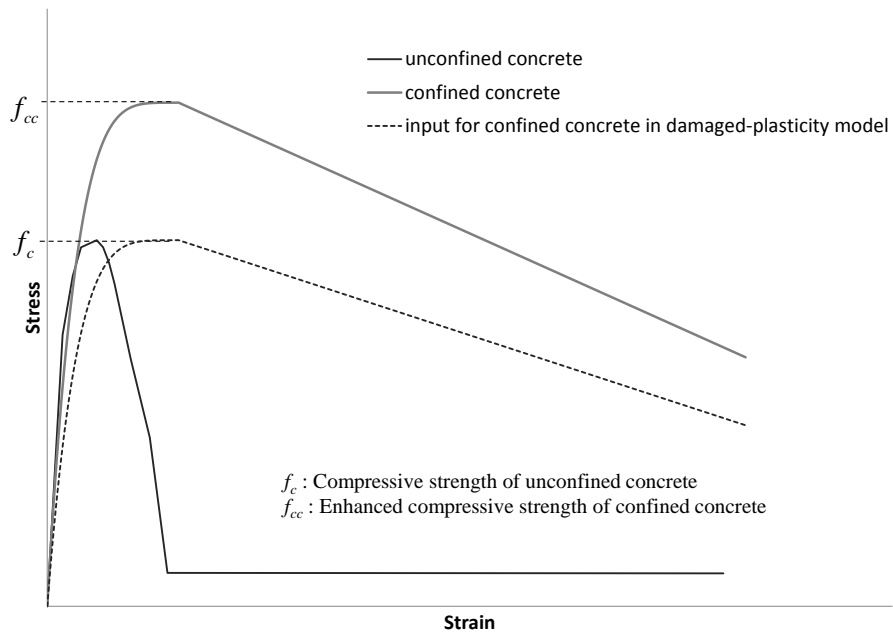


Figure 2.10 – Calibration of input uniaxial compressive stress-strain curve in damaged-plasticity model accounting for confinement effect

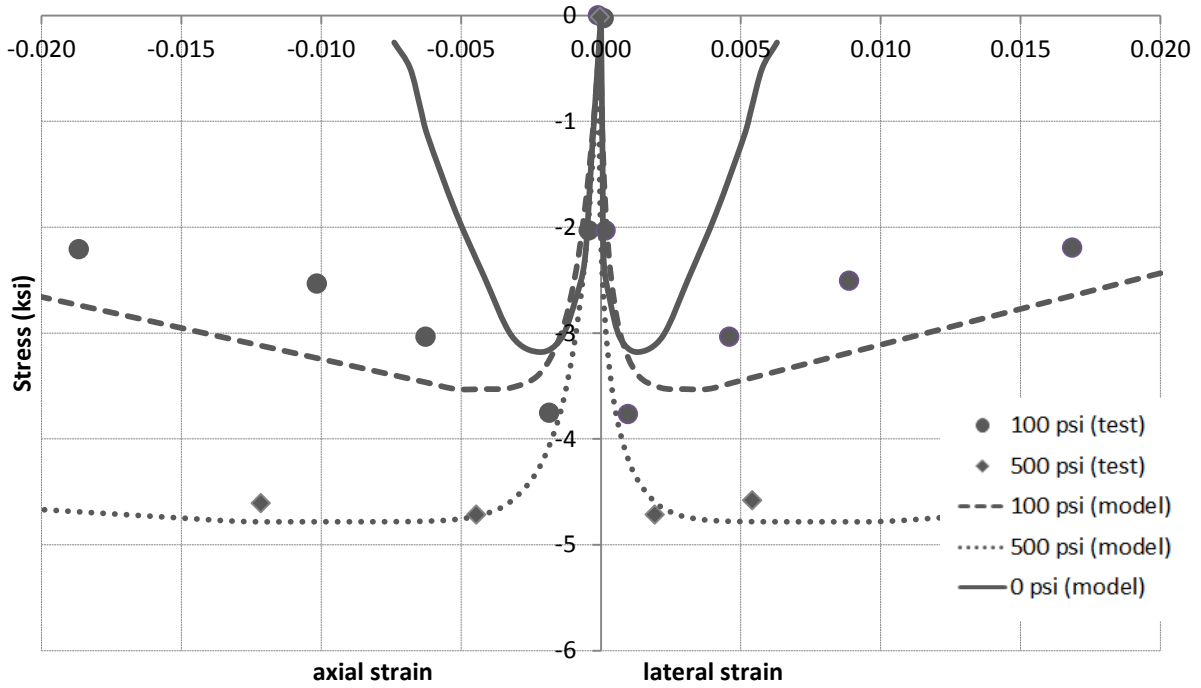


Figure 2.11 – Comparison of model with modified post-peak behavior to experimental results by Hurlbut (1985)

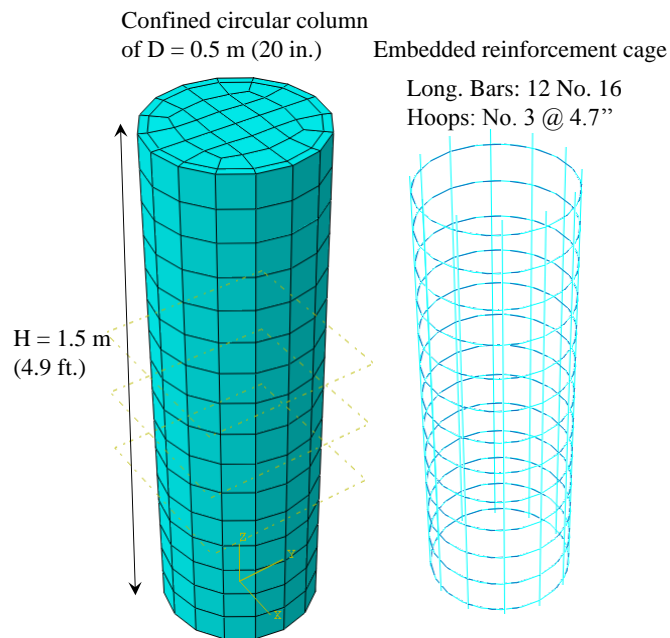


Figure 2.12 – FE model of compression tests on confined circular-sectioned RC columns by Mander et al. (1988b)

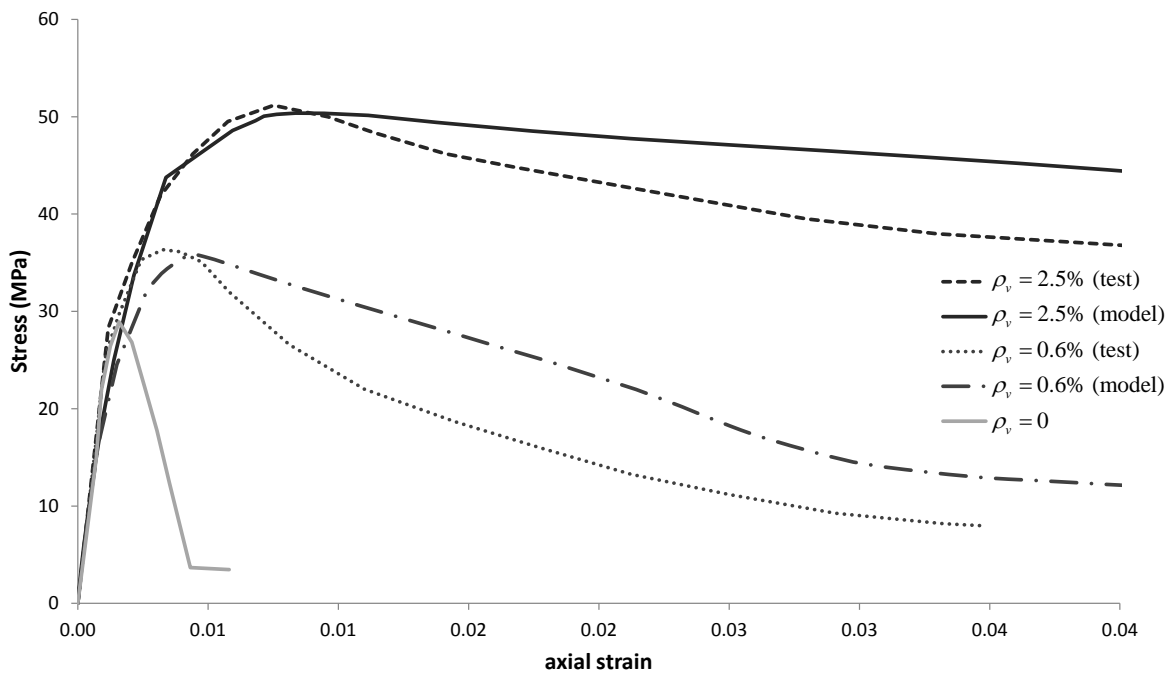


Figure 2.13 – Comparison of model with modified post-peak behavior to experimental results by Mander et al. (1988b)

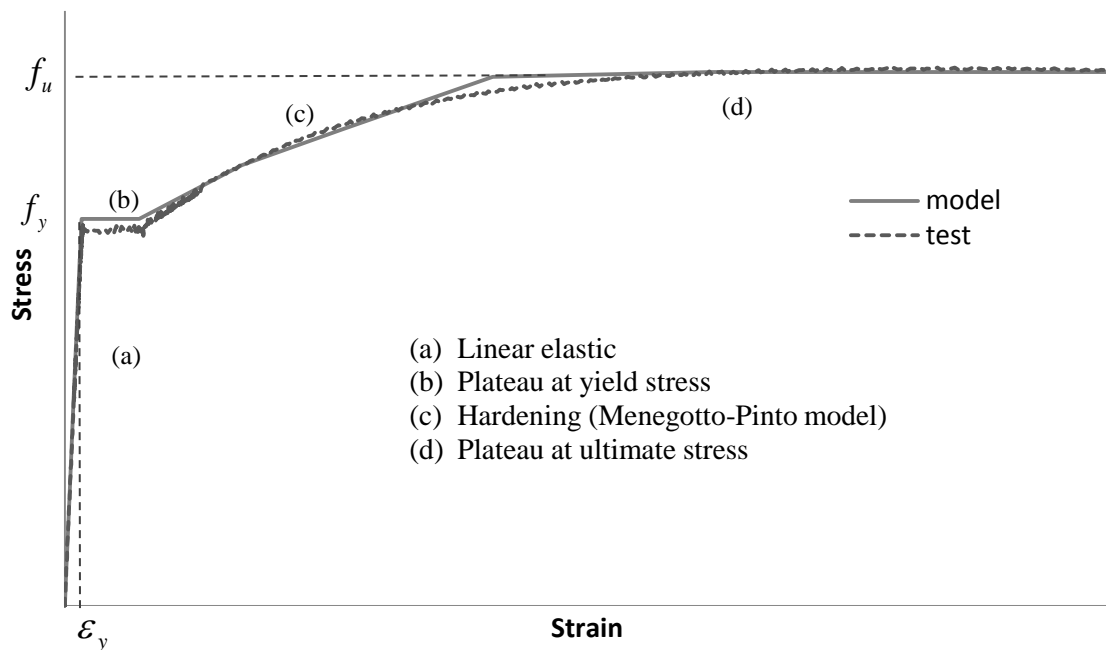


Figure 2.14 – Steel Model for monotonic loading



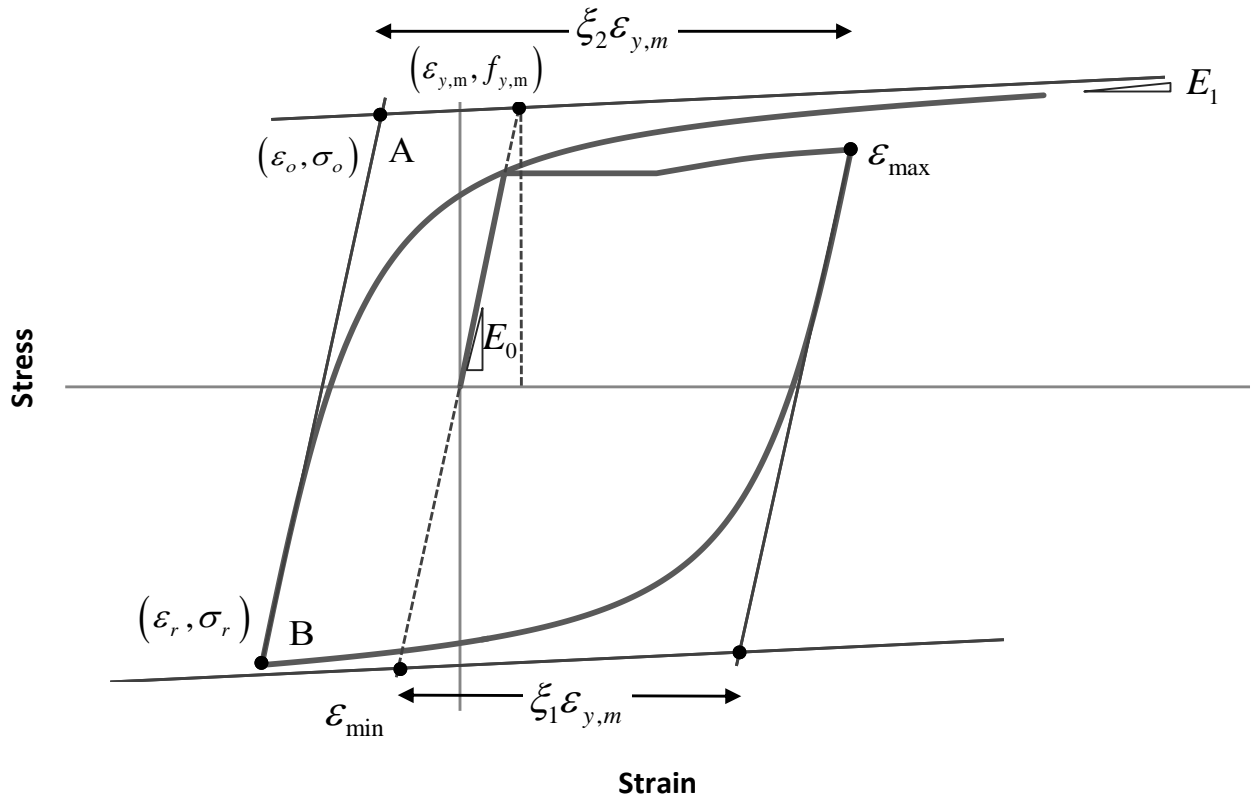


Figure 2.15 –Menegotto-Pinto model for cyclic stress-stain relation

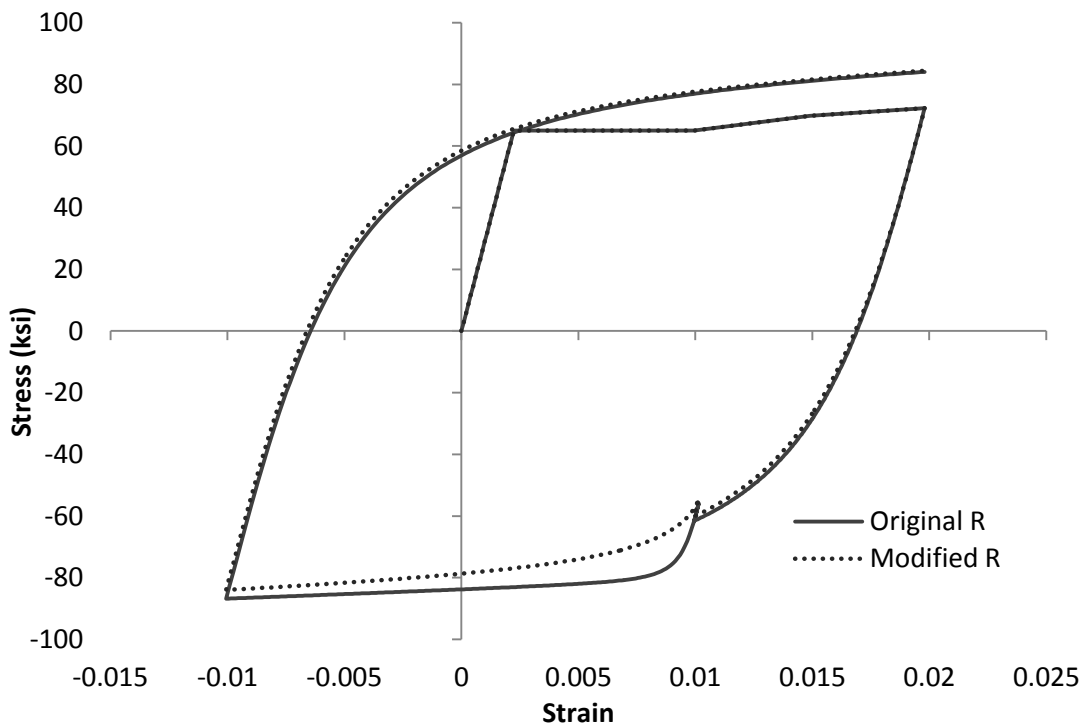
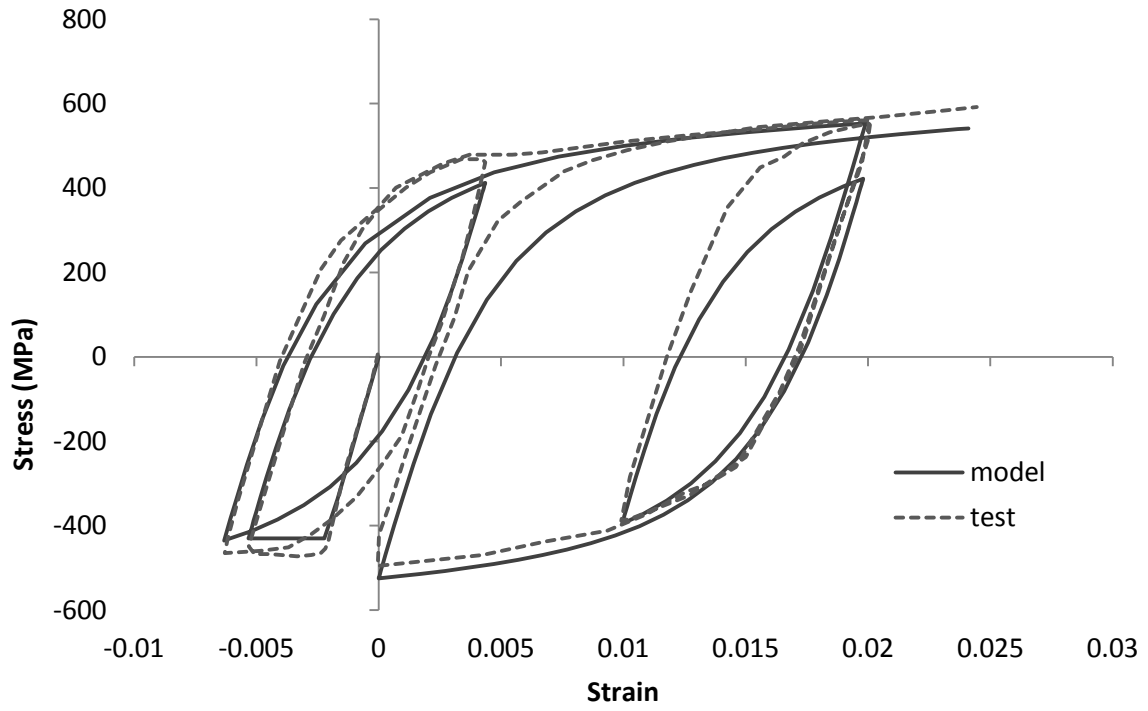
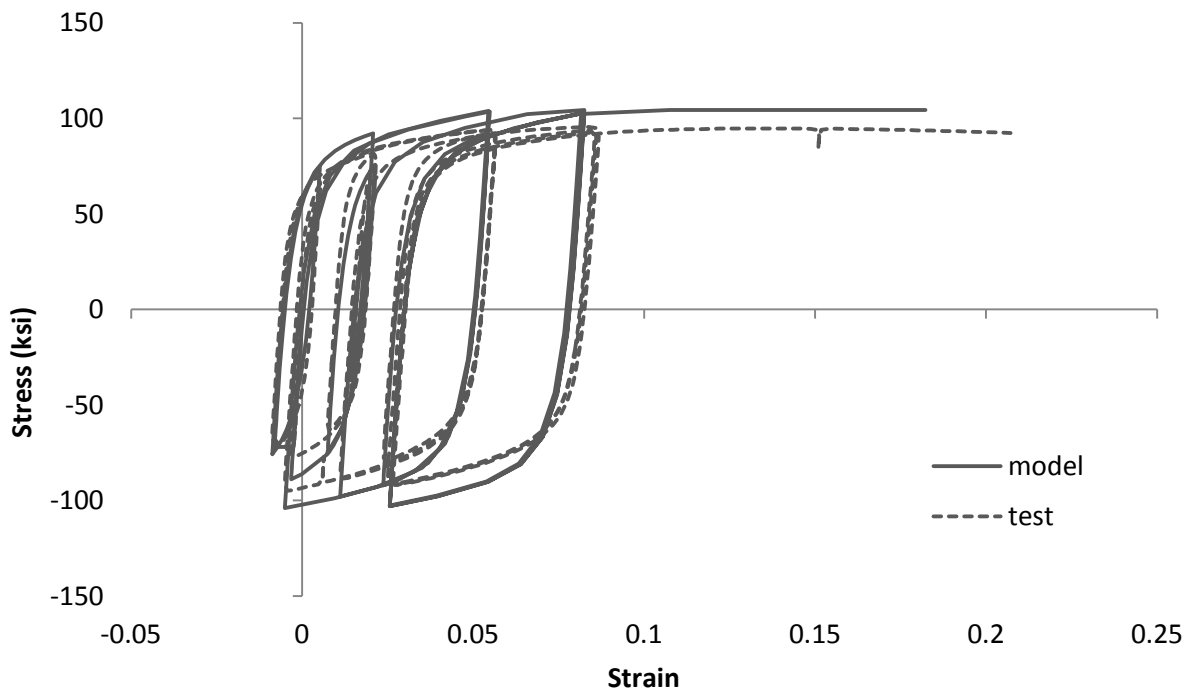


Figure 2.16– Hysteretic curves by Menegotto-Pinto model with partial unloading and reloading

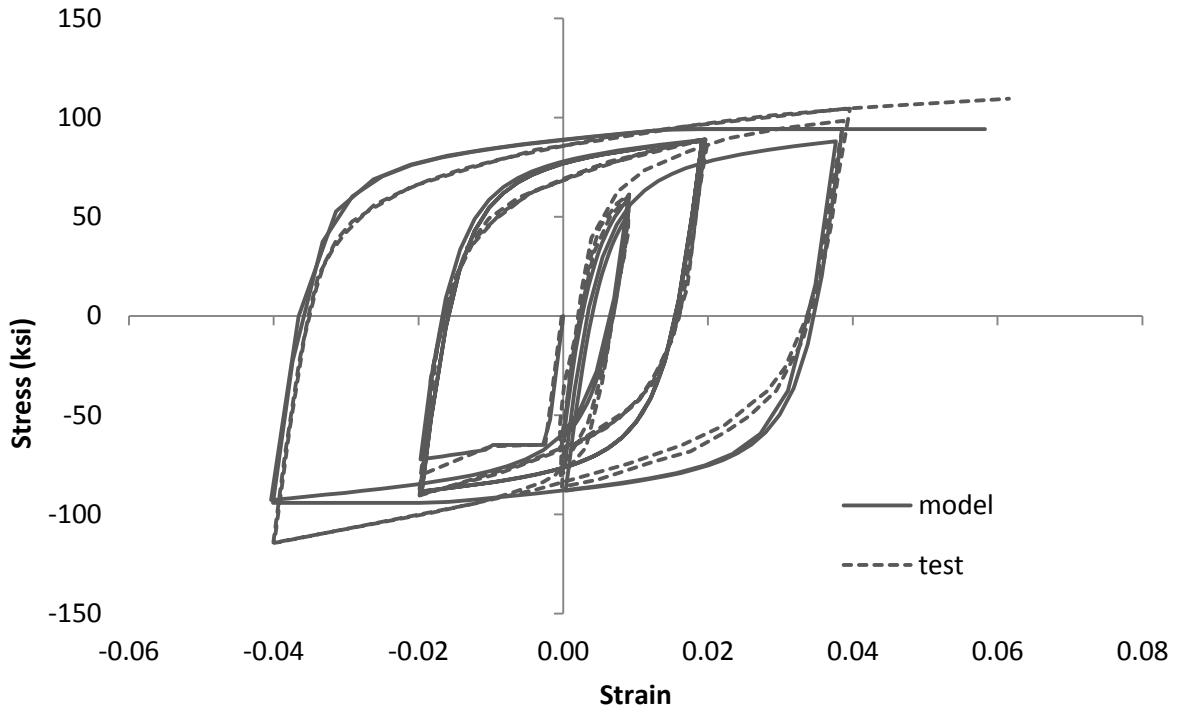


(a)

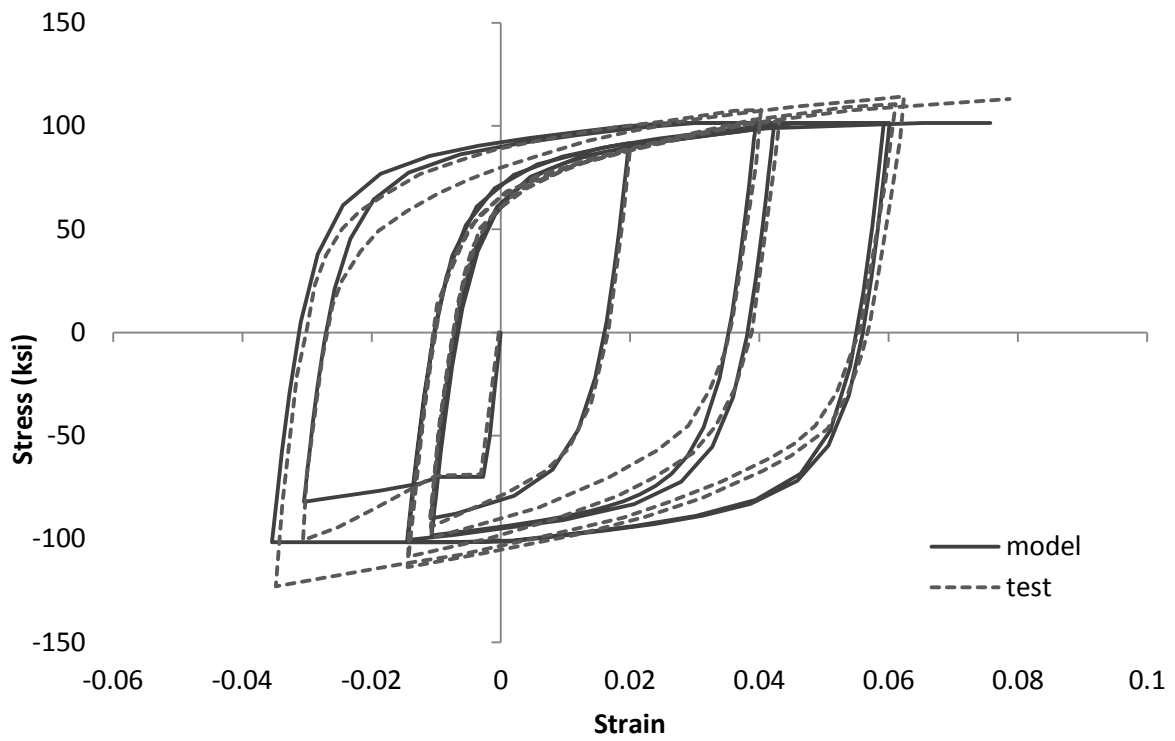


(b)

Figure 2.17 – Cyclic tests of steel reinforcing bars by Dodd and Restrepo (1995)



(a)



(b)

Figure 2.18 – Cyclic tests of steel reinforcing bars by Aktan et al. (1973)

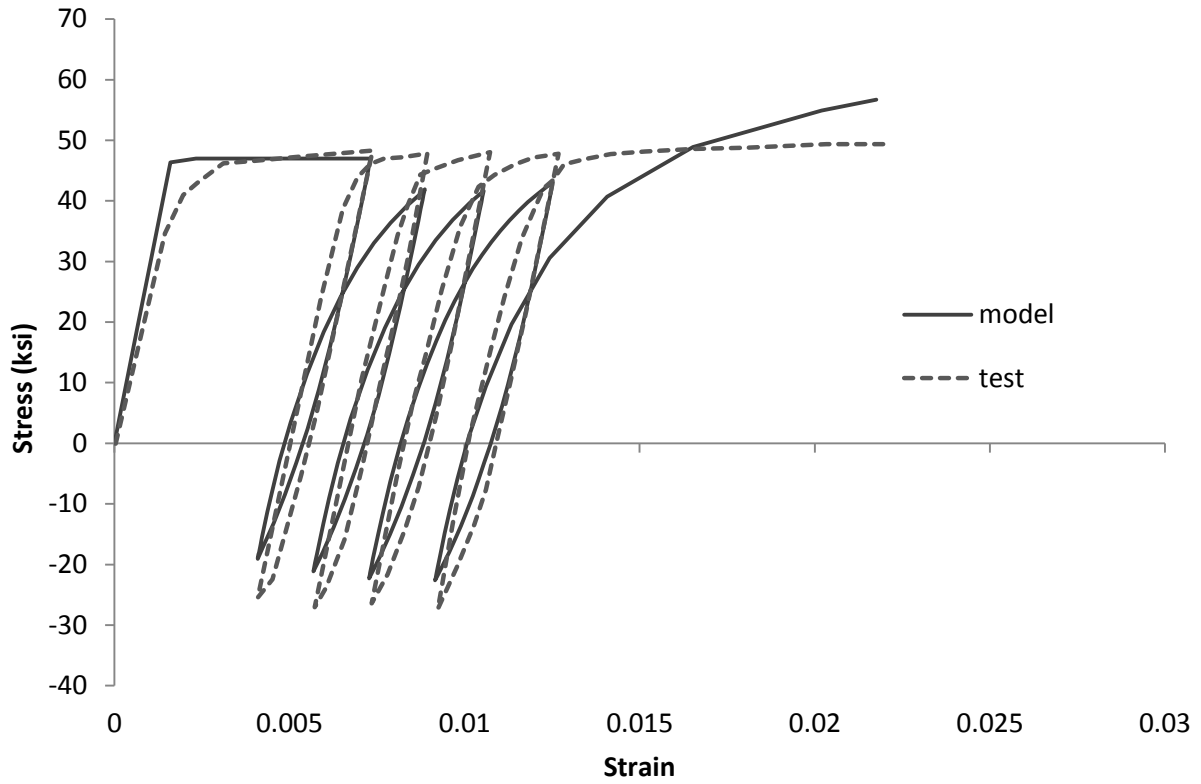


Figure 2.19 – Cyclic test of steel reinforcing bar by Kent and Park (1973)

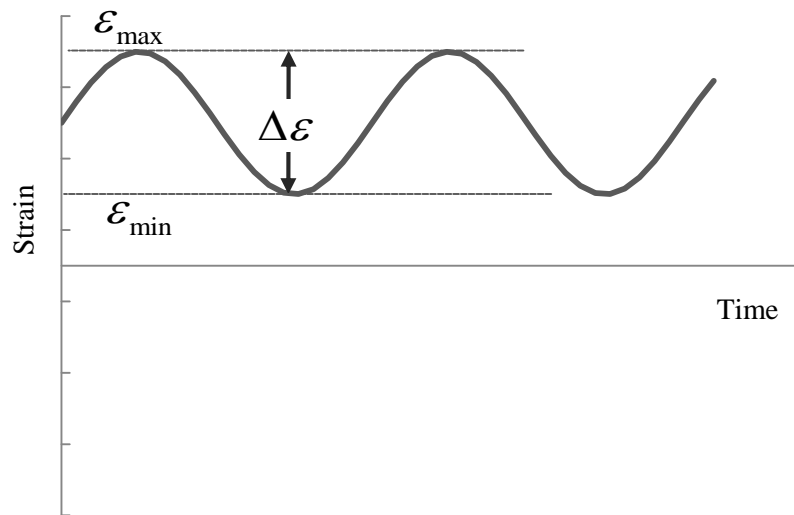


Figure 2.20 – Cycles with constant strain amplitudes

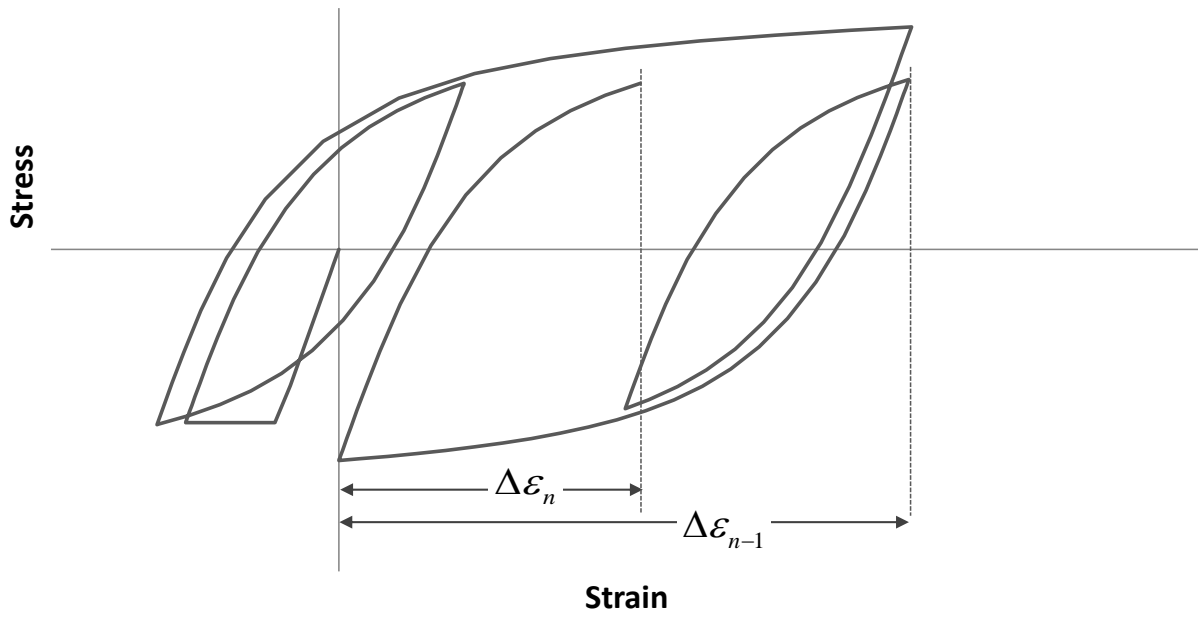


Figure 2.21 – Strain ranges,  $\Delta\epsilon$ , with random strain reversals

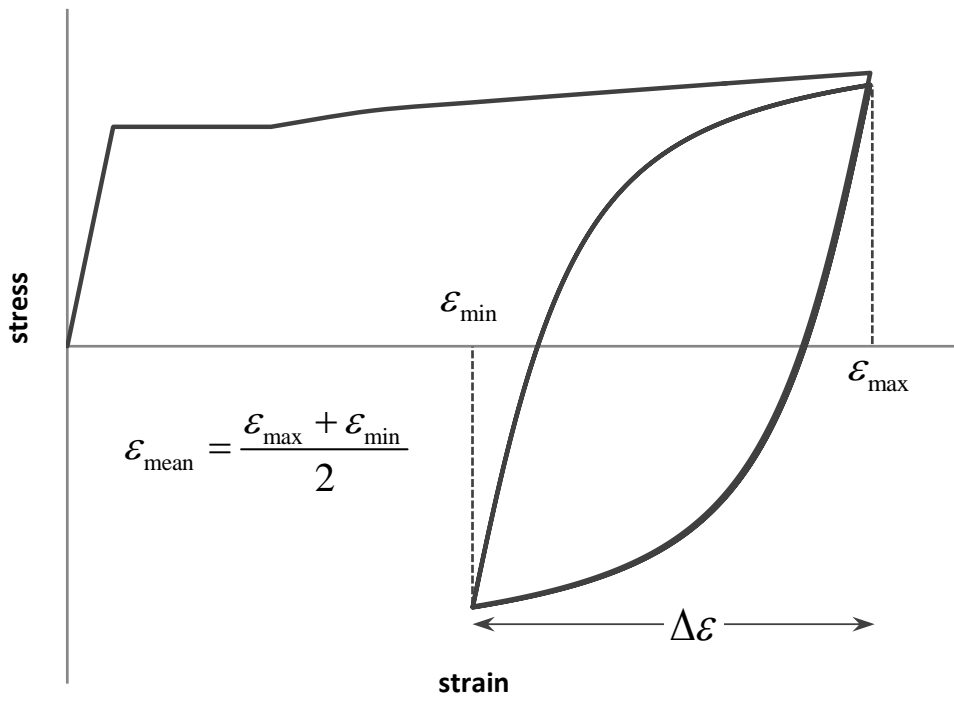


Figure 2.22 – Strain reversals with mean strain,  $\epsilon_{\text{mean}}$

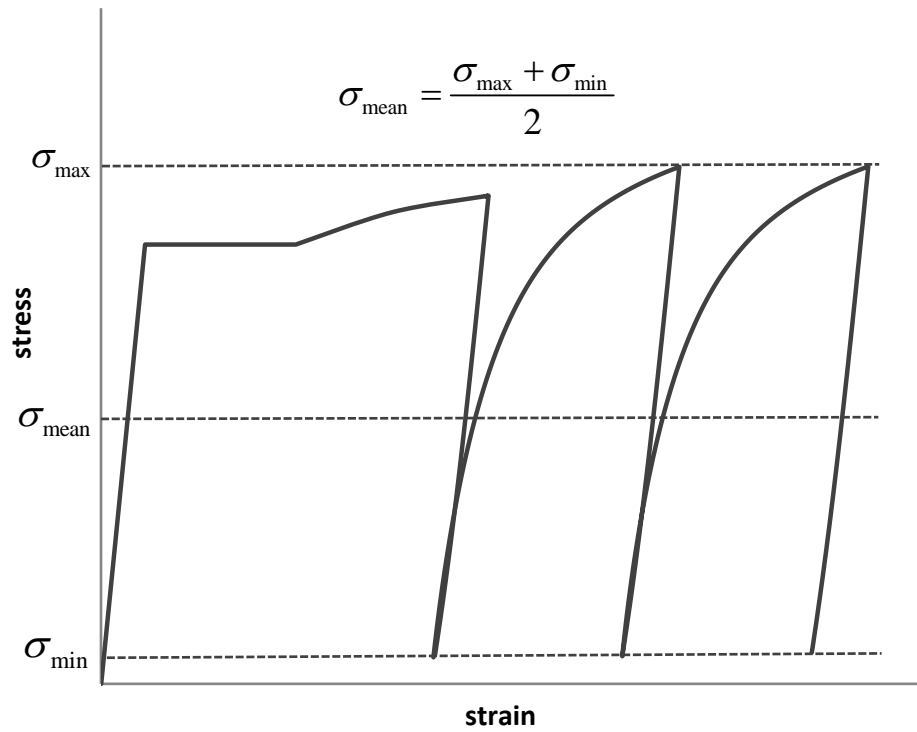


Figure 2.23 – Strain reversals with mean stress,  $\sigma_{\text{mean}}$

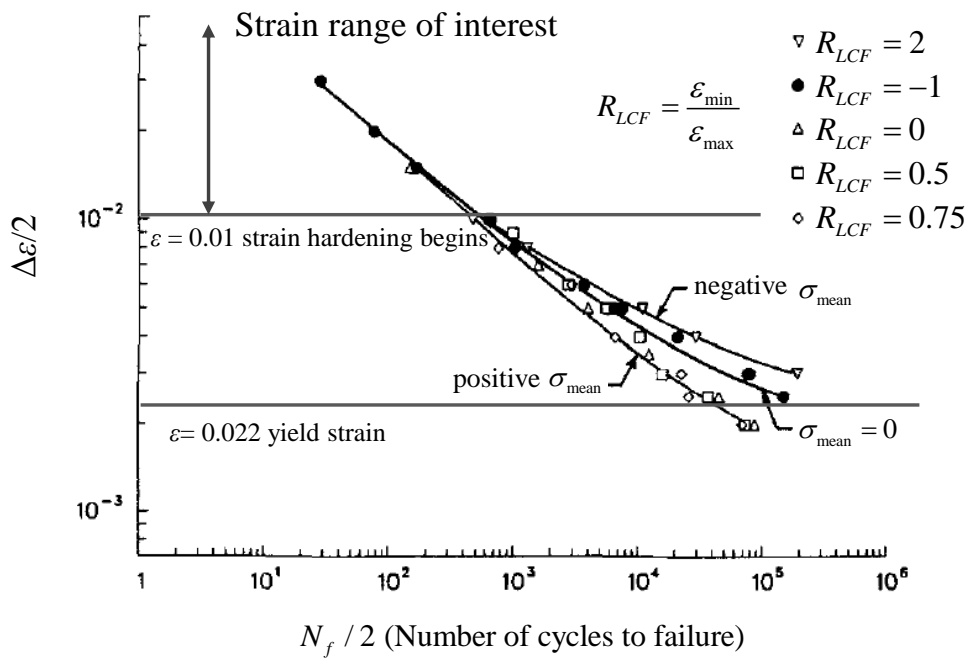
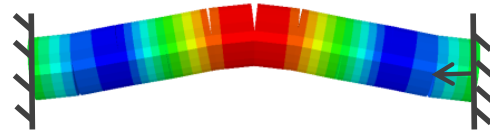


Figure 2.24 – Effect of mean strain and stress on LCF (Koh and Stephens, 1991)



(b) Test apparatus with a buckled bar



(a) FE model of a single bar

Figure 2.25 – LCF test by Kunnath et al. (2009b)

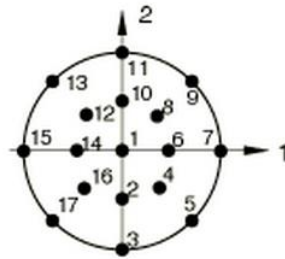
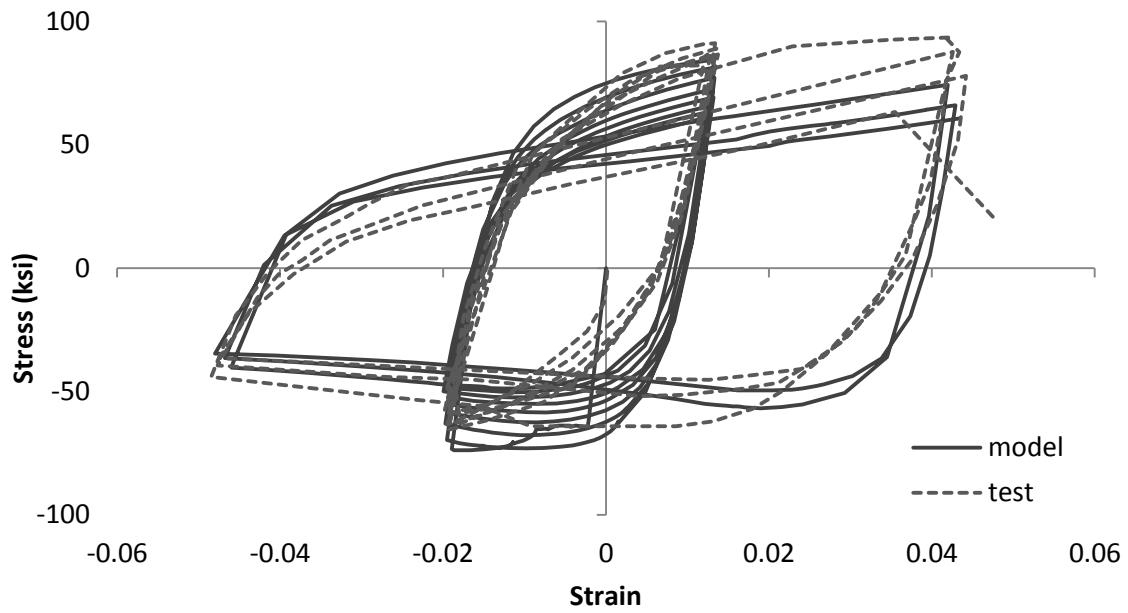
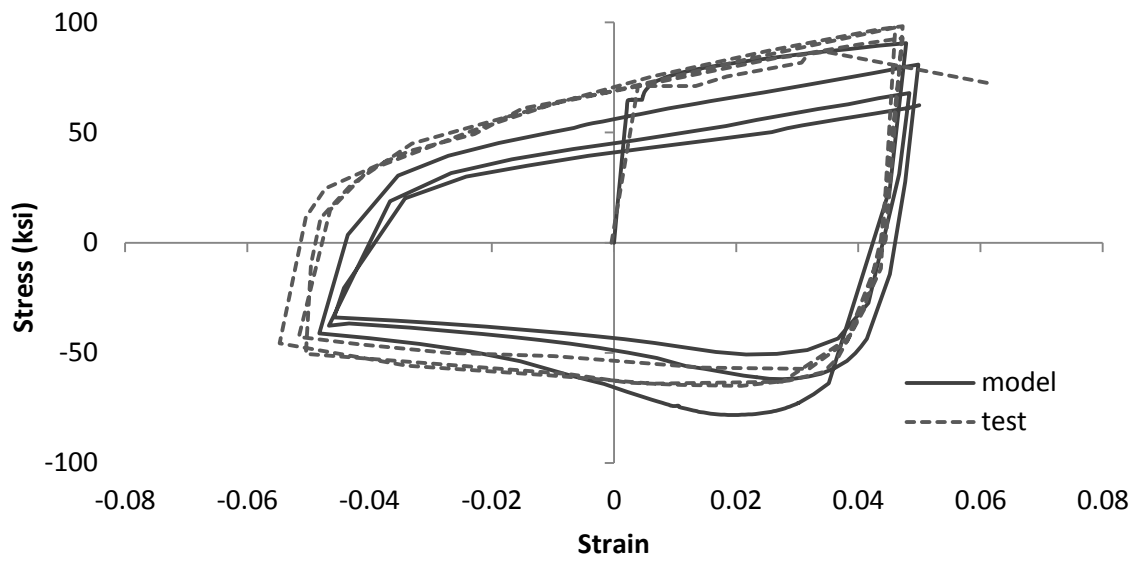


Figure 2.26 – Integration points in the circular section of a beam element in Abaqus



(a) Specimen N11Y4



(b) Specimen N11Y8

Figure 2.27 – Cyclic tests of No. 11 bar specimens by Kunnath et al. (2009b)



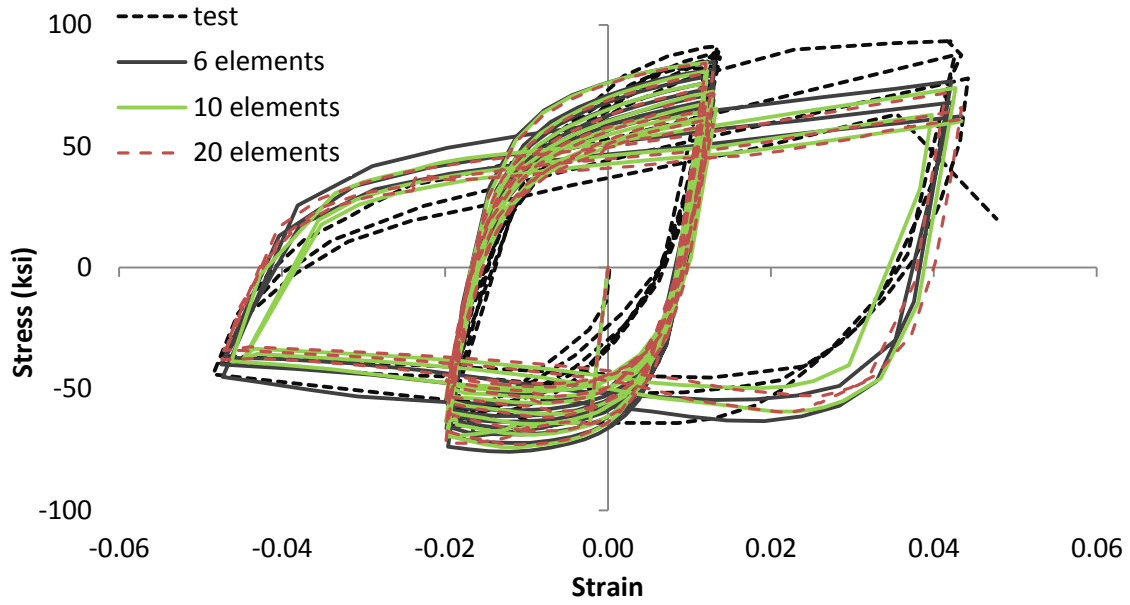


Figure 2.28 – Mesh-size sensitivity study with No. 11 bar (Specimen N11Y4) tested by Kunnath et al. (2009b)

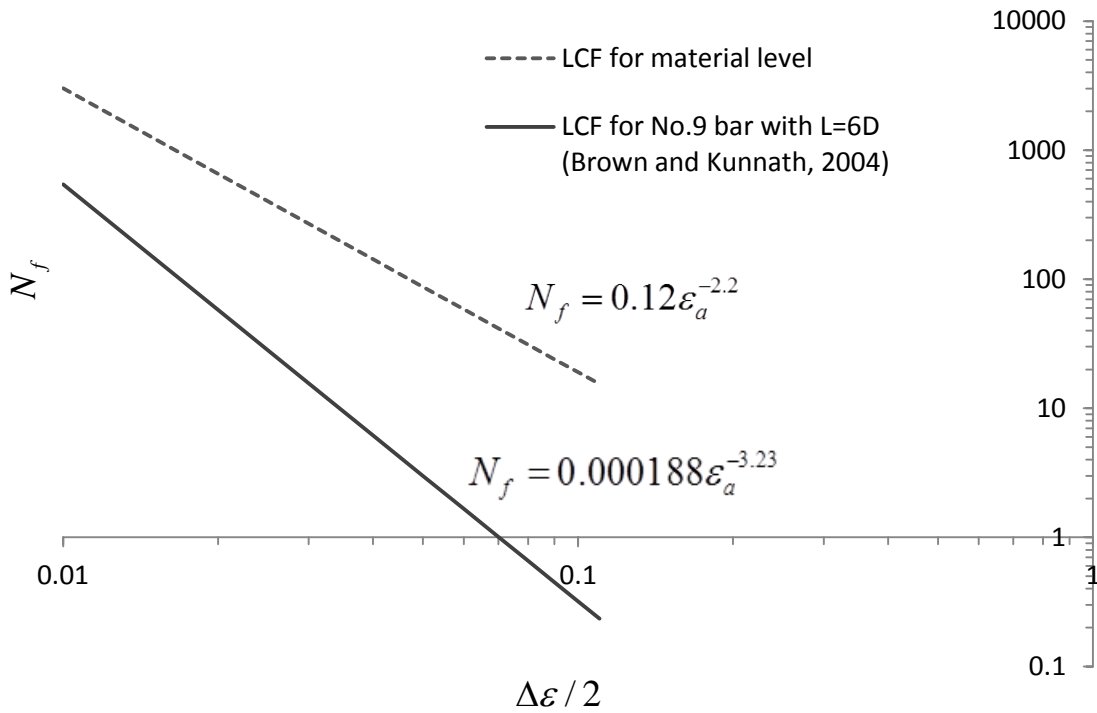


Figure 2.29 – Comparison of LCF laws for material level and bar level

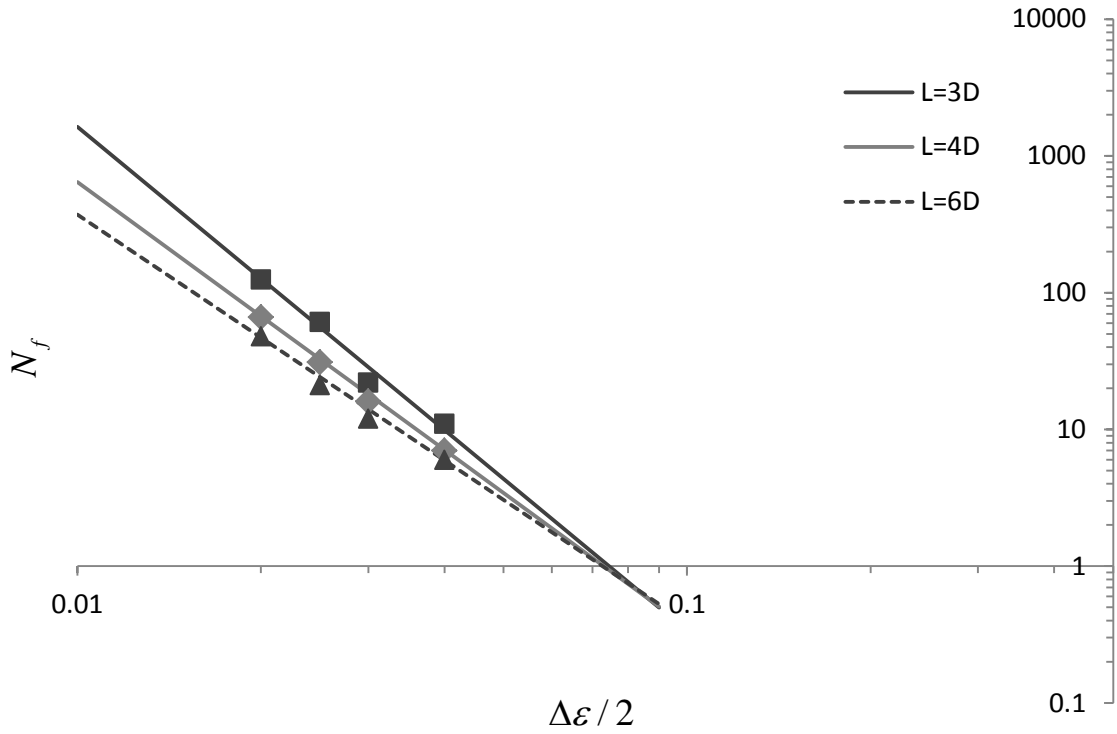


Figure 2.30 – LCF law for No. 9 bars with different slenderness

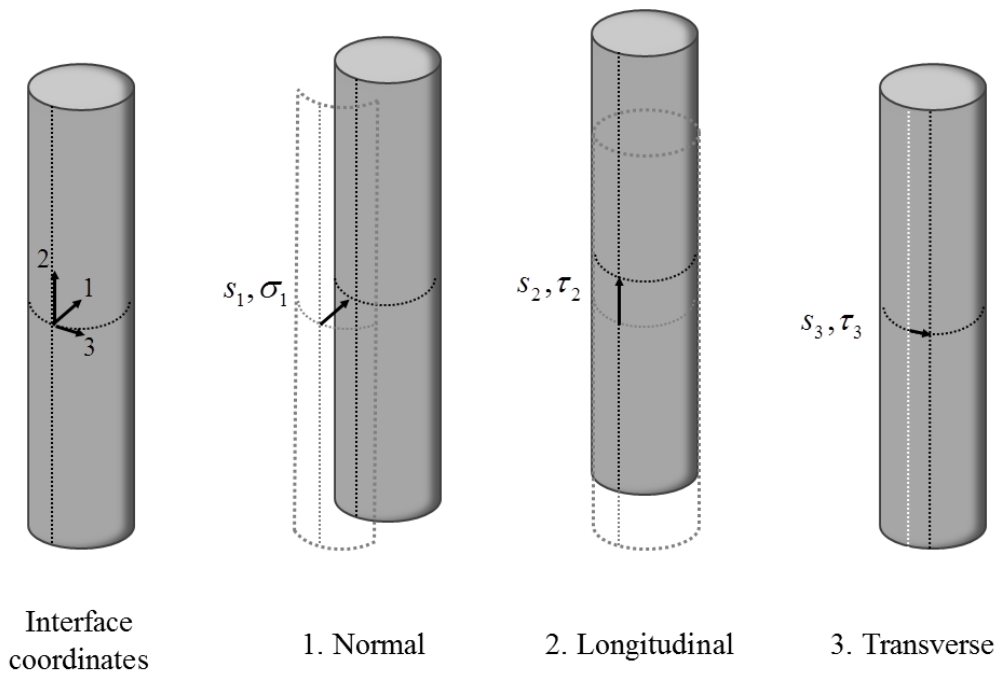
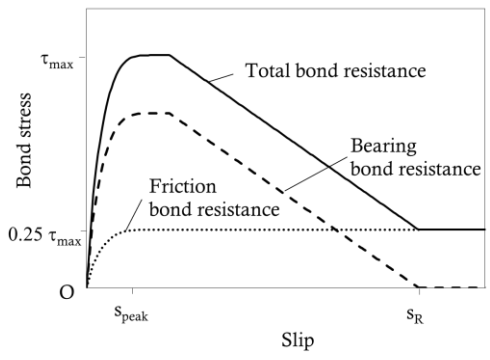
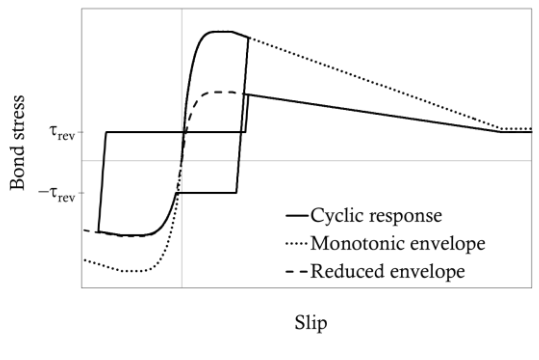


Figure 2.31 – Stresses and relative displacements at the bar-concrete interface

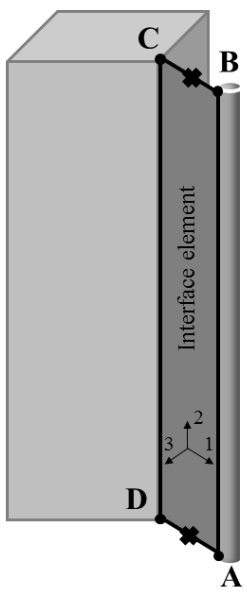
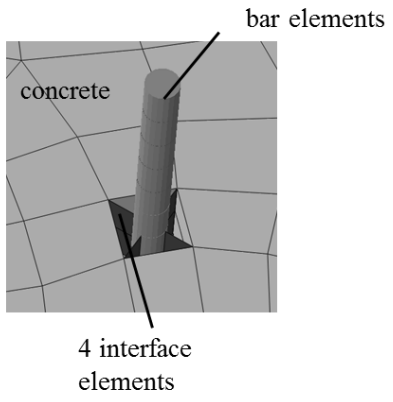


(a) monotonic response



(b) cyclic response

Figure 2.32 – Analytical bond stress-slip model by Murcia-Delso and Shing (2015)



**Relative interface displacements**

$$s_1 = u_{1,bar} - u_{1,concrete}$$

$$s_2 = u_{2,bar} - u_{2,concrete}$$

$$s_3 = u_{3,bar} - u_{3,concrete}$$

- node
- ✱ integration point

Figure 2.33 – Interface element by Murcia-Delso and Shing (2015)



## CHAPTER 3

### FINITE ELEMENT ANALYSES OF PILE SPECIMENS

Finite element analyses (FEA) have been conducted to simulate the structural behavior of the two pile specimens tested under cyclic lateral loading by Papadopoulos and Shing (2014). The finite element (FE) models were first used for the pre-test assessment of the performance of the pile specimens and to assist the development of the loading protocols for the tests. After being validated by the test results and further refined, the FE models have been used in a parametric study to examine the influence of the lineal and angular spacing of the longitudinal bars and the level of axial load on the structural performance of piles of different diameters.

#### 3.1 Finite Element model

Figure 3.1 shows the FE model of Specimen #1 (Papadopoulos and Shing, 2014). Specimen #2 was modeled in the same way. The only difference between Specimens #1 and #2 was in the longitudinal reinforcement. Specimen #1 consisted of 6 No. 11 bars, while Specimen #2 consisted of 10 No. 9 bars, resulting in almost the same longitudinal steel ratio but different bar spacing. Only half of the specimen is represented in the FE model by taking advantage of the symmetry of the specimen about the applied lateral load. Geometric nonlinearity is considered in the FEA.

The damaged-plasticity model presented in Section 2.1 is used to model the unconfined and confined concrete in the piles, while the footings and the pile caps are assumed to remain elastic. The calibration of the damaged-plasticity model has been discussed in Chapter 2. While the compressive properties of the concrete are specified in terms of the stress-strain relation, the tensile properties are defined in terms of the stress-displacement relation. The latter is to avoid the sensitivity of the tensile behavior of concrete to

the element size. For 3-D concrete models whose failure surfaces account for the effect of the hydrostatic stress, the compressive behavior of concrete will not be as sensitive to the element size, as will be demonstrated by the numerical study presented here. The properties of the concrete in the piles, based on the material test data for the two specimens, are summarized in Table 3.1. Parameter  $K_c$ , which controls the shape of the yield surface in the deviatoric plane as well as the slopes of the tensile and compressive meridians, is assigned the value of 1. This is appropriate for the maximum hydrostatic pressure expected for the concrete elements near the toe regions of the pile, and the resulting model can accurately simulate the spalling of the concrete cover.

Contact conditions are imposed at the interface between the pile and the footing. This is to improve the simulation of the opening and closing of large flexural cracks at the base, which cannot be well represented by the damaged-plasticity concrete model, as explained in Section 2.1.

The longitudinal bars are modeled with beam elements using the phenomenological steel law presented in Section 2.2. The material properties for the longitudinal reinforcement are summarized in Table 3.2. The calibration of the stress-strain relation has been discussed in Section 2.2.1. For the calibration of the low cycle fatigue (LCF) parameters, the procedure described in Section 2.2.3 has been followed. For Specimen #1, the LCF law has been calibrated for No. 11 bars with an unsupported length  $s=5.75$  in., while for Specimen #2, the LCF law has been calibrated for No. 9 bars with an unsupported length  $s=5.75$  in. The slip of the longitudinal bars in concrete is also considered by using the phenomenological bond-slip model of Murcia-Delso and Shing (2015), which has been calibrated with the procedure discussed in Section 2.3. Perfect bond is considered for the transverse reinforcement, which is modeled with truss elements, assigned an elasto-plastic law for steel, with a yield stress of 65 ksi and an ultimate stress of 95 ksi.

To investigate whether the height of the elements along the length of the pile will affect the numerical results, an element-size sensitivity analysis has been conducted. Figure 3.2 shows the lateral load-vs.-drift

ratio curves from the FEA of Specimen #1 with different element heights. As shown in the figure, the numerical results are not sensitive to the element size. For the analysis of the pile specimens, an element height of 2 in. has been selected.

## **3.2 Validation of Finite Element Models with Experimental Results**

### **3.2.1 Load – vs. – Displacement Response**

The FE models are subjected to the same vertical and lateral displacement demands as the tested pile specimens. The lateral load-vs.- drift ratio curves obtained for Specimens #1 and #2 by the tests and the FEA are shown in Figure 3.3 and Figure 3.4, respectively. The curves from the FEA provide a good match with the test results. The lateral load capacities obtained from the tests and the FEA are compared in Table 3.3. The FEA underestimate the lateral load capacity by 2% (south direction for Specimen #2) to 11% (north direction for Specimens #1 and #2). The load capacities obtained in the FEA are in general smaller with the crushing of the cover concrete occurring one cycle earlier than that observed in the tests. The gradual drop of the lateral load resistance caused by the  $P-\Delta$  effect of the vertical load and the crushing of concrete at the toes of the piles is well reproduced in the FEA.

The unloading and reloading curves are well reproduced. The pinching due to the closing of flexural cracks is accurately simulated in the FEA because of the contact conditions introduced at the pile-footing interface.

The large drop of the lateral load resistance due to the fracture of longitudinal bars during the last cycles of the tests is simulated by the low-cycle fatigue (LCF) law used in the FE model. The predictions for bar fracture in the FEA are close to the experimental results for both specimens. Bar fracture due to LCF occurs in bar elements very close to the footing-pile interface. Table 3.4 and Table 3.5 show the cycle numbers in which longitudinal bars in Specimens #1 and #2 fractured in the tests and in the FEA. The

numbering of the longitudinal bars in the pile specimens is shown in Figure 3.5. Since only half of the pile is modeled in the FEA, it is assumed that the longitudinal bars on the west side and the east side exhibit the same behavior. When the fracture of the steel occurs, the stress-strain law assumes a gradual drop of stress to enhance the robustness of the numerical solution. Thus, the very steep load drops exhibited by the lateral load-vs.-drift ratio curves from the tests due to bar fracture are not observed in the numerical results.

The FEA verify that the spacing of the longitudinal bars does not have a significant effect on the structural performance of the RC pile specimens. Up to 8% drift, the two specimens exhibit the same lateral load-vs.-drift ratio response. However, the ductility can be affected by the diameter of the longitudinal bars. Larger-diameter bars are more resistant to buckling for the same spacing of the transverse reinforcement. This will delay bar fracture and lead to a more ductile behavior.

### **3.2.2 Flexural Crack Spacing**

In the experimental study (Papadopoulos and Shing, 2014), it was observed that the spacing of longitudinal bars had an influence on the spacing of the flexural cracks in the pile specimens. While the amounts of longitudinal reinforcement in the two specimens were almost the same, the longitudinal bars in Specimen #1 had a larger spacing. Figure 3.6 and Figure 3.7 show that flexural cracks were more widely spaced in Specimen #1 than in Specimen #2. Most of the flexural cracks in Specimen #1 had a spacing between 10 and 12 in. Some had a spacing as small as 6 in. or as large as 18 in. Most of the flexural cracks in Specimen #2 had a spacing between 6 and 12 in., with some at less than 6 in. Moreover, the width of the flexural cracks in Specimen #1 was larger than that in Specimen #2, as observed in later cycles during the tests.

The damaged-plasticity concrete model, used in the FEA, does not represent cracks in a discrete fashion. Rather cracks are represented in a distributed fashion by plastic tensile strains. The normal plastic strains



developed in concrete in the axial direction of the pile in the FEA of the two pile specimens at a drift ratio of 1% are presented in Figure 3.8. In this figure, flexural cracks can be identified as localized plastic tensile strains. As shown in Figure 3.8(a), the spacing of the flexural cracks in Specimen #1 from the FEA is 6 to 8 in. with the maximum normal plastic strain  $\varepsilon_p = 0.0039$ . As shown in Figure 3.8(b), the flexural cracks in Specimen #2 are more closely spaced at about 6 in. with  $\varepsilon_p = 0.0036$ . The concrete elements close to the base of the pile specimens do not develop plastic tensile strains. This is because the opening of the pile-footing contact interface and the slip of the longitudinal bars in tension reduce the tensile stresses in the concrete elements in the vicinity.

Figure 3.8 also shows the extent of flexural cracking in Specimens #1 and #2 from the FEA. For Specimen #1, flexural cracks occur over a height of 5.6 ft. from the base of the pile, while those for Specimen #2 over a height of 5.9 ft. In the tests, flexural cracks in Specimen #1 extended over a height of 5.1 ft. from the base at the south face and 6 ft. at the north face, as shown in Figure 3.6, while those in Specimen #2 extended over a height of 5.5 ft. at the south face and 6 ft. at the north face, as shown in Figure 3.7. The larger extent of flexural cracking in Specimen #2 can be explained by its slightly higher moment capacity, as compared to Specimen 1, as illustrated in Figure 3.9.

### **3.2.3 Strains in Longitudinal Bars**

Figure 3.11 through Figure 3.16 compare the strains in the longitudinal bars of Specimen #1 from the tests and the FEA at drift ratios of 1, 4 and 8%. Overall, the numerical results match the test data reasonably well. For Specimen #1, the tensile strains in Bars 1 and 4 are significantly overestimated at the base of the pile by the FE model at drift ratios of 1 and 4%. It should be noted that the tensile strains in the bars are highly influenced by the integrity of the bond and the surrounding concrete. It is likely that the damage of the concrete and the bond at the base of the pile at these drift levels can be slightly underestimated by the FE model. At larger drift ratios, many strain gages were damaged, resulting in no strain

measurements. Attributed to the bond-slip model, the plastic strain penetration of the longitudinal bars in footing is well captured by the FE model.

Figure 3.17 through Figure 3.22 compare the strains in the longitudinal bars of Specimen #2 from the tests and the FEA at drift ratios of 1, 4 and 8%. The same observations as above have been obtained. In general, it can be observed that Specimen #2 has more severe bar strains developed at the base of the pile than Specimen #1. This can be attributed to the fact that the longitudinal bars in Specimen #2 had a smaller diameter and therefore less bond stress demand and less slip in the vicinity of the flexural crack at the base.

### **3.2.4 Plastic Deformation in the Piles**

The experimental study showed that Specimen #1, which had larger-diameter longitudinal bars and larger bar spacing, had more plastic deformation concentrated near the base as compared to Specimen #2. The FE models provide the same observation, as shown in Figure 3.10, which compares the strain distributions along the longitudinal bars placed at the south face of Specimens #1 and #2 at a drift ratio of 4% from the tests and the FEA. This difference can be explained by the fact that the longitudinal bars in Specimen #2 had a smaller diameter and therefore less bond stress demand and less slip in the vicinity of a flexural crack. This will lead to higher tensile strains in the bars.

### **3.2.5 Stresses in Concrete**

Figure 3.23 show the normal stress-vs.-normal strain curves of concrete elements at the cover and the core of the pile section. In the FEA, the maximum compressive stress in the cover concrete is 5.1 ksi, being very close to the prescribed value of 4.9 ksi for unconfined concrete from material test data. The stress developed in the concrete core element is higher, due to the confining effect of the lateral reinforcement. Moreover, the cover concrete shows a more brittle behavior, compared to the core concrete, as shown in Figure 3.23.

### **3.2.6 Stresses in the Longitudinal Bars**

Figure 3.24 shows the axial stress – strain response in the elements of longitudinal bars #1 and #4 at the base of the pile of Specimen #1. As shown, fracture due to LCF is described with a gentle descending curve in the stress-strain relation till it reaches a residual stress of 10 ksi. As mentioned in Section 3.2.1, the FE models adequately predict the cycles at which the longitudinal bars fractured in the tests.

### **3.3 Parametric Study with Finite Element Models**

By using the FE modeling method validated in the previous section, a numerical parametric study has been conducted to further evaluate the influence of the spacing of longitudinal bars on the structural performance and crack spacing of circular RC piles, and for piles with larger diameters and higher axial load levels. Table 3.6 summarizes the properties of the piles considered in the parametric study. Models D28S1 and D28S2 in the table have the same properties as the two specimens tested by Papadopoulos and Shing (2014). As shown in Table 3.7, these two models are also subjected to higher axial loads in the parametric study. All the pile models considered have the same volumetric ratio of transverse reinforcement, and more or less the same ratio of the cross-sectional area of the longitudinal reinforcement to the cross-sectional area of the pile.

#### **3.3.1 Impact of Lineal Spacing of Bars on Ductility**

The lateral load-vs.-drift ratio curves for Models D28S1 through D28S4 are presented in Figure 3.25. All four specimens have similar lateral load capacities since they are designed with similar longitudinal reinforcement ratios. The spacing of longitudinal bars does not have an effect on the ductility of the piles.

However, similarly to what was observed in the experimental study, the size of the longitudinal bars has a small influence on pile ductility, as it can be seen in Figure 3.25. The fracture of larger-diameter longitudinal bars occurs slightly later because they are more resistant to buckling for the same spacing of

transverse reinforcement. Figure 3.26 shows the cycle numbers at which the longitudinal bars in the piles with diameter equal to 28 in. fractured.

### **3.3.2 Impact of Lineal Spacing of Bars on Flexural Crack Spacing**

Flexural cracks are simulated in the form of plastic tensile strains in the FEA. Figure 3.27 shows the normal plastic strains in concrete in the axial direction of the pile at 1% drift for piles D28S1 through D28S4. It can be observed, as in the experimental study, that flexural cracks are more closely spaced and have smaller widths as the spacing of the longitudinal bars decreases.

### **3.3.3 Piles with Larger Diameters**

Piles D56S1, D56S2, and D56S3 have a diameter of 56 in., a height of 20 ft. and the same angular spacings of longitudinal bars as piles D28S1, D28S2 and D28S3, respectively, as shown in Table 3.6. However, the lineal spacing of the longitudinal bars in these piles is more than doubled, with the concrete cover in the two set of piles remaining the same. The length of the elements along the height of the piles is twice as large as that for the piles with a diameter of 28 in. so that the total number of element layers remains the same. As mentioned in Section 3.1, load-vs.-drift ratio curves from FE models are not sensitive to the size of the elements.

The lateral load-vs.-drift ratio curves for piles D56S1 through D56S3 are shown in Figure 3.28. It can be observed that the lineal spacing of longitudinal bars does not have an impact on the ductility of the piles of larger diameter. Figure 3.29 shows the normalized lateral load-vs.-drift ratio curves for piles D28S2 and D56S2, which have the same angular spacing, but different lineal spacings because of the larger diameter of the latter. For these curves, the loads are normalized by the respective peak load reached in each test. As it can be seen, there is no major difference in the hysteresis curves except that D28S2 shows a more rapid load degradation in later cycles because it has smaller diameter longitudinal bars, which are

more vulnerable to buckling and fracture caused by LCF. Figure 3.30 shows the cycle numbers at which the longitudinal bars in piles D56S1 through D56S3 fractured.

As shown in Figure 3.31, the lineal spacing of the longitudinal bars has a small impact on the width and spacing of flexural cracks, similar to that observed for the smaller diameter piles. A larger bar spacing leads to a wider spacing of flexural cracks and wider crack widths.

Figure 3.32 compares the normal plastic strains in the axial direction of piles D28S2 and D56S2. The diameter of pile D56S2 is twice as that of D28S2, but both piles have a concrete cover of 2 in. Since the longitudinal bars in both piles have the same angular spacing, those in D56S2 have a larger lineal spacing. It can be seen that the flexural cracks in pile D56S2 are more widely spaced than those in pile D28S2. The maximum plastic tensile strain in D56S2 is slightly smaller than that in D28S2. This means that the flexural cracks in D56S2 are wider than those in D28S2 because the element height for the former is twice as large. This conclusion is supported by the results of an element-size sensitivity study conducted on D56S1. Figure 3.33 compares the plastic strains obtained for this pile with element heights of 4 in. and 2 in., respectively. It can be seen that the maximum plastic tensile strain obtained with an element height of 4 in. is slightly less than half of that with a height of 2 in. This confirms the fact that the width of a flexural crack is represented by the plastic elongation of the element, which is proportional to the plastic strain and the element size.

### **3.3.4 Piles Subjected to Higher Axial Loads**

Figure 3.34 and Figure 3.35 show the lateral load-vs.-drift ratio curves for piles D28S1 and D28S2 when they are subjected to higher axial loads that are 15% and 20% of the compressive strength ( $A_c f_c$ ) of the piles, respectively. As the plots show, increasing the axial load increases the lateral load capacity, but it leads to a steeper negative slope in the load-displacement curves because of the  $P-\Delta$  effect of the axial

load. Even for these cases, the lineal spacing of the longitudinal bars has no impact on the ductility of the piles.

### **3.3.5 Impact of Inspection Tubes on Nonlinear Behavior of Piles**

The piles considered in the experimental and numerical studies presented so far did not have voids. However, in actual piles placed in wet drilled holes, PVC inspection tubes are placed around the pile reinforcement cage for gamma-gamma tests. To investigate the impact of the voids introduced by inspection tubes on the structural performance of the piles, Specimen D28S1, which has 6 No. 11 vertical bars, has been re-analyzed with a finite element model incorporating voids. This is referred to as Specimen D28S1-B. As shown in Figure 3.36, the cross-section of this pile has rectangular-shaped voids near the north and south faces, representing 2-in.-diameter inspection tubes placed with a clear spacing of 4 in. from the vertical bars.

The lateral load-vs.-drift ratio curves for Specimens D28S1 and D28S1-B are almost identical, as shown in Figure 3.37. The voids in D28S1-B do not have significant impact on the nonlinear behavior of the piles.

## **3.4 Conclusions**

The FE models developed for the circular RC pile shafts can adequately reproduce the tests conducted by Papadopoulos and Shing (2014). It has been used to further investigate the effect of the lineal spacing of longitudinal bars on the structural performance of the piles.

Both the numerical and experimental observations indicate that the lineal spacing of longitudinal bars does not have any effect on the ductility of the circular piles and the lateral load-vs.-drift ratio response. However, the ductility of a pile can be affected by the size of the longitudinal bars. Larger-diameter bars are more resistant to buckling for the same spacing of the transverse reinforcement, and can therefore lead

to a more ductile behavior of a laterally loaded RC member. A numerical parametric study has confirmed that these observations are valid for pile with larger diameters and subjected to higher axial loads.

The numerical study has also confirmed the fact that the lineal spacing and the size of the longitudinal bars have a small influence on the spacing and the width of flexural cracks. A closer bar spacing with a larger number of smaller-size longitudinal bars leads to smaller crack widths and more closely spaced flexural cracks.

It has been verified by FEA that voids introduced by inspection tubes do not have significant impact on the nonlinear behavior of the piles. Finally, as observed both in the tests and the FEA, a pile with larger-diameter longitudinal bars and larger bar spacing has more concentrated plastic deformation near the base. Bars of smaller diameter have a lower bond stress demand and therefore less bond slip. This leads to higher tensile strains in the bars in the vicinity of flexural cracks.

Table 3.1 – Damaged-plasticity model calibration for concrete in the pile

Parameter	Description	Specimen #1	Specimen #2
$f'_c$ (ksi)	Compressive strength	4.9	5.2
$f'_t$ (ksi)	Tensile strength	$f'_t = 8\sqrt{f'_c}$	
$\sigma_{b0}/\sigma_{c0}$	Controls biaxial compressive strength	0.12	
$\psi$	Dilation angle	20°	
$\varepsilon$	eccentricity	0	
$K_c$	Controls shape of yield surface	1	
$w_c$	Compression recovery factor	0	
$w_t$	Tension recovery factor	1	

Table 3.2 – Steel material parameters for longitudinal reinforcement

Parameter	Description	Specimen #1	Specimen #2
$f_y'$ (ksi)	Yield stress	64	67
$E$ (ksi)	Elastic Stiffness	29000	
$\varepsilon_f'$	1 <sup>st</sup> LCF coefficient	0.0966	0.0936
$c$	2 <sup>nd</sup> LCF coefficient	0.4000	0.4077

Table 3.3 – Lateral load capacity of pile specimens

Specimen no.	Test (kips)	FEA (kips)	FE prediction error
#1 (north)	73	65	0.11
#1 (south)	72	66	0.08
#2 (north)	78	69	0.11
#2 (south)	73	71.5	0.02



Table 3.4 – Cycles at which bars fractured in Specimen #1

Bar no.	Bar fracture in test	Bar fracture in FEA
1	2 <sup>nd</sup> cycle at +10%	1 <sup>st</sup> cycle at -10%
4	2 <sup>nd</sup> cycle at -10%	2 <sup>nd</sup> cycle at +10%

Table 3.5 – Cycles at which bars fractured in Specimen #2

Bar no.	Bar fracture in test	Prediction of bar fracture in FEA
1	1 <sup>st</sup> cycle at +10%	2 <sup>nd</sup> cycle at -8%
4	1 <sup>st</sup> cycle at -10%	1 <sup>st</sup> cycle at +10%
3, 5	1 <sup>st</sup> cycle at -10%	1 <sup>st</sup> cycle at -10%
2, 6	no fracture-	2 <sup>nd</sup> cycle at +10%

Table 3.6 –Piles properties for parametric study

Pile Model	Diameter (in.)	Height (ft.)	Number of bars	Angular spacing (degree)	Lineal spacing (in.)	Longitudinal reinf. ratio (%)	Transverse reinf.	Transverse reinf. ratio (%)
D28S1	28	10	6 No. 11	60	11.0	1.52	No. 6 @5.75''	1.28
D28S2			10 No. 9	36	6.75	1.62		
D28S3			16 No. 7	22.5	4.25	1.56		
D28S4			8 No. 10	45	8.80	1.65		
D56S1	56	20	6 No. 18 & 6 No. 14	60	24.7	1.52	No. 9 @6.0''	1.28
D56S2			10 No.18	36	15.0	1.62		
D56S3			16 No. 14	22.5	9.50	1.46		

Table 3.7 – Pile models with varying level of axial load

Pile Model	Lineal Spacing (in.)	Axial load (% of $A_c f_c$ )
		10 (tested)
D28S1	11	15
		20
		10 (tested)
D28S2	6.75	15
		20

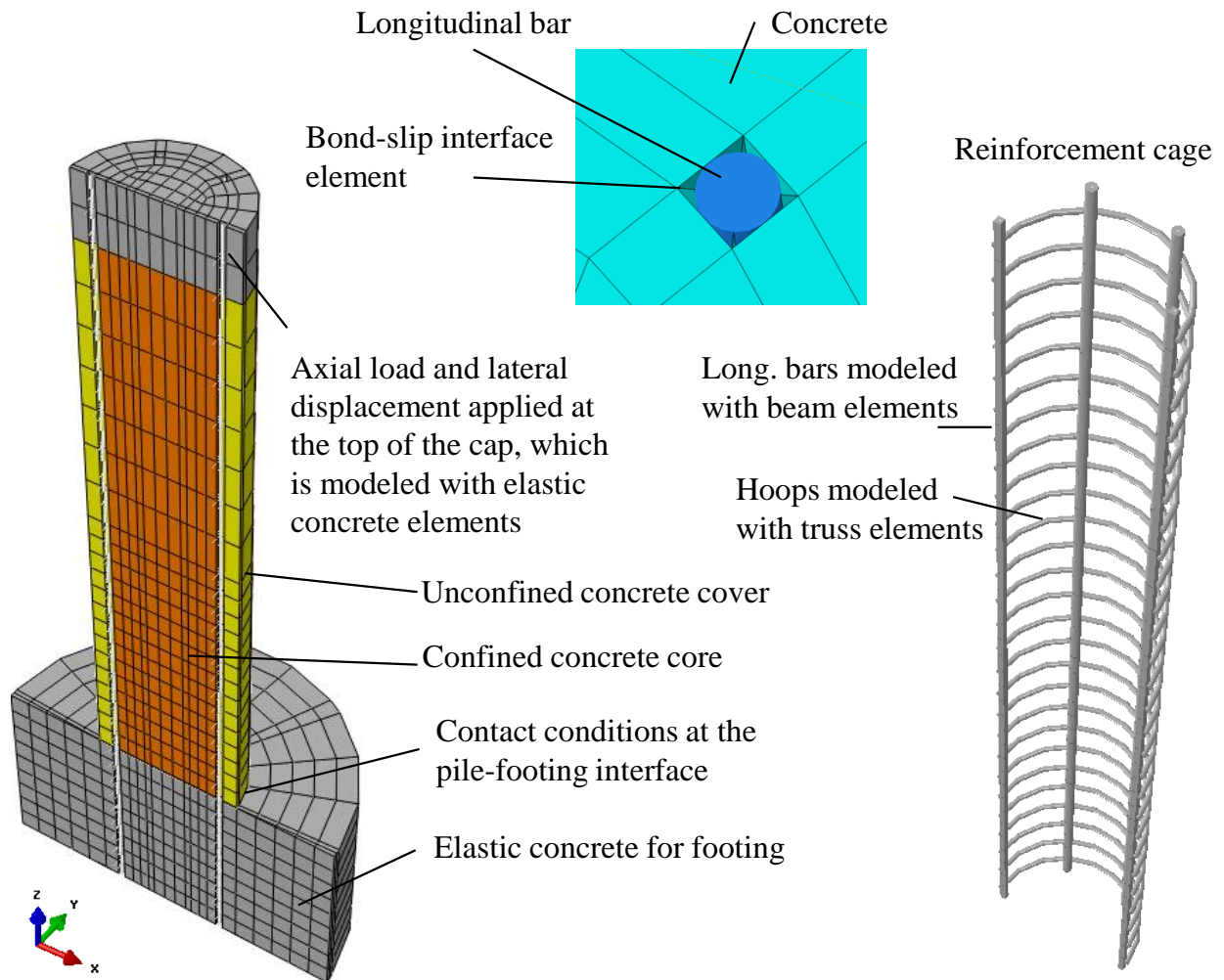


Figure 3.1 – FE model of Specimen #1

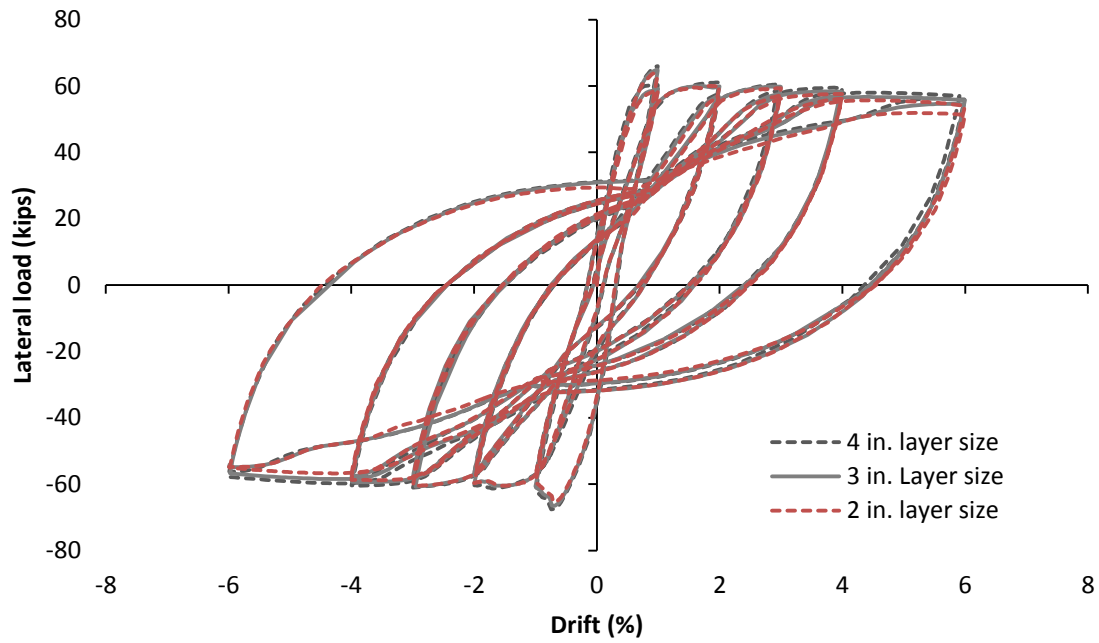


Figure 3.2 – Mesh-size sensitivity study with the FE model of Specimen #1

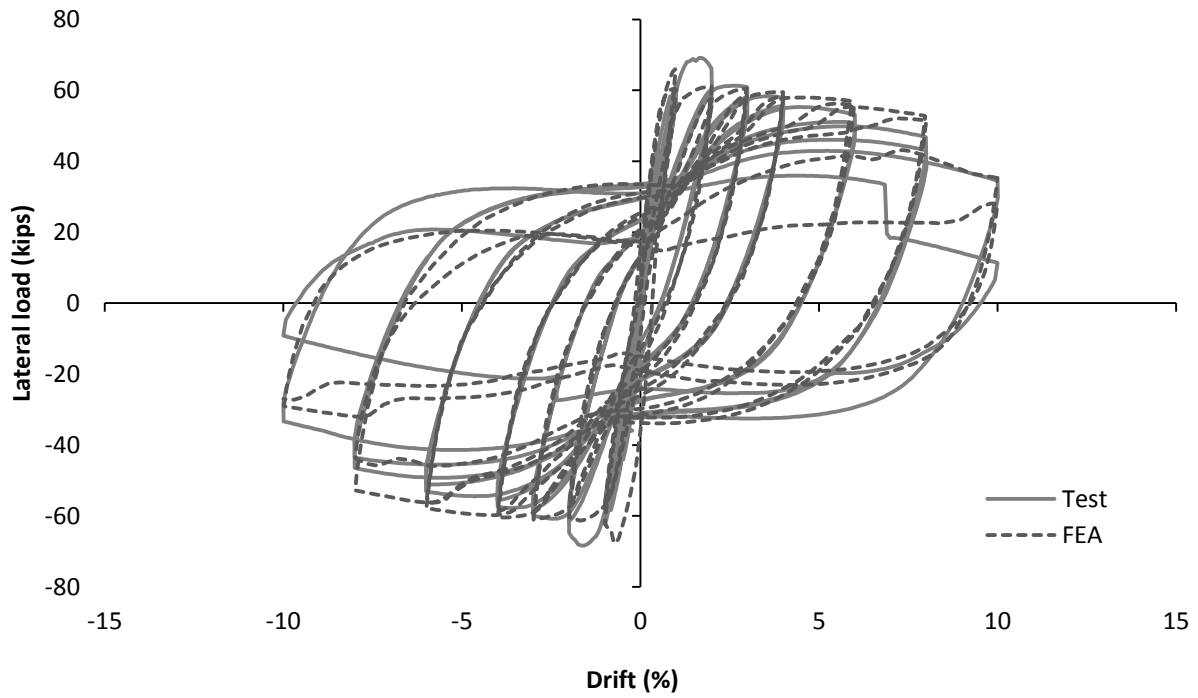


Figure 3.3 - Lateral load-vs.- drift ratio curves for Specimen #1

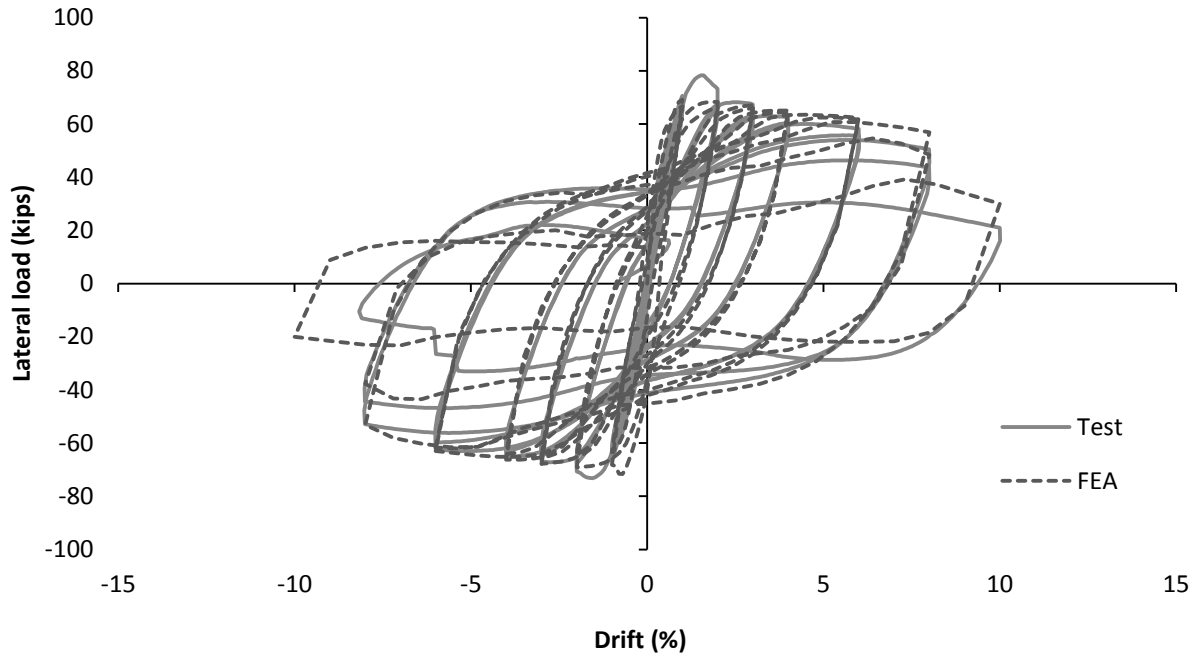


Figure 3.4 – Lateral load-vs.- drift ratio curves for Specimen #2

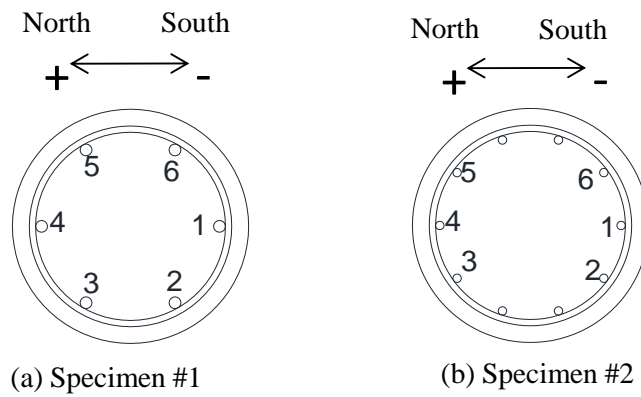
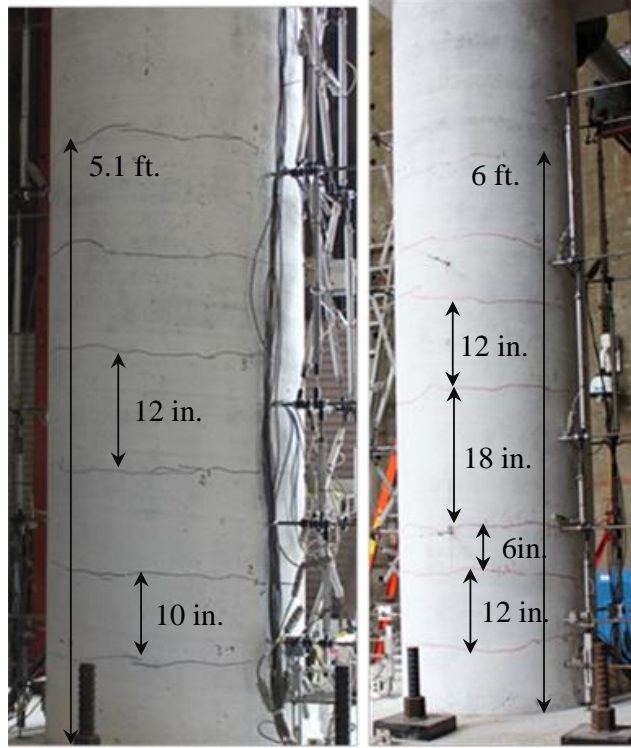


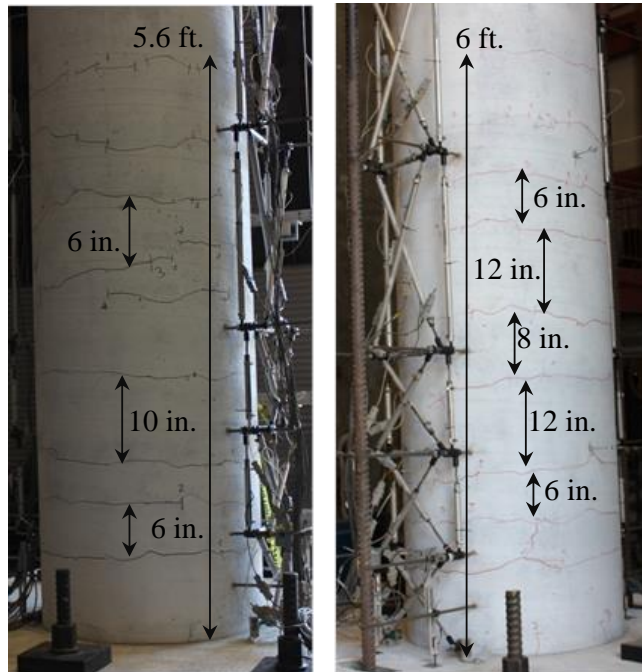
Figure 3.5 – Numbering of longitudinal bars in Specimens #1 and #2



(a) South face

(b) North face

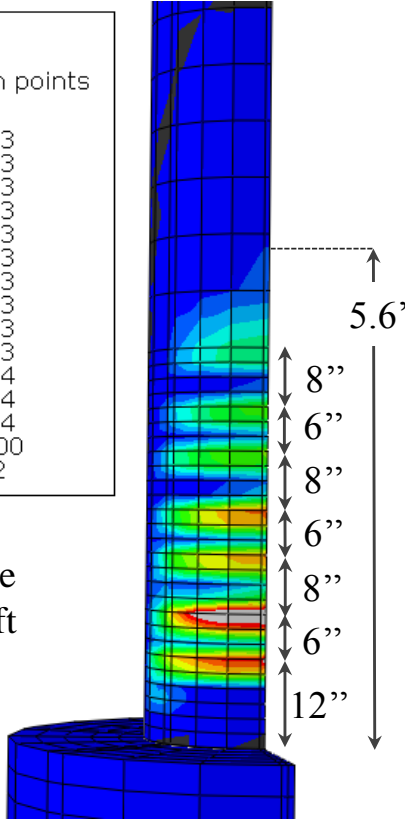
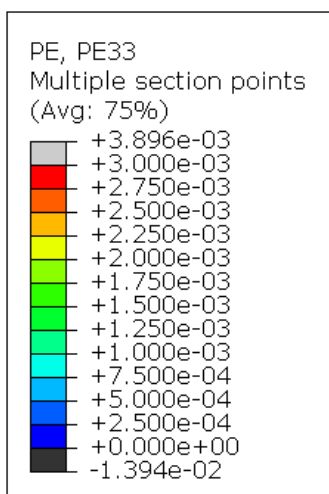
Figure 3.6 – Flexural cracking in Specimen #1 at 1% drift



(a) South face

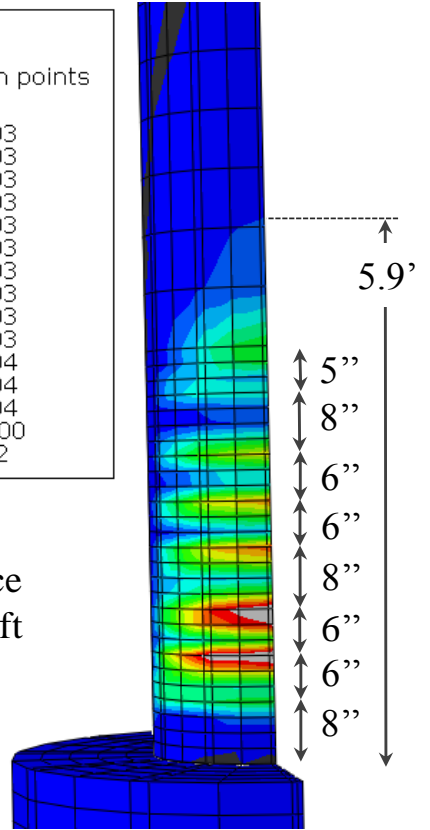
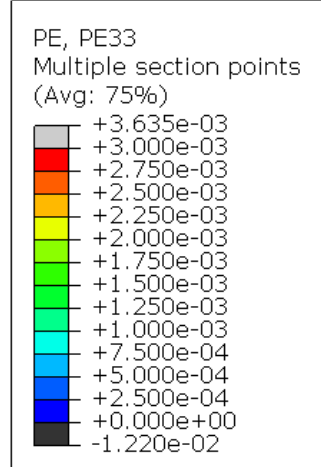
(b) North face

Figure 3.7 – Flexural cracking in Specimen #2 at 1% drift



South face  
at 1% drift

(a) Specimen #1



South face  
at 1% drift

(b) Specimen #2

Figure 3.8 – Normal plastic strains in concrete

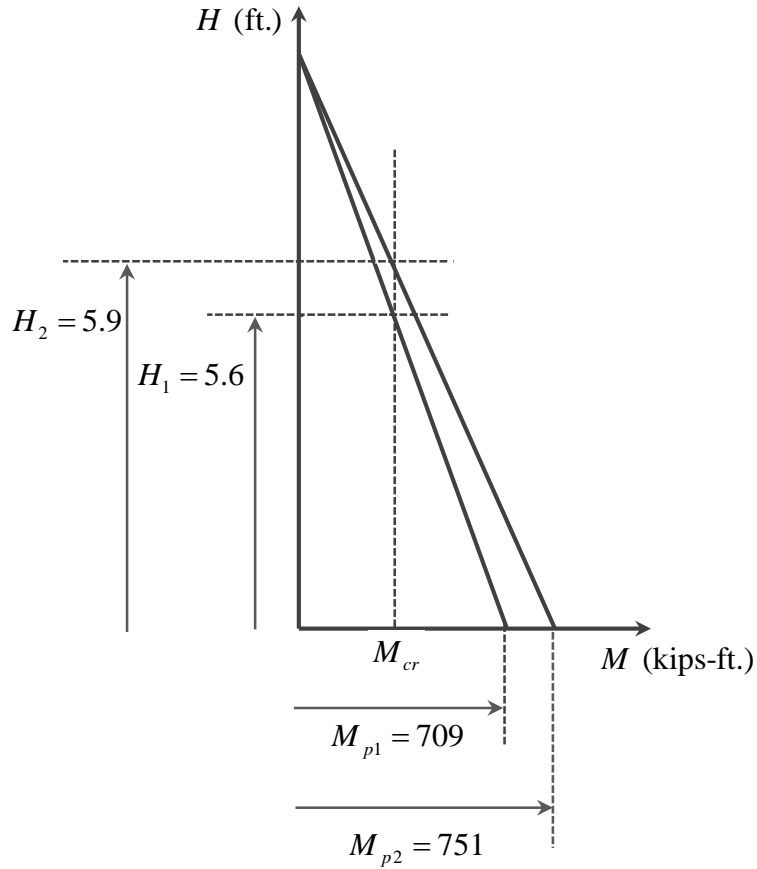


Figure 3.9 – Extent of flexural cracking for moment capacities  $M_{p1}$  (Specimen #1) and  $M_{p2}$  (Specimen #2)

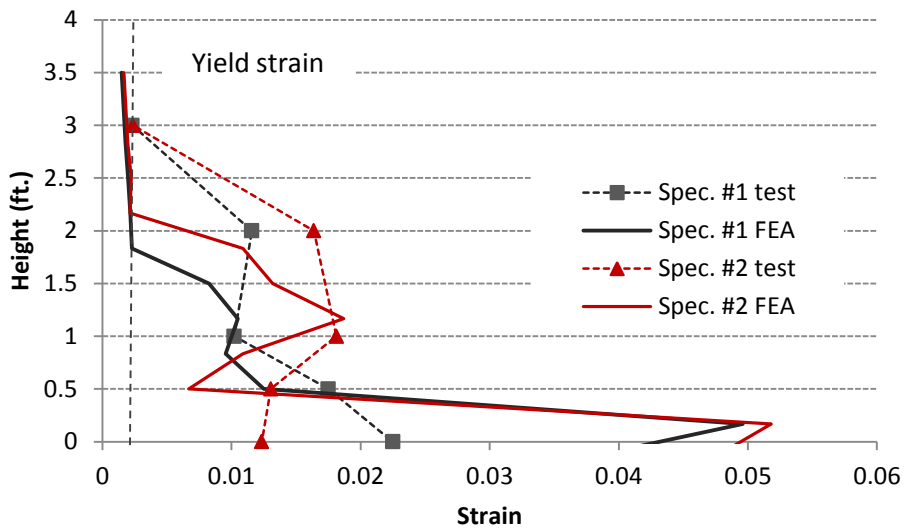
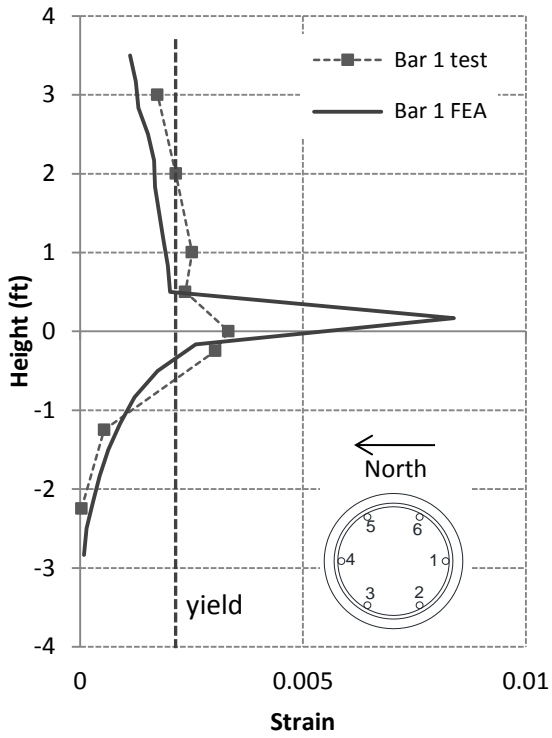
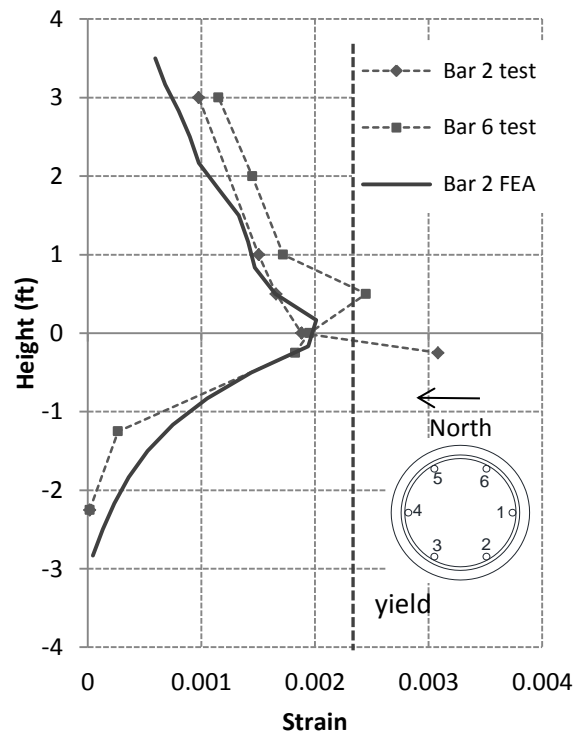


Figure 3.10 – Strains along the longitudinal bar 1 at the south face at +4% drift



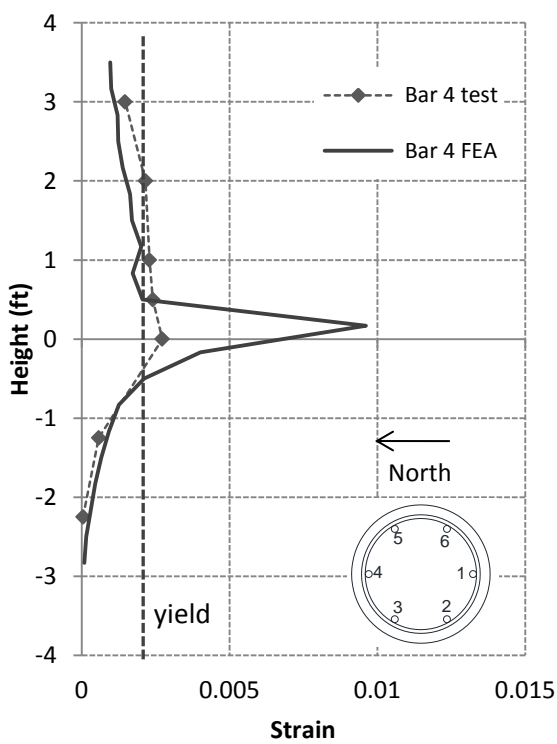


(a) Bar 1

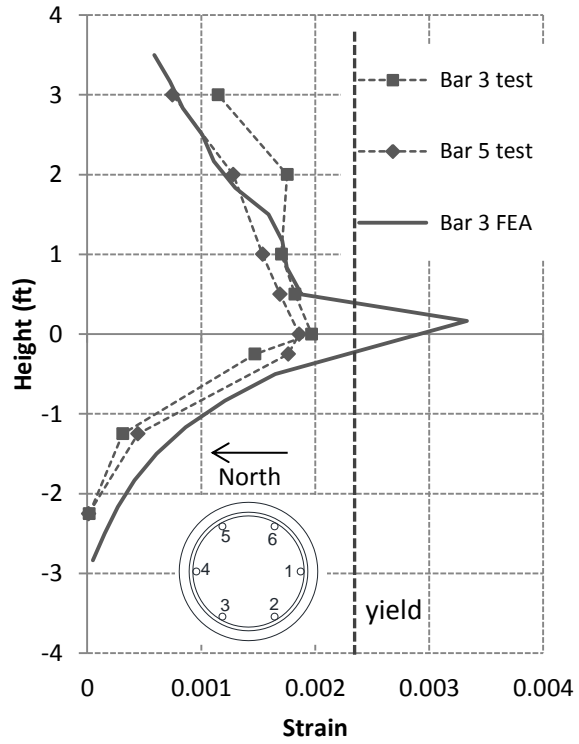


(b) Bars 2 & 6

Figure 3.11 – Strains in bars at the south face of Specimen #1 at +1% drift



(a) Bar 4



(b) Bars 3 & 5

Figure 3.12 – Strains in bars at the north face of Specimen #1 at -1% drift

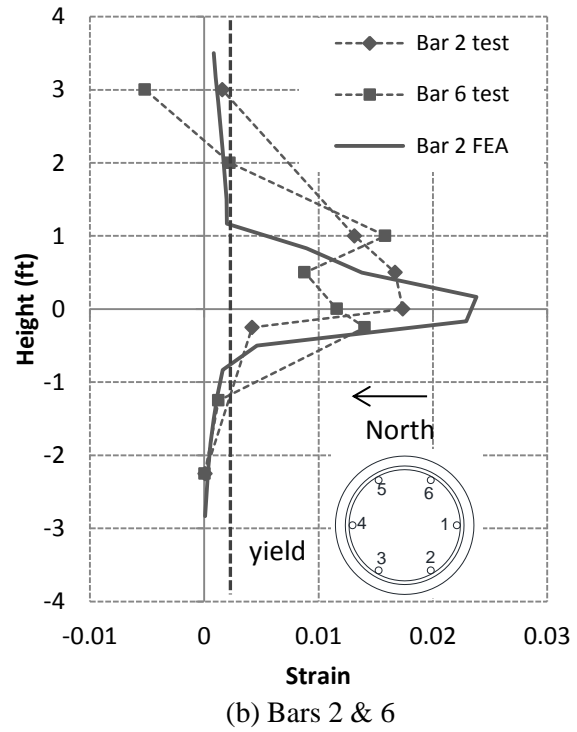
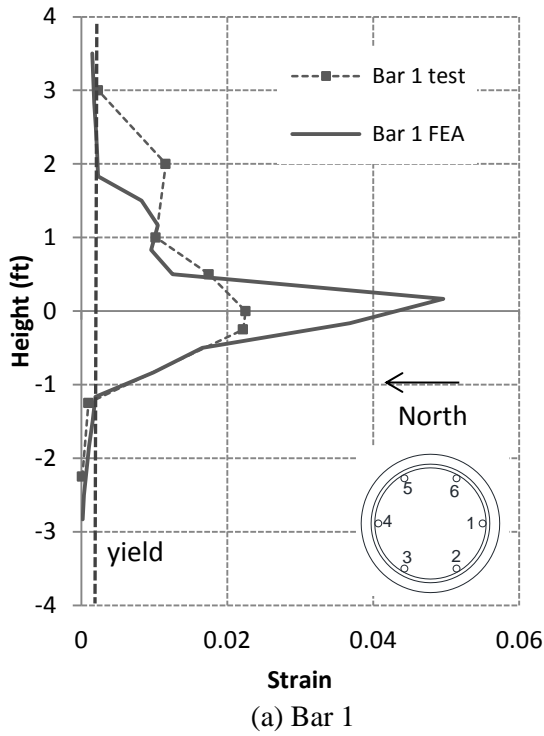


Figure 3.13 – Strains in bars at the south face of Specimen #1 at +4% drift

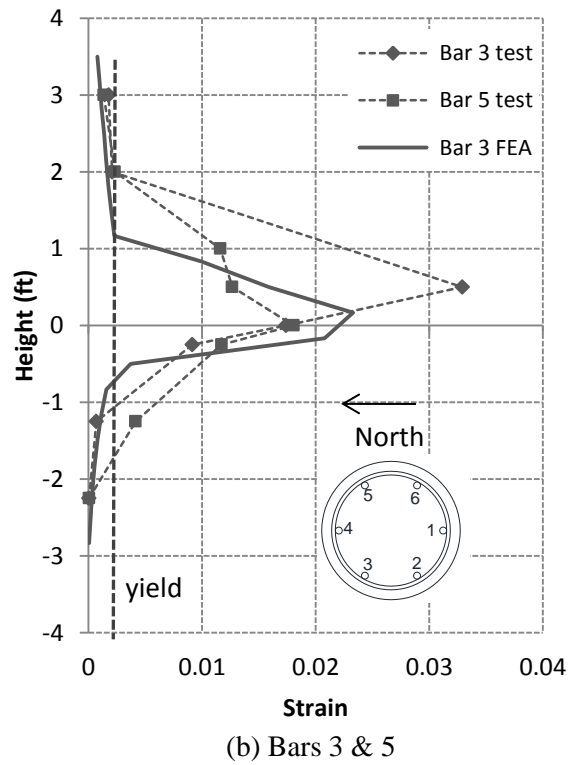
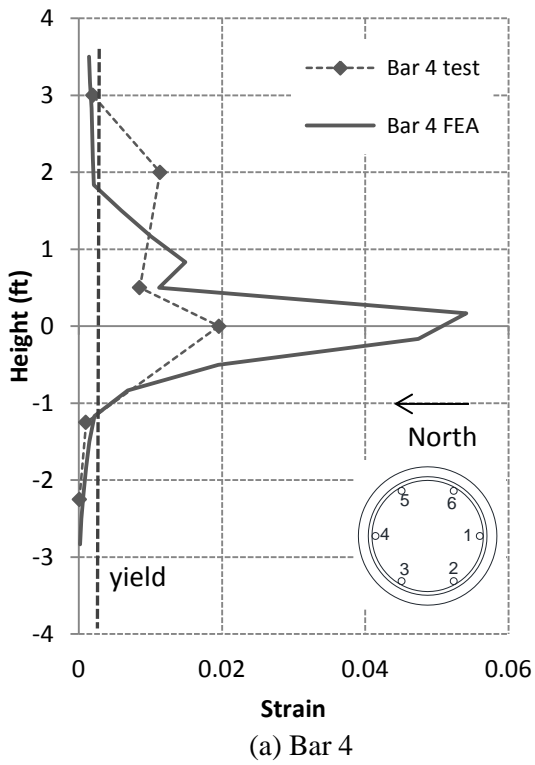
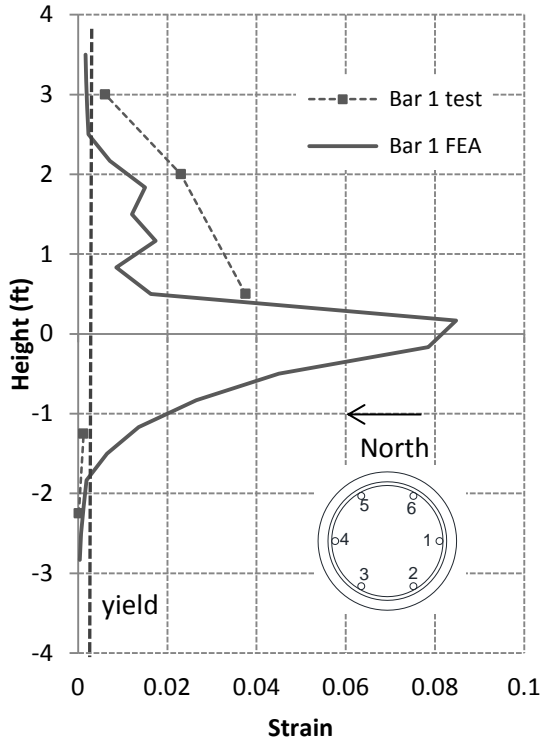
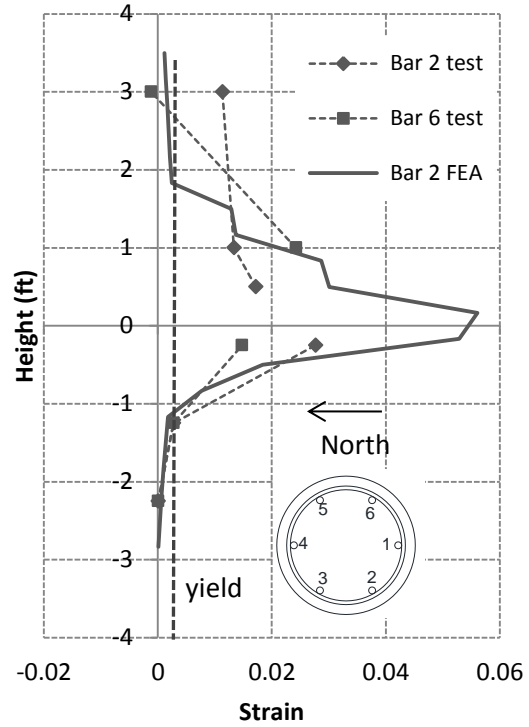


Figure 3.14 – Strains in bars at the north face of Specimen #1 at -4% drift

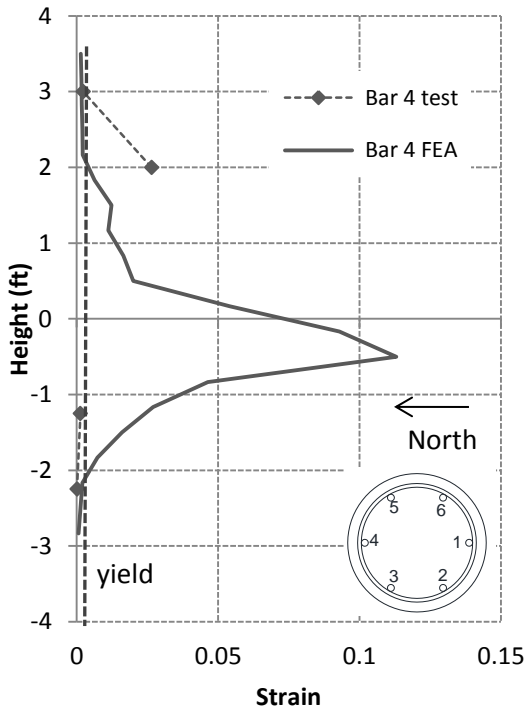


(a) Bar 1

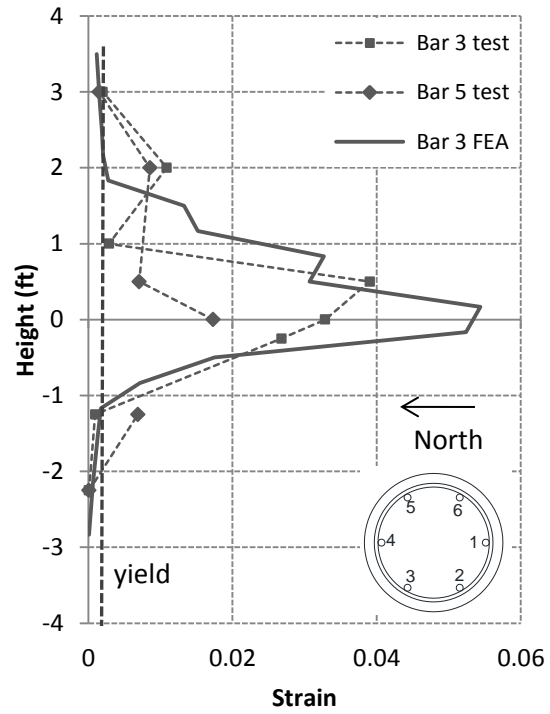


(b) Bars 2 & 6

Figure 3.15 – Strains in bars at the south face of Specimen #1 at +8% drift

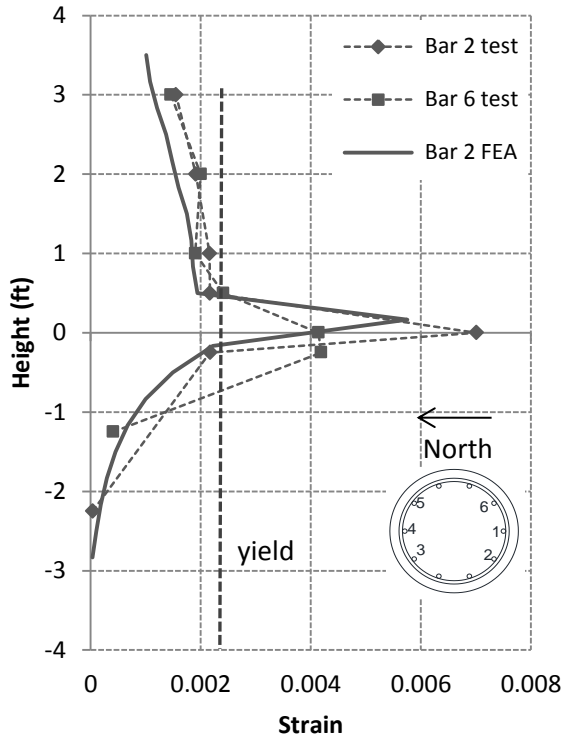
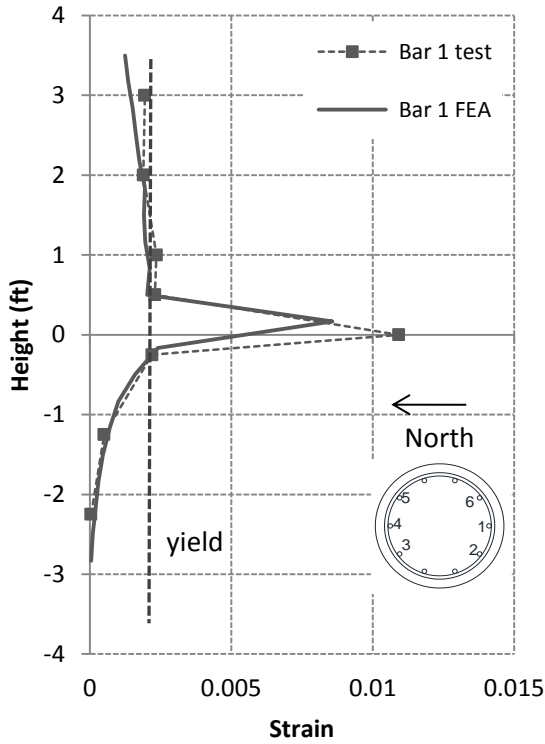


(a) Bar 4



(b) Bars 3 & 5

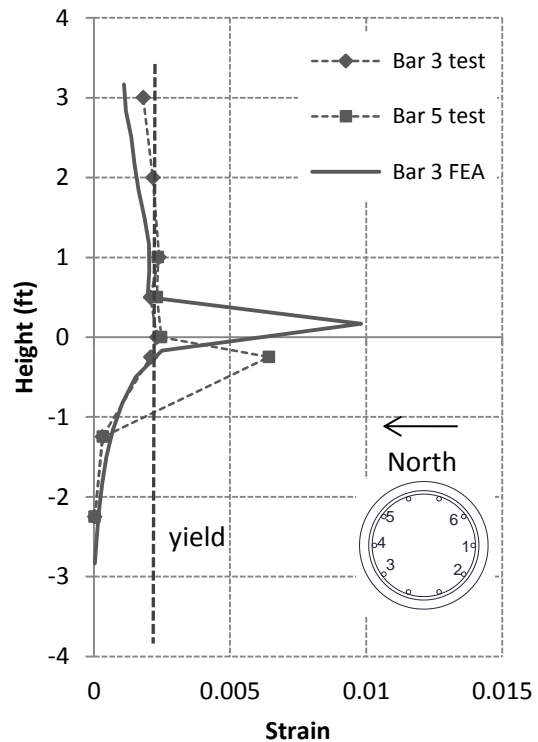
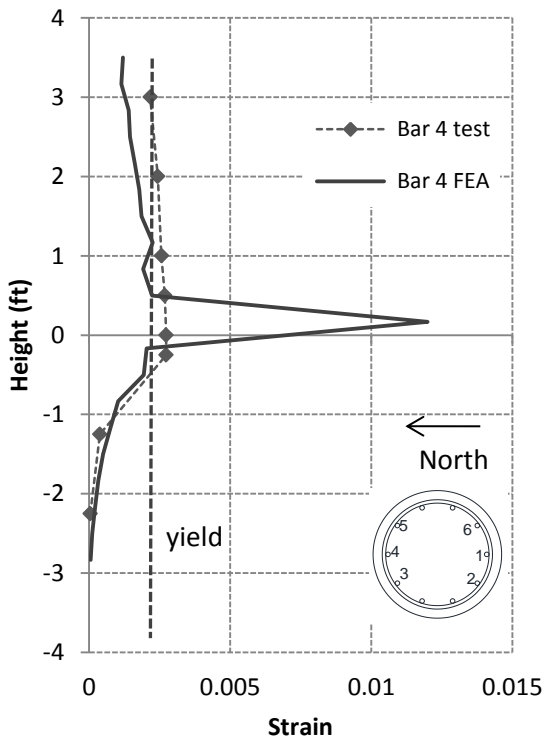
Figure 3.16 – Strains in bars at the north face of Specimen #1 at -8% drift



(a) Bar 1

(b) Bars 2 & 6

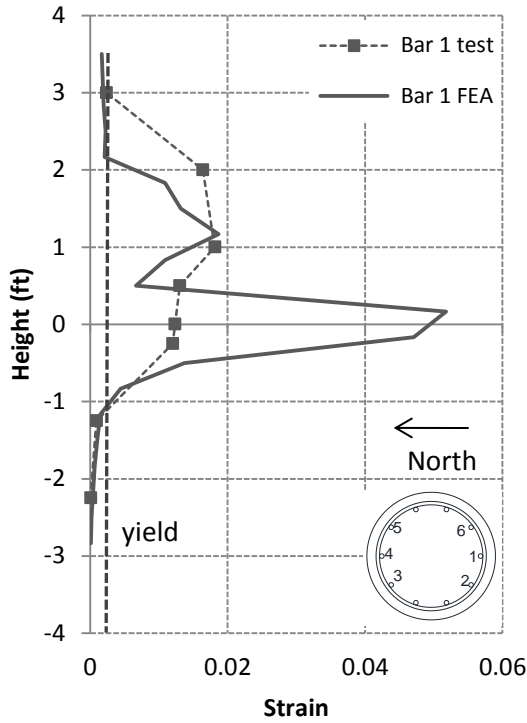
Figure 3.17 - Strains in bars at the south face of Specimen #2 at +1% drift



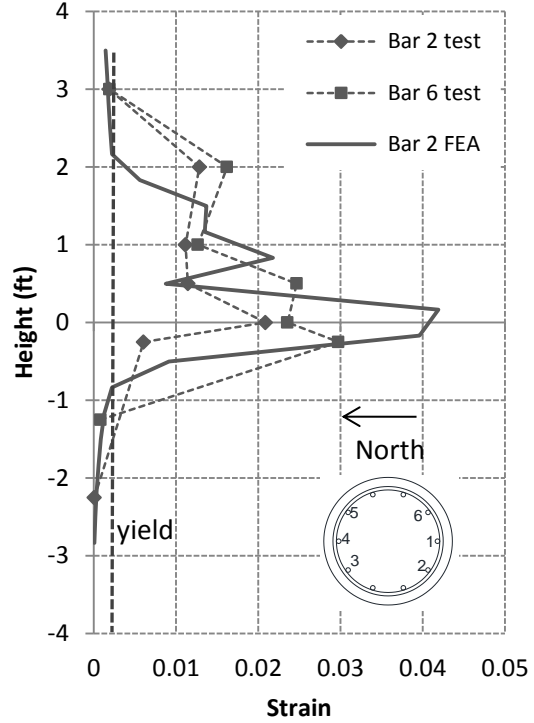
(a) Bar 4

(b) Bars 3 & 5

Figure 3.18 - Strains in bars at north face of Specimen #2 at -1% drift

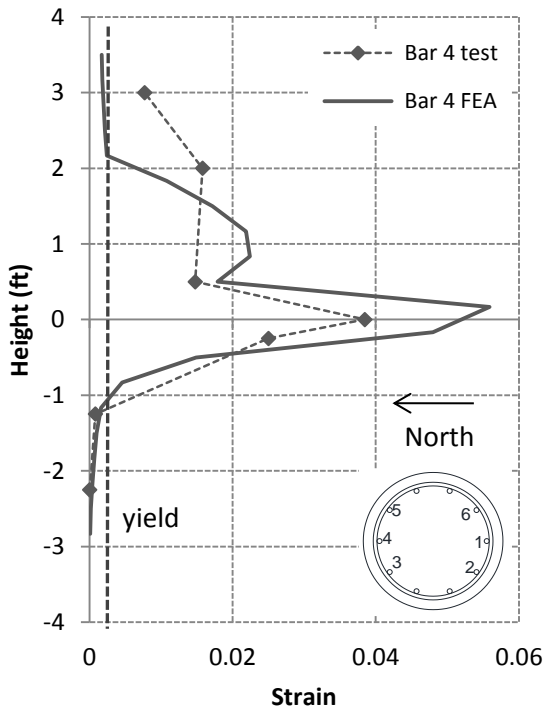


(a) Bar 1

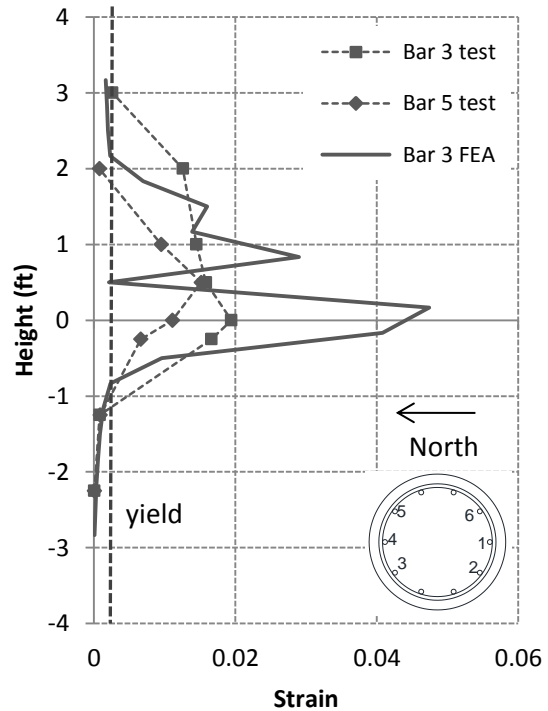


(b) Bars 2 & 6

Figure 3.19 – Strains in bars at south face of Specimen #2 at +4% drift

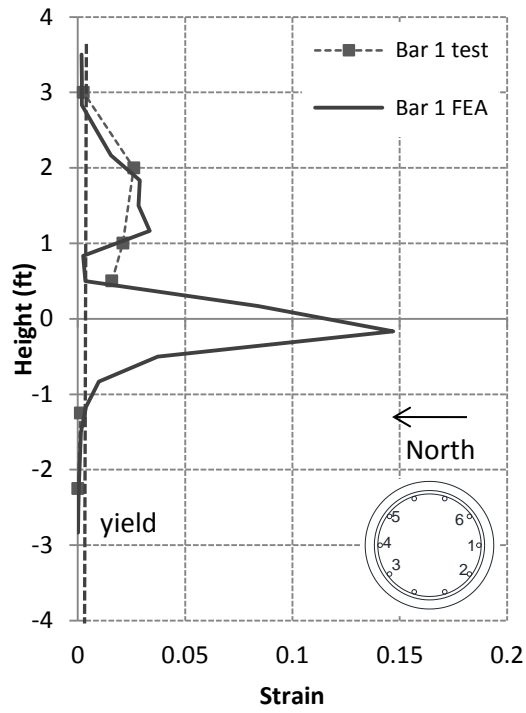


(a) Bar 4

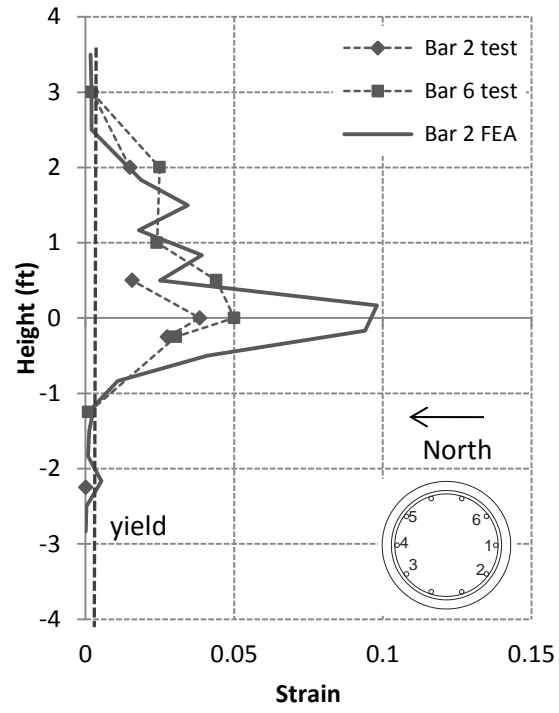


(b) Bars 3 & 5

Figure 3.20 – Strains in bars at north face of Specimen #2 at -4% drift

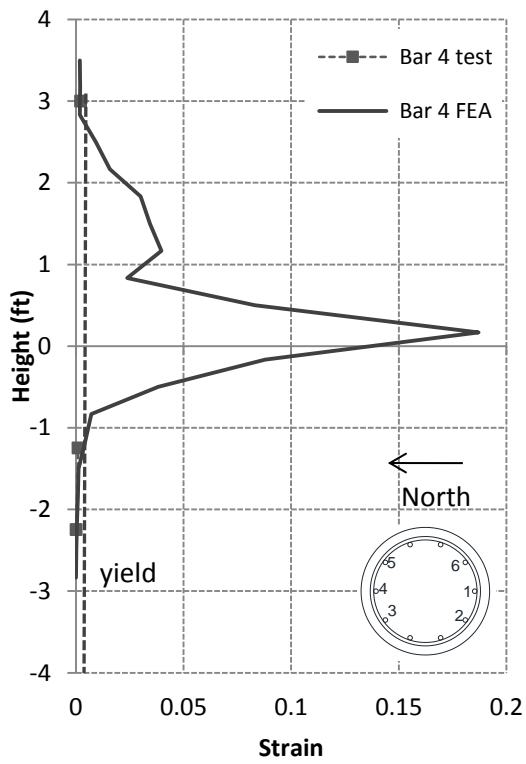


(a) Bar 1

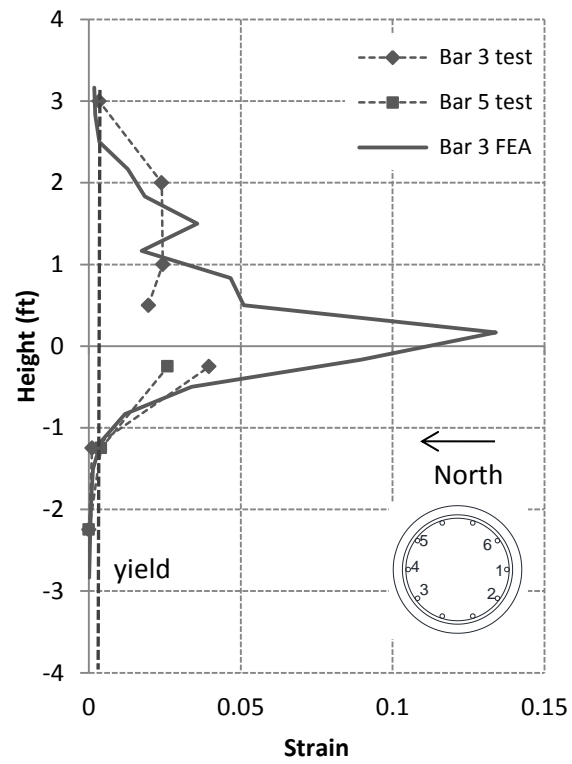


(b) Bars 2 & 6

Figure 3.21 – Strains in bars at south face of Specimen #2 at +8% drift



(a) Bar 4



(b) Bars 3 & 5

Figure 3.22 – Strains in bars at north face of Specimen #2 at -8% drift

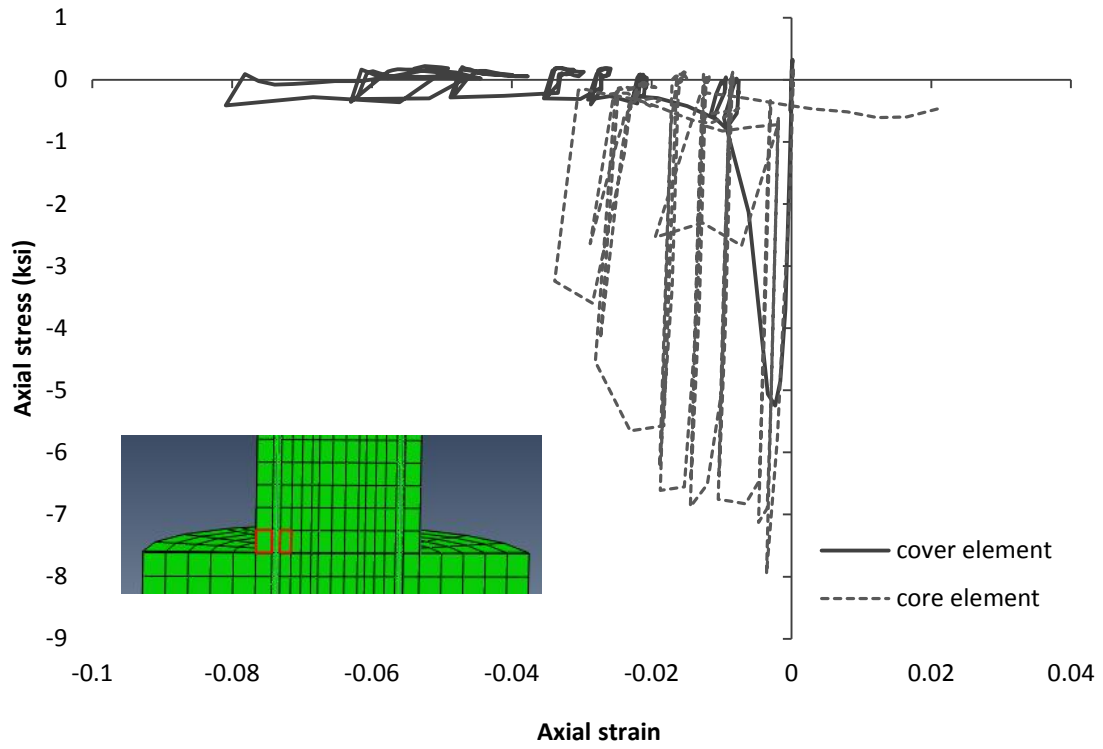


Figure 3.23 – Axial stress-strain curves from cover concrete and core concrete for Specimen #1

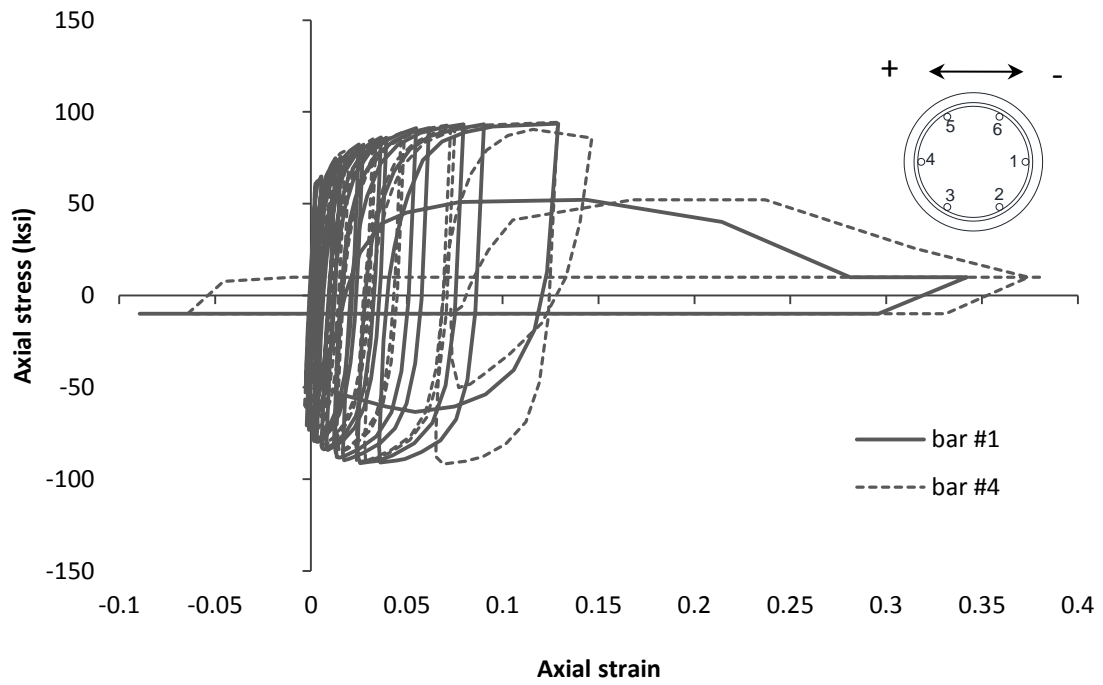


Figure 3.24 – Stress-strain curves for longitudinal bars at the base of the pile of Specimen #1

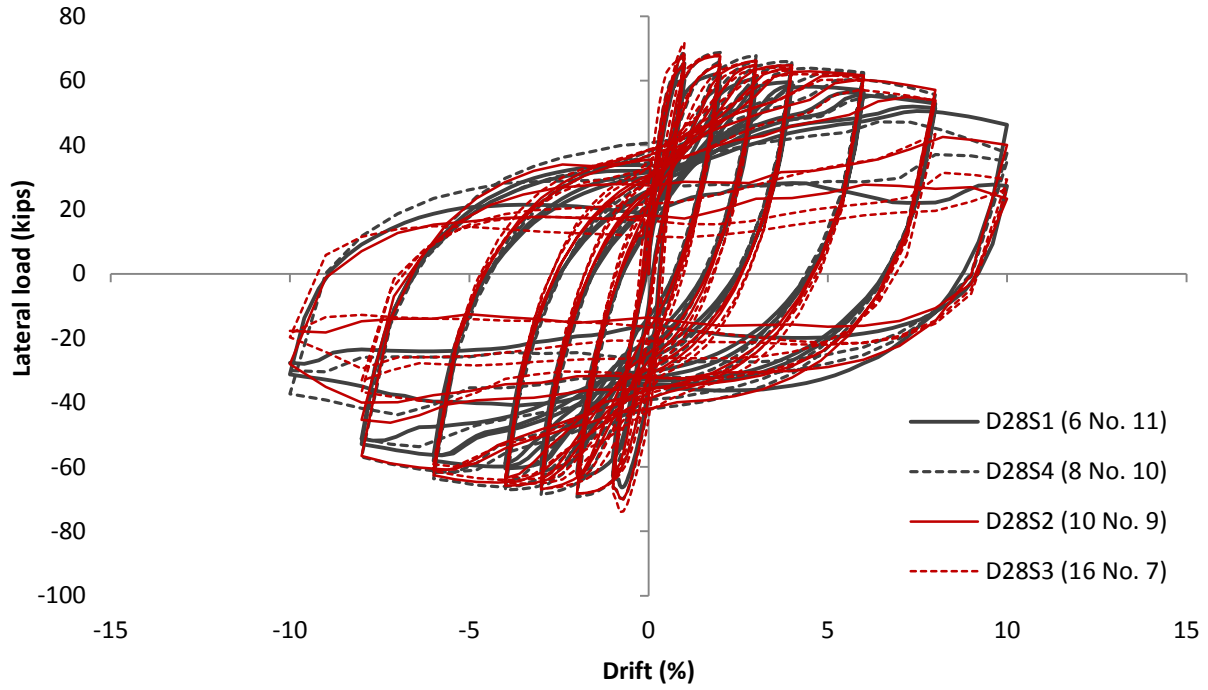


Figure 3.25 – Lateral load-vs.-drift ratio curves for models with  $D=28$  in.

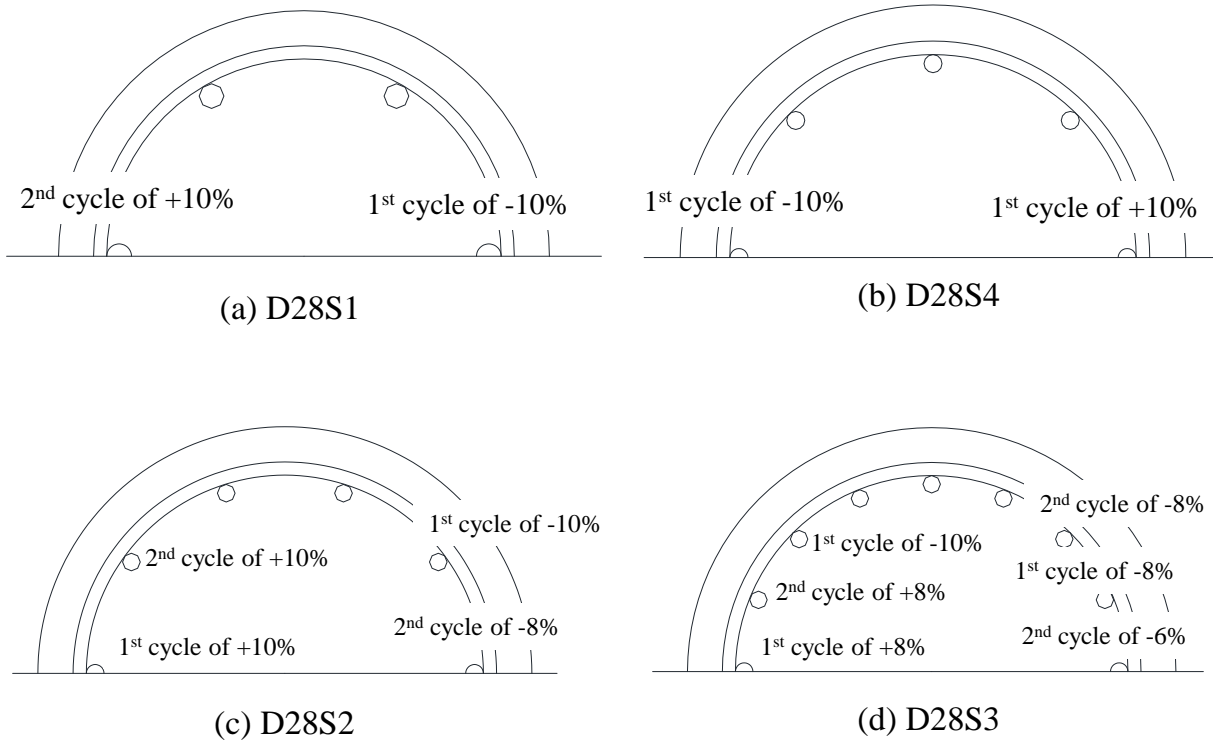
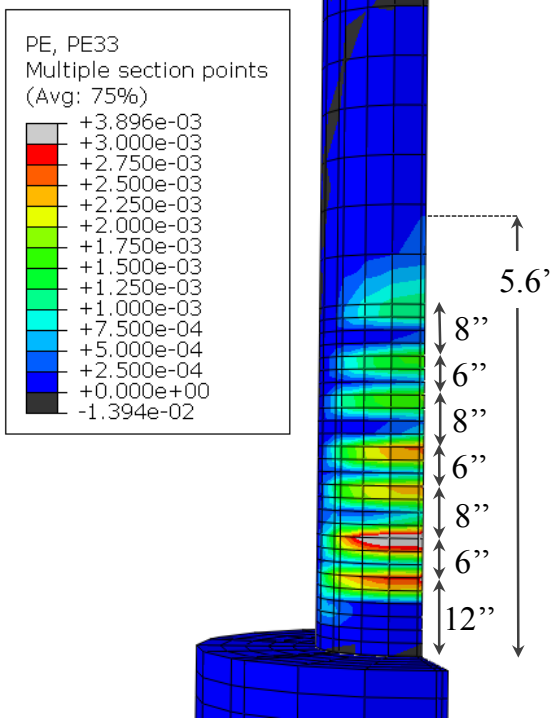
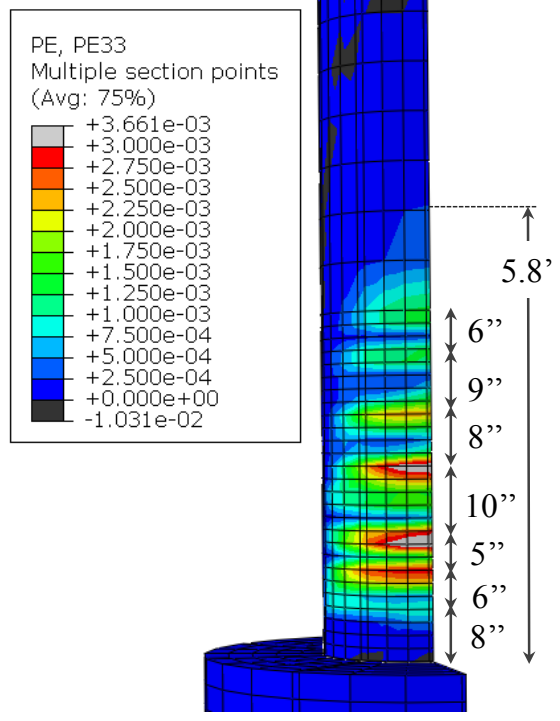


Figure 3.26 – Cycles at which the longitudinal bars fractured for models with  $D=28$  in.

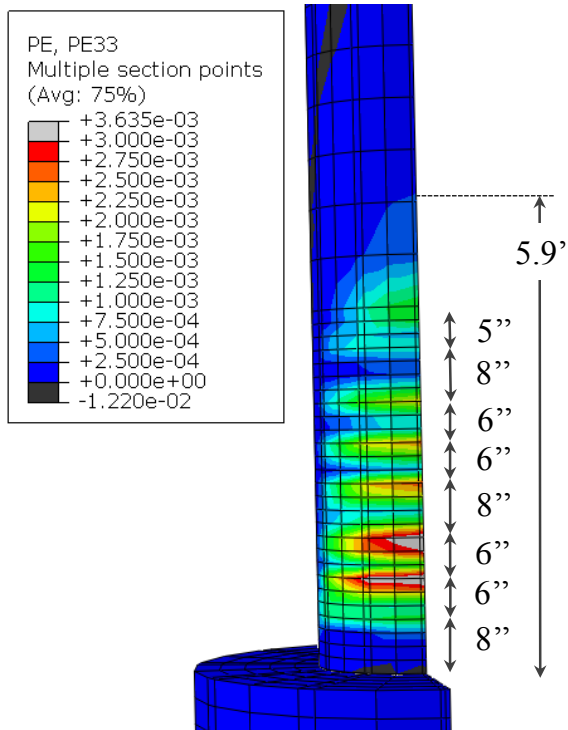




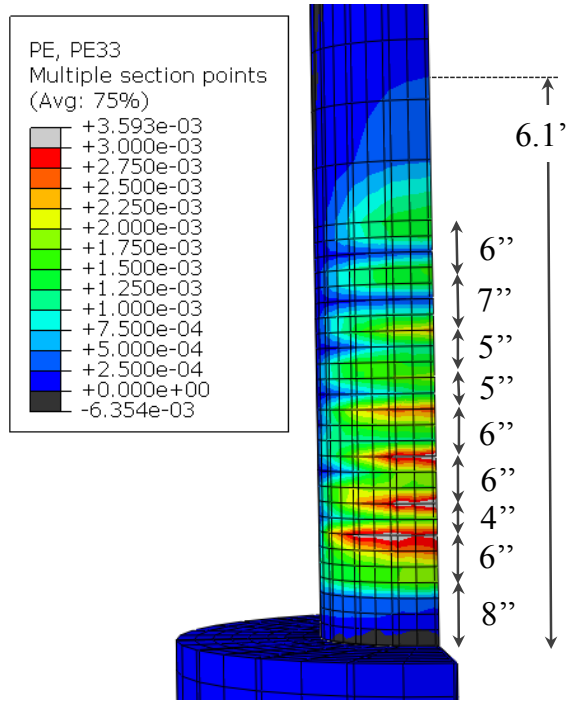
(a) D28S1



(b) D28S4



(c) D28S2



(d) D28S3

Figure 3.27 – Normal plastic strains in the axial direction at 1% drift for models with  $D=28$  in.

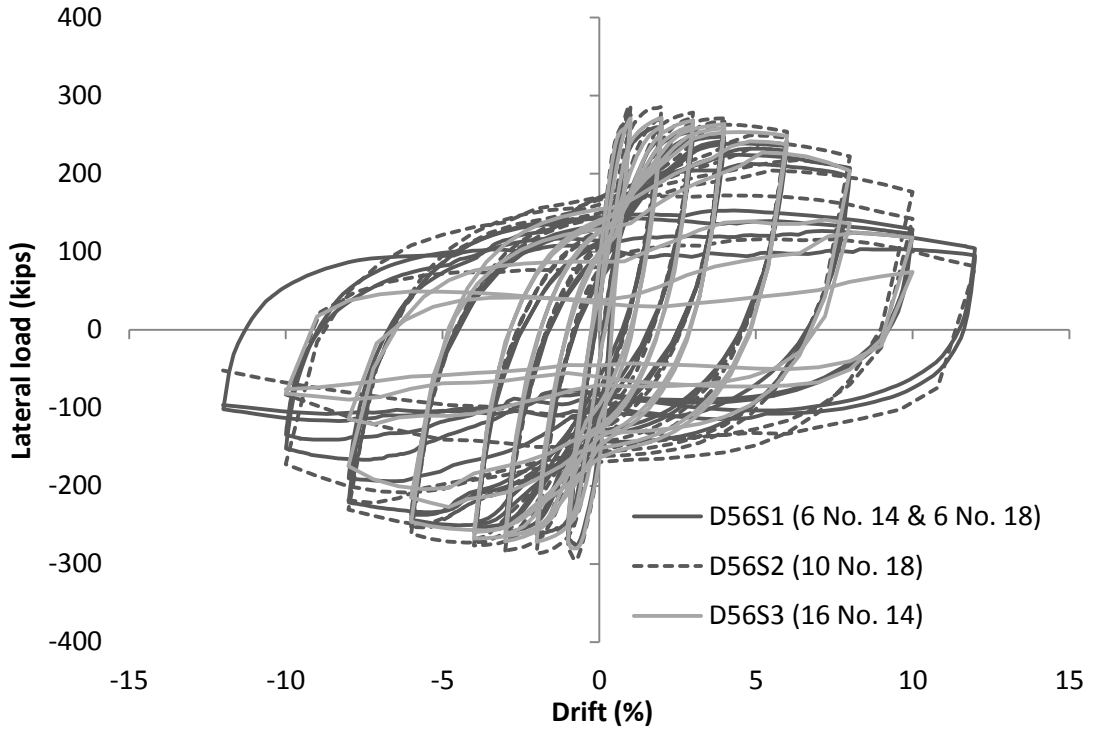


Figure 3.28 – Lateral load-vs.-drift ratio curves for models with  $D=56$  in.

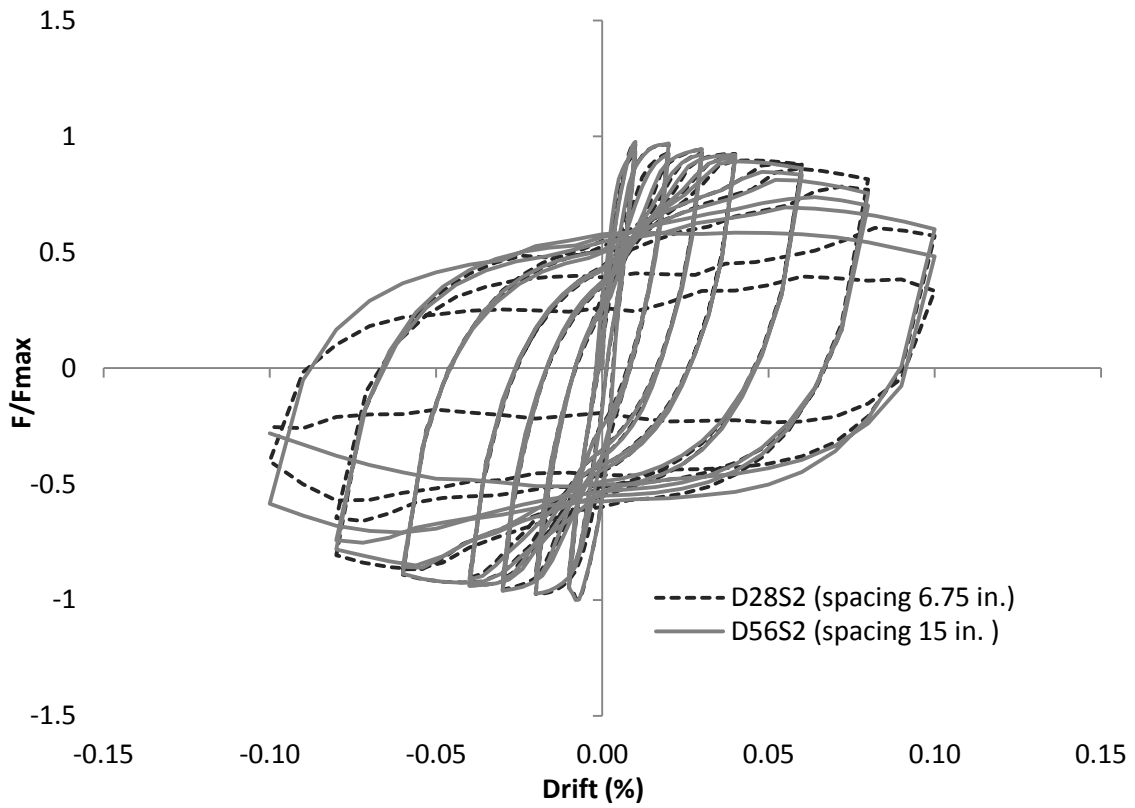


Figure 3.29 – Normalized lateral load-vs.-drift ratio curves of pile models with different diameter

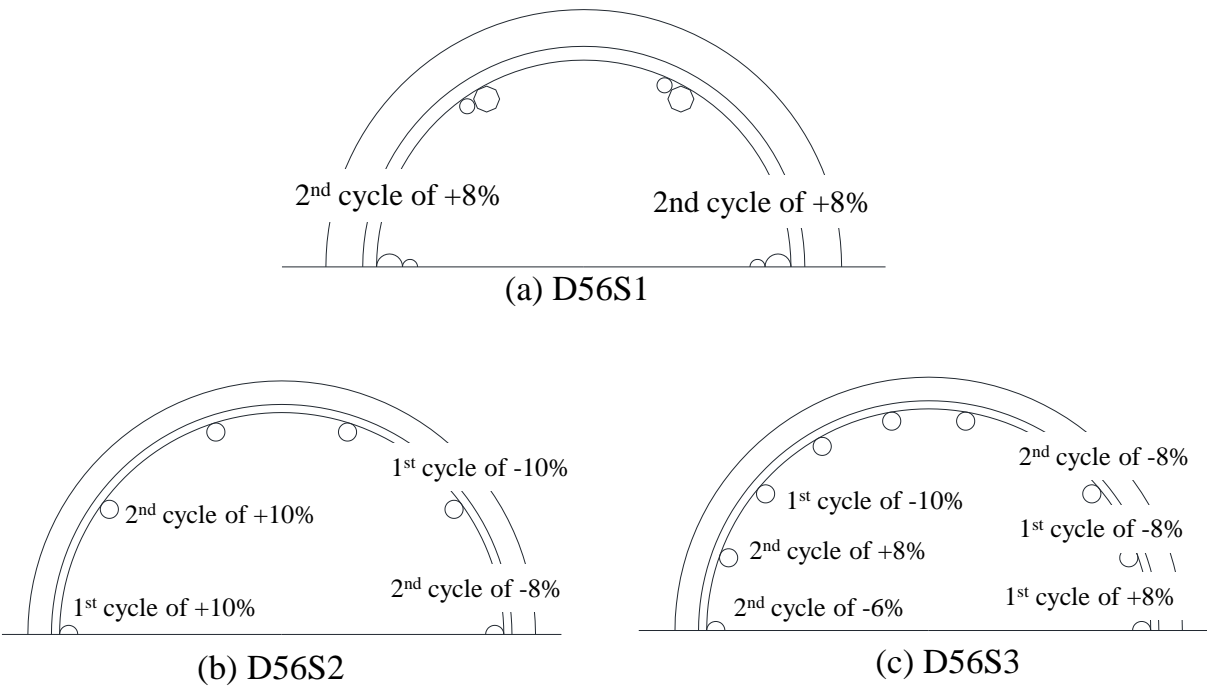
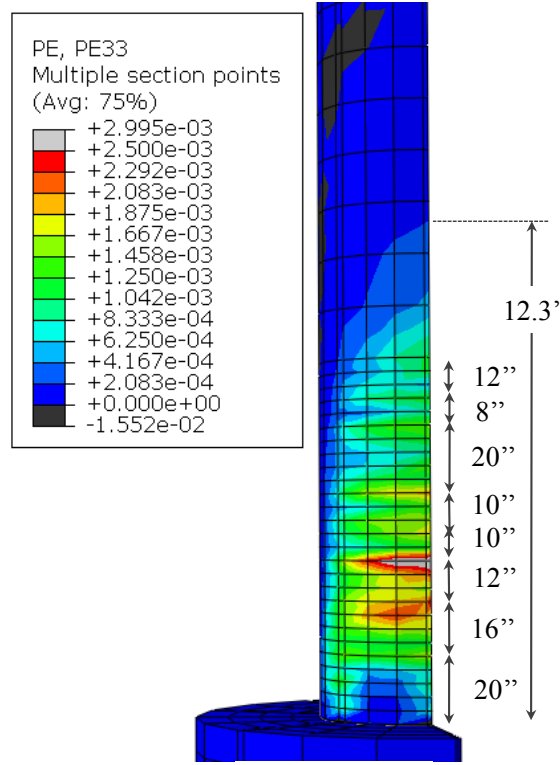
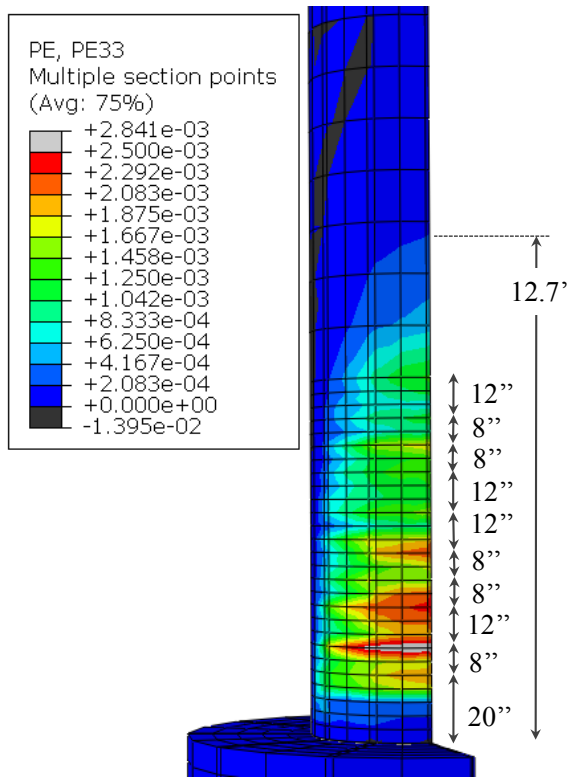


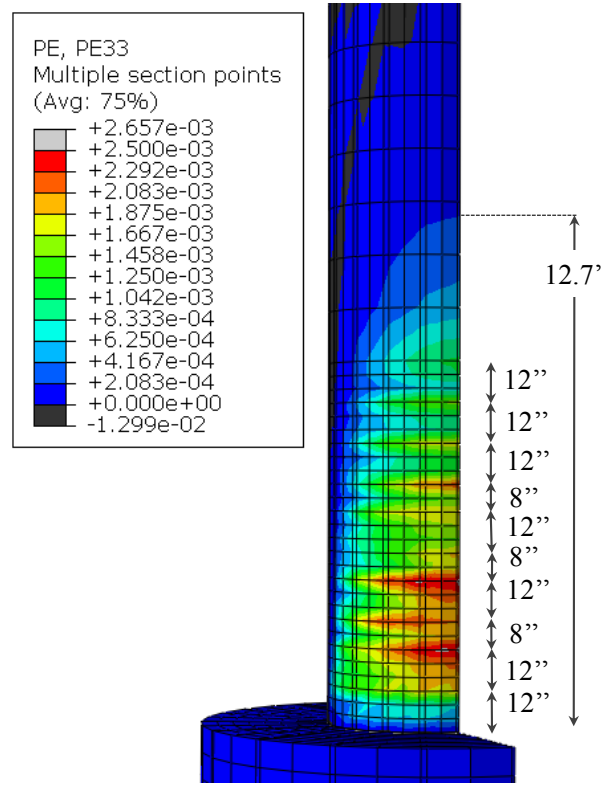
Figure 3.30 – Cycles at which the longitudinal bars fractured for models with  $D=56$  in.



(a) D56S1



(b) D56S2



(c) D56S3

Figure 3.31 – Normal plastic strains in the axial direction at 1% drift for models with  $D=56$  in.

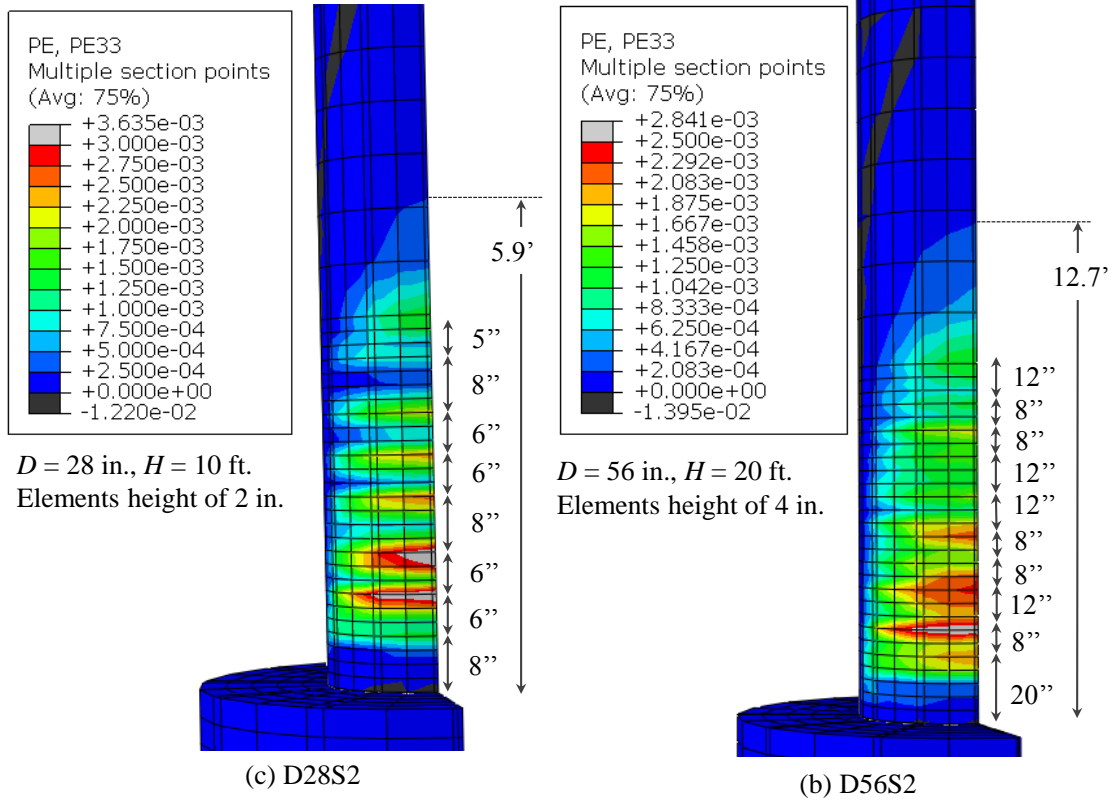


Figure 3.32 – Normal plastic strains in the axial direction at 1% drift for piles D28S2 and D56S2

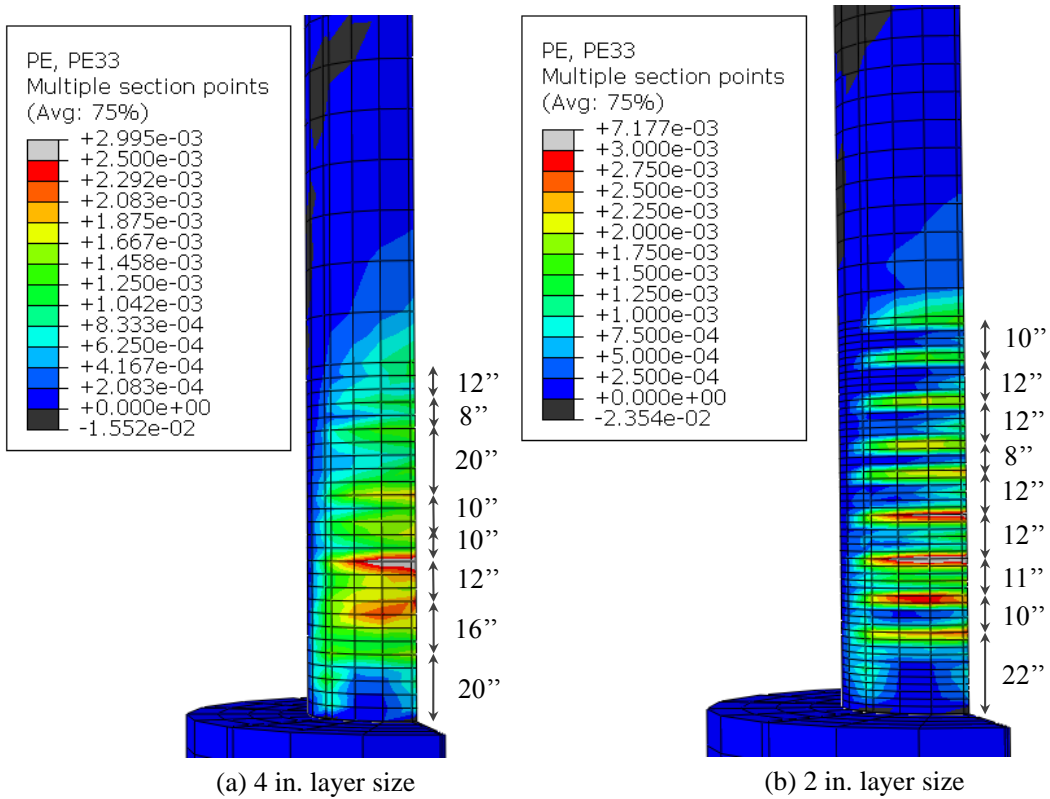


Figure 3.33 – Mesh sensitivity study for the normal plastic strains in pile D56S1

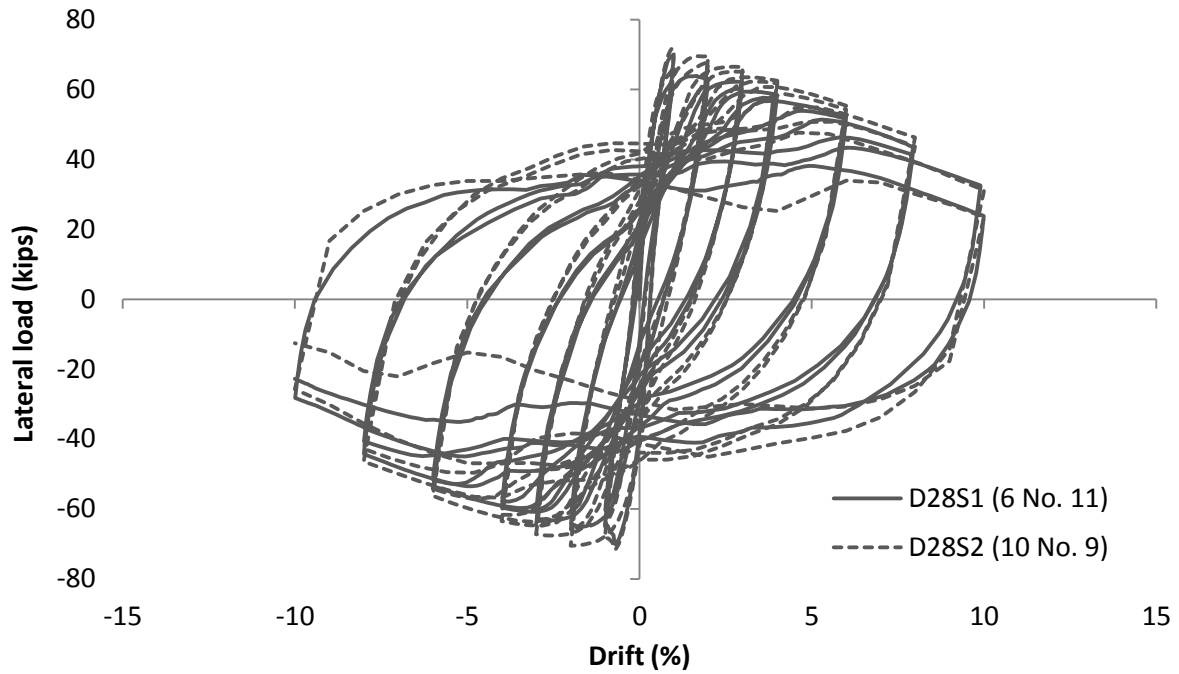


Figure 3.34 – Lateral load-vs.-drift ratio curves for models with axial load equal to  $0.15 A_c f_c$

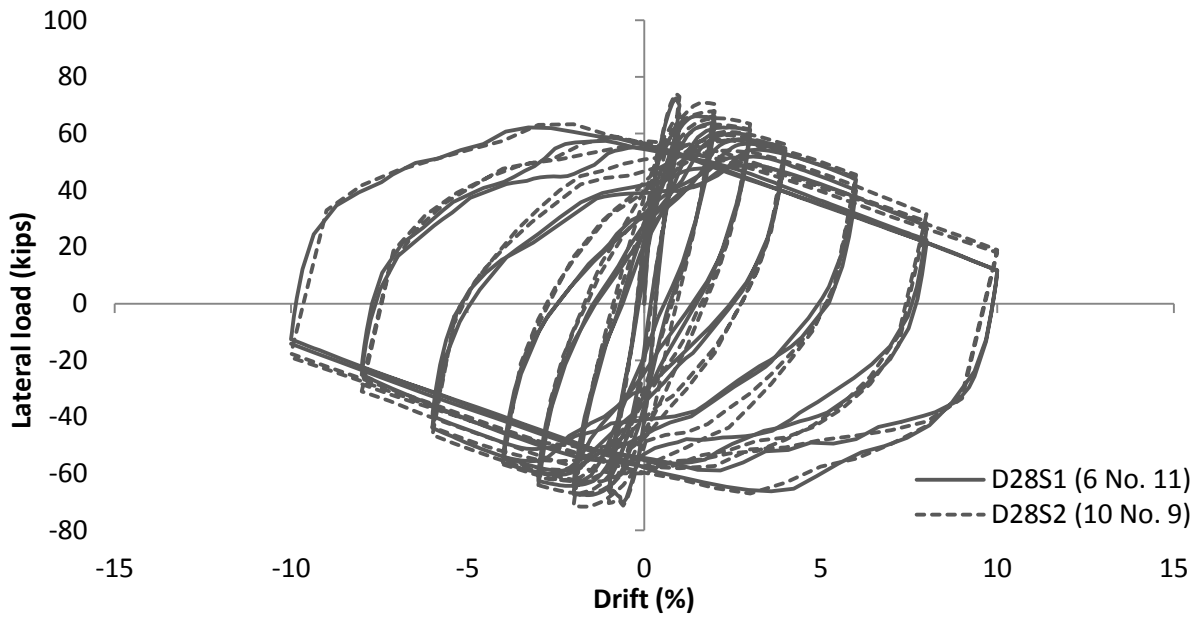


Figure 3.35 – Lateral load-vs.-drift ratio curves for models with axial load equal to  $0.20 A_c f_c$

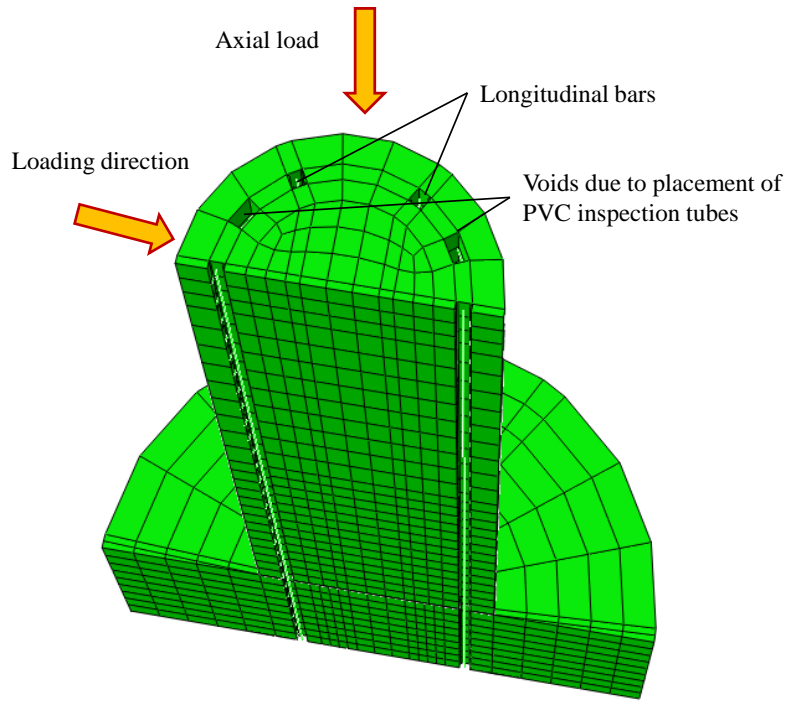


Figure 3.36 – FE model of D28S1-B (with PVC inspection tubes)

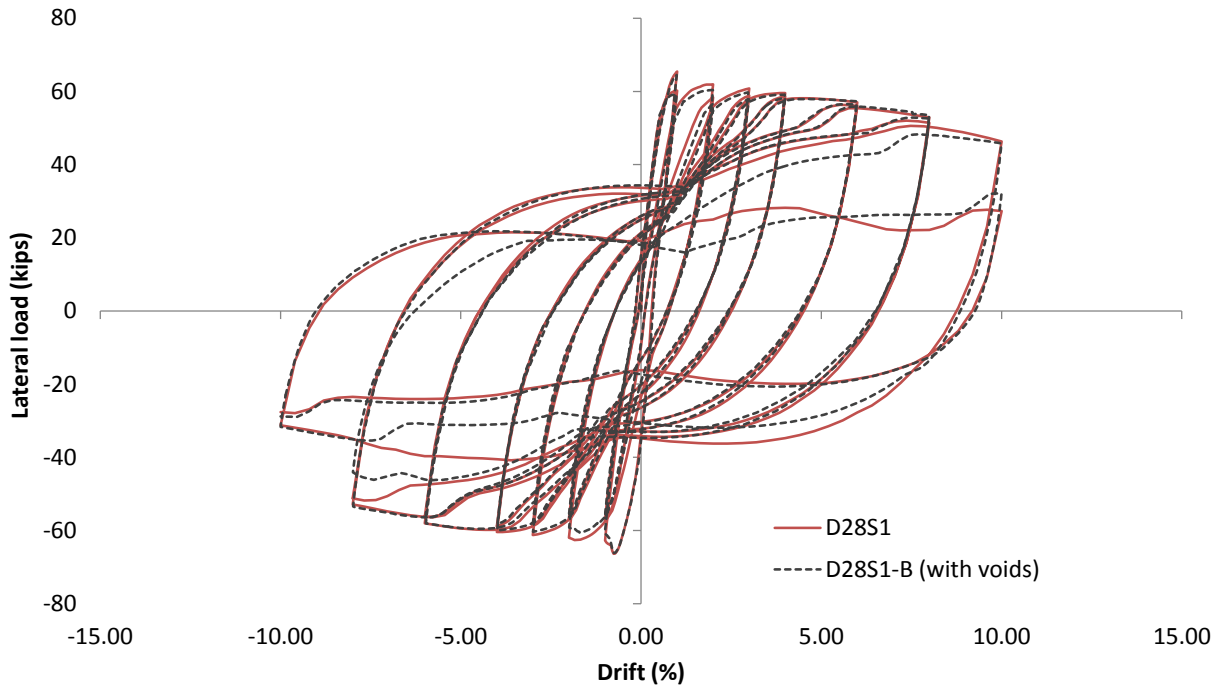


Figure 3.37 – Lateral load-vs.-top drift curve for Specimen D28S1-B (with voids)





## CHAPTER 4

# FINITE ELEMENT ANALYSES WITH MICROPLANE MODEL FOR CONCRETE

An improved version of the microplane model (M7) for concrete proposed by Caner and Bazant (2013a) has been implemented in a user-defined subroutine in Abaqus (Simulia 2012). The model can more accurately simulate the opening and closing of cracks and the confinement effect in concrete than the damaged-plasticity constitutive model provided by Abaqus (Simulia 2012). The limitations of the damaged-plasticity model in simulating the aforementioned phenomena were discussed in Section 2.1 of this report, along with the ad hoc remedies proposed in this study. In this chapter, the key features of the microplane model implemented in Abaqus and its calibration are described. In this study, the microplane model has been calibrated and validated with the experimental data of Hurlbut (1985) and Mander et al. (1988). Furthermore, it has been applied to analyze the nonlinear behavior of the RC pile specimens tested by Papadopoulos and Shing (2014).

### 4.1 Model formulation

The microplane model is formulated in terms of a constitutive relation between the stress and strain components defined on a plane, called a microplane, of any orientation in the material (Brocca and Bazant 2000). It is based on the hypothesis that the free energy density of the material is a sum of the free energy densities associated with microplanes of various orientations. The free energy density for each microplane is defined as a function of the corresponding strain components, which are derived from the strain tensor based on a kinematic constraint. The stresses at the micro and macro levels satisfy equilibrium in an approximate sense by virtue of the principle of virtual work.

As shown in Figure 4.1, the direction of a microplane is identified by a unit normal vector  $\mathbf{n}$ , defined in the global Cartesian coordinates,  $x_1, x_2$ , and  $x_3$ . Each microplane has an associated normal strain component  $\varepsilon_N$  and two shear strain components,  $\varepsilon_M$  and  $\varepsilon_L$ , in directions defined by two orthogonal unit vectors,  $\mathbf{m}$  and  $\mathbf{l}$ , respectively, oriented parallel to the microplane. These strain components are derived from the strain tensor  $\boldsymbol{\varepsilon}$  by projections on  $\mathbf{n}$ ,  $\mathbf{m}$  and  $\mathbf{l}$  as follows.

$$\varepsilon_N = N_{ij}\varepsilon_{ij}, \quad \varepsilon_L = L_{ij}\varepsilon_{ij}, \quad \varepsilon_M = M_{ij}\varepsilon_{ij} \quad (4.1)$$

where

$$N_{ij} = n_i n_j, \quad L_{ij} = (l_i n_j + l_j n_i) / 2, \quad M_{ij} = (m_i n_j + m_j n_i) / 2 \quad (4.2)$$

in which the subscripts  $i, j = 1, 2, 3$ , representing the directions along  $x_1, x_2$ , and  $x_3$ , respectively,  $\varepsilon_{ij}$  denotes the strain tensor, and  $n_i, m_i$ , and  $l_i$  are projections of unit vectors  $\mathbf{n}, \mathbf{m}$ , and  $\mathbf{l}$  on  $x_i$ . Repeated indices in the above equations denote summation over  $i, j = 1, 2, 3$ , e.g.,  $a_i b_i = a_1 b_1 + a_2 b_2 + a_3 b_3$ .

It is impossible for both the stress and strain components on the microplanes to be projections of the stress and strain tensors. Therefore, the static equivalence, or equilibrium, between the stress components,  $\sigma_N, \sigma_L$ , and  $\sigma_M$ , over all the microplanes and the stress tensor  $\boldsymbol{\sigma}$  are enforced in an approximate manner using the principle of virtual work (Bazant, 1984) as follows:

$$\frac{2\pi}{3} \sigma_{ij} \delta \varepsilon_{ij} = \int_{\Omega} (\sigma_N \delta \varepsilon_N + \sigma_L \delta \varepsilon_L + \sigma_M \delta \varepsilon_M) d\Omega \quad (4.3)$$

in which  $\Omega$  is the surface of a unit hemisphere centered at the material point, and  $2\pi/3$  is its volume. The above equation implies that the volume bounded by the microplanes, as shown in Figure 4.1(a), can be represented by a unit sphere, and that the virtual work of continuum stresses within a unit sphere is

equal to the virtual work of the stress components on the surface (microplanes) of the unit sphere. By substituting  $\delta\varepsilon_N = N_{ij}\delta\varepsilon_{ij}$ ,  $\delta\varepsilon_L = L_{ij}\delta\varepsilon_{ij}$ , and  $\delta\varepsilon_M = M_{ij}\delta\varepsilon_{ij}$  into the above equation, and noting that the equation must hold for any virtual strain  $\delta\varepsilon_{ij}$ , the following basic equilibrium relation is obtained:

$$\sigma_{ij} = \frac{3}{2\pi} \int_{\Omega} s_{ij} d\Omega \approx 6 \sum_{\mu=1}^{N_m} w_{\mu} s_{ij}^{(\mu)} \quad (4.4)$$

where

$$s_{ij} = \sigma_N N_{ij} + \sigma_L L_{ij} + \sigma_M M_{ij} \quad (4.5)$$

As shown in Eq. (4.4), the integral is approximated by an optimal Gaussian integration over a spherical surface (Stroud 1971, Bazant and Oh 1985), which is a weighted sum over  $N_m$  microplanes of orientations  $\mathbf{n}_{\mu}$ , with the weights  $w_{\mu}$  normalized so that  $\sum_{\mu=1}^{N_m} w_{\mu} = 1/2$ . The implemented microplane model has 37 microplanes.

The model has four strain-dependent strength (or yield) limits, enforced at the microplane level, called the stress-strain boundaries. These are the volumetric boundary,  $\sigma_V^b$ , the deviatoric boundary,  $\sigma_D^b$ , the normal boundary,  $\sigma_N^b$ , and the shear boundary,  $\sigma_T^b$ , which are presented in Figure 4.2. When the stresses are within the boundaries, the response is elastic. If, during a strain increment, the boundary is exceeded, the stress is reduced to the boundary keeping the strain constant, as illustrated for the normal stress,  $\sigma_N$ , in Figure 4.3.

The volumetric boundary,  $\sigma_V^b$ , is calculated by the following equation:

$$\sigma_V^b = -Ek_1k_3e^{-\varepsilon_V/k_1a} \quad (4.6)$$

in which  $E$  is the elastic modulus of the concrete, and  $k_1$  and  $k_3$  are parameters that need to be calibrated. The physical meaning and suggested values of these parameters are presented in Table 4.1. The volumetric strain,  $\varepsilon_v$ , for each microplane is calculated from the strain tensor in an incremental manner as follows:

$$\varepsilon_v = \varepsilon_v^o + \Delta\varepsilon_v \quad (4.7)$$

where

$$\varepsilon_v^o = \varepsilon_{kk}^o / 3 \quad \text{and} \quad \Delta\varepsilon_v = \Delta\varepsilon_{kk} / 3 \quad (4.8)$$

The superscript  $o$  in the above variables denotes the values attained in the previous step. The variable  $a$  in Eq. (4.6) is defined as follows:

$$a = \frac{k_5}{1 + \varepsilon_e} \left( \frac{\varepsilon_I^o - \varepsilon_{III}^o}{k_1} \right)^{c_{20}} + k_4 \quad (4.9)$$

in which  $k_4$  and  $k_5$  are parameters whose physical meaning and suggested values are presented in Table 4.1.  $\varepsilon_e$  is defined as:

$$\varepsilon_e = \left\langle -\sigma_v^o / E_{N0} \right\rangle \quad (4.10)$$

where  $\langle x \rangle = \max(x, 0)$  (the Macauley brackets),  $\sigma_v^o$  is the volumetric stress attained in the previous step, defined in Eq.(4.23), and  $E_{N0}$  is the undamaged elastic stiffness in the normal direction of the microplane and is calculated as:

$$E_{N0} = \frac{E}{1 - 2\nu} \quad (4.11)$$

with  $\nu$  being the Poisson's ratio, which is set to 0.18. The variables  $\varepsilon_I^o$  and  $\varepsilon_{III}^o$  denote the maximum and the minimum principal strains attained at the previous step. The difference of the principal strains helps to distinguish the compressive behavior of weakly confined concrete, which can have significant strain softening, from that of highly confined concrete, which has milder strain softening.

The deviatoric boundary,  $\sigma_D^b$ , is specified as:

$$\sigma_D^b = -\frac{Ek_1\beta_3}{1 + [\langle -\varepsilon_D \rangle / (k_1\beta_2)]^2} \quad (4.12)$$

where

$$\beta_2 = c_5\gamma_1 + c_7, \quad \beta_3 = c_6\gamma_1 + c_8, \quad \gamma_1 = e^{\gamma_0} \tanh(c_9 \langle -\varepsilon_V \rangle / k_1) \quad (4.13)$$

$$\gamma_0 = f'_{c0} / E_0 - f'_c / E \quad (4.14)$$

in which  $c_i$  ( $i = 5, 6, 7, 8, 9$ ) are parameters that need to be calibrated. The physical meaning and suggested values of these parameters, along with those others used in the calculation of the rest of the stress boundaries, are presented in Table 4.2. The values of parameters  $f'_{c0}$  and  $E_0$  are given in Table 4.2, while  $f'_c$  and  $E$  are the compressive strength and elastic modulus for the concrete being modeled. The deviatoric strain,  $\varepsilon_D$ , is calculated from the normal and volumetric strains as follows:

$$\Delta\varepsilon_D = \Delta\varepsilon_N - \Delta\varepsilon_V, \quad \varepsilon_D^o = \varepsilon_N^o - \varepsilon_V^o, \quad \varepsilon_D = \varepsilon_D^o + \Delta\varepsilon_D \quad (4.15)$$

The normal boundary,  $\sigma_N^b$ , is specified as:

$$\sigma_N^b = Ek_1\beta_1 e^{-\langle \varepsilon_N - \beta_1 c_2 k_1 \rangle / [-c_4 \varepsilon_e \operatorname{sgn}(\varepsilon_e) + k_1 c_3]} \quad (4.16)$$

in which

$$\beta_1 = -c_1 + c_{17}e^{-c_{19}(\varepsilon_e - c_{18})} \quad (4.17)$$

The elastic normal microplane stress (trial elastic stress) is calculated as:

$$\sigma_N^e = \sigma_N^o + E_N \Delta \varepsilon_N \quad (4.18)$$

in which  $E_N$  is the damaged value of the normal microplane elastic stiffness:

$$E_N = E_{N0} e^{-c_{13}\varepsilon_N^{0+}} f(\zeta) \quad \text{for } \sigma_N^o \geq 0 \quad (4.19)$$

but

$$E_N = E_{N0} \quad \text{if } \sigma_N^o \geq E_{N0}\varepsilon_N \quad \text{and } \sigma_N^o \Delta \varepsilon_N < 0 \quad (4.20)$$

$$E_N = E_{N0} \left( e^{-c_{14}|\varepsilon_N^{0-}|/(1+c_{15}\varepsilon_e)} + c_{16}\varepsilon_e \right) \quad \text{for } \sigma_N^o < 0 \quad (4.21)$$

in which  $\varepsilon_N^{0+}$  and  $\varepsilon_N^{0-}$  are the maximum and minimum normal strains reached so far. In Eq. (4.19),

$$f(\zeta) = (1 + a\zeta^2)^{-1}, \quad \text{with } \zeta = \int \langle d\varepsilon_v \rangle \quad \text{and } a = 0.1, \quad \text{which has been specified to avoid negative}$$

dissipation during load cycles. Accurate simulation of the closing of opened cracks during tensile unloading is attained with the stiffness degradation calculated with Eq. (4.19). Parameter  $c_{13}$  controls the unloading slope from tension, with a suggested value of 4,500 (see Table 4.2). Only those microplanes whose normals form a sufficiently small angle with the maximum principal strain direction can reach the post-peak regime. Other microplanes will remain elastic.

Having calculated the elastic normal stress and the volumetric, deviatoric and normal stress boundaries, the vertical drop of stress at constant strain to the stress-strain boundary for the normal stress, as shown in Figure 4.3, is enforced:

$$\sigma_N = \max \left[ \min \left( \sigma_N^e, \sigma_N^b \right), \sigma_V^b + \sigma_D^b \right] \quad (4.22)$$

The volumetric stress is calculated as the average value of the normal stress at every microplane:

$$\sigma_V \approx \frac{1}{2\pi} \sum_{\mu=1}^{N_m} w_{\mu} \sigma_N \quad (4.23)$$

The shear boundary,  $\sigma_T^b$ , is calculated as:

$$\sigma_T^b = \left[ \left( c_{10} \langle \hat{\sigma}_N^o - \sigma_N \rangle \right)^{-1} + (E_T k_1 k_2)^{-1} \right]^{-1} \quad \text{for } \sigma_N \leq 0 \quad (4.24)$$

$$\sigma_T^b = \left[ \left( c_{10} \hat{\sigma}_N^o \right)^{-1} + (E_T k_1 k_2)^{-1} \right]^{-1} \quad \text{for } \sigma_N > 0 \quad (4.25)$$

in which

$$E_T = E_{N0} \frac{1-4\nu}{1+\nu} \quad (4.26)$$

$$\hat{\sigma}_N^o = \langle E_T k_1 c_{11} - c_{12} \langle \varepsilon_V \rangle \rangle \quad (4.27)$$

The elastic shear microplane stress (trial stress) is:

$$\sigma_T^e = \sqrt{\left( \sigma_L^o + E_T \Delta \varepsilon_L \right)^2 + \left( \sigma_M^o + E_T \Delta \varepsilon_M \right)^2} \quad (4.28)$$

in which  $\sigma_L^o$  and  $\sigma_M^o$  are the shear stresses in the  $L$  and  $M$  directions of the microplane in the previous step, and  $\Delta\varepsilon_L$ ,  $\Delta\varepsilon_M$  the equivalent strain increments.

The shear stress return to the boundary is calculated by the following equations:

$$\sigma_T = \min(\sigma_T^b, |\sigma_T^e|) \quad (4.29)$$

$$\sigma_L = (\sigma_L^o + E_T \Delta\varepsilon_L) \sigma_T / \sigma_T^e \quad (4.30)$$

$$\sigma_M = (\sigma_M^o + E_T \Delta\varepsilon_M) \sigma_T / \sigma_T^e \quad (4.31)$$

Having calculated the normal stress,  $\sigma_N$ , and the shear-stress components,  $\sigma_L$  and  $\sigma_M$ , at every microplane, the stress tensor,  $\sigma_{ij}$ , at every integration point is obtained through Eq. (4.4) and (4.5).

The fact that the stress-strain boundaries are reached at different microplanes at different moments of loading is what causes both the pre-peak and post-peak macro-level stress-strain curves to vary their slope gradually. Similarly during macroscopic unloading, different microplanes have the stresses returning into the elastic domain at different moments, which again causes the unloading curves to change the unloading slope gradually.

The calibration of the microplane model involves the determination of the parameters  $E$ ,  $k_i$  and  $c_j$ , which govern the stress-strain boundaries at every microplane. The values shown in Table 4.1 and Table 4.2 are suggested by Caner and Bazant (2013b), and will result in a uniaxial compressive strength of 46.7 MPa and the compressive strain at the peak stress equal to 0.0033, which can be confirmed numerically. To have a different concrete strength, strain at the peak stress, and post-peak behavior under uniaxial compression, the values of  $E$  and  $k_i$  have to be changed, while those of  $c_j$  can remain the same.



In fact, with the set of parameters that determine the reference concrete properties, the desired uniaxial compressive strength,  $f'_c$ , and compressive strain at the peak stress,  $\varepsilon_p$ , can be obtained solely with the values of  $k_1$  and  $E$  calculated with the following equations:

$$k_1 = \tilde{k}_1 \frac{\varepsilon_p}{\tilde{\varepsilon}_p} \quad \text{and} \quad E = \tilde{E} \frac{f'_c}{\tilde{f}'_c} \frac{\tilde{\varepsilon}_p}{\varepsilon_p} \quad (4.32)$$

in which  $\tilde{k}_1$  and  $\tilde{E}$  are the values of the parameters that result in the reference properties  $\tilde{f}'_c$ , and  $\tilde{\varepsilon}_p$ .

For the parameters shown in Table 4.1 and Table 4.2, we have  $\tilde{k}_1 = 1.1 \cdot 10^{-4}$ ,  $\tilde{E} = 25,000$  MPa,  $\tilde{f}'_c = 46.7$  MPa, and  $\tilde{\varepsilon}_p = 0.0033$ . Changing the value of  $E$  results in a vertical scaling transformation of the stress-strain curve, such that all the stresses are scaled by the ratio  $E / \tilde{E}$  with no change of strains. Changing the value of  $k_1$  results in a radial scaling of the stress-strain curve, in which all the distances from the origin are scaled by the ratio  $k_1 / \tilde{k}_1$ .

## 4.2 Validation and Calibration of the Microplane model

The microplane model has been calibrated and verified by Caner and Bazant (2013b) for a range of strain histories. In this study, the performance of the model in capturing the compressive behavior of confined concrete has been further examined. For this purpose, the tests of Hurlbut (1985) on the compressive behavior of concrete under different lateral confining stresses, the test by van Mier (1986) on the uniaxial compressive behavior of unconfined concrete, and the tests of Mander et al. (1988b) on the compressive behavior of circular columns with different amounts of lateral steel confinement are considered. For these analyses, the default values of some of the modeling parameters have been changed as shown in Table 4.3.

The finite element (FE) model used to simulate the tests of Hurlbut (1985) is presented in Figure 2.8. The default values of  $k_i$  (for  $i = 2, \dots, 5$ ) and  $c_j$  (for  $j = 1, \dots, 20$ ), which are presented in Table 4.1 and Table 4.2, are first used, while  $E = 26,030 \text{ MPa}$  and  $k_1 = 0.5 \cdot 10^{-4}$  (see Table 4.3), which have been selected to capture the compressive behavior of the concrete. As shown in Figure 4.4, the microplane model is capable of reproducing the effect of the lateral confining stress on the compressive strength and the post-peak slope of the stress-strain curve. However, for the case of uniaxial compression with no confining stress, the microplane model shows a relatively ductile behavior, with the stress-strain curve similar to that for the 100-psi confining stress. To examine this further, the uniaxial compression test of van Mier (1986) is considered. As shown in Figure 4.5, the microplane model demonstrates a more ductile post-peak behavior than the test. To have a more brittle behavior under uniaxial compression, the model has been re-calibrated with the values of  $k_2$  and  $k_3$  changed to one. With  $k_2 = k_3 = 1$ ,  $E = 27,865 \text{ MPa}$ , and  $k_1 = 1.65 \cdot 10^{-4}$ , the model gives  $f'_c = 21.4 \text{ MPa}$  and  $\varepsilon_p = 0.0015$ . As shown in Figure 4.5, this results in a much better match of the test data. This value of  $k_2$  and  $k_3$  is used for unconfined concrete in all subsequent analyses, as shown in Table 4.3.

With the aforementioned recalibration, the microplane model was further evaluated with the experimental results of Mander et al. (1988b) on the compressive behavior of circular-sectioned RC columns with different amounts of lateral confining steel. The calibration of the model to yield the concrete properties of the tests is summarized in Table 4.3. The same FE model as that presented in Figure 2.12 is used. However, in contrast to the damaged-plasticity model, which requires different input uniaxial compressive stress-strain relations for different amounts of confining steel, as discussed in Chapter 2, the microplane model uses the same calibration for different confinement levels. As shown in Figure 4.6, the FE model satisfactorily captures the effect of the lateral confining steel on the compressive strength and the ductility of the RC columns.

Unlike the damaged-plasticity model provided in Abaqus (Simulia, 2012), the microplane model is able to simulate the tensile unloading and reloading behavior of concrete in an accurate manner. To demonstrate this, a single solid element, as shown in Figure 4.7, is subjected to uniaxial cyclic tension and compression. Both the damaged-plasticity model and the microplane model are considered. Figure 4.8 shows the stress-strain curves obtained with the two different constitutive models. It can be seen that the damaged-plasticity model shows early crack closing with an unrealistically large residual tensile strain due to its inability to represent severe degradation of the tensile stiffness during unloading, as pointed out in Chapter 2, while the microplane model shows a satisfactory performance.

### **4.3 Finite Element Analysis of pile specimens with the microplane model**

The microplane model is used in the finite element analysis of the pile specimens tested by Papadopoulos and Shing (2014). As shown in Figure 4.9, the FE model for the pile specimens is similar to the one presented in Section 3.1, except that the contact conditions at the pile-footing interface have been eliminated. This is because the microplane model can adequately simulate the opening and closing of flexural cracks. Table 4.3 summarizes the values of  $E$  and  $k_1$  selected to match the properties of the concrete in the piles. The longitudinal bars and the confining hoops are modeled in the same way as that presented in Section 3.1. Bond-slip between the concrete and the longitudinal bars is also modeled in the same manner.

#### **4.3.1 Specimen #1**

Figure 4.10 shows the lateral load-vs.-top drift curves obtained for Specimen #1 by the test and the FE model. The curve from the FEA matches the test result well in terms of the lateral-load capacity, the post-peak behavior, and the pinching due to the opening and closing of flexural cracks. The drop of the lateral-load resistance at the 2<sup>nd</sup> cycle of 10% drift, due to the fracture of the longitudinal bars, is also reproduced by the FEA with the use of the phenomenological LCF law for steel presented in Section 2.2.2. Figure

4.11 shows the deformed shape of Specimen #1 at the end of the 2<sup>nd</sup> cycle of 10% drift. With the elimination of the contact conditions at the pile-footing interface, flexural cracking tends to largely concentrate in the first layer of the concrete elements at the base of the pile. The opening and closing of flexural cracks is accurately simulated. Figure 4.12 and Figure 4.13 show the axial stress-strain responses of concrete cover and core elements at the toe of the pile in Specimen #1. The microplane model is capable of accurately simulating the opening and closing of flexural cracks.

As shown in Figure 4.12, an element in the concrete cover experiences large tensile strains, which goes back to almost zero before developing a maximum compressive stress of 6 ksi, which is slightly larger than the prescribed unconfined compressive strength of 5 ksi. This slight increase in strength can be attributed to the confinement effect provided by the footing. Similar observations can be made for an element in the concrete core, which develops a high compressive stress of 9 ksi due to the confinement provided by the transverse reinforcement.

Table 4.4 summarizes the cycles in which the longitudinal bars of Specimen #1 fractured in the test and in the FEA, showing a close correlation of the experimental and numerical results. The positions of Bars 1 and 4, along with the cycles in which they fracture in the FEA, are shown in Figure 4.14.

The strains in the longitudinal bars on the south side of the pile at different drift levels are plotted in Figure 4.17 through Figure 4.19. The strains predicted in the FEA are compared to the test results in these plots. In general, the numerical results match the test data well. However, at locations close to the pile-footing interface, the tensile strain in Bar 1, which is at the extreme position on the south side, at pile drift ratios of 1% and 4% is significantly over-estimated in the FEA. As discussed in Sec. 3.2.3, one possible explanation is that the damage of the concrete and the bond at the base of the pile at these drift levels can be slightly under-estimated by the FE model and the tensile strain in a bar is highly sensitive to the damage. It is interesting to note that the FEA accurately captures the strains in the longitudinal bars embedded inside the footing.

### **4.3.2 Specimen #2**

Specimen #2, which consisted of 10 No. 9 longitudinal bars, is also modeled with the microplane model. Figure 4.15 shows the good match of the lateral load-vs.-top drift curves obtained from the test and the FEA. The numerical results for Specimen #2 are similar to those for Specimen #1. Table 4.5 summarizes the cycles in which the bars fractured in the test and in the FEA. The FE model is able to accurately predict the LCF of the longitudinal bars. Figure 4.16 shows the positions of the longitudinal bars, along with the cycles in which the bars fractured.

Similar to the analyses presented in Chapter 3, the results here show that the difference in the lineal spacing of longitudinal bars for the two specimens does not have any effect on the ductility of the lateral load-vs.-drift ratio response. The size of the longitudinal bars, however, can have an effect to the ductility of the pile. The No. 9 longitudinal bars of Specimen #2, fractured earlier than the No. 11 longitudinal bars of Specimen #1. Smaller-diameter bars are less resistant to buckling for the same spacing of the transverse reinforcement, and can therefore lead to a less ductile behavior of a laterally loaded RC member.

The strains in the longitudinal bars placed on the south side of the pile at different drift levels are shown in Figure 4.20 through Figure 4.22. Except for some discrepancies observed at the pile-footing interface, like those observed for Specimen 1, the strains in the longitudinal bars obtained from the FE model satisfactorily match the experimental data.

### **4.3.3 Flexural Crack Pattern**

Figure 4.23 shows the normal strains developed in concrete, in the axial direction of the pile, at a drift ratio of 1% in the FEA of the two pile specimens. In this figure, flexural cracks can be identified as localized tensile strains. The maximum tensile strains developed in Specimen #1 are larger than those in Specimen #2, consistent with the experimental observations. Moreover, the flexural cracks in Specimen

#2 spread over a larger distance than those in Specimen #1. However, the spacings of the flexural cracks are more or less the same for the two cases, with Specimen #2 showing a slightly smaller spacing between the first two cracks near the base.

#### **4.4 Summary and Conclusions**

The new microplane model developed by Caner and Bazant (2013a) has been implemented in a user-defined subroutine in Abaqus (Simulia 2012) and has been calibrated and verified with the tests of Hurlbut (1985), van Mier (1986) and Mander et al. (1988b). It has been employed to analyze the nonlinear behavior of the RC pile specimens tested by Papadopoulos and Shing (2014). The microplane model can simulate the nonlinear behavior of concrete more accurately than the damaged-plasticity model. More specifically, it can adequately represent large stiffness degradation during unloading and reloading in tension. Thus, the finite element models can accurately capture the pinching effect in the load-displacement curve for a pile. Furthermore, the microplane model can accurately reproduce both the enhanced compressive strength and the more ductile post-peak behavior of confined concrete. The damaged-plasticity model can only reproduce the enhanced compressive strength but not the enhanced ductility of confined concrete. Even though this limitation of the damaged-plasticity model can be artificially circumvented by modifying the input uniaxial compressive behavior of concrete, the remedy is far from exact. It cannot represent the variation of confinement pressure across a member section. While this may not be an important issue for tension-controlled flexural members, it can lead to inaccurate results for compression-controlled members, such as members subjected to high axial loads.

Table 4.1 – Free parameters of microplane model by Caner and Bazant (2013b)

Parameter	Value	Description
$\nu$	0.18	Poisson's ratio
$E$	25,000 MPa	Elastic modulus
$k_1$	$1.1 \cdot 10^{-4}$	Radial scaling parameter
$k_2$	110	Controls the horizontal asymptote value in the shear boundary
$k_3$	30	Controls the shape of the volumetric boundary
$k_4$	100	Controls the shape of the volumetric boundary
$k_5$	0.0001	Controls the volumetric-deviatoric coupling at low pressures

Table 4.2 – Fixed parameters of microplane model by Caner and Bazant (2013b)

Parameter	value	meaning
$f'_{c0}$	15.1 MPa	Reference compressive strength for low-strength concrete
$E_0$	20,000 MPa	Reference elastic modulus for low-strength concrete
$c_1$	0.089	Controls the uniaxial tensile strength
$c_2$	0.176	Controls the roundness of the peak in uniaxial tension
$c_3$	4	Controls the slope of the post-peak tail in uniaxial tension
$c_4$	50	Controls the slope of the post-peak tail in uniaxial compression
$c_5$	3,500	Controls the volumetric expansion under compression
$c_6$	20	Controls the roundness of the peak in volumetric expansion under compression
$c_7$	1	Controls the slope of the initial post-peak curve in uniaxial compression
$c_8$	8	Controls the peak strength in uniaxial compression
$c_9$	0.012	Controls the peak roundness in uniaxial compression
$c_{10}$	0.33	Controls the effective friction coefficient
$c_{11}$	0.5	Initial cohesion in frictional response
$c_{12}$	2.36	Controls the change of cohesion with tensile volumetric strains
$c_{13}$	4,500	Controls the unloading slope in tension
$c_{14}$	300	Controls the unloading slope at low hydrostatic compression
$c_{15}$	4,000	Controls the transition from unloading slope at high confinement to that at low confinement

$c_{16}$	60	Controls the unloading slope at high hydrostatic compression
$c_{17}$	1.4	Controls the tensile strength
$c_{18}$	0.0016	Controls the tensile cracking under compression
$c_{19}$	1,000	Controls the tensile softening rate under compression
$c_{20}$	1.8	Controls the volumetric-deviatoric coupling at high pressures

Table 4.3 – Calibration of microplane model

Test	Concrete	$k_2, k_3$	$E$ (MPa)	$k_1$ ( $\times 10^{-4}$ )	$f'_c$ (MPa), $\varepsilon_p$
Hurblut (1985)	Confined	default	26,030	0.5	22.1, 0.0015
van Mier (1986)	Unconfined	default	25,200	0.5	21.4, 0.0015
	Unconfined	1, 1	27,865	1.65	21.4, 0.0015
Mander et al. (1988b)	Confined	default	34,035	0.5	28.9, 0.0015
	Unconfined	1, 1	37,630	1.65	28.9, 0.0015
Papadopoulos and Shing (2014)	Confined	default	40,630	0.5	34.5, 0.0015
	Unconfined	1, 1	44,920	1.65	34.5, 0.0015

Table 4.4 – Cycles at which bars fractured in Specimen #1

Bar no.	Bar fracture in test	Bar fracture in FEA
1	2 <sup>nd</sup> cycle at +10%	1 <sup>st</sup> cycle at -10%
4	2 <sup>nd</sup> cycle at -10%	2 <sup>nd</sup> cycle at +10%

Table 4.5 – Cycles at which bars fractured in Specimen #2

Bar no.	Bar fracture in test	Bar fracture in FEA
1	1 <sup>st</sup> cycle at +10%	2 <sup>nd</sup> cycle at +8%
4	1 <sup>st</sup> cycle at -10%	2 <sup>nd</sup> cycle at -8%
3, 5	1 <sup>st</sup> cycle at -10%	1 <sup>st</sup> cycle at -10%
2, 6	no fracture	2 <sup>nd</sup> cycle at +10%



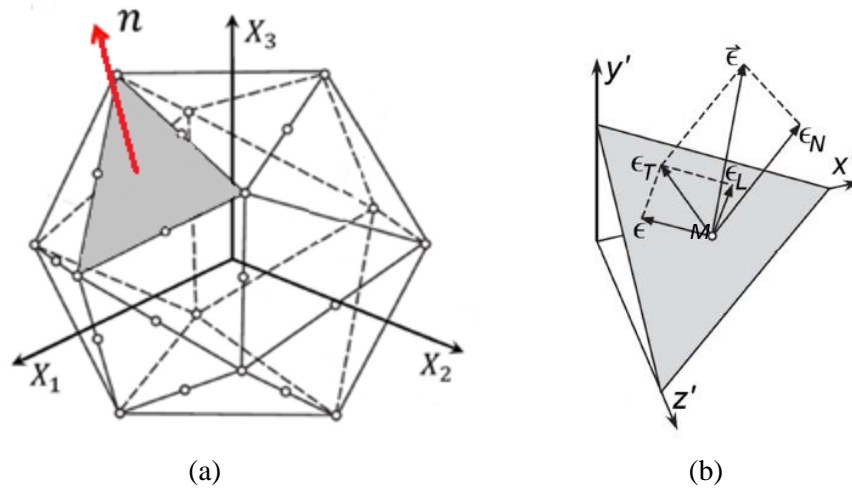


Figure 4.1 – (a) System of discrete microplanes, (b) Microplane strain vector and its components (Caner and Bazant, 2013a)

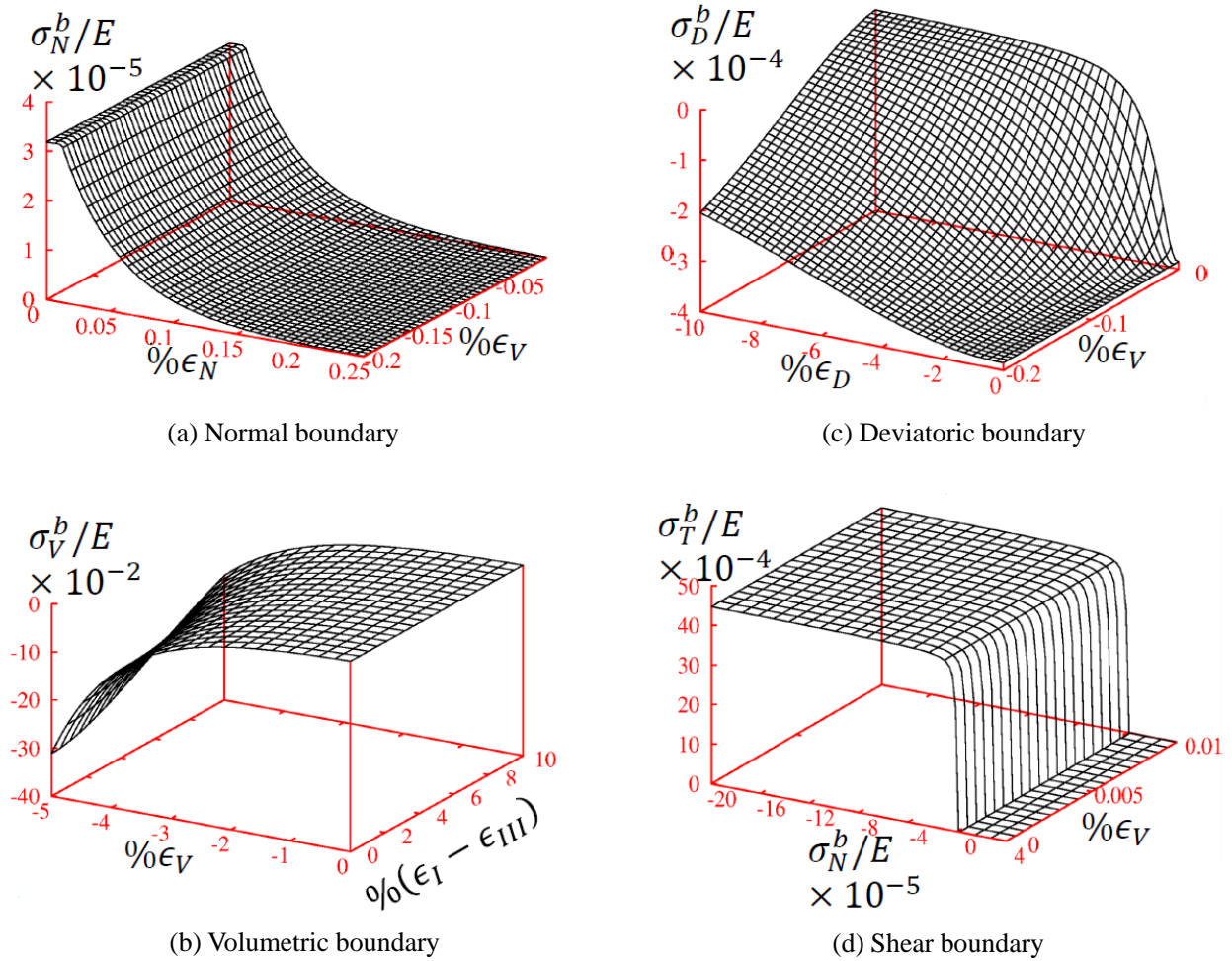


Figure 4.2 – Stress-strain boundaries of the microplane model (Caner and Bazant, 2013a)

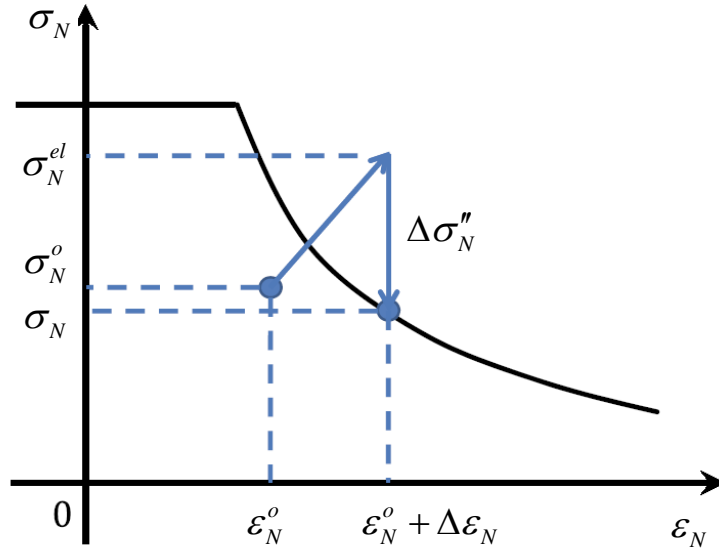


Figure 4.3 – Vertical return to normal boundary when the boundary is exceeded by an elastic trial stress in a finite load step (Caner and Bazant, 2013a)

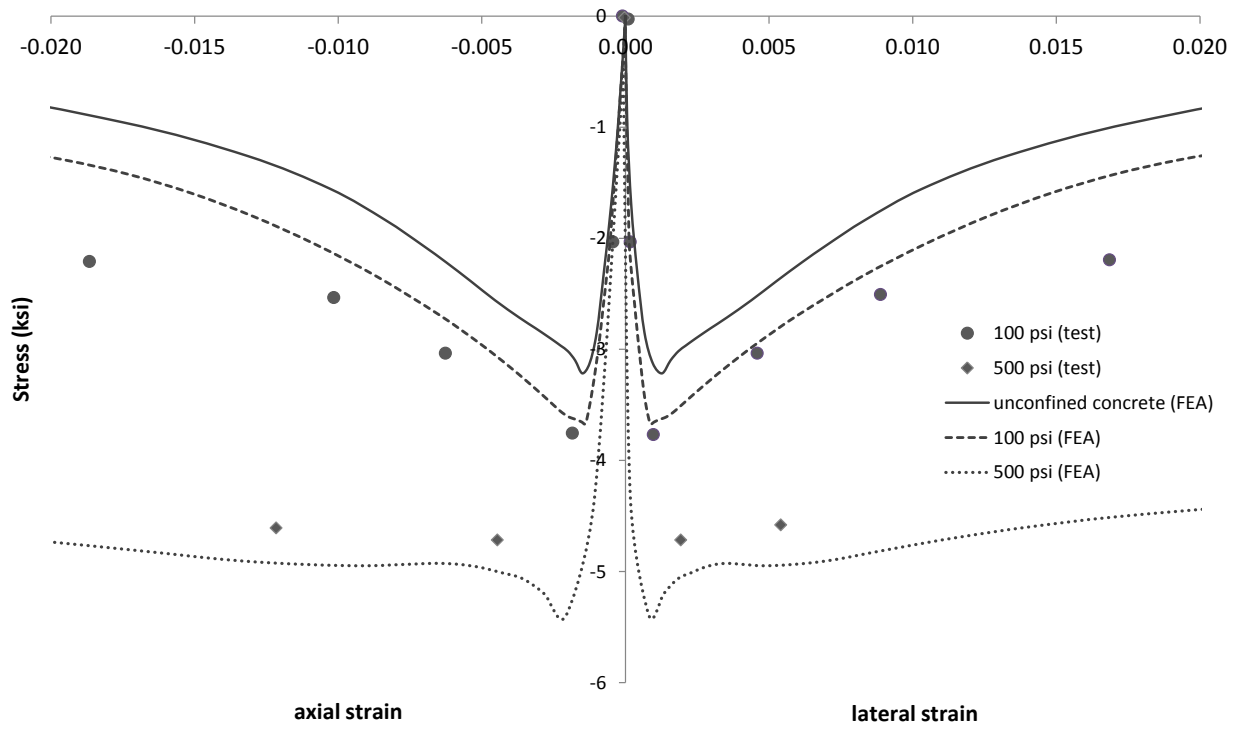


Figure 4.4 – Comparison of microplane model with default parameters to experimental results by Hurlbut (1985)

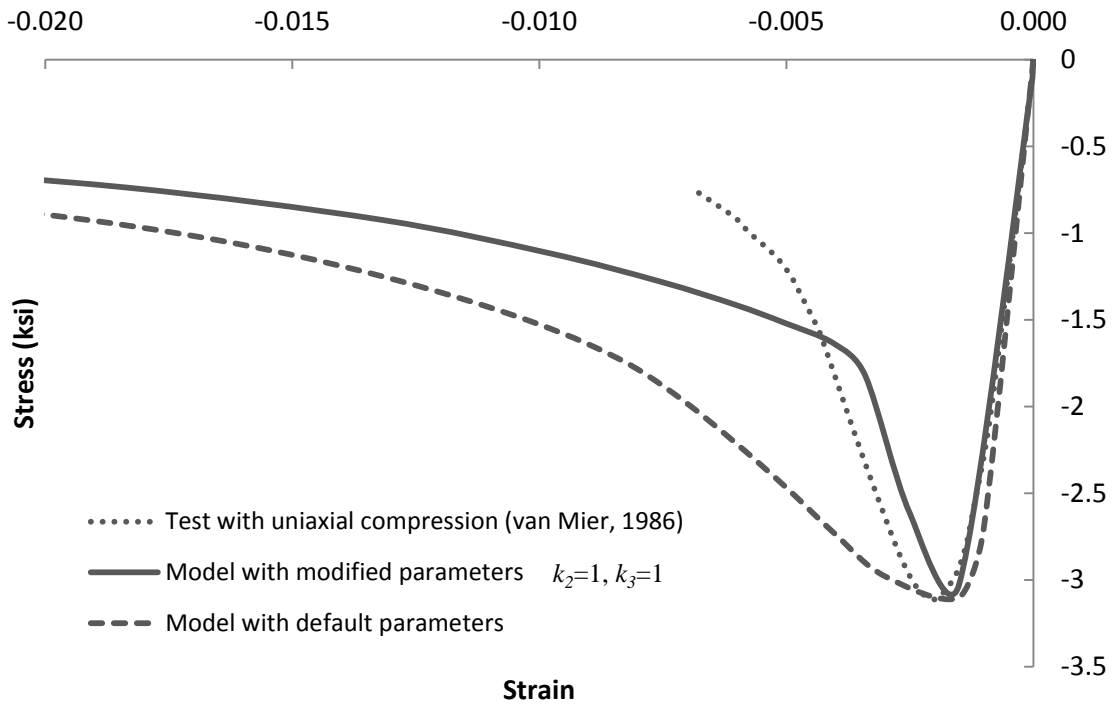
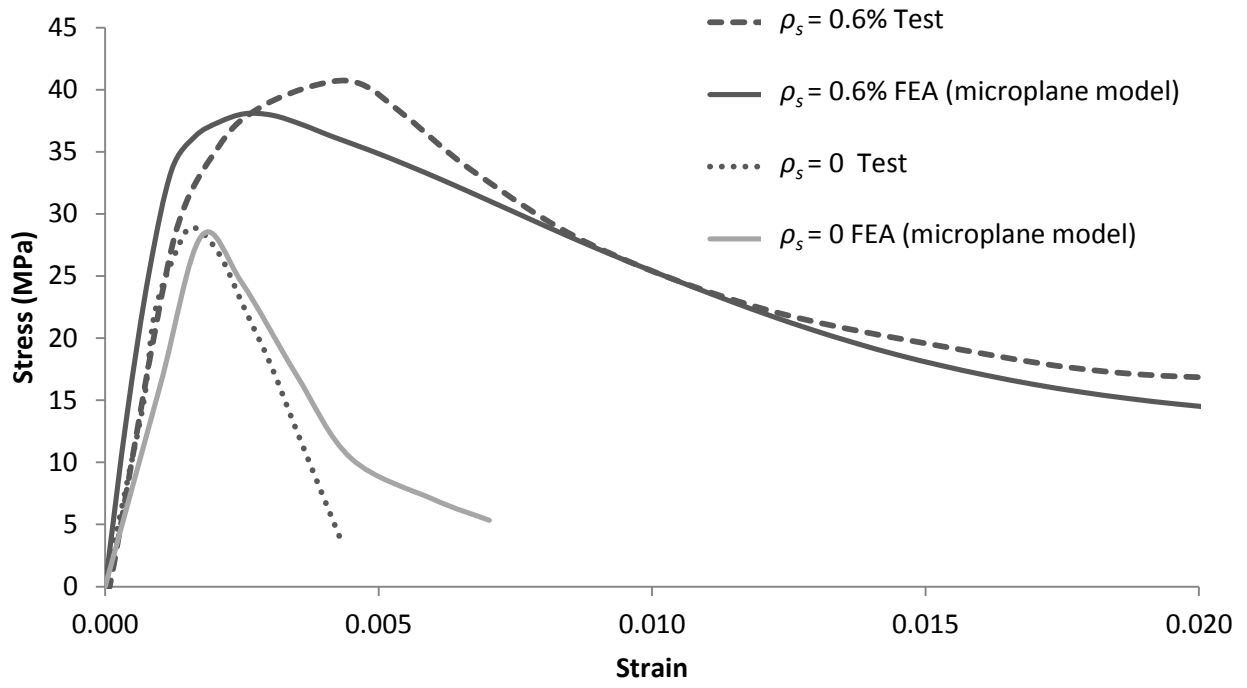
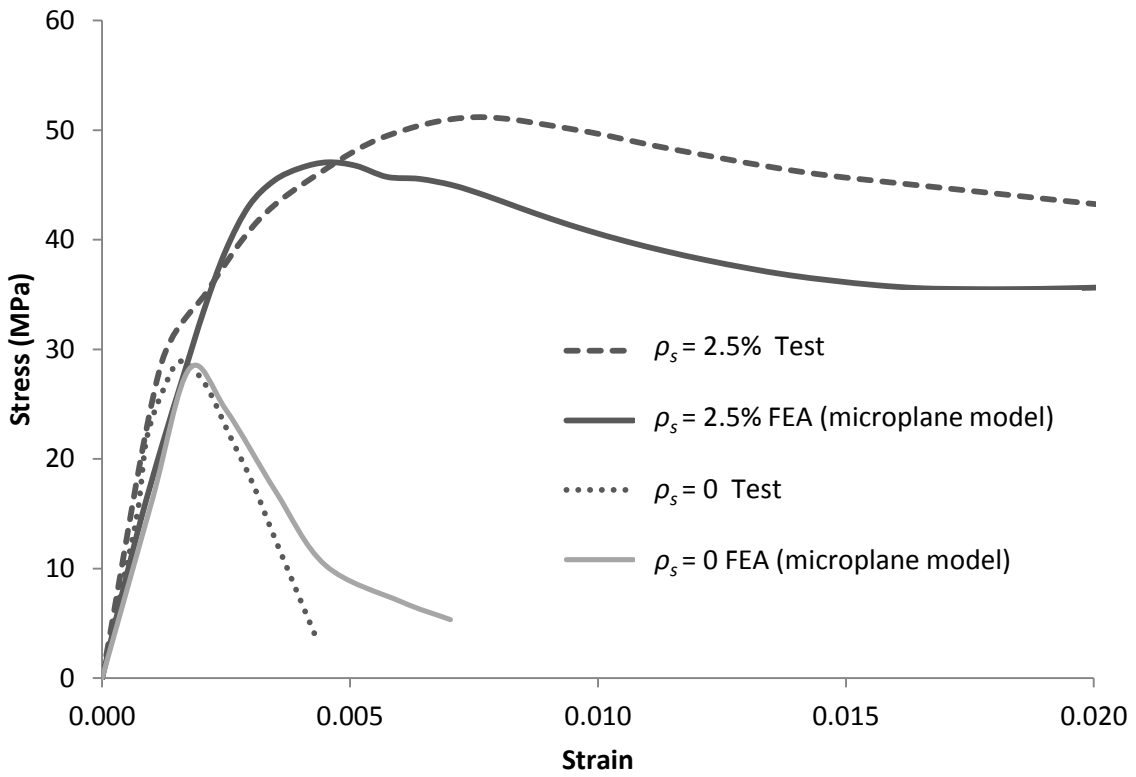


Figure 4.5 – Comparison of microplane model to uniaxial compression test by van Mier (1986)



(a)  $\rho_s = 0.6\%$



(b)  $\rho_s = 2.5\%$

Figure 4.6 – Comparison of microplane model to experimental results by Mander et al. (1988b)

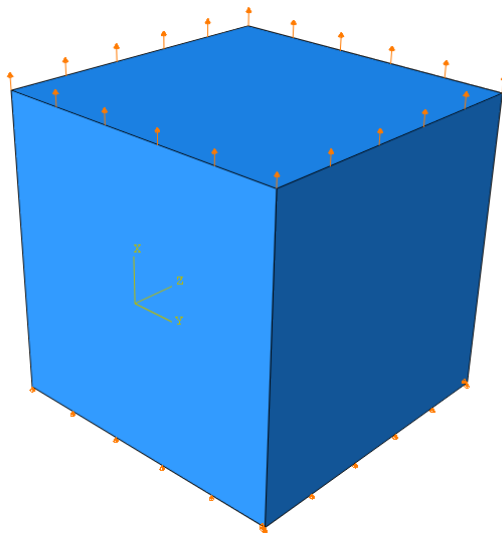


Figure 4.7 – Model for cyclic loading in tension

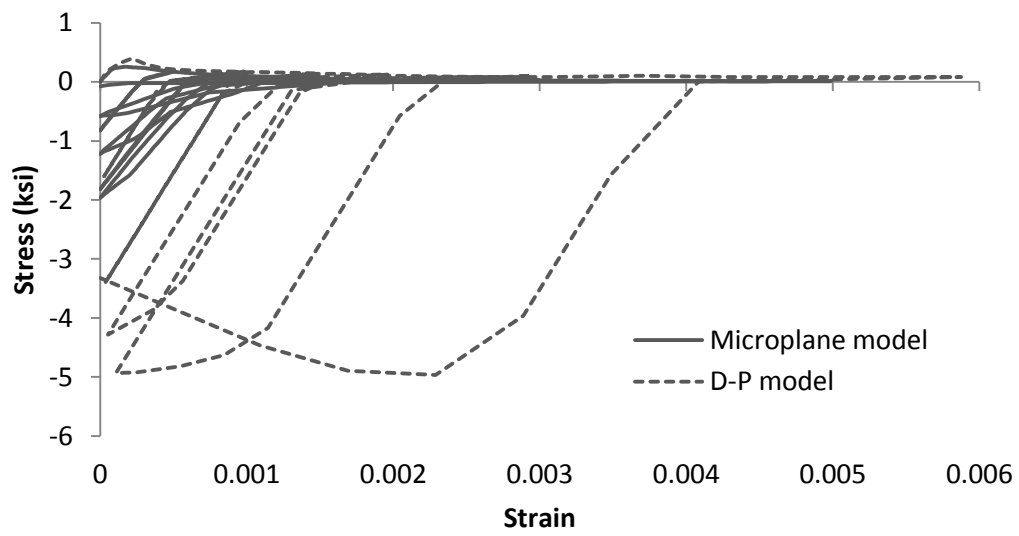


Figure 4.8 – Comparison of microplane model and D-P model under cyclic loading in tension

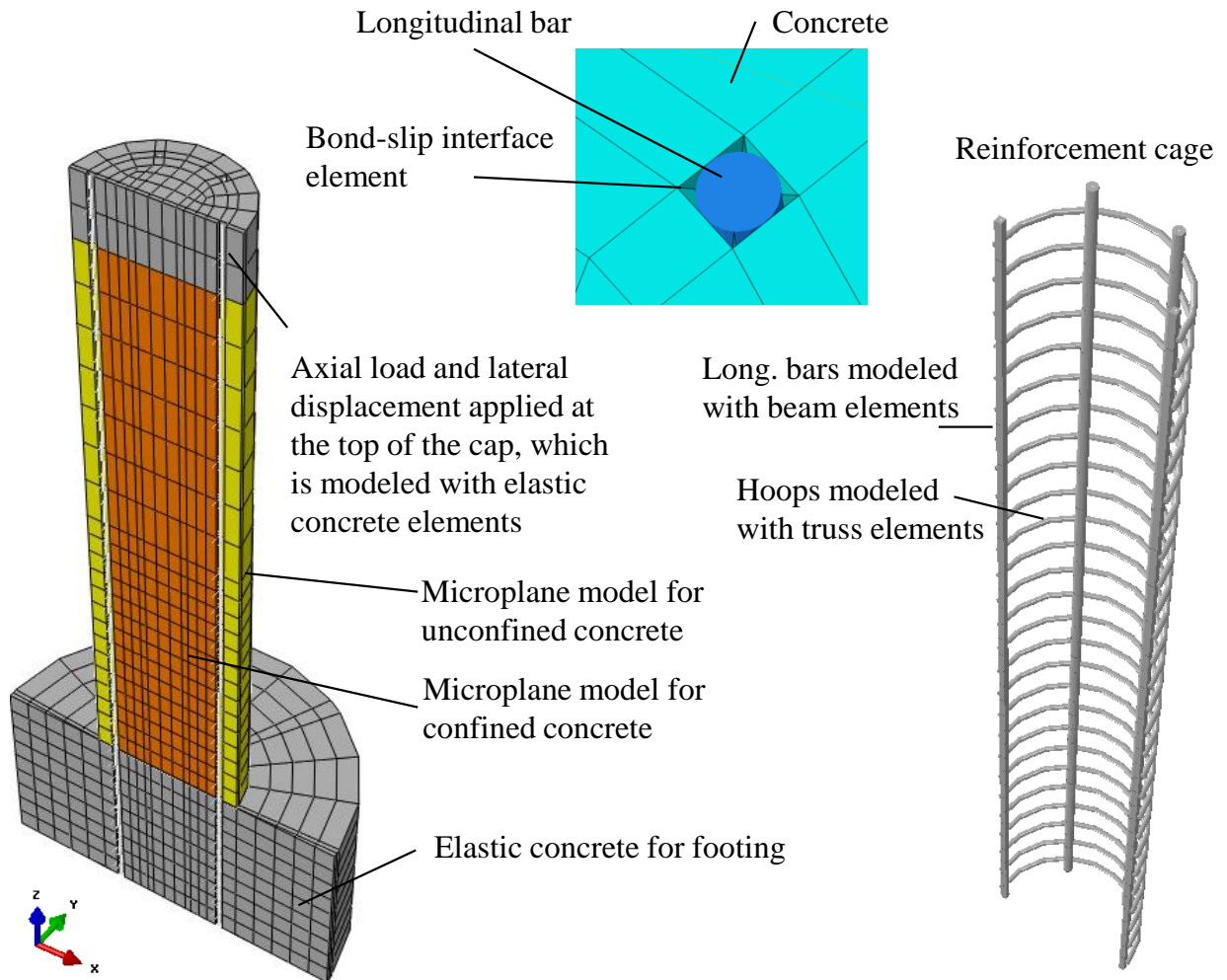


Figure 4.9 – FE model of Specimen #1 assembly with microplane model for concrete

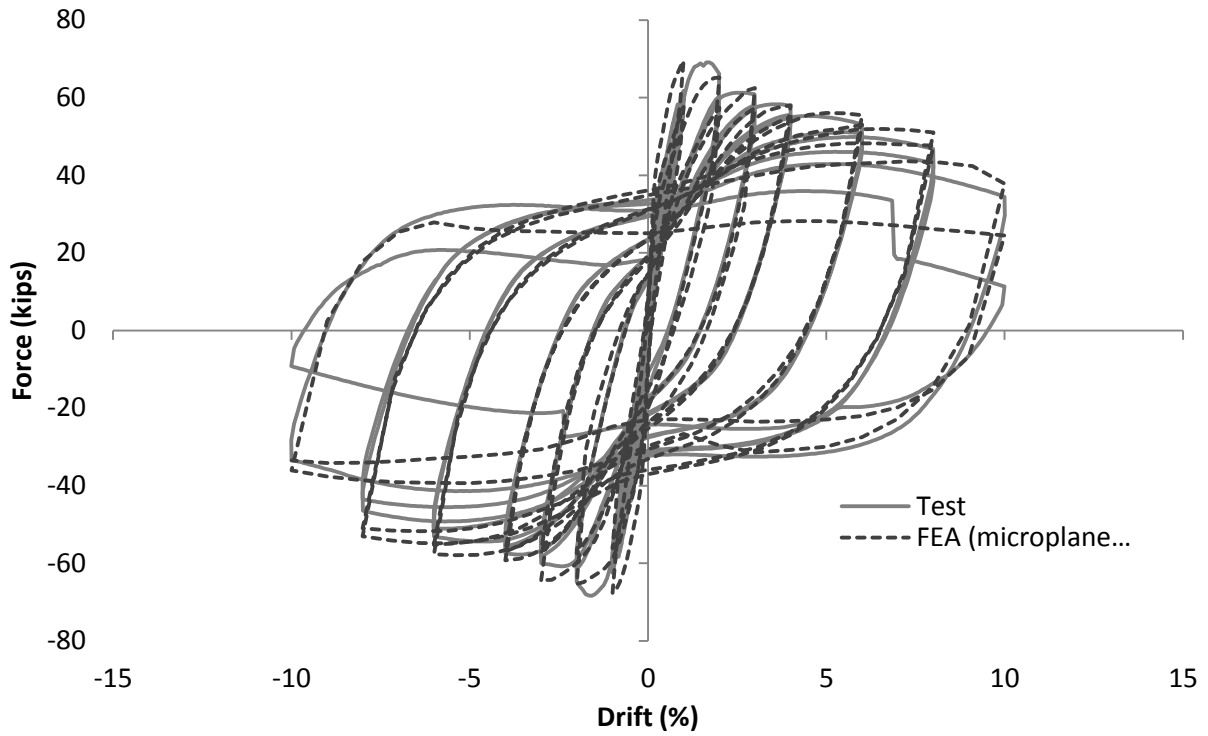


Figure 4.10 – Lateral load-vs.-top drift ratio curves for Specimen #1

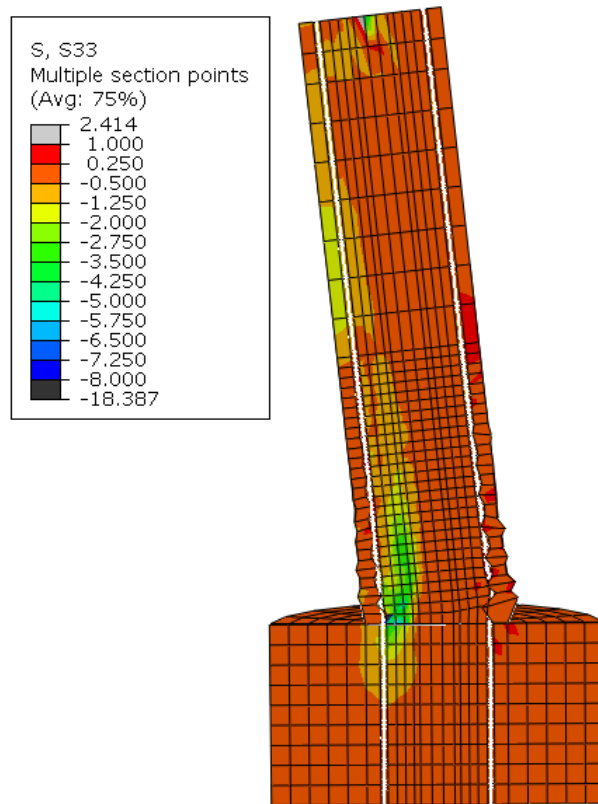


Figure 4.11 – Deformed shape of FE model of Specimen #1 at 10% drift

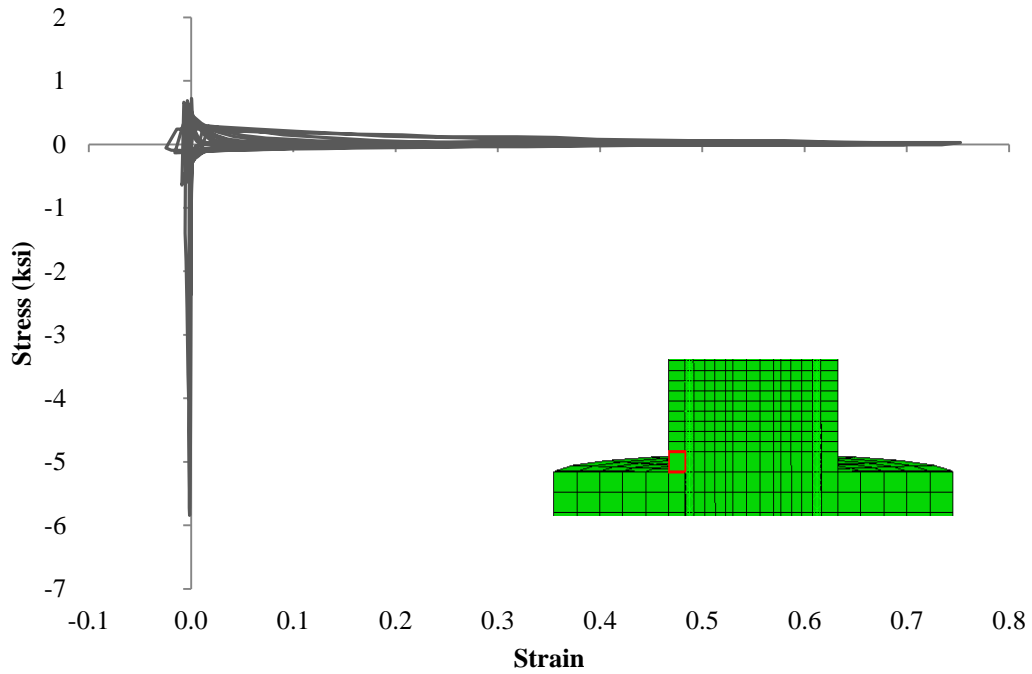


Figure 4.12 – Axial stress-strain curve for cover concrete at the base of Specimen #1

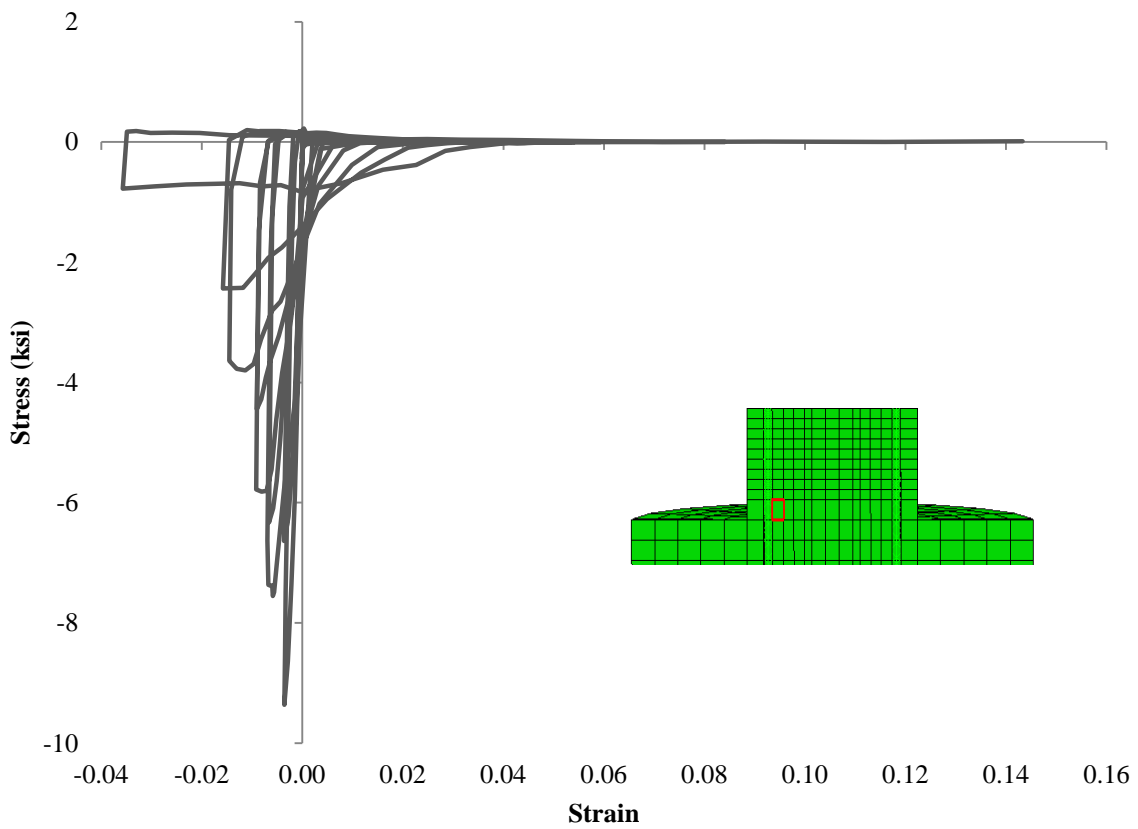


Figure 4.13 – Axial stress-strain curve for core concrete at the base of Specimen #1



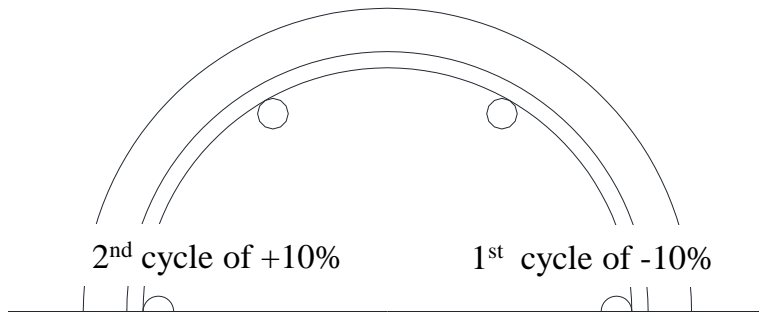


Figure 4.14 – Cycles at which bars fracture in the FEA of Specimen #1

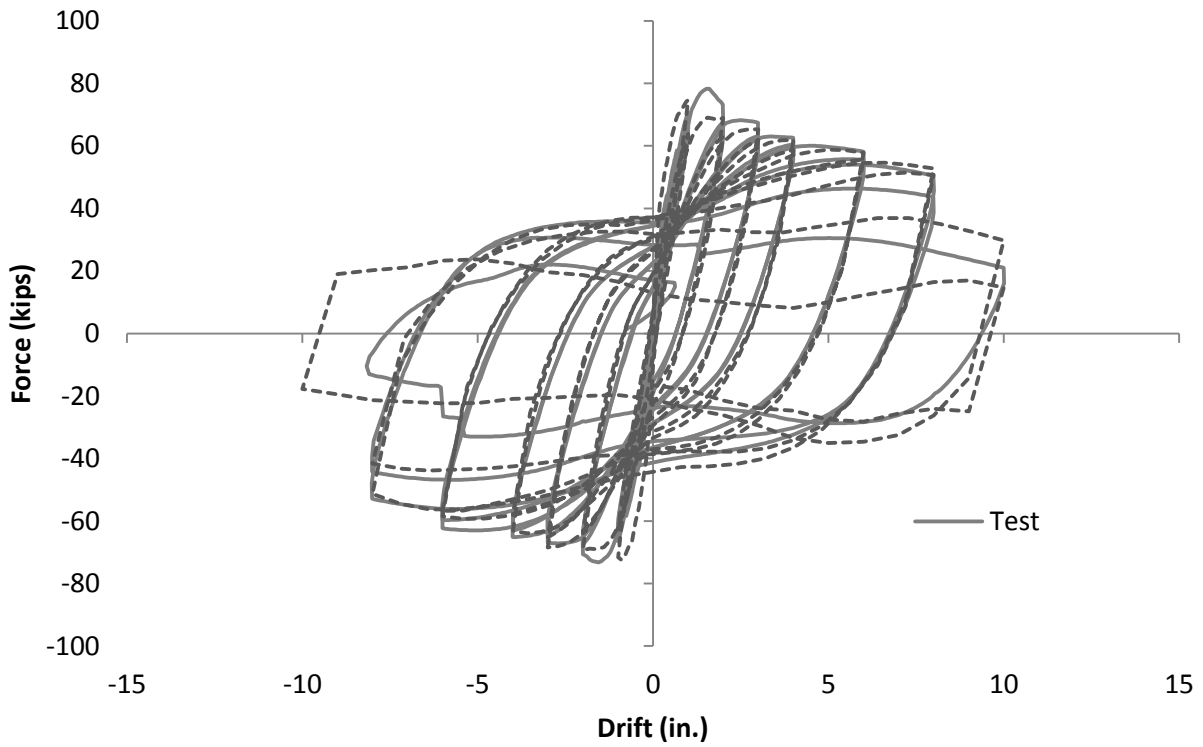


Figure 4.15 – Lateral load-vs.-top drift ratio curves for Specimen #2

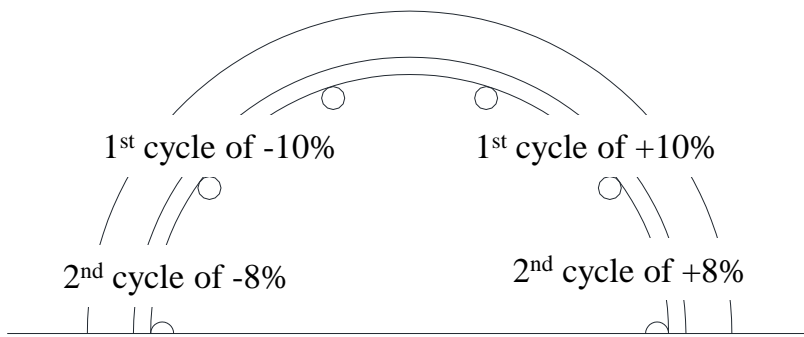


Figure 4.16 – Cycles at which bars fracture in the FEA of Specimen #2

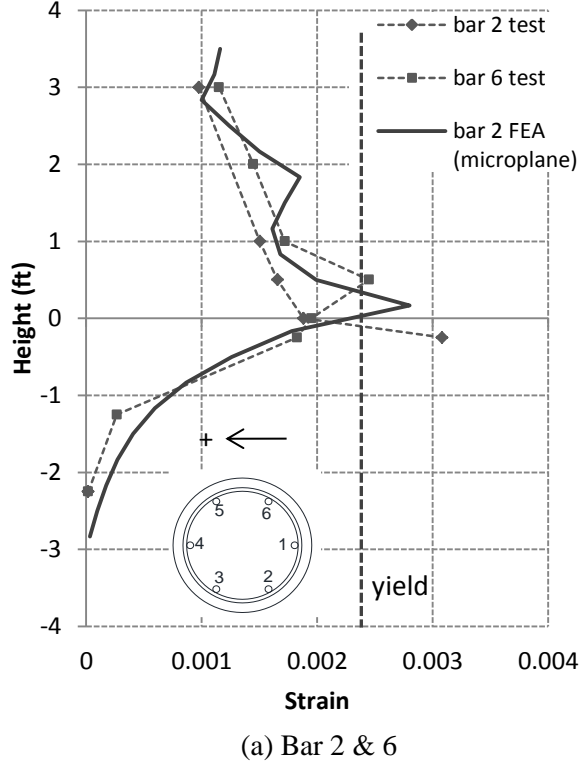
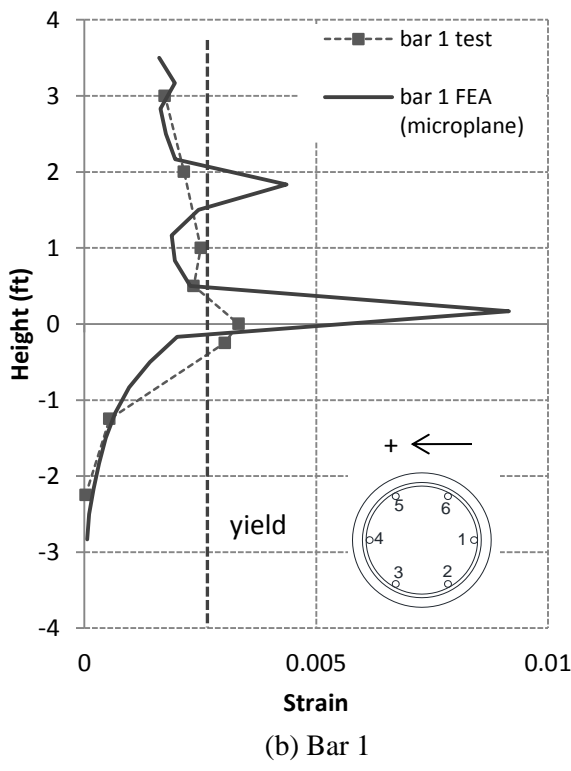


Figure 4.17 – Strains in bars at south face of Specimen #1 at +1% drift

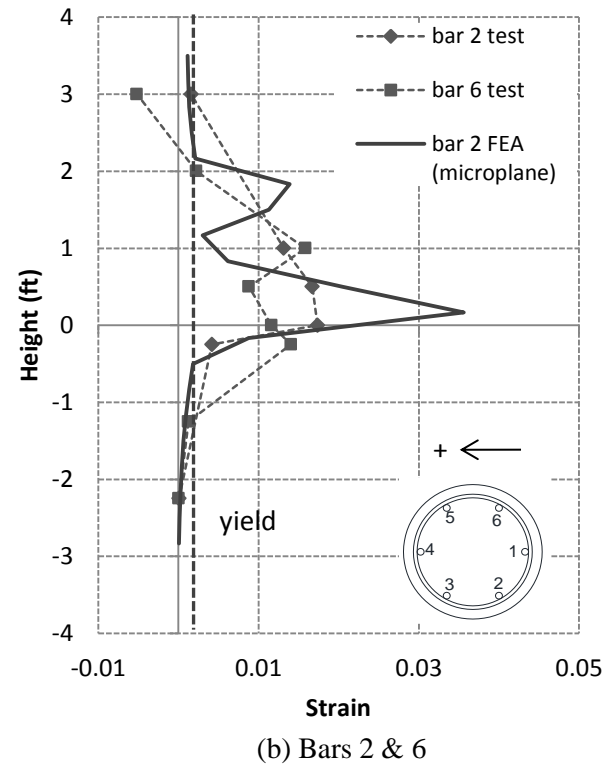
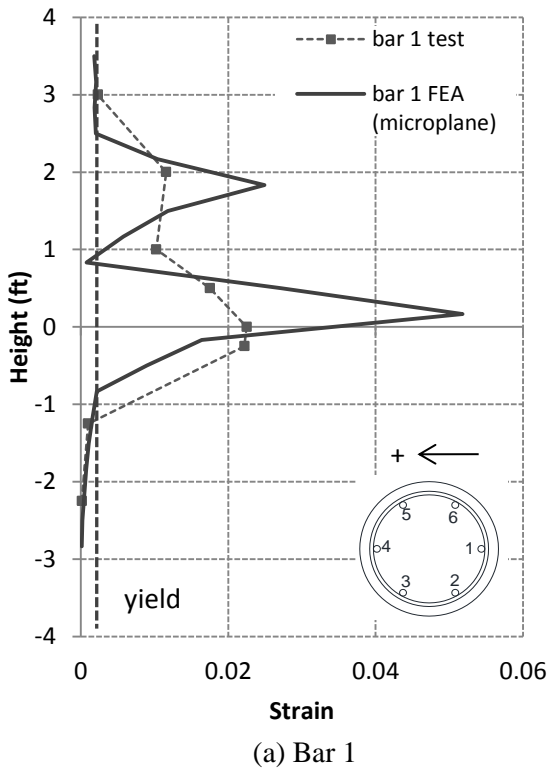
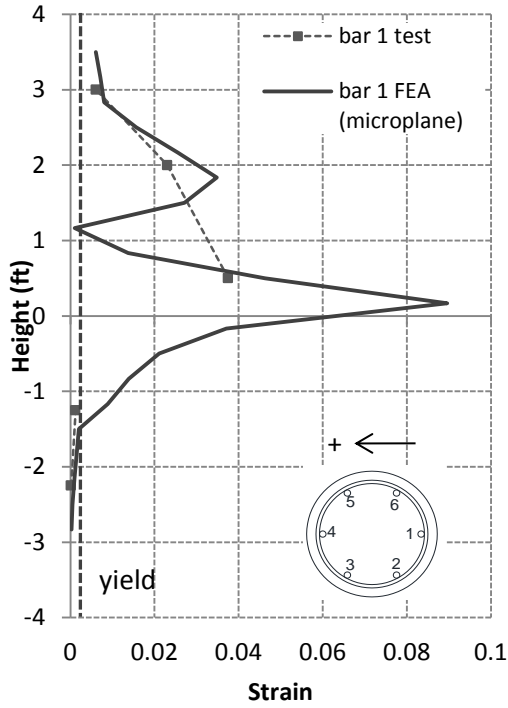
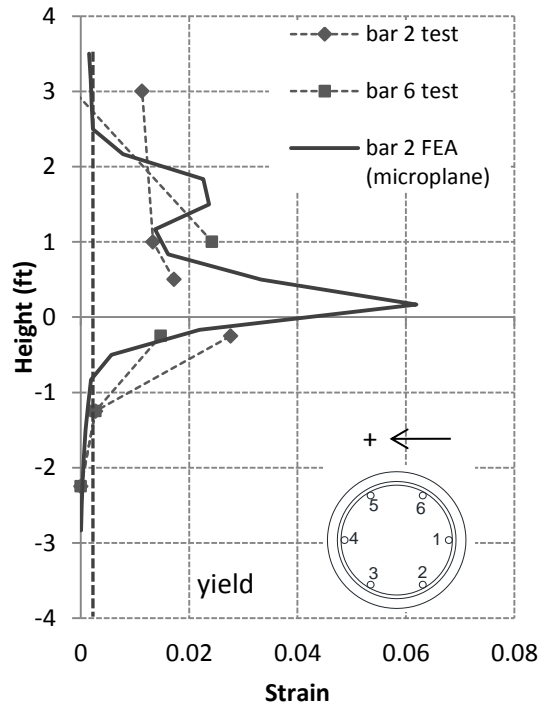


Figure 4.18 – Strains in bars at south face of Specimen #1 at +4% drift

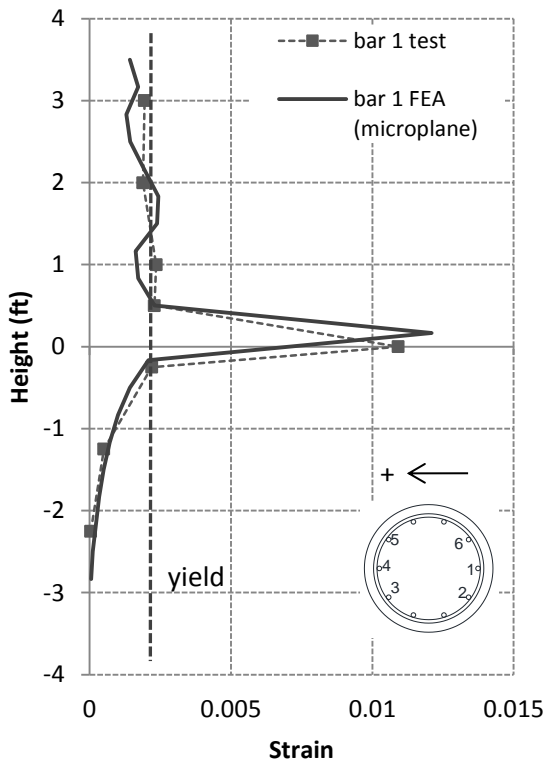


(a) Bar 1

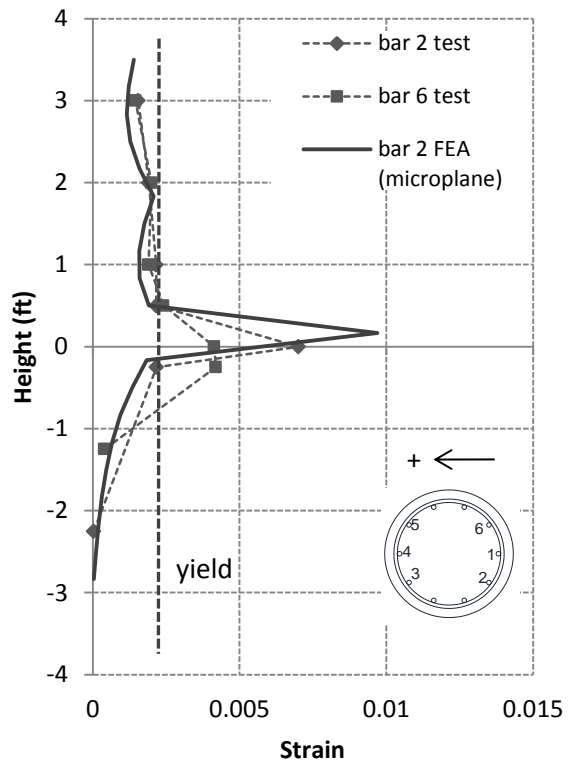


(b) Bars 2 & 6

Figure 4.19 – Strains in bars at the south face of Specimen #1 at +8% drift

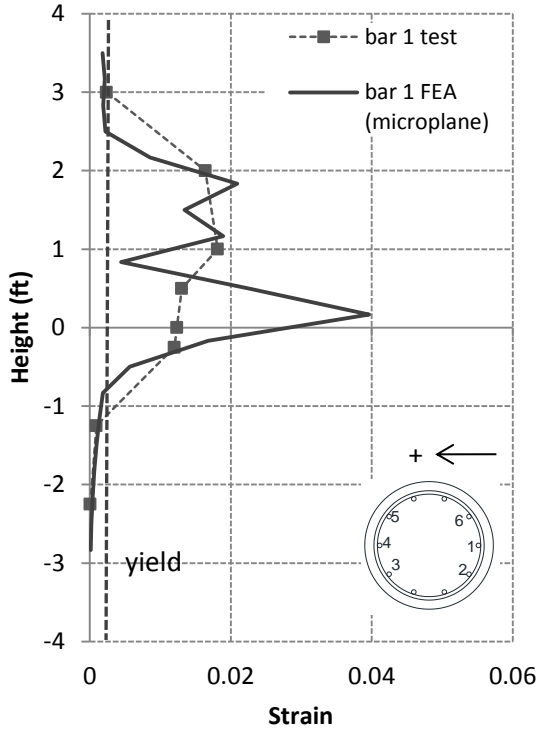


(a) Bar 1

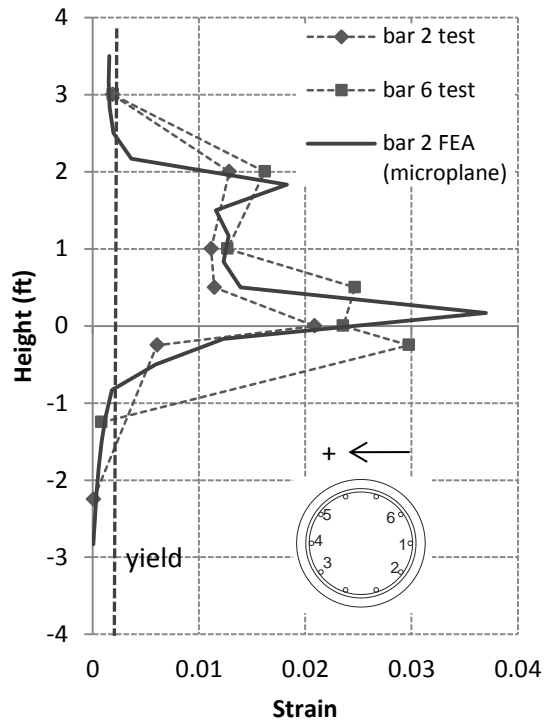


(b) Bars 2 & 6

Figure 4.20 – Strains in bars at south face of Specimen #2 at +1% drift

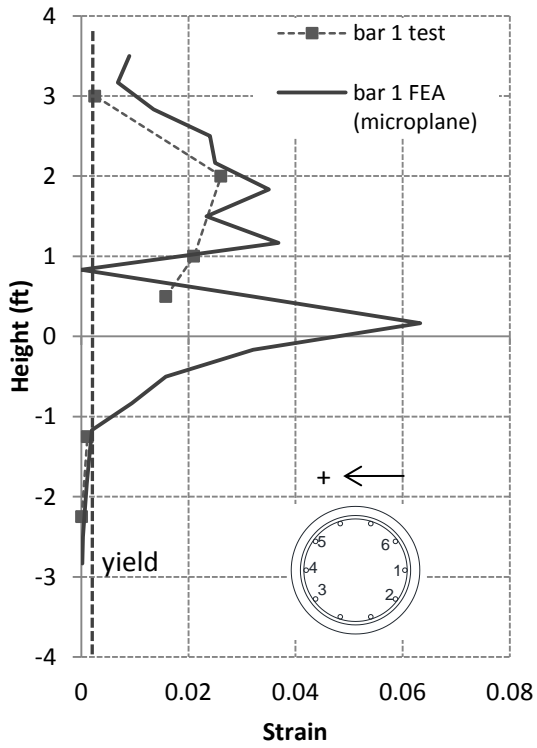


(a) Bar 1

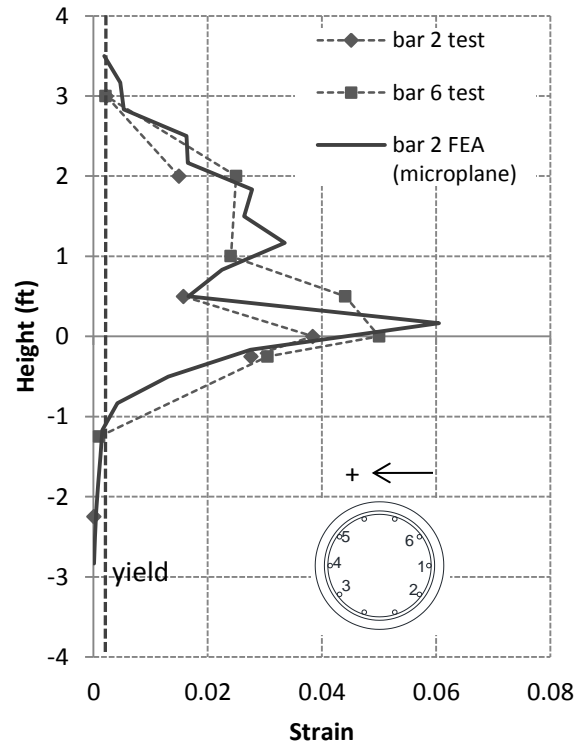


(b) Bars 2 & 6

Figure 4.21 – Strains in bars at south face of Specimen #2 at +4% drift



(a) Bar 1



(b) Bars 2 & 6

Figure 4.22 – Strains in bars at south face of Specimen #2 at +8% drift

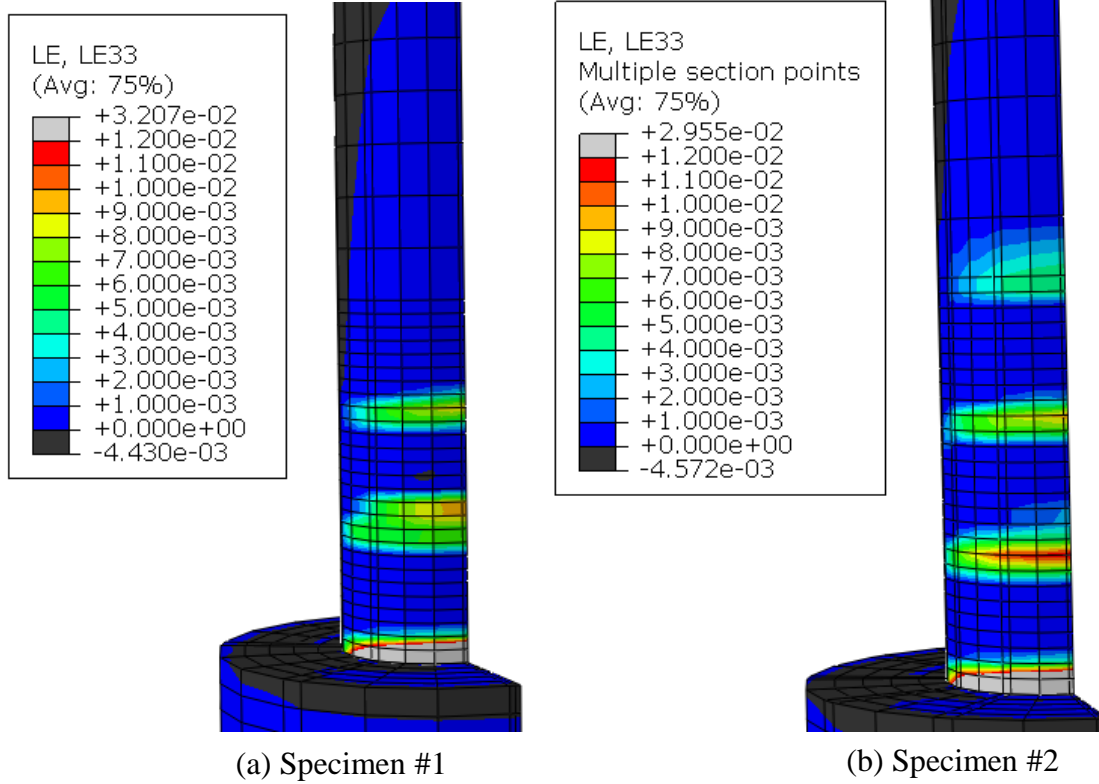


Figure 4.23 – Normal strains in concrete at 1% drift



## CHAPTER 5

### SUMMARY AND CONCLUSIONS

#### 5.1 Summary

This report presents a numerical investigation of the influence of the spacing of longitudinal bars on the structural performance of circular RC pile shafts. Three-dimensional nonlinear finite element (FE) models have been developed for RC pile shafts, and used for a numerical parametric study to confirm and generalize the experimental observations from the two pile specimens tested by Papadopoulos and Shing (2014). The modeling method has been validated by the experimental data. For the finite element analysis, a phenomenological stress-strain law for steel has been developed, accounting for the low-cycle fatigue of bars under large-amplitude cyclic strain reversals.

The damaged-plasticity model provided in Abaqus has been used to model the behavior of concrete. It is based on the model proposed by Lubliner et al. (1989) and modified by Lee and Fenves (1998). Two limitations of the model have been identified and remedies have been developed to partially circumvent them. The first limitation is that the model cannot capture the increase in the ductility of concrete in compression as the confinement pressure increases. To circumvent this limitation, the slope of the decaying branch of the input uniaxial compressive stress-strain curve has to be modified a priori based on the level of the confinement pressure or the amount of the confinement steel. The second limitation is that the model is not able to represent large stiffness degradation during unloading and reloading in tension, resulting in a large residual tensile strain upon unloading when large crack opening has occurred. This prevents the finite element models from accurately capturing the pinching effect in the load-displacement curve for a pile. To overcome this problem, contact conditions have to be introduced to represent major flexural cracks in a discrete manner.

In view of the aforementioned problems of the damaged-plasticity model, a new microplane model for concrete developed by Caner and Bazant (2013a) has been implemented in Abaqus. It does not have the deficiencies identified with the damaged-plasticity model. The calibration of the microplane model has been improved to simulate the compressive behavior of unconfined concrete more accurately, and the model has been successfully used to capture the behavior of the two pile specimens.

A phenomenological bond-slip law, developed by Murcia-Delso and Shing (2013), has been used to model the bond-slip behavior between the longitudinal bars and the surrounding concrete. The parametric study considers piles of different diameters, with different lineal and angular spacings of the longitudinal bars, and with different levels of the axial load.

## **5.2 Conclusions**

The finite element models developed here can adequately reproduce the behavior of two circular RC pile shafts tested in the laboratory. A numerical parametric study has been conducted with finite element models. The study has confirmed the experimental findings that the lineal spacing of the longitudinal bars does not have any impact on the ductility of an RC circular pile. The spacing can be larger than the 8-in. maximum permitted by the Caltrans and AASHTO specifications without compromising the structural performance of the circular RC member. However, from the standpoint of construction convenience and assuring consistent behavior under lateral loading in any direction, the specification in Section 8.18.1.2 of Caltrans Bridge Design Specifications (2004) that the number of longitudinal bars shall not be less than six (6) is reasonable. This implies that the angular spacing for longitudinal bars should be no greater than  $60^\circ$ , which is also the largest considered in this study.

The size of the longitudinal bars can affect the ductility of a pile, for the same spacing of the lateral reinforcement. The load degradation in a pile is often associated with the spalling of the cover concrete, and the buckling and the fracture of the longitudinal bars in the plastic-hinge region of the pile. Larger-



diameter bars are more resistant to buckling for the same spacing of the lateral reinforcement and therefore result in a more ductile behavior. The parametric study has also confirmed that a smaller lineal spacing with smaller-size longitudinal bars can lead to more closely spaced flexural cracks with smaller widths. Furthermore, the voids introduced at the locations of the PVC inspection tubes do not have significant impact on the nonlinear behavior of the piles. These observations are true for piles of different diameters and subjected to different levels of axial loads.



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