



FINAL REPORT

Multimodal Transportation Facility Resilience Index

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Nii Attoh-Okine - University of Delaware
Lindsay Ivey-Burden – University of Virginia

Prepared by:
University of Virginia
PO Box 400742
Charlottesville, VA 22904

University of Delaware
301 Du Pont Hall
Newark, DE 19716

Prepared for:
Mid-Atlantic Transportation Sustainability University Transportation Center
University of Virginia
Charlottesville, VA 22904

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16. Abstract A new paradigm for complex systems performance and maintenance decision making is developing in the form of resilience engineering. Depending on the subject area, different definitions of resilience exist. In this project, we adopt a definition appropriate for resilience in transportation systems: the ability of the system to recover and adapt to external shocks, which include natural, intentional and technogenic disasters and failure due to poor design. These disturbances can ultimately affect the smooth and efficient operation of systems and may demand a shift of process, strategies and/or coordination. This project builds off existing research and uses graph theory methods to develop a methodology to determine the resilience index of any transportation infrastructure system. This project also introduces weighting into the methodology based on traffic volume. Two weighting strategies are offered. It is shown that the inclusion of either weighting strategy increases the resilience of infrastructure systems and provides a more complete model. Finally, the methodology developed is applied to the network of major state and federal highways in Albemarle County, Virginia, to illustrate the process of determining a transportation infrastructure system's resilience index.			
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Executive Summary

The information contained in this report is organized as two separate but related research studies. Collectively, these studies investigate the impact of disruptions in a transportation network.

The first report, uses graph theory to quantify resilience in a small transportation network. This report is particularly interesting because a new methodology was used in which segments within the network were weighted by traffic count. This new methodology was then applied to the highway transportation network in Albemarle County, and disruptions in the network were taken as downtime of local bridges within the county. It was found that the methodology worked fairly well, and that including traffic counts made a significant difference in the calculation of resilience within the network as opposed to considering each possible route to have equal importance within the overall network.

The second report is a state of the art review on coastal flooding of transportation systems. It is estimated that sea level rise will have a major impact on the transportation systems and other critical infrastructure. Therefore, the ability to correctly predict the effects of vulnerable areas and their interaction with other infrastructure systems is of critical importance. This second report is intended to identify and understand the key variables at play in coastal flooding so that the methodology from the first report can be accurately used on a coastal transportation system with flooding.

TABLE OF CONTENTS

Executive Summary	4
Introduction.....	7
Motivation and Objectives	11
Literature Review	12
Highway Systems	13
Graph Theory.....	16
Basics and Definitions	17
Graph Theory in Resilience Engineering.....	21
Methodology	29
Example Network.....	29
Albemarle County Highway Network	34
Results and Discussion	38
Unweighted Network.....	38
Average Shortest Path Distance	39
Diameter.....	45
Link Density and Average Node Degree	47
Weighted Network 1	49
Average Shortest Path Distance	49
Diameter.....	51
Weighted Network 2	53
Average Shortest Path Distance	54
Diameter.....	56
Summary of Results	57
Conclusions.....	57
Future Work.....	59
References	60
Appendix A: Bridge Node Information	63
Appendix B: Intersection Node Information.....	64
Appendix C: Link Information	65
Appendix D: Link Density and Average Node Degree Plots for Weighted Networks	67

LIST OF FIGURES

Figure 1. Resilience Triangle [5].....	8
Figure 2. 3-D Resilience Triangle [6].....	10
Figure 3. Speed resiliency on the Mauston to Portage section during the February 2008 event [13].....	15
Figure 4. Simple Network	17
Figure 5. The Seven Bridges of Konigsberg [18]	21

Figure 6. a) Fully Connected Network, and b) Disconnected Network Resulting from Node Removal.....	26
Figure 7. Example Network	30
Figure 8. Link Density Response of Example Network	32
Figure 9. Average Node Degree for Example Network	32
Figure 10. Average Shortest Path Distance for Example Network.....	33
Figure 11. Map of Albemarle County Roads Analyzed	34
Figure 12 a.) Map of Albemarle County Highway Network, and b.) Enhanced View of Charlottesville to show detail.....	36
Figure 13. Average Shortest Path Distance for Unweighted Network.....	39
Figure 14. Location of Removed Nodes	40
Figure 15. Disconnected Subgraphs due to Removal of Nodes 47, 52, 35, and 6	41
Figure 16. Disconnected Subgraphs due to Removal of Node 38	43
Figure 17. Disconnected Subgraphs due to TNRS-a	43
Figure 18. Disconnected Subgraphs due to TNRS-b	44
Figure 19. Diameter for Unweighted Network	45
Figure 20. Comparison of Average Shortest Path Distance and Diameter Plots for the Unweighted Network	46
Figure 21. Link Density for Unweighted Network	47
Figure 22. Average Node Degree for Unweighted Network	47
Figure 23. Average Shortest Path Distance for Weighted Network 1	49
Figure 24. Comparison of Average Shortest Path Distance Plots for the Unweighted Network and WN1	50
Figure 25. Diameter for Weighted Network 1	51
Figure 26. Disconnected Subgraphs due to removal of Nodes 37 and 6.....	53
Figure 27. Average Shortest Path Distance for Weighted Network 2	54
Figure 28. Diameter for Weighted Network 2	56

LIST OF TABLES

Table 1: Summary of Graph Theory Properties [16]	20
Table 2. Arithmetic Properties of Example Network.....	31
Table 3. Summary of Resilience Indices	57

Introduction

Resilience engineering is developing as a new model for complex systems performance and maintenance decision-making. People use engineered systems every day and rely on them to function as designed, even after a disturbance like a severe weather event or a terrorist attack. The study of the ability of these systems, like a highway network or public transit mode, to function adequately after experiencing some external shock is the basis of the study of resilience. Broadly, resilience is the ability of an entity to recover from or adjust easily to misfortune or change. This definition is a helpful starting point when considering transportation infrastructure systems, but the complex and dynamic nature of these systems necessitates a more specific definition of resilience. Resilience is a measure of the ability of a system to remain in a “safe envelope” under accident conditions, or its ability to safely and efficiently absorb changes of state variables while minimizing the duration and severity of any deviations from target performance levels [1, 2, 3].

The goal of this project is to develop a framework for measuring and quantifying the resilience of transportation infrastructure systems. One widely used model is the R4 framework, developed by University of Buffalo’s Multidisciplinary Center for Earthquake Engineering Research (MCEER). In R4, resilience is broken down into four properties: robustness, redundancy, resourcefulness, and rapidity. Robustness is the ability of systems and the elements that comprise them to withstand stress without loss of function, and redundancy is a measure of how many elements are substitutable in a system. Resourcefulness is the capacity to identify issues and mobilize resources to

solve them, while rapidity is a measure of the time the system and/or its elements require to recover from loss of function as a result of some stressor [4]. Most resilience engineering studies use the basis of R4 in their analysis and try to build on it in some useful way. This study is no different. In R4, each property is measured and reported separately. This study will develop a method to quantify all four properties of a system's resilience as a single value.

One way to represent resilience is graphically, using quality of infrastructure (QoI) curves and resilience triangles. Figure 1 plots a QoI curve for a system against time. The metric used to plot the QoI curve is case-dependent and can change based on what is important to the stakeholders for each system. For example, a good metric to use to represent QoI for an airport after an earthquake would be the percentage of flights coming in and going out compared to pre-earthquake numbers. A variety of other metrics could be gathered about the airport's infrastructure, such as the number of long-term parking spots available in the days and weeks following the earthquake. However, this information would not be as helpful in determining the overall resilience of the airport to the earthquake or to any other natural disasters or external shocks.

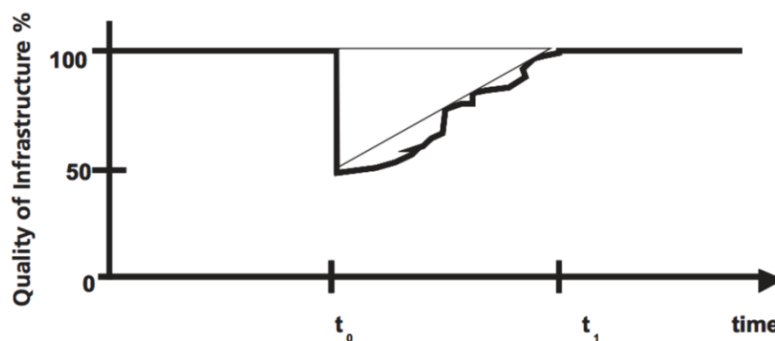


Figure 1. Resilience Triangle [5]

[5]

Plots like Figure 1 offer a straightforward view of what happens to a system's ability to perform at peak levels following some disaster or event. Before time t_0 , the QoI curve is at 100%, indicating the system is functioning as designed. At t_0 , some event occurs that drops the QoI curve to 50%. Between t_0 and t_1 , the QoI curve gradually increases until the quality of infrastructure returns to 100%. This recovery will usually not be uniform or smooth, as shown in the figure. Resilience triangles are typically shown on the same plot as the QoI curve, as in Figure 1, and are a tool used to idealize the recovery of the system and quickly calculate resilience of the system.

Resilience triangles like that in Figure 1 can account for three of the four aspects of MCEER's R4 framework. Rapidity is measured by the time required to restore the system to full functionality, shown on the horizontal axis. Robustness and redundancy are both implicitly represented by the initial drop seen in QoI on the vertical axis. A smaller initial loss of functionality can signal information about the state of the system, but usually the magnitude of the initial loss correlates to at least one of the following three factors: the severity of the event itself, the robustness of the system, or the level of redundancy present in the system [5]. However, plots like Figure 1 are not the only representation needed when discussing resilience; there is a lot of information they do not provide, such as the costs associated with returning the system to full functionality or the resourcefulness of the entity examined. Adapting the plot to add a third dimension to account for resourcefulness, as shown in Figure 2, gives a more complete view of a system's resilience according to MCEER's R4 framework.

As more resources are mobilized after an event, the recovery time shortens. Theoretically, if enough resources were available, recovery time could be reduced until

it was practically zero, but this is not possible in practice, due to necessary planning time before repairs can begin and different regulations in place depending on the location of the system [6].

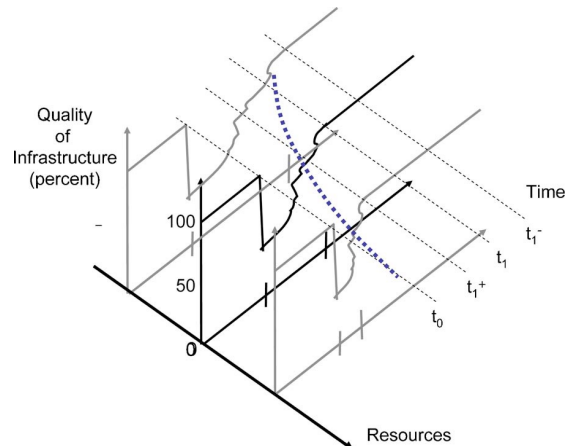


Figure 2. 3-D Resilience Triangle [6]

There are cases in which the quality of infrastructure curve never reaches 100% after an event. One example is New Orleans, Louisiana after it was devastated by Hurricane Katrina in August 2005. One year after the storm, the city's population was only 40% of what it was before Katrina hit; as of June 2015, almost a decade after the hurricane, population was 80% of what it had been pre-Katrina [7, 8]. The fact that population has still not reached the same levels as before the storm and that it has taken such a long time to achieve growth confirms what most already knew, that New Orleans' infrastructure before Hurricane Katrina was not very resilient.

On the other end of the spectrum, there are examples in which repairs necessitated by some external shock to an infrastructure system have increased the quality of that system over pre-event levels. One such case is the World Trade Center complex in lower Manhattan. After the terrorist attacks of September 11, 2001, all seven buildings in the complex were destroyed. The site is still being redeveloped, but once completed it will include 14.6 million square feet of floor space, an increase of

more than 1 million square feet [9]. Additionally, site development includes the construction of an expanded transit hub that will provide more transportation links to the site than were available before 2001 [9].

Motivation and Objectives

Transportation infrastructure systems are some of the largest and most widely used engineered systems in the world; most people have a daily need to get from one place to another, and transportation networks are vital in the distribution of goods from production centers to points of consumption. While the quality of these infrastructure systems varies wildly, they have one thing in common: potential economic and productivity losses should a disaster occur. Disturbance in these systems also has the potential for massive loss of life.

In addition to this risk, transportation infrastructure is crucial to the movement of necessary consumer goods such as food and clothing from points of production to points of sale and consumption. This journey can often be quite long, crossing many state lines, regional borders or even entire oceans. Should there be a disruption in the transport of these goods, consumer wellbeing would suffer along with the economies of the producing and consuming nations.

While development of a resilience index could not prevent a disaster from occurring, it would be helpful in minimizing the effects of an external shock on a transportation infrastructure system and optimizing recovery and restoration efforts. A resilience index would help decision makers prioritize maintenance work and identify systems that should be retrofit. If systems that are not as resilient as we might like them

to be can be identified, we can decrease the likelihood of injury or fatalities during catastrophic events and lessen the adverse economic effects, in addition to reducing recovery time.

Additionally, identifying the resilience indices of various infrastructure systems will increase disaster preparedness and enable better planning by emergency response and relief organizations. By having a more complete picture of how systems could be affected by various external shocks, planners can allocate more time and resources to more likely scenarios. Disaster planning also increases the ability of first responders to improvise in the field and adapt to the specific disaster scenario that might not have been predicted and explicitly planned for [7].

The purpose of this project is to develop and implement a framework for measuring the resilience of multimodal transportation infrastructure systems such as ports, highway systems, train stations, airports, etc. through development of a resilience index. Graph theory will be used to accomplish this goal, and the analysis will include weighting to account for traffic volume in the network. This project will consider natural and artificial external shocks as well as technogenic disasters through the implementation of different shock simulation strategies. The method will then be applied to the network of major state and federal highways in Albemarle County, Virginia.

Literature Review

This section will summarize research that studies the resilience of highway systems. This summary highlights the myriad ways resilience of transportation infrastructure has been studied in the past and shows that there are many ways to analyze the same problem. This study uses graph theory to study resilience, and this section will also present an introduction to graph theory and define several terms that will be used throughout. Then, this section presents a summary of how researchers have used graph theory and network science to evaluate transportation networks, identify their critical nodes and links, and determine their resilience.

Highway Systems

There are almost 250 million cars and trucks operating in the U.S. today, or almost one per person, and most will, at some point in their service life, be driven on an interstate highway [10]. The U.S. interstate highway system includes almost 50,000 miles of roadways, bridges, and tunnels and connects the country's big cities and small towns to one another. The interstate highway system is vital for the movement of both people and goods across the country, and as such it is critical that it be resilient to external shocks. Because it is so vast, it presents a unique challenge to those who wish to study its resilience.

In a report to Congress regarding seismic risk to highway infrastructure, it was established that a national database on seismic design and retrofit status of the highway system does not exist [11]. The Federal Highway Administration (FHWA) has developed software to estimate the loss of highway system capacity due to earthquakes, and this could possibly be used to model capacity loss for other shocks [11]. In the 20th century, the principal focus was on improving the resilience of highway

structures such as bridges, and only recently has the focus turned to evaluating the system as a whole. Even with this new focus on considering the whole system, bridges remain the most vulnerable piece of highway infrastructure, especially to seismic events [11].

One study defined the seismic resilience of highway bridges through the use of a loss function and a recovery function. The loss function includes direct and indirect losses suffered during restoration of a degraded system, and the recovery function models the quality of the infrastructure over time as the bridge is being restored. This research was applied to a California bridge that had suffered earthquake damage to its piers. The piers were retrofit with steel jackets, increasing their rotational ductility and decreasing the bridge's vulnerability to seismic events. Not only did the applied retrofit increase the seismic resilience of the bridge from 57.5% to 99.9%, the authors found that it was also cost effective. The financial benefits continued to increase with the service life of the bridge [12].

A study published in 2010 used data from two weather events (a blizzard in February 2008 and flooding in June 2008) to determine resiliency of an interstate corridor in Wisconsin. The approximately 290-mile stretch of I-90/94 runs southeast from Hudson, Wisconsin, on the border with Minnesota, through the state to its border with Illinois in Beloit, Wisconsin. The test corridor was described as a "critical backbone for freight and passenger mobility and accessibility in Wisconsin," as well as significant through traffic of passengers and freight between the Minneapolis and Chicago metropolitan areas and beyond [13]. The study used truck count and average truck speed through the different segments of the corridor as their quality of infrastructure

(QoI) metrics to construct QoI curves and resilience triangles for the events. Figure 3 shows one of the curves constructed, using average truck speeds for the 40-mile segment between the small cities of Mauston and Portage in the days surrounding the February 2008 blizzard.

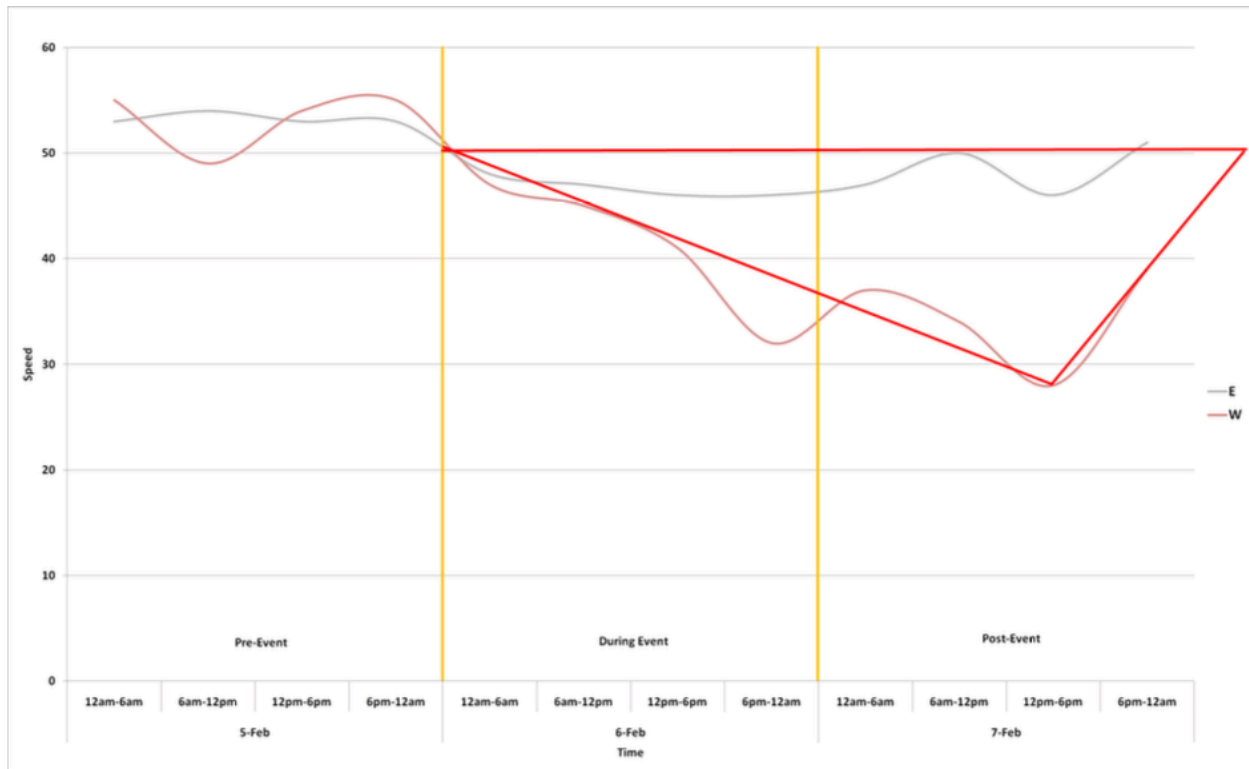


Figure 3. Speed resiliency on the Mauston to Portage section during the February 2008 event [13]

The authors of this study assert that two measures of the R4 framework can be measured from a plot such as the one in Figure 3: robustness and rapidity. Robustness is represented by the downward sloping section of the QoI curve, and rapidity by the section with positive slope. The authors fit resilience triangles to their data, seen in red in Figure 3, and then calculated the slopes and angles of the triangle's sides that corresponded to robustness and rapidity. They categorized their measures of robustness and rapidity as high, moderate or low depending on the measured angles. For robustness, measured by the downward sloping side of the resilience triangle, it's

better to have a smaller angle, indicating a gentler or smaller decline in the QoI metric. However, for rapidity, larger angles are desirable because they indicate quicker recovery. The thresholds between the three categories are the same for robustness and rapidity, 11.3° and 26.6° . For the case in Figure 3, the robustness angle is 21° , indicating moderate robustness, and the rapidity angle is 51° , indicating high rapidity. Different parts of the test corridor had distinct reactions to the two weather events. The more northern segments were affected less by both weather events. The blizzard had a bigger effect on the southern segment of the route, while a central segment was most heavily affected by flooding [13].

The studies discussed above, while useful in the study of transportation system resilience, offer only pieces of the puzzle that is the study of resilience. The results are case-specific and the metrics are often difficult to observe or calculate. The methods will need to be revised in order to apply them to other systems or systems subject to different disturbances. This study will fill the gaps left by these other studies by developing a method to determine the resilience index of any transportation infrastructure network subjected to any type of external shock.

Graph Theory

This project uses graph theory and network analysis to determine the resilience of a transportation infrastructure system. Graph theory and network science have been employed across various disciplines: in chemistry it has been used in drug design, and engineers have used it to evaluate complex infrastructure systems [14]. Recently, graph theory was even used to determine which characters hold the most power in the popular fantasy series “Game of Thrones” [15].

Basics and Definitions

A network consists of a set of nodes – points representing a piece of infrastructure, such as a bridge or airport – and a set of links that connect them. A simple example network consisting of 4 nodes (n) and 4 links (m) is shown in Figure 4 below, and will be used to illustrate some of the pertinent terminology used in graph theory that will be used throughout this study.

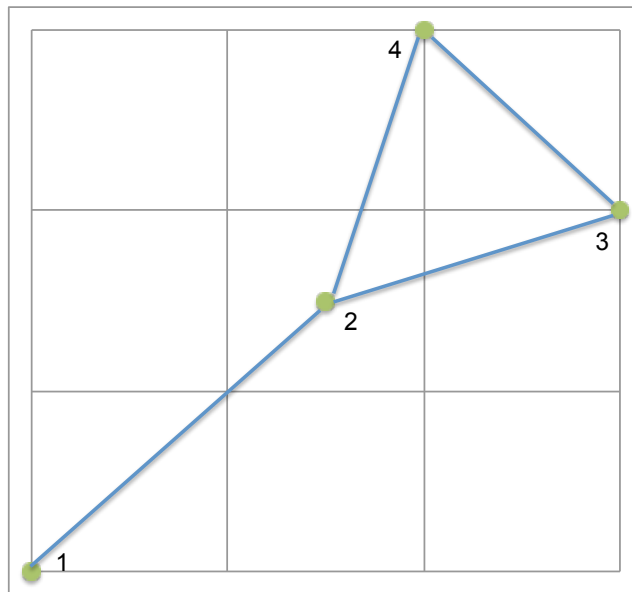


Figure 4. Simple Network

Links can be *directed* or *undirected*. A directed link allows travel in only one direction and is indicated with arrows, whereas an undirected link functions regardless of direction. All the links in this study are undirected.

A *path* between a pair of nodes exists if the nodes are connected by a link or several links passing through other nodes. If a path exists between every pair of nodes

in the network, the network is *fully connected*. If not, it is *disconnected*. The simple network shown in Figure 4 is fully connected.

The *path distance* is the number of links in the path. Path distance can also be calculated using the length of each link in the path. In the network in Figure 4, there are two paths connecting nodes 1 and 4. The first path is 1-2-4, containing 2 links, and the second is 1-2-3-4, containing 3 links. The *shortest path* between nodes 1 and 4 is 1-2-4, and its path distance is 2.

The *diameter* of the network is the maximum value of the set of shortest paths between every pair of nodes in the network. The diameter of the simple network is 2.

Matrix methods are commonly used to represent and analyze networks. A network's *adjacency matrix*, A , is an n -by- n square matrix that represents linkages in a network. If a link exists between nodes i and j , the element $A(i,j)$ is 1; if there is no link between the two nodes, the element is 0. Diagonal elements are always 0, and if the network has undirected links the matrix is symmetric. The adjacency matrix for the simple network is shown below.

$$A = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$$

Various parameters are defined that describe the degree of connectedness of a network; these will be used to study the network's resilience. The parameters that will be used in this study are link density, average node degree, average shortest path distance, diameter, and betweenness centrality.

Link density is the relationship between the total number of links (m) in the network and the maximum number of links the network could support if every node (n)

were connected to every other node by a single link. Link density is defined by Equation 1 below.

$$\text{Link Density} = \frac{2m}{n(n-1)} \quad [16] (1)$$

Another important network property is *average node degree*. The *degree* of a node is how many links are connected to it. For a network with undirected links, average node degree can be calculated using Equation 2 below.

$$\text{Average Node Degree} = \frac{2m}{n} \quad [16] (2)$$

The *average shortest path distance* for a network considers the shortest paths between every pair of nodes in the network, and can be calculated using equation 3 below.

$$\text{Average Shortest Path Distance} = \sum_i \sum_j \frac{l(i,j)}{n(n-1)} \quad [16] (3)$$

where $l(i,j)$ denotes the length of the shortest path between any two nodes i and j .

Betweenness centrality is an attribute of each node as opposed to one that describes the entire network. A node's betweenness centrality measures how often that node lies on the shortest path between other pairs of nodes in the network. A node need not have high degree or be centrally located in the network to have a high betweenness centrality. Betweenness centrality of a node is the ratio of the number of shortest paths between any pair of nodes (excluding the one in question) that pass through that node and the total number of shortest paths in the network (excluding those that begin and end at the node in question). The value of betweenness centrality is always between 0 and 1 and its formula is given in Equation 4 below.

$$\text{Betweenness Centrality of Node } i = \frac{1}{(n-1)(n-2)} \sum_{j,k \neq i} a_{jk(i)} \quad [16] (4)$$

Where $a_{jk(i)}$ denotes if the shortest path between nodes j and k passes through node i .

This value is 1 if the shortest path passes through node i and 0 if it does not.

The terms defined above are summarized in Table 1.

Table 1: Summary of Graph Theory Properties [16]

Metric	Calculated for	Definition	Equation
Link Density	Network	The fraction between the total and the maximum number of links	$\frac{2m}{n(n-1)}$
Average Node Degree		The average value of the node-degree distribution	$\frac{2m}{n}$
Average Shortest Path Distance		Average value of the distances between all pairs of nodes	$\sum_{i,j} \frac{l(i,j)}{n(n-1)}$
Diameter		Maximum shortest path distance between all pairs of nodes	$\max(L(i,j))$
Betweenness Centrality	Node	Proportion of shortest paths that run through a given node	$\frac{1}{(n-1)(n-2)} \sum_{j,k \neq i} a_{jk(i)}$

When using graph theory to study a network's resilience, the same basic method applies no matter the type of network. First, selected network properties are calculated. Then, nodes are removed from the system one at a time and the properties are recalculated. Two node removal strategies will be used in this study: a random node removal strategy (RNRS), and a targeted node removal strategy (TNRS). RNRS simulates disturbances to the system that have the same likelihood of occurring at any point in the system, like weather events or power outages. TNRS simulates deliberate attacks to important points in the network.

The first documented use of graph theory was by mathematician Leonhard Euler in 1741. He used what would become graph theory in his analysis of the problem known as “The Seven Bridges of Königsberg.” The city of Königsberg, Prussia (modern day Kaliningrad, Russia) is divided into four separate landmasses by the Pregolya River. At the time, seven bridges connected the different landmasses (five of which still stand today). The layout of bridges and waterways is shown in Figure 5 below. The problem involved designing a walk through the city that involved crossing each bridge exactly once. It was not required that the walk begin and end in the same place. Many had tried to find a solution, but it was not until Euler modeled the problem as a graph, using the land masses as nodes and the bridges as links, that it was shown it couldn't be done [17].

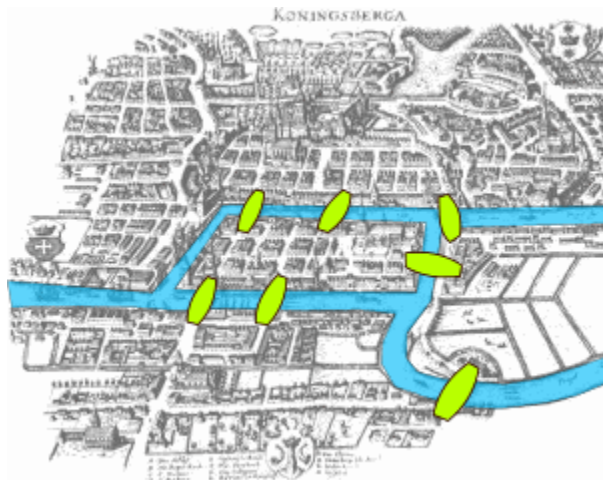


Figure 5. The Seven Bridges of Königsberg [18]

Graph Theory in Resilience Engineering

Several studies have been performed using graph theory to study existing transportation networks. In a needs assessment report, Ham and Lockwood defined

critical assets in the nation's highway transportation network as "those major facilities the loss of which would significantly reduce interregional mobility over an extended period and thereby damage the national economy and defense mobility" [19]. There are several topological network properties that can be used to identify these critical assets and aid in the prioritization of on-site evaluation and maintenance work. These topological properties rank the criticality and importance of the nodes and links in a network.

Ranking nodes by criticality and importance is the first step of implementing a targeted node removal strategy when using graph theory to study a network's resilience. The two topological properties most often used to determine the importance of nodes in a network are node degree and betweenness centrality. It's reasonable to assume that node degree and betweenness centrality are correlated for most networks and provide a good ranking of node importance. This is true for small networks, but the correlation breaks down as networks get larger [20]. Guimera and Amaral performed an analysis of the worldwide airport network that modeled airports as nodes and non-stop flights as links. Their results showed that the most central airports (represented by nodes with high degree) were not always the best connected to the rest of the network (nodes with high betweenness centrality). This is a reasonable result considering the size of their network: 3,883 nodes and over 27,000 links [21].

Reducing a network's functionality by removing the smallest possible amount of nodes is the goal of a targeted node removal strategy. Another study that used betweenness centrality to identify the most critical nodes recognized that by removing nodes with high betweenness, they disrupted the highest proportion of shortest paths in

the graph. This affects movement through the graph and sends many paths on longer detours. This reduction in mobility is the very definition of a critical point in a graph [22].

In a study of the topological properties of the Italian airport network, betweenness centrality was used to locate the most important hubs in the network to prioritize maintenance at those locations [23]. Several studies found that when performing an analysis that includes targeted node removal to simulate deliberate attacks to a network, ranking the nodes based on betweenness centrality has a greater impact on topological properties than by ranking the nodes based on degree [20, 21]. Studies have also been done that remove nodes based on node degree, but these are less common than those that use betweenness centrality to rank nodes [Holmgren]. Betweenness centrality will be used in this study to determine node criticality for TNRS.

Employing a targeted node removal strategy to evaluate the network's response to disruption must also consider if the order of node removal will follow the initial node criticality ranking or if the ranking should be recalculated after each removal. A recalculated ranking after each node removal simulates a very sophisticated attack in which the perpetrators have knowledge of how the system will adapt to changes. In some cases, a node that originally had a very high degree or betweenness centrality could be isolated by the removal of one of its neighboring nodes, decreasing its degree or betweenness centrality and thus its importance to the network. Some studies only remove nodes based only on initial rankings but these might not be as useful as those studies that also use recalculated lists depending on the motivations and goals of the project [25].

In their research, Berche et. al analyzed the public transit networks of 14 cities around the world using 16 attack strategies. Half of these were based on removing nodes based on an initial node importance ranking and the other half used rankings that had been recalculated after each removal. They found that performing node removal based on recalculated importance ranking often led to steeper declines in the network's topological properties [26]. An analysis of a power supply and distribution also used initial and recalculated rankings and came to similar conclusions [24]. This study will use both initial and recalculated ranking to perform TNRS.

Others have developed different methods to determine which of a network's nodes are most critical. Ukkusuri and Yushimoto took a unique approach to determine which elements were most critical to a transportation network. They modeled the transit network in Manhattan during peak morning rush hour. Their network included bridges and tunnels that connect Manhattan to New Jersey and New York City's other boroughs, as well as the subway and bus systems within Manhattan itself. They chose to use average travel time as their metric for network performance. Travel time depends on the user's choice of route and travel mode, and user factors congestion into their decision-making process. Congestion is a function of the choices of all other network users [27].

The authors conducted their analysis using a network game with selfish players, each looking to optimize their own travel time with no regard for how their decisions affected other network users. With the original average travel time established, links were removed from the network one at a time, replacing the removed link before removing another one. The authors compared the average travel time data after they

had removed each link in turn. They found that removing the bridges and tunnels into Manhattan had the greatest effect on average travel time. This result is not surprising, because they were modeling the network during peak morning rush hour, but it highlights the usefulness of network analysis and average travel time as a metric [27].

Depending on what type of network is being analyzed, there are various useful metrics that can be used to evaluate its functionality and resilience. Travel time is a useful metric, but it can be difficult calculate. It is dependent on speed limits, frequency of public transit, and congestion, among other variables [27]. Many analyses, this study included, use average shortest path as a metric because it gives similar information about the state of the network with fewer variables to determine, especially if the transportation network being analyzed is unimodal [24, 25, 26]. Using average shortest path distance to assess criticality does miss the effect of congestion on a network's performance, but this is acceptable to many applications of graph theory analysis, depending on the priorities of the research [28].

For some networks, a problem can arise when the removal of a node from the graph causes the network to be disconnected. In a fully connected graph, there is a path between any node and all other nodes in the network; this is not the case in a disconnected graph. Disconnected graphs form two or more subgraphs, as shown in Figure 6. The shortest path between any pair of nodes on different subgraphs becomes infinite. When this happens, researchers advocate using a metric called *inverse average shortest path distance*, which is calculated in the same way as the average shortest path distance from Equation 3 but with the infinite values replaced by zeros [20, 24, 26]. A decrease in inverse average shortest path distance corresponds to a

decrease in network performance as more and more pairs of nodes become disconnected.

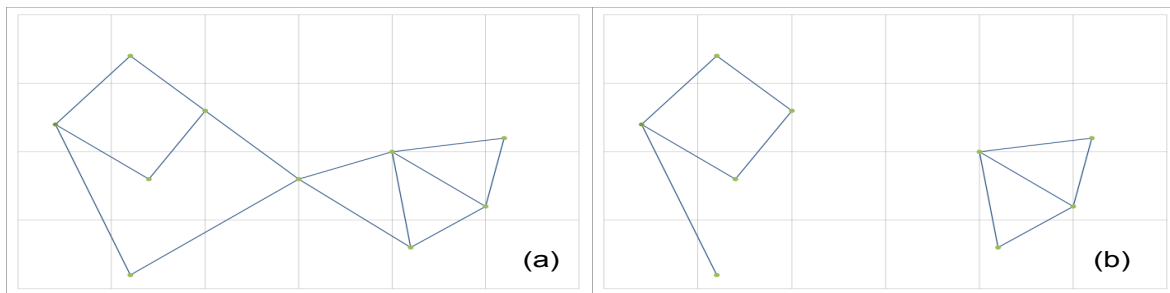


Figure 6. a) Fully Connected Network, and b) Disconnected Network Resulting from Node Removal

Several studies have been performed using graph theory and network science to evaluate the resilience of transportation networks. One study evaluated the rail and road networks in Florida, modeling rail stations and intersections as nodes. The criticality of the nodes was then ranked according to their betweenness centrality values. This ranking was used to remove nodes from the network to simulate a disturbance, then the effect of removal on the average shortest path and on the diameter of the network was observed. The authors of this study do not offer a quantitative measure of resilience; instead they state that based on their observations the network is “relatively resilient to disruptions” [25].

A study of the transportation infrastructure in Melbourne, Australia, compared the resilience of three of the city’s transportation modes: the train, tram and street networks. Travel time was used as the metric to assess the network’s performance. A simplifying assumption was made to assign the same speed limit across the entire street network. Four different speed limits were modeled. The results of the study indicated that the tram system was the most resilient, followed by trains and then street travel. The researchers did not offer quantitative values for resilience but did recognize that the resilience of the street network was dependent on the speed limit, with higher speed

limits leading to lower resilience [29]. These qualitative assessments are certainly useful for some applications but in-depth transportation planning requires a more detailed, quantitative result.

Some researchers have developed graph theory methods to study transportation infrastructure resilience that yields quantitative results. Ip and Wang model the transportation network connecting several cities, with cities as nodes and the routes along different travel modes that connect them as links. The authors introduce weighting in their model by assigning node size according to city population and assigning the links a *reliability score*. This reliability score is between 0 and 1 and represents the probability that at any given time there will be a disturbance at that link, rendering it unusable. They also introduce the concept of *independent paths*. There can be an infinite number of paths through a network connecting a pair of nodes; paths are said to be independent if they do not require traveling along a link used by another path connecting the same pair of nodes. There are a finite number of independent paths connecting every pair of nodes [30].

Ip and Wang define the resilience of each node as the weighted sum of the number of reliable independent paths connecting it to all other nodes in the network. For example, if a node has a resilience value of 2.25, there are about 2 independent paths between it and every other node. Resilience of the entire network is the weighted average of the resilience of each node [30]. While this is a useful result, it requires knowledge of the type of transportation network being analyzed to be meaningful. A resilience value of 2 would likely be sufficient for a rail network, but indicates a lack of connectivity in an urban environment with several available travel modes.

Another concept introduced by Ip and Wang is *friability*. Friability is a measure of the reduction in the network's resilience due to the removal of a node or link. Friability can also be used as a method of ranking criticality of nodes and links. The elements with the highest friability are the most critical to the operation of the network, as their elimination has the greatest impact on the network's resilience [31].

The study discussed above added weighting to the network's nodes, but weighting can also be added to links. This study will use weighted links. A study of the worldwide airport network included 3,880 nodes (airports) and almost 19,000 links (direct flights operating during one calendar year). The analysis also included data on the distance between each pair of airports with a direct flight link and the number of available seats on each route. The authors recognized that the weight assigned to each link should be a function of the link's most important characteristics: distance and available seats. As the number of available seats increases, the effective distance between the nodes decreases because more seats enable more frequent and faster travel between the two locations [32]. They use Equation 5, shown below, to determine the weight of each link.

$$w_{ij} = \frac{d_{ij}}{s_{ij}} \quad [32] \quad (5)$$

where w_{ij} is the weight of the link that connects nodes i and j , d_{ij} is the distance between nodes i and j , and s_{ij} is the number of available seats on direct flights connected nodes i and j .

Methodology

Using the methodology and parameters of graph theory to study transportation networks and their resilience outlined in the previous section, this section will outline the steps taken in this study to incorporate weighted links into the methodology. Before the method was applied to the network of major state and federal highways in Albemarle County, Virginia, a smaller, simpler example network was analyzed to highlight the method and illustrate it in a manageable way. This section will also explain the development of the Albemarle County network and the tools used to build it and perform the analysis.

Example Network

The network shown in Figure 7 was analyzed as an illustrative example prior to performing the analysis on larger, more complex networks. Three network properties – link density, average node degree, and average shortest path distance – were used to show how the analysis functions.

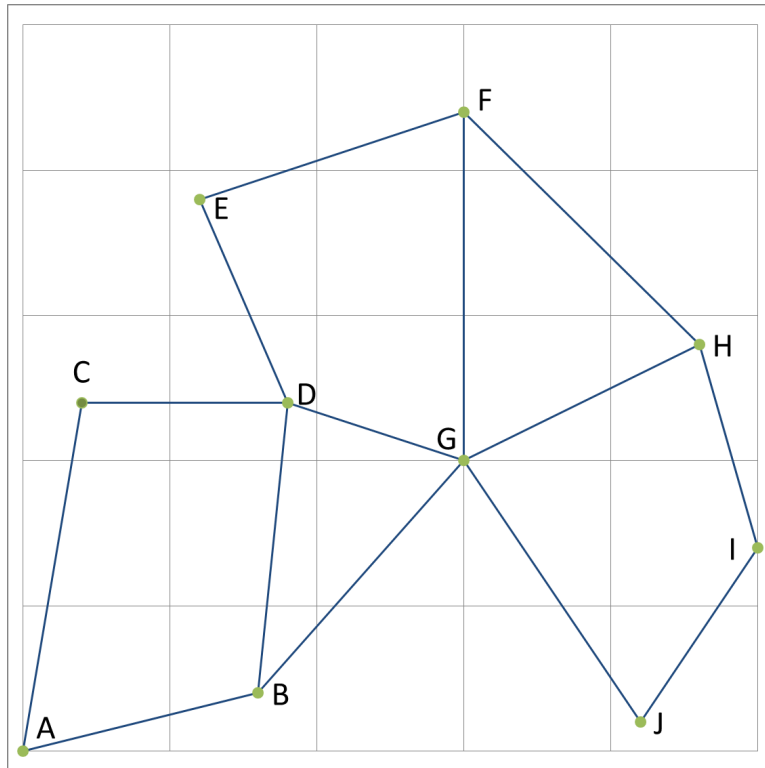


Figure 7. Example Network

Link density and average node degree are calculated using Equations 1 and 2, respectively. For this network, the link lengths are included in the shortest path calculations. The location of each node on the grid is used to determine the length of each link. Each gridline in Figure 7 represents 5 units. For example, the link connecting nodes C and D measures 7 units in length. The average shortest path distance was calculated using Equation 3.

To analyze the response of the network to a disturbance, nodes will be removed from the network and the arithmetic properties will be recalculated. Because the network is small and consists of only 10 nodes, the illustrative example contains three rounds of analysis: the first with all nodes operational, the second with one node removed, and the third with one additional node removed for a total of two nodes removed.

Two node removal strategies were used: random node removal (RNRS) and targeted node removal (TNRS). RNRS simulates disturbances such as weather events that are equally as likely to affect any point in the network, while TNRS can simulate an intentional attack on a specific point in the network. For RNRS, a random number generator determined the nodes to be removed. Node F was removed first, followed by Node H. Using TNRS, nodes are removed in order of node degree from highest to lowest. Node G, with degree 5, was removed first. Node D, which had a degree of 3 after the removal of node G, was removed next. The arithmetic properties for the network with all nodes and with selected nodes removed are shown in Table 2 below.

Table 2. Arithmetic Properties of Example Network

RNRS			
Node(s) Removed	Link Density	Average Node Degree	Average Shortest Path Distance
n/a	0.311	2.8	8.89
F	0.306	2.44	8.84
F, H	0.321	2.25	9.07
TNRS			
G	0.25	2	13.27
G, D	0.214	1.5	3.92

To see how the network is responding to the disturbance of node removal, the properties are plotted against the percentage of nodes removed, shown in Figures 8, 9, and 10 below.

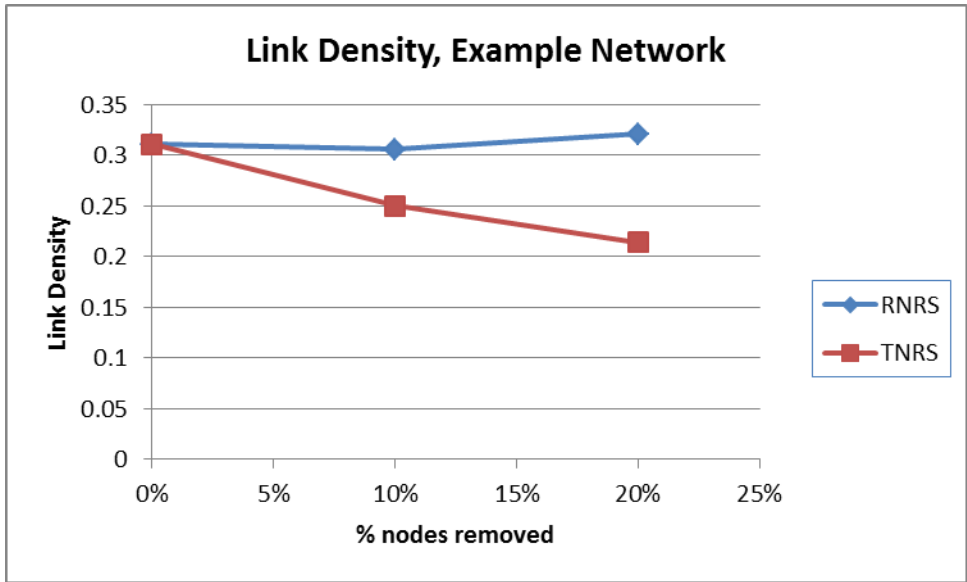


Figure 8. Link Density Response of Example Network

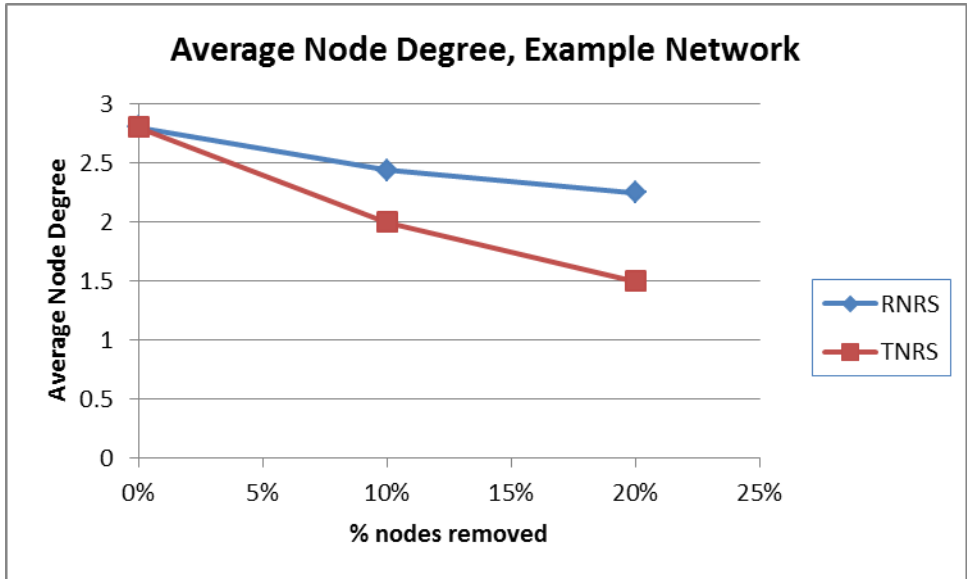


Figure 9. Average Node Degree for Example Network

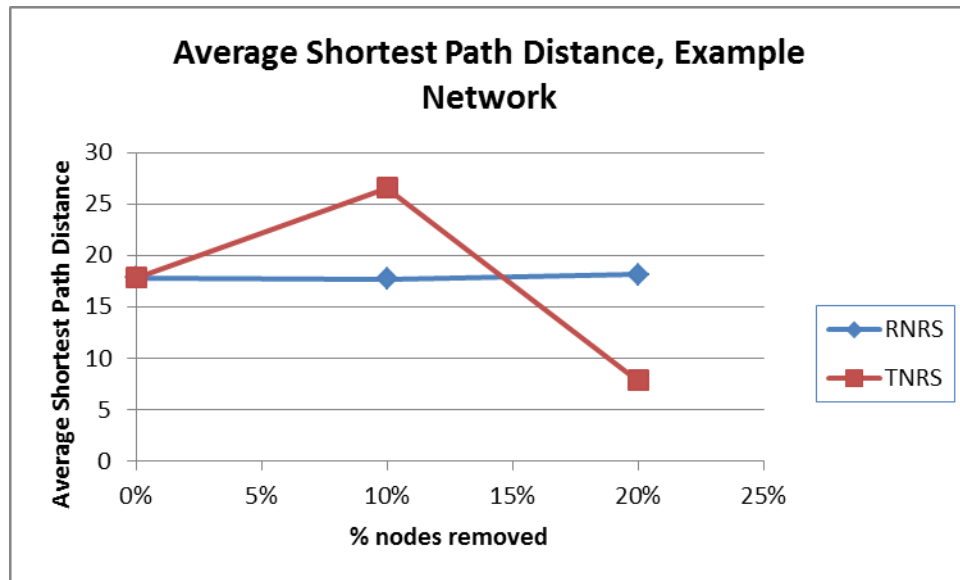


Figure 10. Average Shortest Path Distance for Example Network

Figure 10 shows an intersection of the two average shortest path distance curves at approximately 15% node removal. This point of convergence is called the *critical point* and represents the point at which the system has the same reaction to both node removal strategies. The network is resilient up to that point; it loses resilience to disturbance once more than that percentage of nodes has been removed [33, 34]. This value is the network's resilience index. For this example, the network is resilient to external shock as long as the disturbance removes less than 15% of the network's nodes. At any higher percentage of node removal, the system loses efficiency and is said to not be resilient.

The link density and average node degree curves in Figures 8 and 9, respectively, do not intersect. This is due in part to the small size of the example network. Depending on the metric and the type of network being analyzed, it's possible that the curves on plots such as the ones shown here will never intersect. When this occurs, the resilience index is determined from plots using metrics where the curves do intersect.

Albemarle County Highway Network

Finally, the method illustrated here was applied to a considerably more complex network, the highway system of major federal and state highways in Albemarle County, Virginia. The network consists of 10 routes totaling 176 miles of roadway, and all routes allow traffic in both directions. A map of the included routes is shown in Figure 11.

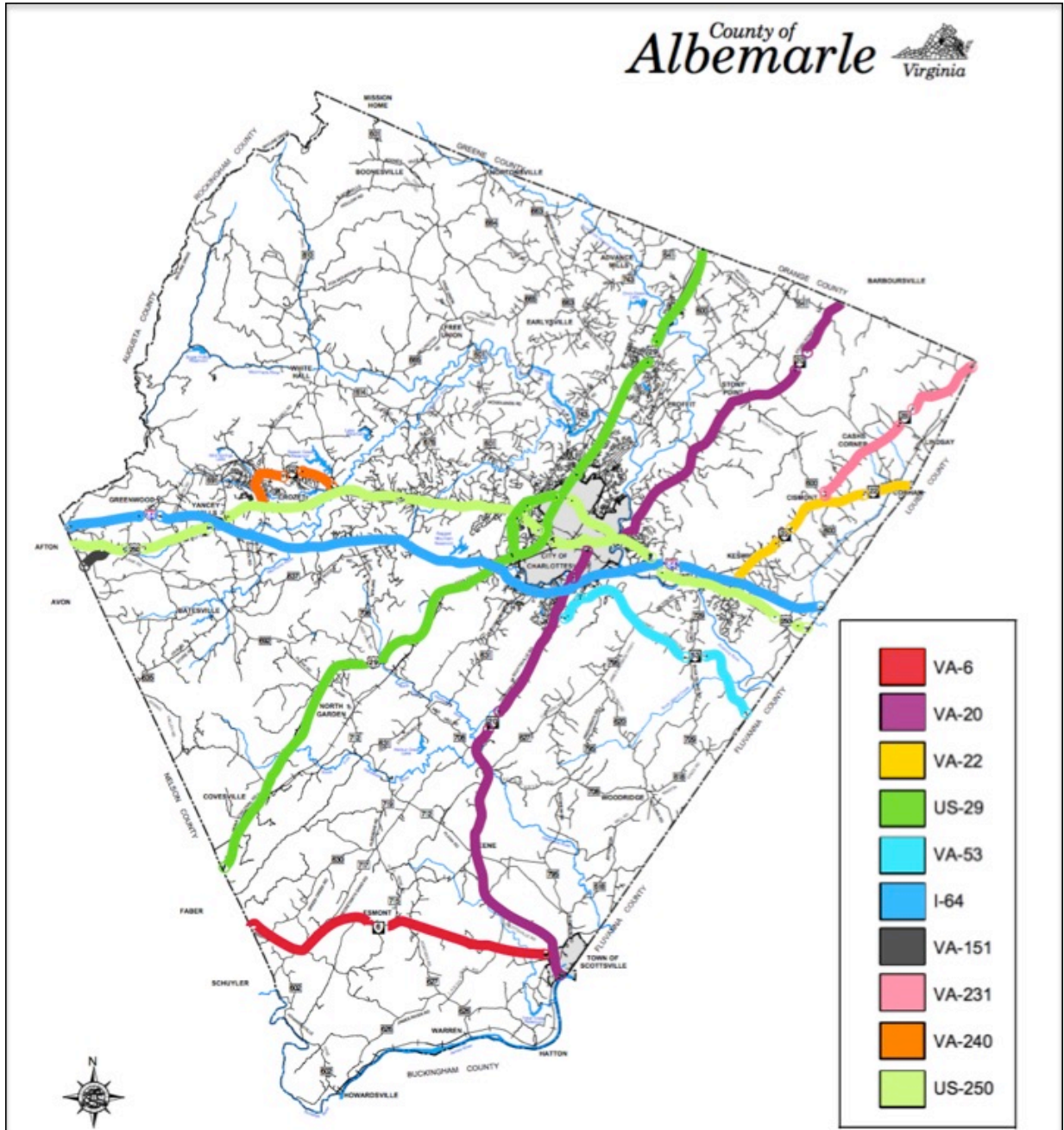


Figure 11. Map of Albemarle County Roads Analyzed

The goal of this example is to illustrate how this method can be used to evaluate the resilience of a transportation infrastructure system. Specifically, the effect of bridge outages on a highway system was investigated here. Nodes were placed at the location of bridges along the selected routes. The National Bridge Inventory was used to identify bridges along the routes shown in Figure 11, and the GIS tool ArcMap was used to show their location. All roadway sections were modeled as undirected links. Twin bridges were modeled as a single node. The analysis was performed in Matlab. Due to the nature of Matlab's built-in network analysis tools, nodes were also placed at the intersections between two routes, and between a single route and the Albemarle county line. However, because the goal of this study was to evaluate the effect of bridge outages, only the nodes representing bridges were removed during the analysis.

The network studied is shown in Figure 12; it has 80 nodes, 57 of which represent bridges, shown in purple, and 23 intersections, shown in orange. More information about the bridges and intersections are given in Appendices A and B, respectively. The network has 86 links of various lengths. ArcMap was also used to determine the length (in miles) of each link in the network. A list of the links including the length of each is given in Appendix C. Matlab assumes all links in a network have a length of 1 unless otherwise specified. This can be altered by adding a weight to each link, which the program treats as a distance [35]. The analysis was first performed with link lengths included.

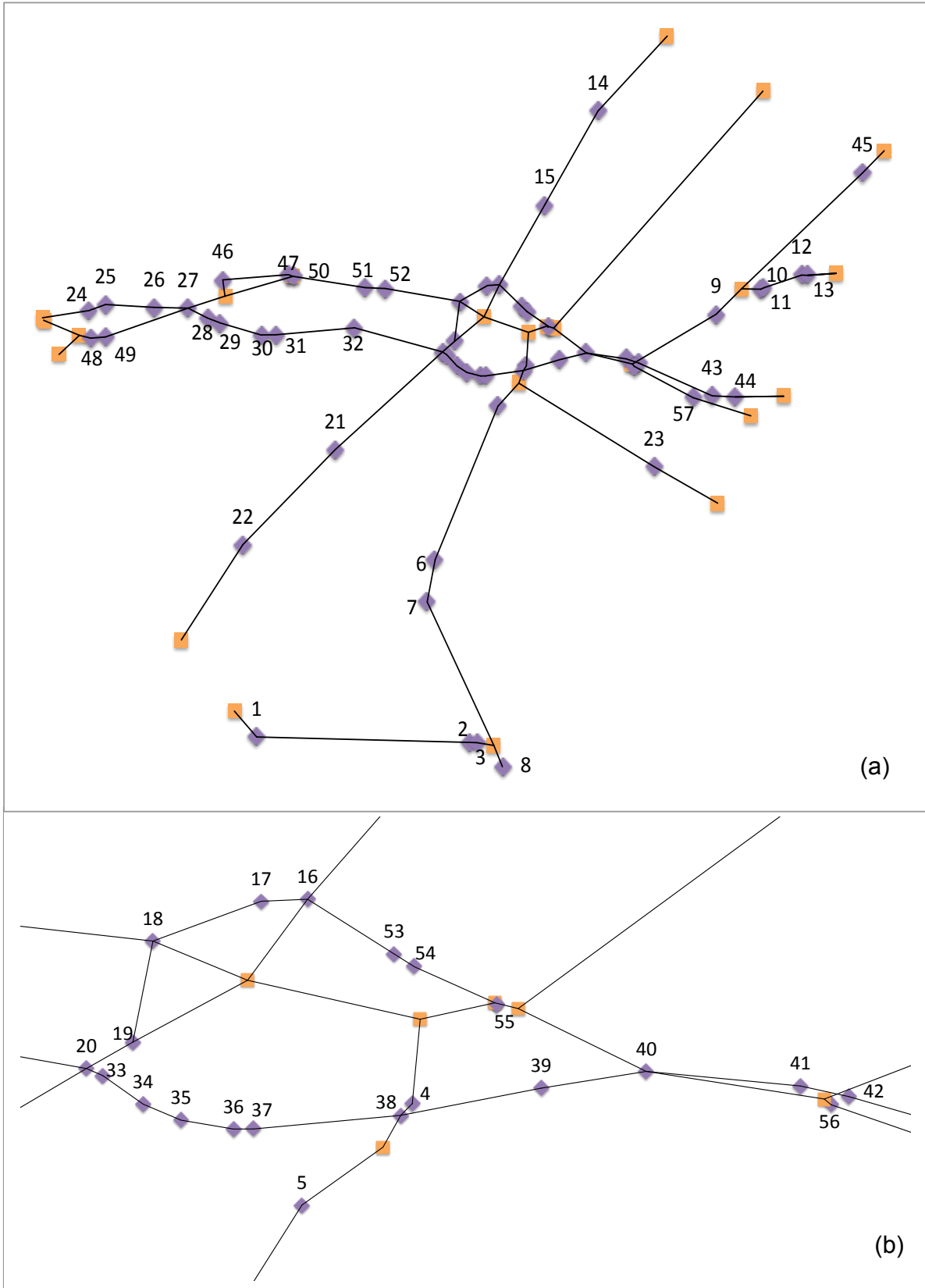


Figure 12 a.) Map of Albemarle County Highway Network, and b.) Enhanced View of Charlottesville to show detail

The goal of this study is to evaluate the effect that adding weight to links has on the network's parameters. Weights were assigned according to the importance of each link. To model the importance of each roadway section in Albemarle County, annual average daily traffic (AADT) data was used. AADT counts are from 2014 and were published by the Virginia Department of Transportation (VDOT) [36]. VDOT reports AADT for sections of the roadway of various lengths. The boundaries of these sections were either a county line or an intersection with another road. These boundaries did not always align with the bridge locations. Where they did, the AADT for those links is precisely known. For the roadway sections where the VDOT sections did not match the links in the studied network, a weighted average was taken to estimate the AADT. The AADT values computed for each link are shown in Appendix C.

Because weights had already been added to the links to represent the link lengths, these weight values were altered to incorporate AADT data. Two methods were used to accomplish this. The first altered the weight value directly proportional to AADT, and the second considered the order of magnitude of the AADT. Formulas for the altered weights are shown in Equations 6 and 7 below.

$$\text{Altered Weight 1} = \frac{\text{Link Length}}{\left(\frac{\text{AADT}}{1,000}\right)} \quad (6)$$

$$\text{Altered Weight 2} = \frac{\text{Link Length}}{\log_{10}(\text{AADT})} \quad (7)$$

The values for each link weight for both weighting schemes are shown in Appendix C.

With the networks created, average shortest path distance, diameter, link density, and average node degree were calculated for each. Then, nodes were removed using RNRS and TNRS. For RNRS, a random number generator determined the order of node removal. Two strategies were used for TNRS, both using betweenness centrality to rank nodes. The first, TNRS-a, involved removing nodes

based on the node ranking of the initial network. For the second method, TNRS-b, the betweenness centralities were recalculated after each node removal to determine the next node to be removed. After each node removal, the four properties were recalculated.

Results and Discussion

This section presents the results for the unweighted Albemarle County highway network and for the two weighting schemes tested. In all plots shown in this section, the values were normalized to show the change from each property's value before any nodes were removed. The blue series, RNRS, shows data for node removal based on a random number generator. The red series, TNRS-a, shows data for node removal based on the betweenness centralities of the original network. The method involving recalculating betweenness centralities after every node removal is shown by TNRS-b, the green series. The first green data point shown is the last point before the two TNRS strategies diverge.

The unweighted network considered only the distance between each node in the analysis. Weighted Network 1 modified the weight directly proportional to AADT using Equation 6, while Weighted Network 2 considered the order of magnitude of AADT using Equation 7.

Unweighted Network

This section presents the results for the unweighted network, which includes the link lengths in the analysis.

Average Shortest Path Distance

Figure 13 shows the average shortest path distance results for the unweighted Albemarle County highway network.

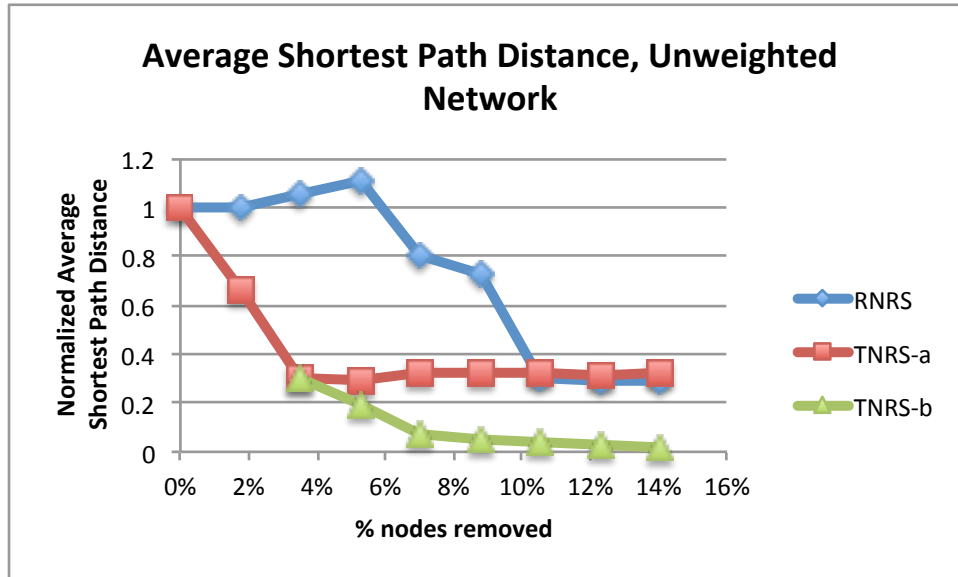


Figure 13. Average Shortest Path Distance for Unweighted Network

The RNRS and TNRS-a curves intersect at around 10.5% of nodes removed. This indicates that the Albemarle County highway network is resilient to external shocks as long as the event disturbs fewer than 10.5% of the network's bridges. If an event renders more than 10.5% of the studied bridges unusable, the network loses functionality and is not resilient.

The TNRS-b does not intersect with either other curve after it diverges from the TNRS-a curve. Instead, it quickly falls to near zero after about 7% of the nodes are removed. This suggests that the network is not resilient to a sophisticated targeted attack and that the system would be effectively shut down shortly after such an event.

The RNRS curve increases through the first three node removals. This occurs because none of those three nodes divided the network into disconnected subgraphs. The first three nodes removed were 47, 52, and 35. These nodes represent bridges on

VA-240 east of Crozet, US-250 between Crozet and Charlottesville, and I-64 between US-29 and VA-20, respectively. Their locations are shown in Figure 14 below in blue. The orange nodes representing intersections are not shown in any network images in this section. With these nodes removed, the network was still fully connected, and a path existed between every pair of remaining nodes. The shortest paths that previously used these nodes were rerouted and their length increased, leading to the increase in average shortest path distance for the entire network.

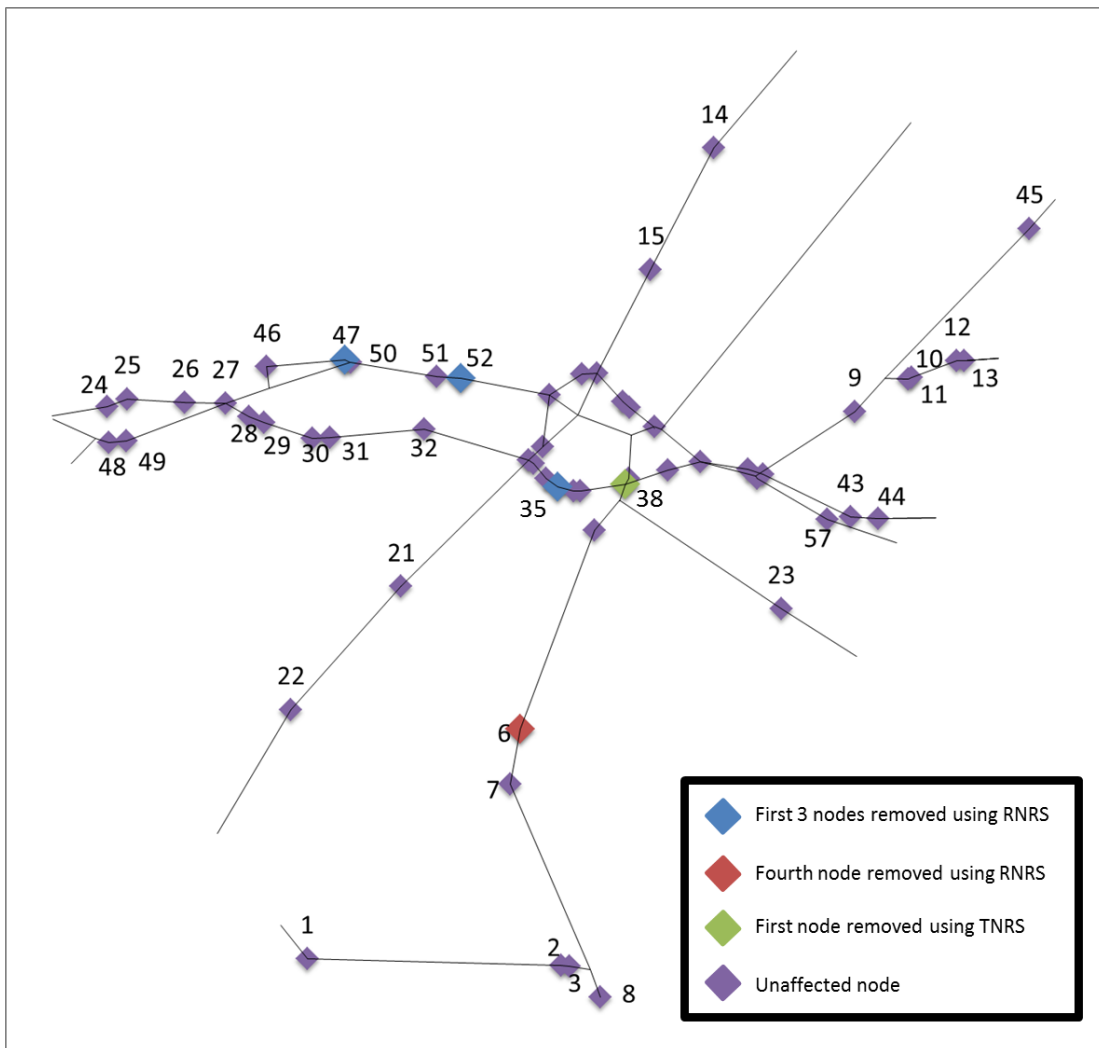


Figure 14. Location of Removed Nodes

With the fourth node removal, the average shortest path distance began to decrease. The fourth node removed, 6, represents a bridge on VA-20 south of Charlottesville, and its location is shown in red in Figure 14. While not one of the most centrally located nodes in the network, its removal created two separate subgraphs and disconnected the Scottsville area and the entire stretch of VA-6 in Albemarle County from the rest of the network, shown in Figure 15. The average shortest path distance plot is shown in the upper left of Figure 15, and the orange highlighted area shows the drop in average shortest path caused by the node elimination shown in the figure.

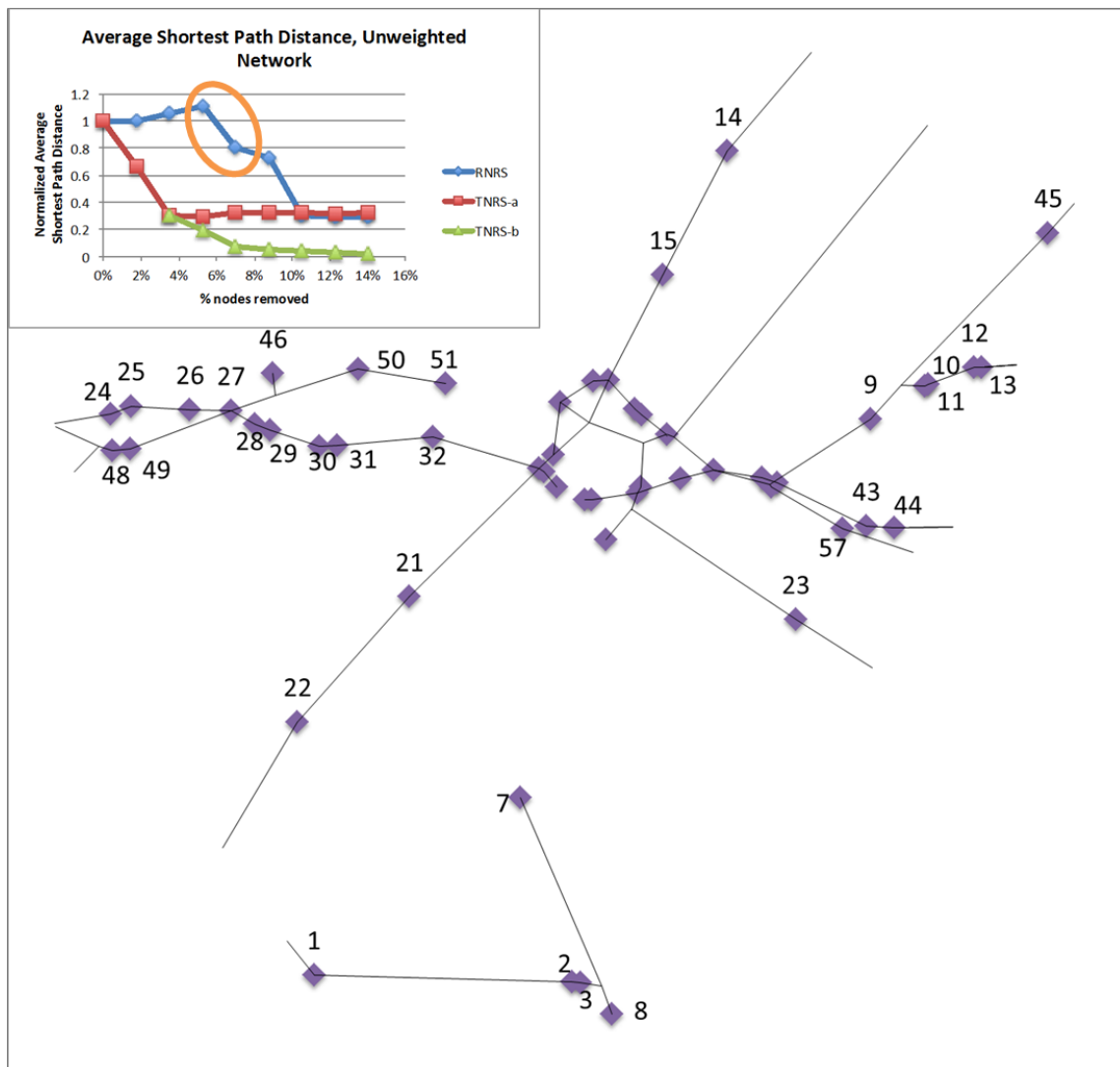


Figure 15. Disconnected Subgraphs due to Removal of Nodes 47, 52, 35, and 6

There is no longer a shortest path connecting every pair of nodes in the network, and the path distance between disconnected nodes becomes infinite. These infinite values were replaced with zeros to give the average inverse shortest path distance. A decrease in the average inverse shortest path distance indicates loss of network functionality as more and more path distances become infinite and are replaced with zeros.

The first node removed using both targeted node removal strategies is node 38, representing a bridge that forms the intersection between I-64 and VA-20. Its location is shown in green in Figure 14, and the resulting disconnected subgraphs are shown in Figure 16. Because the network is now disconnected, the average inverse shortest path is used. The upper left corner of Figure 16 highlights the decrease in average shortest path distance caused by this node's removal.

The red TNRS-a curve decreases sharply with the first two node removals and then levels out beginning with the third node removal. After the second node removal, the original network has been separated into three disconnected subgraphs, shown on the left of Figure 17.

The leveling-off effect is seen because the nodes are removed based on the initial betweenness centrality ranking. Node 4 is the third node removed in TNRS-a because it originally has a high betweenness centrality. After node 38 is removed, node 4 is left with only one link connected to it. When node 4 is removed, there is not much effect on the network because the node's degree was only 1. This effect continues through TNRS-a and explains the flat section of the data after the third node removal highlighted in the bottom center of Figure 17. Even after six additional nodes are

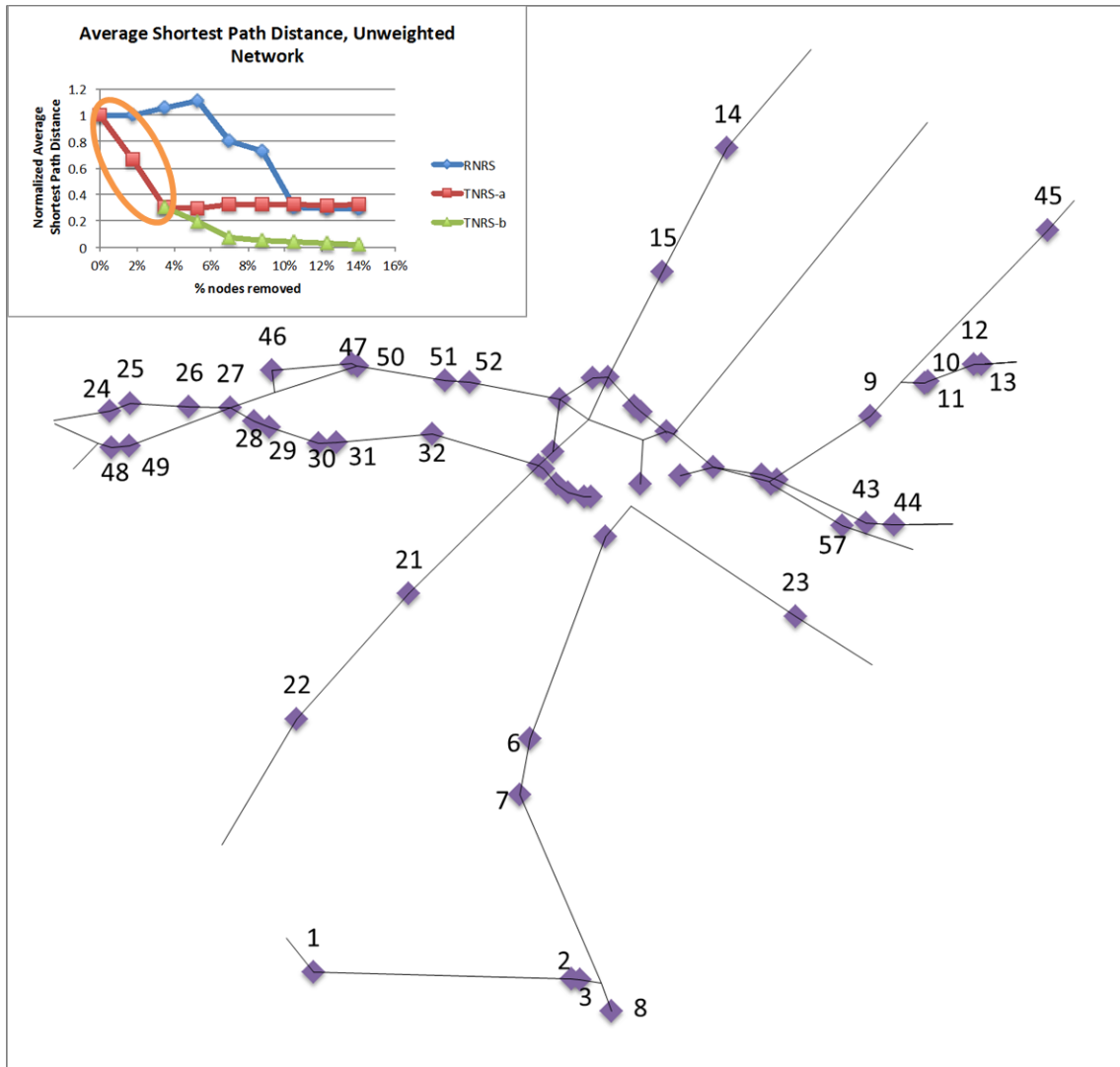


Figure 16. Disconnected Subgraphs due to Removal of Node 38

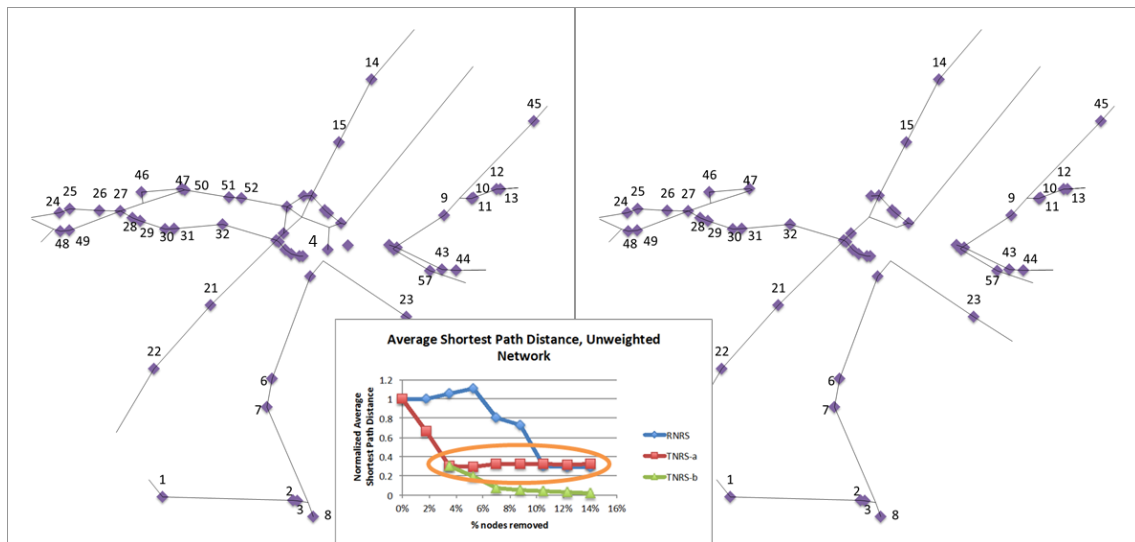


Figure 17. Disconnected Subgraphs due to TNRS-a

removed, the network is still comprised of the same three subgraphs, shown on the right of Figure 17. A difference between the two networks is visible, but no additional disconnected subgraphs have been created.

A flat section is not seen in TNRS-b because the betweenness centralities are recalculated after each node removal to maximize the detrimental effect on the network. After all eight rounds of node removal using TNRS-b, the network has been divided into 12 disconnected subgraphs, shown in Figure 18. This is why the TNRS-b data decreases throughout the analysis.

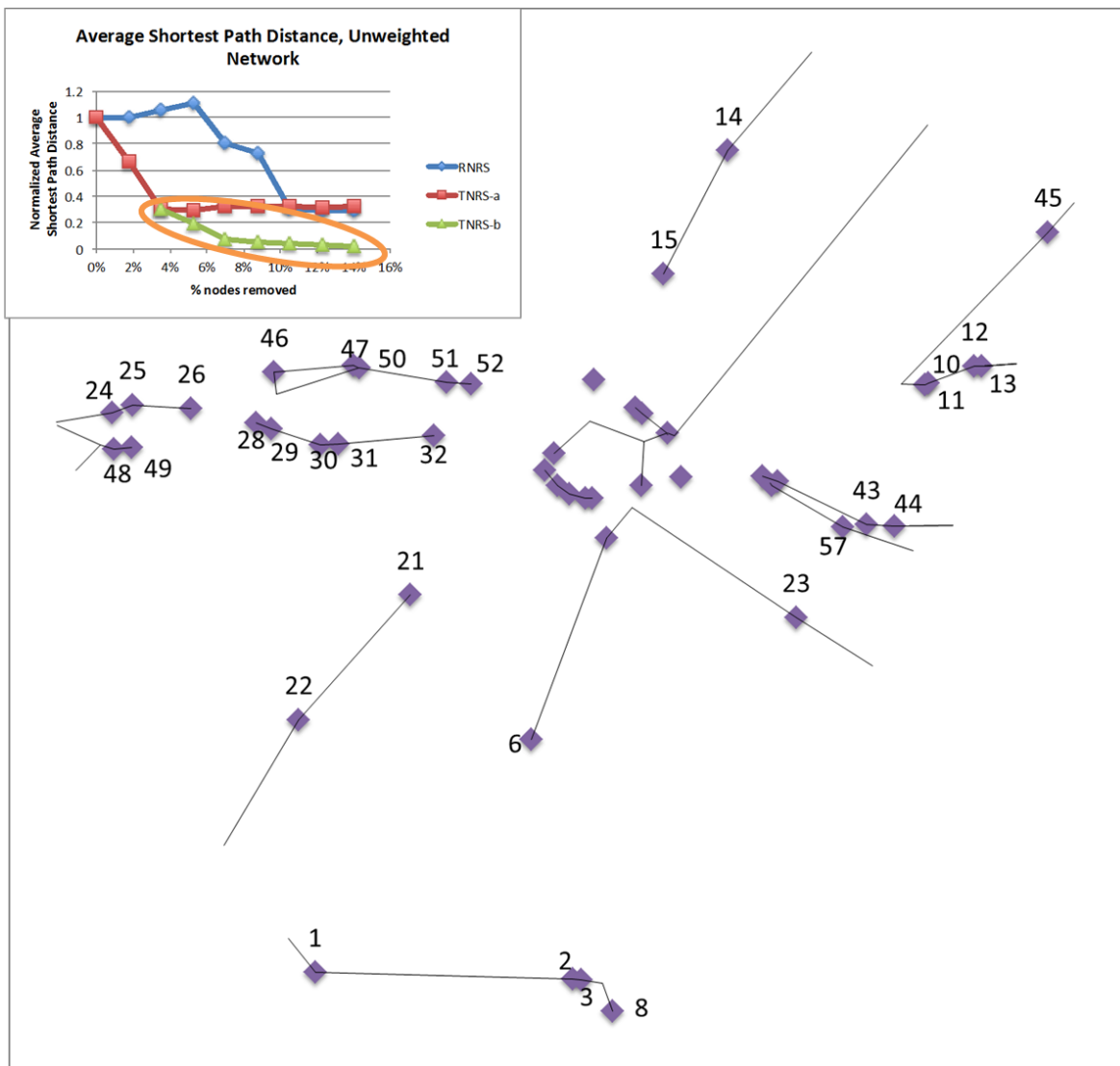


Figure 18. Disconnected Subgraphs due to TNRS-b

Diameter

Diameter calculations for the unweighted network are shown in Figure 19 below.

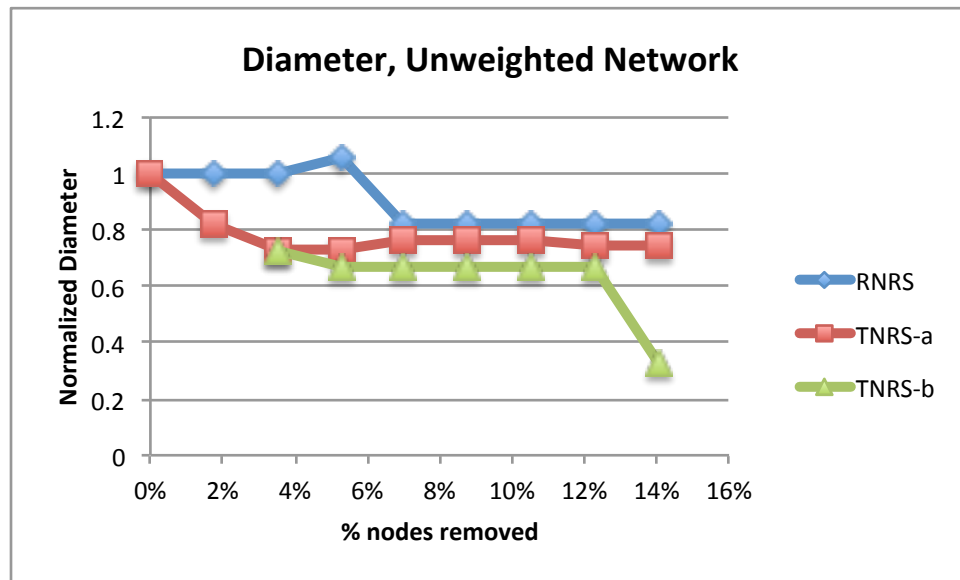


Figure 19. Diameter for Unweighted Network

The network's diameter is the shortest path distance for the pair of nodes that are farthest apart, so not every node removal will cause a change in the network's diameter. If the node removed is not on the shortest path connecting the pair of nodes that are the farthest apart, the network's diameter will likely not be affected. This explains the long periods of constant diameter in the plot above.

The exception occurs when a node with high betweenness is removed if that node is not on the diameter's path. Removal of a node with high betweenness requires the network to reroute many shortest paths, making them longer. One of these new shortest paths may be longer than the network's existing diameter, increasing the value of the property. This is the cause of the increase in diameter on the blue RNRS curve seen at around 6% of nodes removed and is due to the third node removal.

Any decrease in the network's diameter is a sign that the node removal divided the network into disconnected subgraphs. This is similar to the cause of decreases in

the average shortest path distance when the network becomes disconnected. The path distance between the pair of nodes that are the farthest apart becomes infinite in a disconnected graph, and its value is replaced by zero. The diameter of a disconnected graph is essentially the diameter of its largest subgraph, leading to the decreases seen in Figure 19.

The diameter curves do not intersect, so the critical point for the unweighted network is not as clear as it was using average shortest path distance. The difference between diameter values in the first few rounds of node removal was not as pronounced as the difference in average shortest path distance between curves, highlighted by the comparison of the two plots shown in Figure 20.

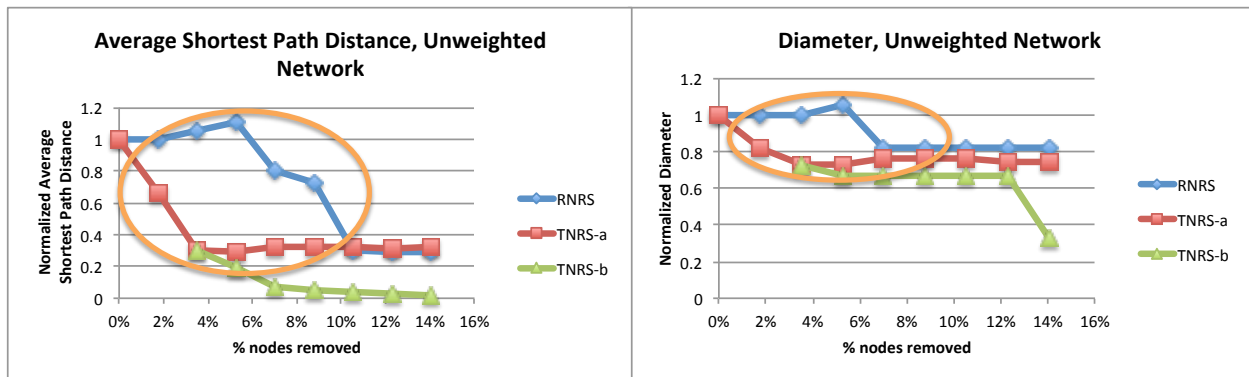


Figure 20. Comparison of Average Shortest Path Distance and Diameter Plots for the Unweighted Network

At around 7% of nodes removed, the RNRS and TNRS-a diameter curves are within 7.5% of each other. This is the critical point for the network, indicating that the network is resilient to external shock as long as fewer than 7% of nodes are removed. This is below the resilience index of 10.5% found when using average shortest path distance. In this case, using diameter leads to a decreased resilience index for the same network.

Link Density and Average Node Degree

Figures 21 and 22 show the results for link density and average node degree, respectively, for the unweighted network.

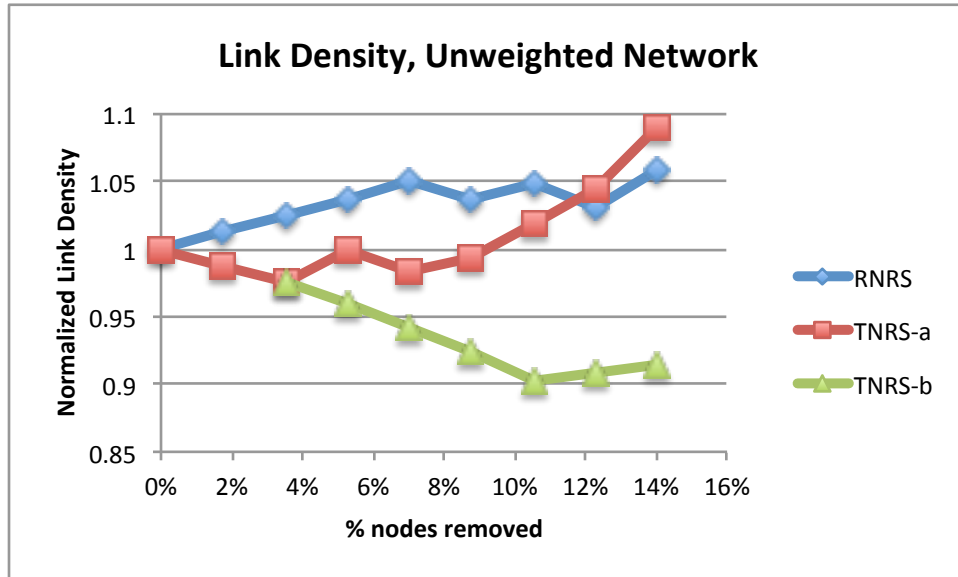


Figure 21. Link Density for Unweighted Network

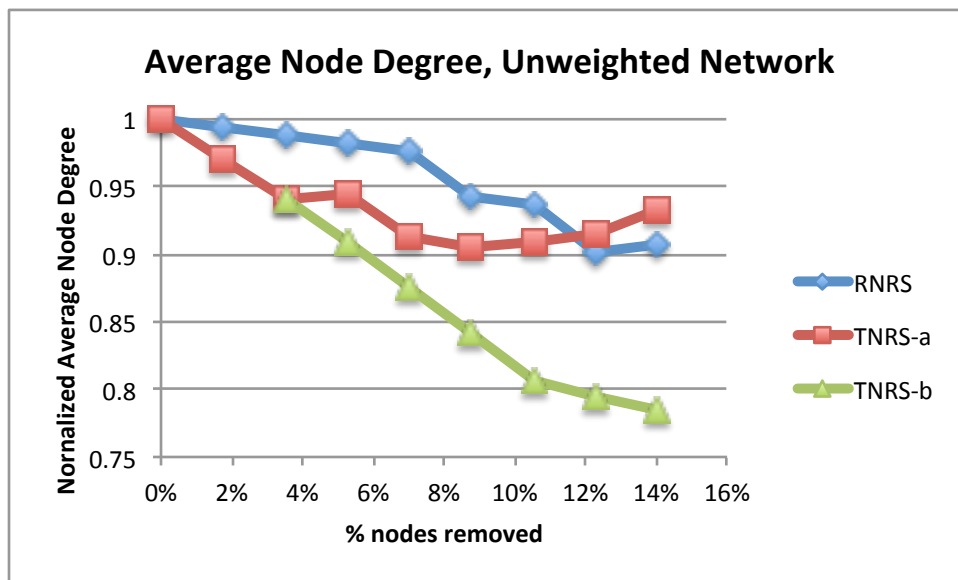


Figure 22. Average Node Degree for Unweighted Network

Both plots show an intersection between the RNRS and TNRS-a curves at 12% nodes removed. However, these do not represent the network's critical points. Link density and average node degree are useful network properties in many modeling scenarios and should be included in the analysis of various transportation infrastructure

systems. However, for the highway system being modeled here, with bridges as nodes and roadway sections as links, these metrics are not as useful as the two previously discussed.

Link density is a measure of how connected the network is. The network's link density is the proportion of the number of links in the network to the maximum number of links the network could support if every pair of nodes in the network was connected by a single link. Transportation infrastructure networks, including highway systems like the one studied here, are generally not designed to have high link density, and it would be impractical to do so. Link density is not as useful a metric as diameter or average shortest path distance.

Similarly, average node degree is not the best metric to consider when modeling a highway system in the way done in this study. Because the system models bridges as links, the majority of the nodes will have a degree of 2, representing the roadway that extends beyond the bridge in both traffic directions. The exception is bridges that located at intersections of two routes in the model, where it is assumed that a disruption to the bridge would disrupt traffic on both the route carried and the route crossed. In the Albemarle County network, only seven of the 57 nodes have this feature. Average node degree would be a more appropriate metric when considering other transportation infrastructure systems, such as airport networks or railway systems that are designed to have more than two links at each node.

Additionally, normalized link density and average node degree values calculated and shown in Figures 21 and 22 do not deviate from the original value as much as the average shortest path distance or diameter do. The RNRS and TNRS-a curves for

average shortest path distance in Figure 13 drop to 30% of their original value, and the TNRS-b curve falls to practically zero. In comparison, the RNRS and TNRS-a curves for link density and average node degree remain within 10% of the original value in either direction. Only the TNRS-b curves fall significantly, but only to around 90% for link density and 78% for average node degree. This confirms that removing nodes based on recalculated betweenness centrality rankings leads to greater disturbance in the system. Plots for link density and average node degree will not be discussed for the weighted networks studied but are shown in Appendix D.

Weighted Network 1

This section shows the results of the analysis of Weighted Network 1, in which the link weights include link length and AADT data, calculated using Equation M6.

Average Shortest Path Distance

Figure 23 shows the average shortest path distance curves for Weighted Network 1 (WN1).

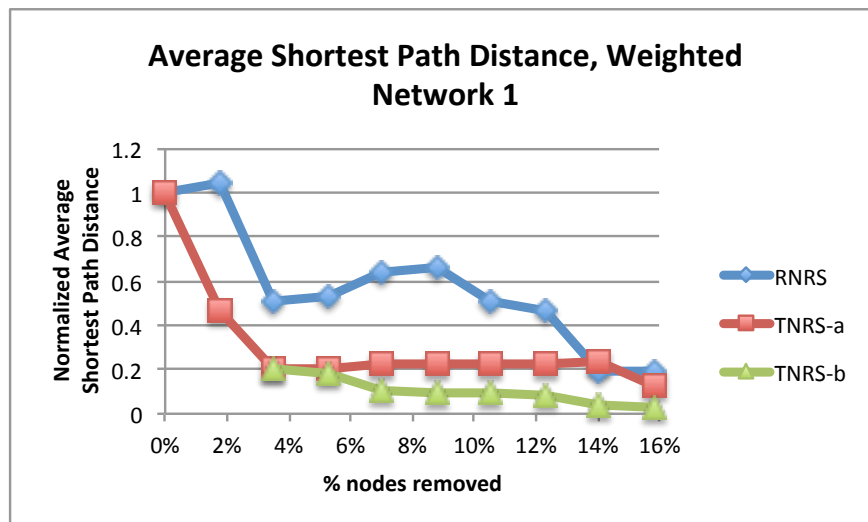


Figure 23. Average Shortest Path Distance for Weighted Network 1

The average shortest path distance plot for WN1 is similar to the same plot for the unweighted network in that the RNRS and TNRS-a curves intersect, but the TNRS-b curve does not intersect with either other curve. The critical point at which the RNRS and TNRS-a curves intersect occurs at around 14% of nodes removed, indicating the system is resilient to external shocks as long as fewer than 14% of the network's nodes are eliminated. This is higher than the unweighted network's value of 10.5%. This indicates that including the AADT data into the weighting of the links using Equation 6 increases the resilience of the system. Previously, using the unweighted network, the analysis was not able to take into account the importance of each route being studied. With AADT data included, the model is more complete. It now has the capability to recognize that removing a bridge on a less traveled road such as VA-6, where the AADT is 1150, should not affect the network's properties as much as removing a bridge on a more popular route, such as the U.S. 29 bypass, where AADT reaches 50,000.

One notable difference between the unweighted and WN1 average shortest path distance plots is that the RNRS curve in WN1 drops significantly after the second node removal, whereas the same curve in the unweighted plot increases from its original value until after the fourth node removal. The two plots are shown side-by-side in Figure 24 for comparison.

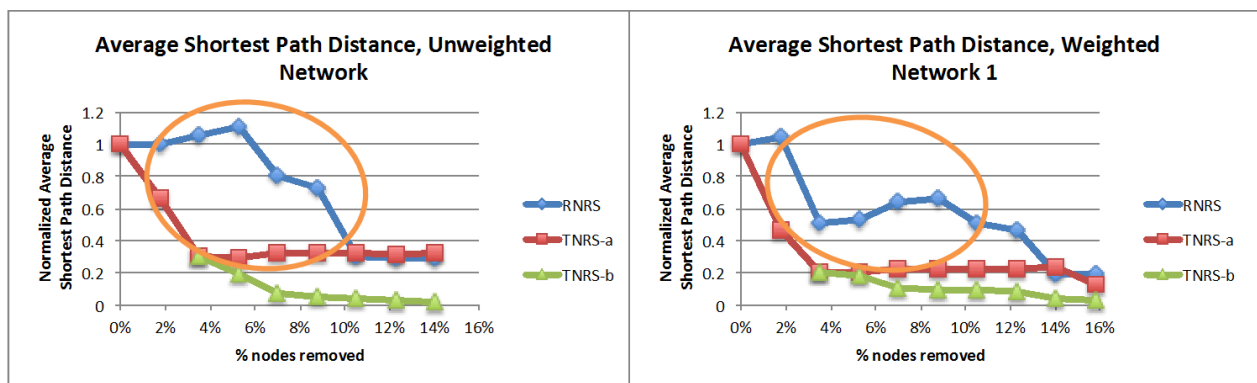


Figure 24. Comparison of Average Shortest Path Distance Plots for the Unweighted Network and WN1

The second node removed from WN1 using RNRS was node 6, a bridge on VA-22 south of Charlottesville, mentioned previously and shown in red in Figure 16. This is the same node that caused the drop in the RNRS curve for the unweighted network. The same phenomenon occurred for WN1: the node's removal created two disconnected subgraphs, leading to many shortest path values being replaced by zeros. However, with weighting included, the analysis was able to recognize that even though removing this node disconnected the network, it was not a very important node. The AADT of both links connected to that node is 7,000, which is on the low end of AADT values in the network. Later node removals did not further disconnect the network, and so increases in average shortest path distance were observed in the RNRS curve from the second node removal until the fifth, shown on the right in Figure 24.

Diameter

Figure 25 shows the diameter curves for WN1.

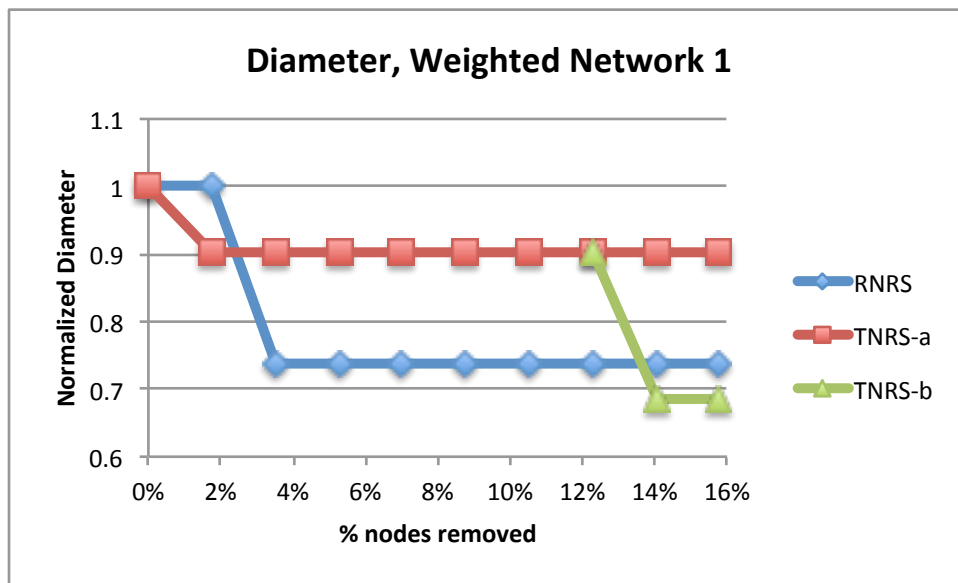


Figure 25. Diameter for Weighted Network 1

The RNRS and TNRS-a curves intersect at around 3% nodes removed. This would indicate that the network is resilient to external shock only as long as less than 3% of nodes are removed. This is much lower than 14%, the resilience index observed for WN1 using average shortest path distance. This phenomenon can be explained by a limitation in the weighting scheme used. The first node removed, 37, had no effect on the network's diameter. Node 6 was the second node removed. This node has been discussed previously and is shown in red in Figure 14. Its removal divides the network into two disconnected subgraphs, shown in Figure 26, with the corresponding drop in diameter highlighted in orange in the upper left. The southern subgraph includes the Scottsville area, the section of VA-20 south of Carters Mountain Road, and the entire section of VA-6 in Albemarle County.

The section of VA-6 connecting nodes 1 and 2 is 9.4 miles long. It is the second-longest link in the entire network. As previously discussed, VA-6 is the least-traveled road in the network, with an AADT of 1150. Because the weight of the link is the link's distance divided by its AADT, as per Equation 6, the weight of the VA-6 link becomes artificially inflated because the numerator is relatively large and the denominator is relatively small, leading to a larger link weight. With the network fully connected, the diameter's path traveled through node 6. With it removed, a different, shorter path becomes the network's diameter. This explains the sharp drop in the network's diameter after node 6 is removed. This same thing would have happened had any of the following nodes been removed instead of node 6: 1, 2, 3, 5, or 7. These six nodes are critical to the diameter analysis. It's likely that a different RNRS order would have yielded different results and that the blue RNRS curve in the upper left of Figure 26

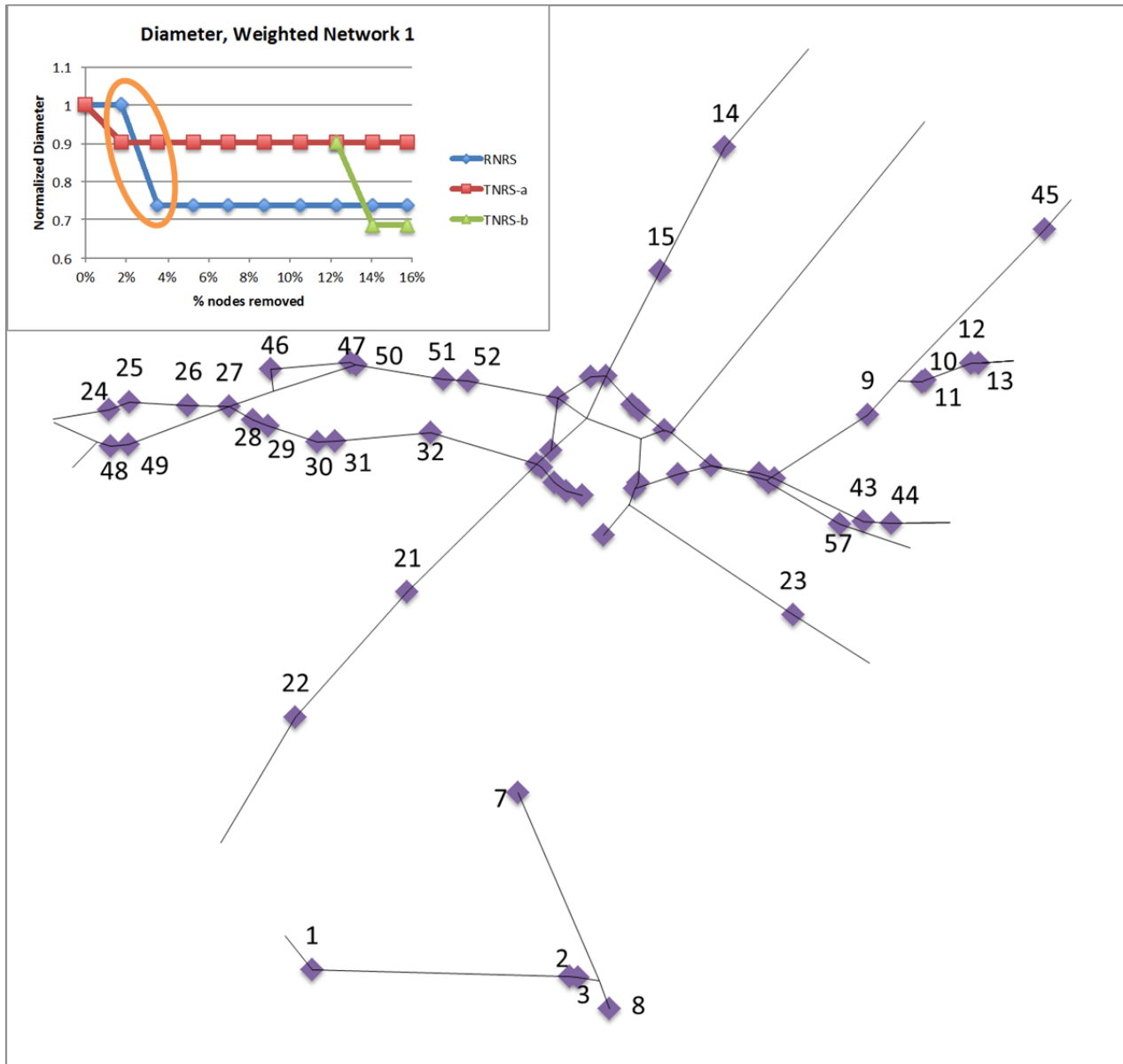


Figure 26. Disconnected Subgraphs due to removal of Nodes 37 and 6

would have remained above the red TNRS-a curve, giving a different resilience index for the network closer to the 14% index observed by measuring average shortest path distance.

Weighted Network 2

This section shows the results of the analysis of Weighted Network 2 (WN2), for which the link weights include link length and AADT data, calculated using Equation 7.

Average Shortest Path Distance

Figure 27 shows the average shortest path distance curves for WN2.

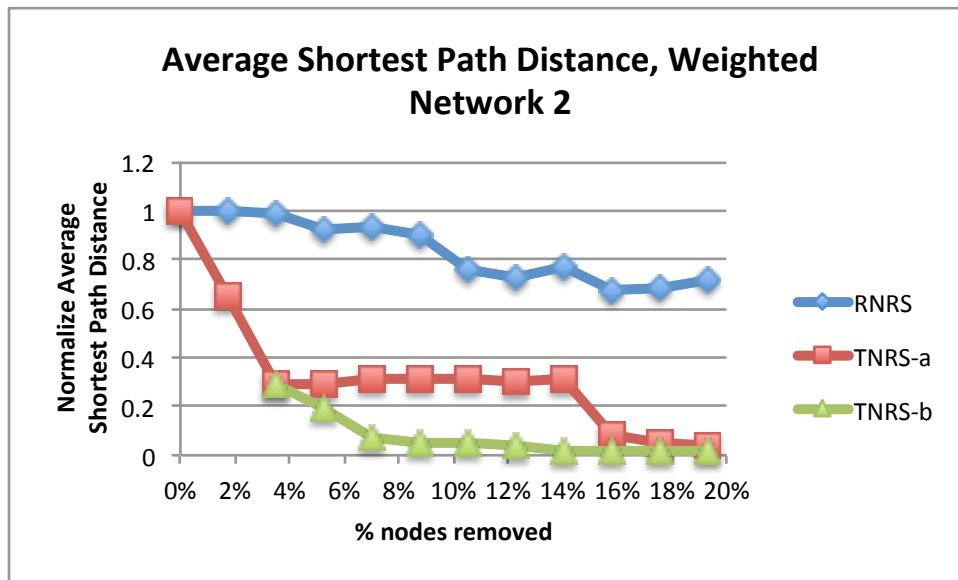


Figure 27. Average Shortest Path Distance for Weighted Network 2

The average shortest path distance plot for WN2 presents a special case because the RNRS and TNRS-a curves neither intersect nor come close enough to each other to determine the critical point of the network. The analysis was extended to include three additional rounds of node removal to bring the number of nodes removed to 11. This was done in an attempt to see if the curves would intersect. Instead of the extra round bringing the RNRS and TNRS-a curves closer together, it actually led them farther apart. After the 10th and 11th node removals, the RNRS values increased while the TNRS-a values decreased. At 19% nodes removed, the TNRS-a and TNRS-b curves had similar values, but both were practically zero, so this does not indicate a critical point. Additionally, comparing two different TNRS schemes is not as useful as comparing RNRS to TNRS when determining resilience index, because it is known that the TNRS-b curve will always be below the others.

The RNRS curve in Figure 27 does steadily decrease as more nodes are removed, but a sharp decrease like those seen in similar plots for the unweighted network and WN1 (Figures 13 and 23, respectively) is not seen here. Instead, the average shortest path distance never falls below 65% of its original value. In contrast, both TNRS curves fall to less than 30% of the original values after only two node removals. The TNRS-b curve quickly falls to near zero, and the TNRS-a curve also reaches that point later in the analysis. This indicates that the network is relatively resilient to random disturbances but very vulnerable to targeted attacks. This is one characteristic of a scale-free network. Some examples of scale-free networks are cells, the Internet, and social networks [37]. The node degree distribution of a scale-free network follows a power law distribution as opposed to being clustered around a mean. This leads to increased redundancy in the network and therefore a higher tolerance to random disturbance. However, due to the power law nature of node degree distribution, a few nodes will have very high degrees, and their removal could devastate the system [38]. Even though WN2 follows the same node degree distribution as the unweighted network and WN1, it behaves like a scale-free network when average shortest path distance is used as a metric. A resilience index of the type discussed in this study is not available for a scale-free network.

Diameter

Figure 28 shows the average shortest path distance curves for WN2.

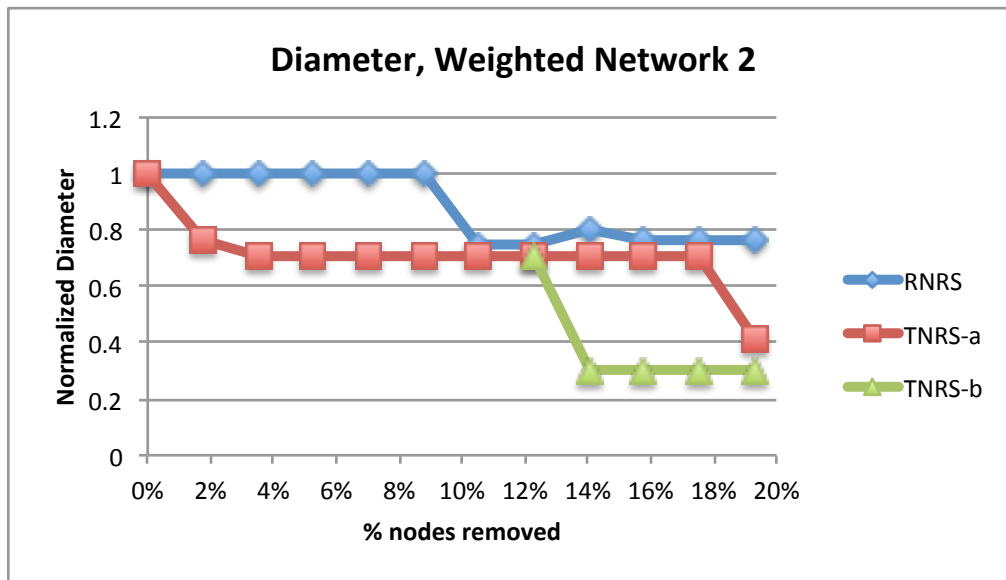


Figure 28. Diameter for Weighted Network 2

Unlike the plot for average shortest path distance of WN2 discussed earlier, some conclusions can be drawn about WN2 from the diameter plot. The diameter plot for WN2 is similar to that of the unweighted network seen in Figure 19 because the curves do not intersect. However, the RNRS and TNRS-a curves do approach each other at around 10.5% nodes removed. At that point, the values are 5% different, so that point may be called the critical point and 10.5% is the network's resilience index. Because there is no resilience index available for the average shortest path distance of WN2, 10.5% will be considered WN2's resilience index. As long as fewer than 10.5% of nodes are removed, the network is resilient to external shocks.

Summary of Results

Table 3 below gives a summary of the results discussed previously. The smaller value for each network is the controlling value, except in the case of WN1, where the resilience index based on diameter calculations might be misleading.

Table 3. Summary of Resilience Indices

Resilience Indices	Average Shortest Path Distance	Diameter
Unweighted Network	10.5%	7%
WN1	14%	3% *
WN2	n/a **	10.5%
<i>* as previously discussed, possibly unreliable</i>		
<i>** displays characteristics of scale-free network</i>		

Conclusions

The goal of this study was to incorporate weighting based on traffic information into a methodology for calculating a transportation network's resilience index using graph theory. Two weighting schemes were proposed: one using direct proportionality of traffic volume and the other considering the traffic volume's order of magnitude. The method was applied to a network of state and federal highways in Albemarle County, Virginia. The unweighted network's resilience index was found to be 7%. The direct proportionality method, used in WN1, led to the highest resilience index for the network, 14%. The order of magnitude method, used in WN2, also yielded a higher resilience index – 10.5% – than that of the unweighted network.

Using the direct proportionality method of WN1, the resilience index of the network increased by 100%. Twice as many nodes may be removed from the system before it is not resilient to external shock. The order of magnitude method increased the resilience index by 50%. The fact that both weighting methods increased the resilience index of the network highlights the importance of adding weights to links in analyses such as the one performed here: it offers a more complete picture of the system, and failing to include it can deflate the network's resilience index.

This study is not without its limitations. It is primarily intended to highlight the methodology used to determine a transportation network's resilience index. The use of the Albemarle County highway network is purely illustrative, and the results discussed are not meant to be used in transportation planning or maintenance efforts. In performing this analysis on the Albemarle County highway network, some simplifying assumptions were made that likely artificially deflated the resilience indices of the network. Should these be corrected, the resilience indices of the network would likely increase.

Twin bridges were modeled as a single node in this analysis. It's unlikely that both would be disabled at the same time, so if one is impassable the other could likely be used to carry traffic in both directions. The example discussed here does not consider this effect. Similarly, bridges that carry one route in the study while crossing another were modeled as a single node. This means that should that node be removed, traffic would be impeded on both the route carried and route crossed. This might be the case for a bridge collapse when both routes would be closed to traffic, but it does not

consider maintenance efforts in which every care is taken to keep as many traffic lanes open as possible.

This analysis considered a total of 10 routes that run through Albemarle County. There are many smaller roads that traverse the county that were not modeled here. This likely led to underestimations of the network's resilience because, in the event of a bridge outage on one of the routes studied, there are ways to reroute traffic around the outage using routes not studied here.

Future Work

There are many aspects of this study that can be expanded into opportunities for further research. In future studies, RNRS analyses for each network could be run multiple times with different node removal orders. Because the order of node removal is left up to chance in RNRS, only running the analysis once might be insufficient, especially for smaller networks. This was seen in the diameter plot for WN1, shown in Figure 25. Taking the average values of several RNRS analyses of the same network would likely lead to a more accurate resilience index for the network. The method could also be improved by the ability to partially reduce a node's functionality. In the analysis presented here, the options for a node are binary: it's either on or off. If the node's functionality could be decreased without rendering it completely inoperative, this feature could be used to simulate maintenance efforts in which care is taken to not completely impede traffic.

Further study should be done to see if the scale-free behavior observed in the average shortest path distance plot for WN2 is a feature of the weighting method or a

peculiarity of the example network used here. First, the method could be applied to other types of transportation infrastructure systems, such as airport networks and railway systems, to see if they exhibit the same behavior when the order of magnitude weighting scheme is used. If they do, more in-depth analysis should be performed to determine why using the order of magnitude weighting scheme leads to scale-free behavior in transportation networks.

This method could be used to further develop the resilience index of the Albemarle County highway network. The graph would need to include not only the 10 routes studied here, but also the smaller routes that were ignored in this example. Additionally, a directed graph could be used to model traffic in each direction separately. This would eliminate the need for twin bridges to be modeled as a single node. If a bridge that has a twin is removed from the network, conditional links could be employed to reroute traffic across the other bridge, simulating how these issues are handled in the real world.

After the methodology presented here is refined, it has many real world applications and opportunities for further study. Some researchers even foresee using graph theory and resilience analysis to aid in transportation system planning and design [17].

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Appendix A: Bridge Node Information

Node #	Road Carried	Structure Number	Year Built	Lanes Carried	Bridge Kind	Bridge Type
1	VA-6	415	1932	2	concrete	deck arch
2		408	1935	2	concrete	tee beam
3		407	1935	2	concrete	tee beam
4	VA-20	443	1970	2	prestressed concrete	stringer/multi-beam or girder
5		420	1932	2	concrete	slab
6		27152	2004	2	steel continuous	stringer/multi-beam or girder
7		23360	1992	2	prestressed concrete	slab
8		447	1968	2	steel	stringer/multi-beam or girder
9	VA-22	454	1932	2	concrete	slab
10		452	1932	2	concrete	slab
11		451	1932	2	concrete	slab
12		449	1923	2	concrete	slab
13	US-29	448	1935	2	prestressed concrete	box beam or girders-multiple
14		481	1965	2	steel	stringer/multi-beam or girder
15		25821	1897	4	steel continuous	stringer/multi-beam or girder
16		unknown	2012	6	steel	stringer/multi-beam or girder
17		475	1977	4	steel	stringer/multi-beam or girder
18		621	1961	5	steel	stringer/multi-beam or girder
19		484	1970	4	steel	stringer/multi-beam or girder
20		552	1970	3	prestressed concrete	stringer/multi-beam or girder
21		461	1976	2	steel	stringer/multi-beam or girder
22		25120	1997	2	concrete	stringer/multi-beam or girder
23	VA-53	27374	2005	2	steel	stringer/multi-beam or girder
24	I-64	517	1974	2	steel	stringer/multi-beam or girder
25		507	1974	2	steel	stringer/multi-beam or girder
26		759	1972	2	steel	stringer/multi-beam or girder
27		546	1969	2	prestressed concrete	stringer/multi-beam or girder
28		550	1969	2	steel continuous	stringer/multi-beam or girder
29		696	1969	2	prestressed concrete	stringer/multi-beam or girder
30		554	1969	2	steel continuous	stringer/multi-beam or girder
31		556	1969	2	prestressed concrete	stringer/multi-beam or girder
32		572	1970	2	steel	stringer/multi-beam or girder
33		562	1970	3	steel	stringer/multi-beam or girder

Node #	Road Carried	Structure Number	Year Built	Lanes Carried	Bridge Kind	Bridge Type	
34	I-64	564	1970	2	steel	stringer/multi-beam or girder	
35		568	1970	2	prestressed concrete	stringer/multi-beam or girder	
36		682	1969	4	steel	stringer/multi-beam or girder	
37		522	1969	3	prestressed concrete	stringer/multi-beam or girder	
38		526	1969	3	steel	stringer/multi-beam or girder	
39		534	1969	2	steel continuous	girder and floorbeam system	
40		530	1969	2	steel continuous	frame	
41		540	1969	2	concrete	tee beam	
42		536	1969	2	steel	stringer/multi-beam or girder	
43		657	1969	2	steel	stringer/multi-beam or girder	
44		544	1969	2	steel continuous	stringer/multi-beam or girder	
45		VA-231	581	1939	2	concrete	slab
46		VA-240	589	1921	2	concrete	tee beam
47			591	1921	2	prestressed concrete	box beam or girders-multiple
48	US-250	602	1945	2	prestressed concrete	box beam or girders-multiple	
49		601	1945	2	steel	stringer/multi-beam or girder	
50		598	1942	2	steel	stringer/multi-beam or girder	
51		596	1936	2	concrete	frame	
52		610	1932	3	concrete	slab	
53		unknown	2006	5	steel	stringer/multi-beam or girder	
54		unknown	2013	4	steel	stringer/multi-beam or girder	
55		23447	1992	7	steel continuous	stringer/multi-beam or girder	
56		595	1939	2	prestressed concrete	box beam or girders-multiple	
57		607	1932	3	concrete	slab	

Appendix B: Intersection Node Information

Node #	Feature 1	Feature 2
58	I-64	Nelson County Line
59	US-250	Nelson County Line
60	VA-151	Nelson County Line
61	US-29	Nelson County Line
62	VA-6	Nelson County Line
63	VA-53	Fluvanna County Line
64	US-250	Fluvanna County Line
65	I-64	Fluvanna County Line
66	VA-22	Louisa County Line
67	VA-231	Louisa County Line
68	VA-20	Orange County Line
69	US-29	Greene County Line
70	US-250	VA-151
71	US-250	VA-240 (south of Crozet)
72	US-250	VA-240 (east of Crozet)
73	VA-6	VA-20
74	VA-22	VA-231
75	JS-29 BUS	US-250 BUS
76	VA-20	US-250 BUS
77	VA-20	VA-53
78	JS-250 BUS	US-250 BYP
79	JS-250 BYP	VA-20
80	US-250	VA-22

Appendix C: Link Information

link #	route	start node	end node	distance (miles)	AADT	WN1 Weight	WN2 Weight	
1	VA-6	62	1	2.24	1144	1.96E+00	7.31E-01	
2		1	2	9.38		8.20E+00	3.07E+00	
3		2	3	0.31		2.72E-01	1.02E-01	
4		3	73	0.68		5.97E-01	2.23E-01	
5	VA-20	68	79	13.55	13096	1.03E+00	3.29E+00	
6		76	4	1.49	12795	1.17E-01	3.63E-01	
7		4	38	0.25		1.94E-02	6.05E-02	
8		38	77	0.50	22000	2.26E-02	1.14E-01	
9		77	5	1.30	7059	1.85E-01	3.39E-01	
10		5	6	6.84		9.68E-01	1.78E+00	
11		6	7	1.68		2.38E-01	4.36E-01	
12		7	73	7.02		9.95E-01	1.82E+00	
13		73	8	0.87		1.23E-01	2.26E-01	
14		80	9	3.79		7728	4.90E-01	9.75E-01
15	9	74	1.30	1.69E-01	3.36E-01			
16	VA-22	74	10	0.93	1800	5.18E-01	2.86E-01	
17		10	11	0.12		6.90E-02	3.82E-02	
18		11	12	1.68		9.32E-01	5.15E-01	
19		12	13	0.25		1.38E-01	7.64E-02	
20		13	66	0.68		3.80E-01	2.10E-01	
21		69	14	3.17		41995	7.55E-02	6.85E-01
22	US-29	14	15	4.10	9.77E-02		8.87E-01	
23		15	16	3.54	8.43E-02		7.66E-01	
24	US-29 bypass	16	17	0.50	37000	1.34E-02	1.09E-01	
25		17	18	1.37	47000	2.91E-02	2.93E-01	
26		18	19	1.55	45000	3.45E-02	3.34E-01	
27	US-29	16	75	1.37	24714	5.53E-02	3.11E-01	
28	business	75	19	1.93	11975	1.61E-01	4.72E-01	
29	US-29	19	20	0.62	51000	1.22E-02	1.32E-01	
30		20	21	6.03		4.16E-01	1.45E+00	
31		21	22	5.78		14484	3.99E-01	1.39E+00
32		22	61	4.66			3.22E-01	1.12E+00
33	VA-53	77	23	7.77	7576	1.03E+00	2.00E+00	
34		23	63	1.80		2.38E-01	4.64E-01	
35	I-64	58	24	1.93	33000	5.84E-02	4.26E-01	
36		24	25	0.75		2.26E-02	1.65E-01	
37		25	26	2.05		6.21E-02	4.54E-01	
38		26	27	1.43		4.33E-02	3.16E-01	
39		27	28	0.87	38000	2.29E-02	1.90E-01	
40		28	29	0.62		1.64E-02	1.36E-01	
41		29	30	1.74		4.58E-02	3.80E-01	
42		30	31	0.62		1.64E-02	1.36E-01	
43		31	32	3.23		8.50E-02	7.06E-01	

link #	route	start node	end node	distance (miles)	AADT	WN1 Weight	WN2 Weight
44	I-64	32	20	3.79	39000	9.72E-02	8.26E-01
45		20	33	0.19	48000	3.88E-03	3.98E-02
46		33	34	0.62		1.29E-02	1.33E-01
47		34	35	0.50		1.04E-02	1.06E-01
48		35	36	0.25		5.18E-03	5.31E-02
49		36	37	0.19		37000	5.04E-03
50		37	38	1.55	4.20E-02		3.40E-01
51		38	39	1.55	4.20E-02		3.40E-01
52		39	40	1.12	3.02E-02		2.45E-01
53		40	41	1.68	37169	4.51E-02	3.67E-01
54		41	42	0.50		1.34E-02	1.09E-01
55		42	43	3.23		8.69E-02	7.07E-01
56		43	44	0.93		2.51E-02	2.04E-01
57		44	65	0.25		6.69E-03	5.44E-02
58	VA-151	60	70	1.12		9700	1.15E-01
59	VA-231	74	45	6.84	4900	1.39E+00	1.85E+00
60		45	67	1.24		2.54E-01	3.37E-01
61	VA-240	71	46	0.62	5883	1.06E-01	1.65E-01
62		46	47	3.36		5.70E-01	8.90E-01
63		47	72	0.19		3.17E-02	4.95E-02
64	US-250	59	70	1.74	6200	2.81E-01	4.59E-01
65		70	48	0.50	6235	7.97E-02	1.31E-01
66		48	49	0.62		9.97E-02	1.64E-01
67		49	27	3.67		5.88E-01	9.66E-01
68		27	71	1.62	11000	1.47E-01	4.00E-01
69		71	72	2.98	9100	3.28E-01	7.53E-01
70		72	50	0.06	12538	4.96E-03	1.52E-02
71		50	51	2.98		2.38E-01	7.28E-01
72		51	52	0.81		6.44E-02	1.97E-01
73		52	18	3.17		2.53E-01	7.73E-01
74	US-250 business	18	75	1.18	12000	9.84E-02	2.89E-01
75		75	76	2.17	22502	9.66E-02	5.00E-01
76		76	78	0.87	13555	6.42E-02	2.11E-01
77	US-250 bypass	16	53	1.43	31805	4.49E-02	3.17E-01
78		53	54	0.31	32474	9.57E-03	6.89E-02
79		54	78	1.06		3.25E-02	2.34E-01
80	US-250	78	55	0.06	30458	1.91E-03	1.38E-02
81		55	79	0.19		6.12E-03	4.16E-02
82		79	40	1.74		5.71E-02	3.88E-01
83		40	80	2.05		22000	9.32E-02
84		80	56	0.12	5200	2.39E-02	3.34E-02
85		56	57	2.67		5.14E-01	7.19E-01
86		57	64	1.62		3.11E-01	4.35E-01

Appendix D: Link Density and Average Node Degree Plots for Weighted Networks

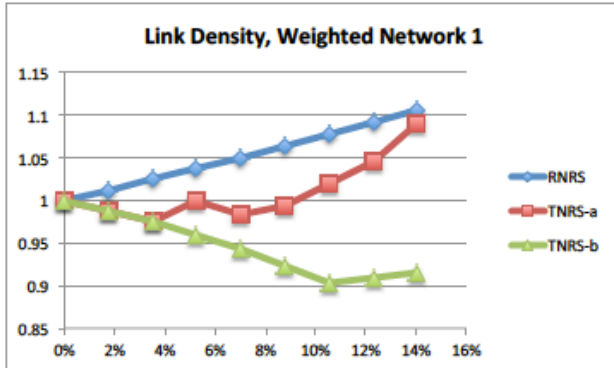


Figure D1: Link Density for Weighted Network 1

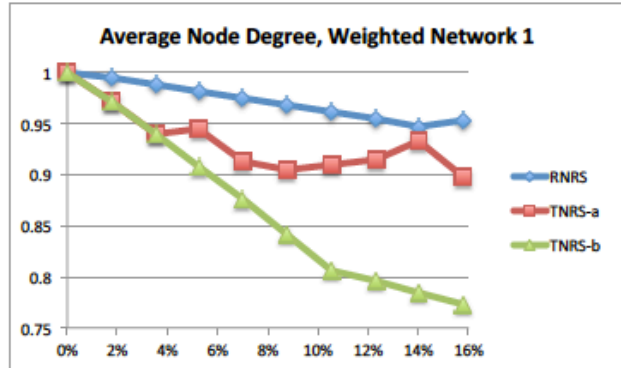


Figure D2: Average Node Degree for Weighted Network 1

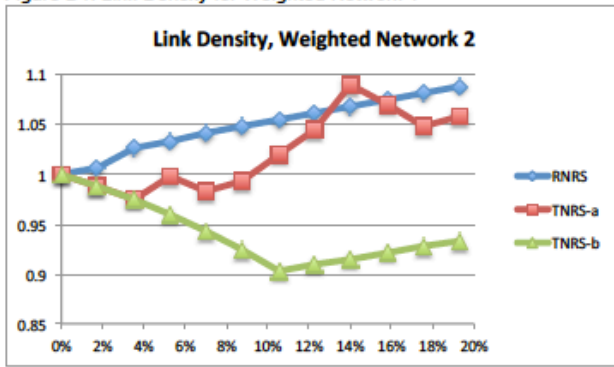


Figure D3: Link Density for Weighted Network 2

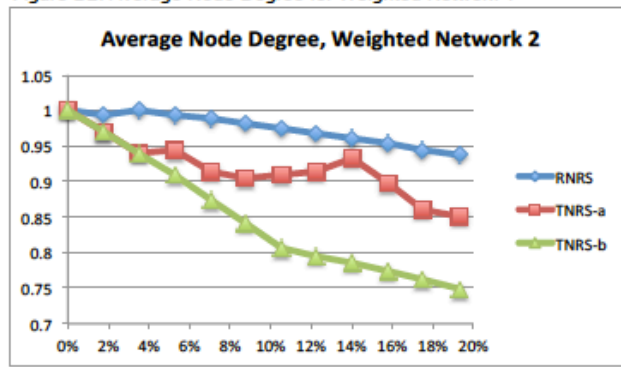


Figure D4: Average Node Degree for Weighted Network 2

Table of Contents

1. Introduction	70
1.1 Background	70
1.2 Purpose	70
1.3 Methodology	70
2. Concepts of Resilience	70
2.1 Definitions	71
2.2 Resilience Quantification Methods	74
2.3 Risks and Resilience	77
3. Transportation Resilience	79
4. Coastal Resilience Analysis	83
4.1 Introduction	83
5. Resilience: Coastal Flooding and Transportation System	85
5.1 Introduction	85
6. Concluding Remarks	87
7. References	87

List of Figures

Figure 1. High resilience of a system against a disturbance.	72
Figure 2. Low resilience of a system against a disturbance.	72
Figure 3. Medium resilience of a system against a disturbance.	73
Figure 4. Resilience taxonomy [10].	74
Figure 5. Conceptualized resilience triangle from disaster research [11].	75
Figure 6. Conceptualized resilience triangle for a major weather event [13].	76
Figure 7. Perspectives, concepts, and methodologies in resilience engineering.	79
Figure 8. Sea level rise impacts.	84
Figure 9. Cascading impacts of sea level rise on infrastructure systems [28].	86
Figure 10. Role of adaptive strategies and tactics in reducing impacts and consequences [29].	87

List of Tables

Table 1. Comparison between risk management and resilience.	77
Table 2. Resilience perspectives [19].	78
Table 3. Proposed principles of resilience for the transport system [21].	80
Table 4. Summary of qualitative and quantitative measurement approaches [21].	81
Table 5. Summary of five key indicators of climate change [27].	84

1. Introduction

1.1 Background

The issue of coastal sea level rise has many regions and cities in the U.S. initiated plans and strategies to minimize the effect of the sea level rise. The sea level rise will have major impact on the transportation systems and other critical infrastructure. The ability to correctly predict the effects on the vulnerable areas and the interaction with other infrastructure systems is of paramount importance. There have been various initiatives of this topic, both at the federal and regional level.

1.2 Purpose

The purpose of this report is to provide a synthesis of coastal flooding on transportation systems, by highlighting

- a) The state of the art
- b) The key variables and parameters needed by decision makers for design and planning
- c) To understand the dynamic nature of resilience approaches/methods
- d) To show that coastal flooding may have different effects on different parts of critical infrastructure network.

1.3 Methodology

The approach used to attain the objective (purpose) of this report involves:

- a) Study of scientific and technical papers on the subject
- b) Case studies published by national and international consultants on the subject
- c) Reports published by the Federal government
- d) Critical review of the analytical approaches used by different reports/papers to address coastal flooding/transportation resilience
- e) Recommendation on methods to quantitatively address resilience of such complex systems.

Concepts of Resilience

1.4 Definitions

The concept of resilience has emerged as a characteristic of complex, dynamic systems in a range of disciplines, including ecology, economics, and environmental studies. The concept of resilience was introduced by Holling in the field of ecology [1]. According to Holling, resilience determines the persistence of relationships within systems and is a measure of the ability of these systems to absorb change of state variables, driving variables, and parameters, and still persist.

Hale et al. [2] defined resilience as the ability for a condition to stay in a safe envelope under accident conditions. Hollnagel et al. [3] described resilience as the move towards proactive safety instead of the past practice of reactive safety. Sheridan on the other hand attempts to explain resilience as a safety buffer system for engineered systems. Vugrin et al. [4] define a system's resilience based on occurrence of disruptive event. The authors explained that resilience is the ability of systems to reduce "efficiently" both the magnitude and duration of the deviation from target "system performance" levels.

The definition addresses a critical point that a system may have different resilience to different disruptions and the efficient operation of the system will depend on various factors, including the age of the system, the condition of the system and previous maintenance and rehabilitation records of the infrastructure. Another key component is the system performance that should be addressed in relative terms, before and after disruptions.

Gluchshenko and Foerster [5] discuss ways to measure resilience:

- Qualitative Measures:
 - High resilience - this is when the time of deviation is considerably longer than time of recovery;
 - Medium resilience - this is when the time of deviation and time of recovery are approximately equivalent;
 - Low resilience - this is when time of deviation is considerably shorter than time of recovery.

- Quantitative Measures:
 - Degree of recovery in a specified period;
 - Overall time a system needs to come back to the reference state;
 - Overall cost of the "comeback".

The reference state may be realistic or nonrealistic depending on the existing operational conditions. Figure 29 to Figure 31 depict different times of deviation initial distribution and times of recovery.

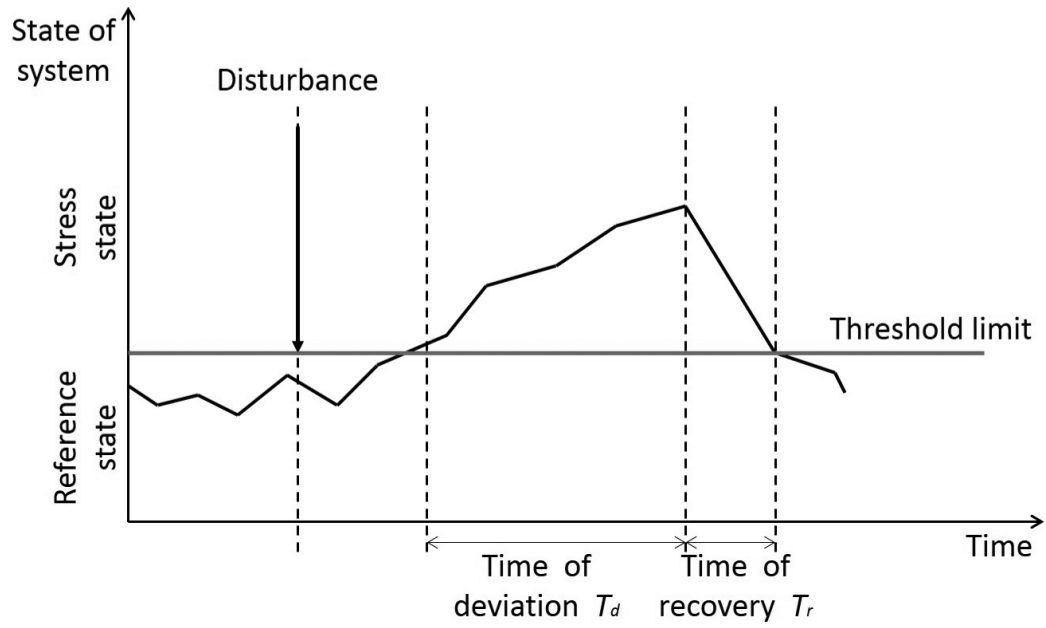


Figure 29. High resilience of a system against a disturbance.

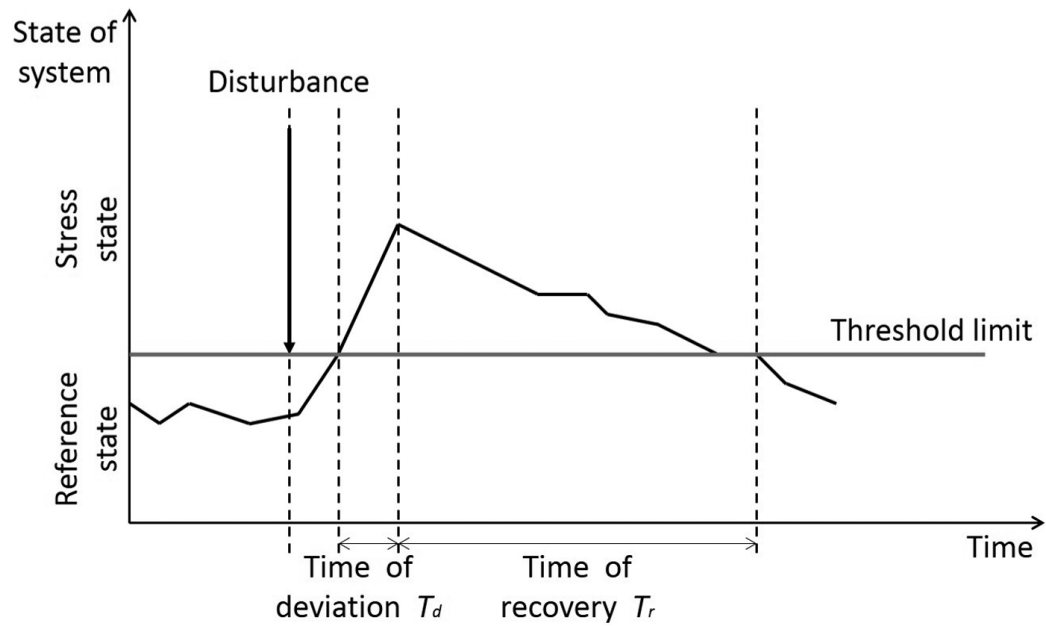


Figure 30. Low resilience of a system against a disturbance.

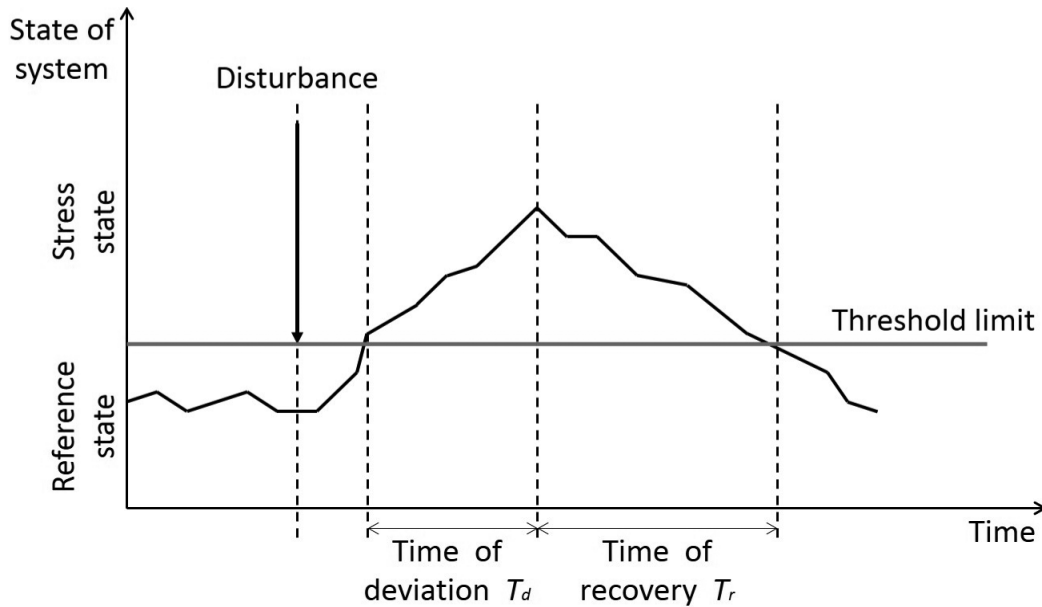


Figure 31. Medium resilience of a system against a disturbance.

Lebel [6] defines resilience as “the potential of a particular configuration of a system to maintain its structure/function in the face of disturbance, and ability of the system to reorganize following the disturbance-driven change and measured by size of stability domain.” Walker et al. [7] defined resilience as “the capacity of a system to absorb disturbance and reorganize while undergoing change so as to still retain essentially the same function, structure, identity and feedbacks.” Holling et al. [8] identified the rate and speed of return to preexisting conditions after disturbance as resilience. Resilience formulation, analysis, and interpretation are highly dependent on the scale of analysis. Different levels will have different objectives and interpretations. Insufficient infrastructure system resilience can lead to frequent damage and disruption, unsatisfactory recovery, high economy cost, and safety; this can permanently cause the likelihood of major loss of the systems.

Although there are different definitions, this report will only focus on the following: (1) resilience is the capacity to cope with unanticipated dangers after they have manifested and learn how to bounce back; (2) resilience is the potential for a system to maintain its structure and form in the presence of external events. Godschalk [9] presented the series of characteristics of resilient systems; these include the following:

- Redundancy—systems designed to ensure that failure in a particular node or section will not affect other nodes or sections
- Diversity—multiple components or nodes against specific threat
- Efficiency—positive ratio of energy supplied to energy delivered
- Autonomy—capability to operate independent of outside control
- Strength—power to resist external events
- Interdependence—integrated system components to support each other

- Adaptability—capacity to learn from experience and flexibility to change.

Jackson and Ferris [10] proposed 14 top level (resilience taxonomy) characteristics, organized in terms of capacity, flexibility, tolerance, and cohesion (Figure 32). Furuta (2000) also noted that the essential characteristics of resilience include (1) flexibility—the ability to restructure itself in response to both external and internal changes; (2) margin—how closely the system is operating with reference to the boundary; (3) buffering capacity—the magnitude of disruptions that the system can absorb, which can be quantified using the resilience triangle; and (4) tolerance—how the system behaves near and around the boundary.

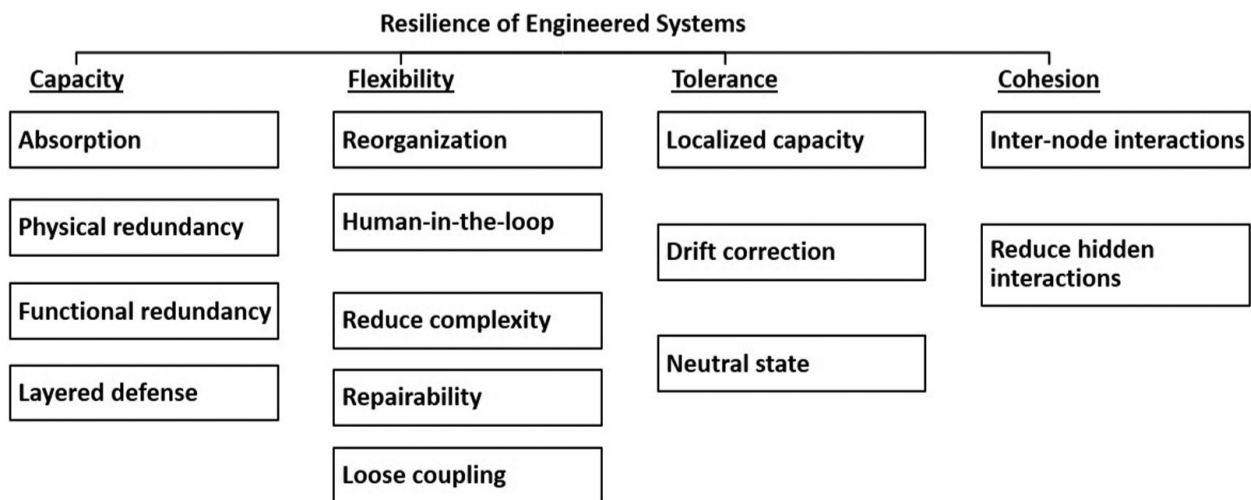


Figure 32. Resilience taxonomy [10].

1.5 Resilience Quantification Methods

Tierney and Bruneau [11] showed how resilient systems reduce the probabilities of failure and how therefore resilience can be measured by the functionality of an infrastructure system after external shock and also by the time it takes to return to present-level performance. The authors proposed a “resilience triangle” that can be a measure to address the resilience of the system. Figure 33 is a conceptualized resilience triangle. The resilience triangle can be used to address issues such as what mitigation measures can be implemented during restoring of infrastructure to acceptable functionality and service. The vertical axis of the resilience triangle can have different quantities depending on the objective of the resilience analysis, such as quality index, functionality, and satisfaction. For example, during and after an earthquake, the quantity to address social and psychological needs can be satisfaction. Tierney and Bruneau [11] developed the four Rs, a determinant for resilience within the earthquake community. They are (1) robustness—the ability to withstand external force without significant loss of performance and serviceability, (2) redundancy—the extent to which the system and system requirements satisfy functional requirements, (3) resourcefulness—the ability to diagnose and prioritize problems and to initiate solutions by identifying and mobilizing both technical and nontechnical information, and (4) rapidity—the time it takes to address and restore functionality of the system.

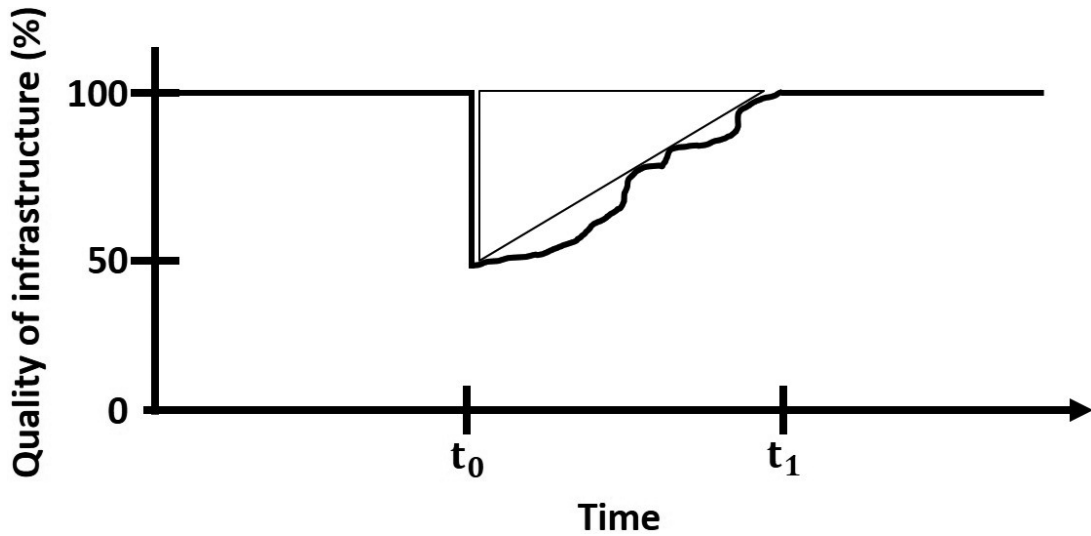


Figure 33. Conceptualized resilience triangle from disaster research [11].

Bruneau and Reinhorn [12] in the form of quality function $Q(t)$ developed an equation in terms of capacity of the full-functioning structural systems, post-event capacity, and an empirical parameter. The integration of the area under the quality function $Q(t)$ between different intervals is labeled as resilience:

$$\text{Resilience} = \frac{\int_{t_1}^{t_2} [Q(t)] dt}{(t_2 - t_1)}, \quad (1)$$

where t_1 and t_2 are the times before and after the external shock. The equation (1) was developed by the earthquake community and is more appropriate for a single infrastructure. Bruneau and Reinhorn [12] expanded the initial concept to three and four dimensions to capture resourcefulness and redundancy. Using the resilience triangle concept, Adams et al. [13] developed a resilience triangle for a major weather event (Figure 34). Li and Lence [14] refined the resilience index developed by Hashimoto et al. [15]. The resilience is defined as follows:

$$\text{Re}(t_1, t_2) = \left[\frac{g(t_2) \geq 0}{g(t_1) \geq 0} \right], \quad (2)$$

where $\text{Re}(t_1, t_2)$ is the resilience between t_1 and t_2 ; $g(t_1)$ and $g(t_2)$ are the performance at t_1 and t_2 respectively.

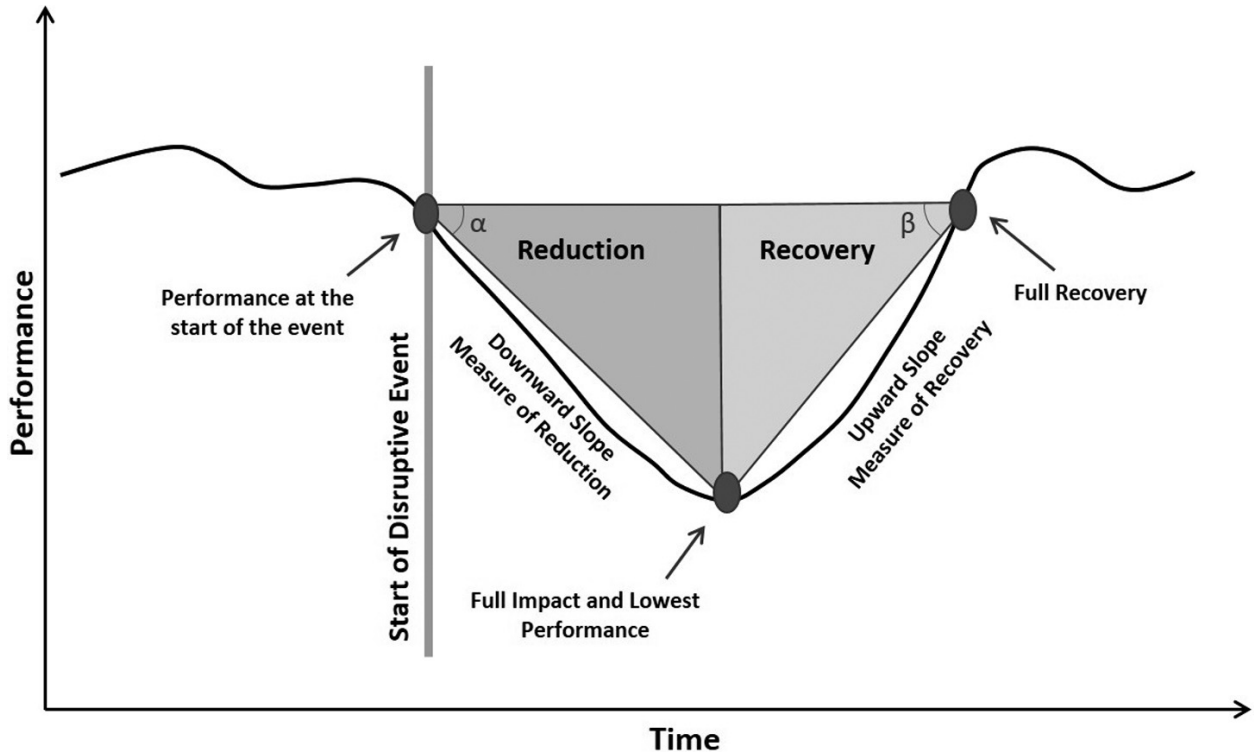


Figure 34. Conceptualized resilience triangle for a major weather event [13].

Vugrin et al. [16] developed resilience cost based on two key components: the systemic impact (SI) and total recovery effort (TRE). SI is the impact the system disruption has on productivity, the difference between a targeted system performance (TSP) and actual system performance (SP) after disruption. SI is determined by finding the area under the curve:

$$SI = \int_{t_0}^{t_f} [TSP(t) - SP(t)] dt. \quad (3)$$

Using the recovery response performance curve:

$$TRE = \int_{t_0}^{t_f} [RE(t)] dt. \quad (4)$$

In case $RE(t)$ is zero, there is no loss in systems performance. Vugrin et al. [16] discussed two types of resilience cost measurements: (i) optimal cost and (ii) recovery-dependent (RDR) cost. The RDR cost is the resilience cost of the systems, and a particular recovery state is determined as follows:

$$RDR(RE) = \frac{SI + \alpha TRE}{\int_{t_0}^{t_f} [TSP(t)] dt}, \quad (4)$$

where α is the normalization factor that allows engineers and decision makers to assign a weighting factor to SI and TRE. Using the ideas presented by Fiksel [17], Vugrin et al. [16] developed a concise explanation for resilience capacities. The absorptive capacities are more about the system's ability to automatically absorb impact and minimize the performance with a little effort. Adaptive capacity, on the other hand, addresses the degree

to which the system is capable of self-organization for recovery of the system’s intended performance, and finally, the restorative capacity is the ability of the system to repair easily, including self-healing. The self-healing and repairs may depend on the degree of disruption.

1.6 Risks and Resilience

There is an intuitive similarity between the fields of risk assessment and resilience concepts. Conceptual developments as presented can be extended to general infrastructure systems [18]. The authors summarized and compared the approaches used in risk management and resilience theories. The authors presented the following comparison:

The authors highlighted that a combined risk and resilience approach has the potential to

- Overcome the gaps of incomplete prediction and lack of comprehensiveness in a risk assessment approach;
- Improve the anticipation of system failure and the ability to respond in an adaptive way;
- Provide a method of evaluating response to unforeseen impacts and disturbances;
- Respond in such a way that the resilience of the system is not diminished; and
- Extend the range of responses to allow consideration of alternative, stable system states.

Resilience approaches in most cases require preparing for the unexpected and risk analysis assumes the premise that hazards are identifiable. Table 4 shows the difference between risk management and resilience.

Table 4. Comparison between risk management and resilience.

Risk management	Resilience
Operational planning and practice	Theory validation and quantification
Deconstructionist approach	Holistic approach
Clearly defined objectives and measures	Overall measure of sustainability
Likelihood of failure and magnitude	Position adaptive cycle and threshold
Internal causation	External causation
Expected Perturbations	Unexpected perturbation
Failure of man-made thresholds	Collapse of breaking-point thresholds
Laws of science and engineering	Complex systems and stable state
Fast-to-medium variable	Both fast and slow variables
Adjust performance to avoid collapse	Accepts inevitability of collapse
Encourages maintenance of known	Multiple stable basin acceptable
Failure triggers corrective action	Collapse is followed by natural reorganization

Park et al. [19] presented a more extensive comparison of risk and resilience perspectives as shown in Table 4. The comparison was grouped under (1) design principles, (2) design objectives, (3) design strategies, (4) relation to sustainability, (5) mechanisms of

coordinating response, and (6) mode of analysis. Table 5 is the table presented by Park et al. [19]. It is worth noting that the resilience approach is mostly based on the unexpected, but risk analysis proceeds from the premise that the hazards are identifiable.

Table 5. Resilience perspectives [19].

<p>Design Principles</p> <ul style="list-style-type: none"> – Failure can be tolerated at subsystems level to reduce overall system failure – Minimization of consequences of failure and rapid recovery times – Adaptation to changing conditions – Adaptation to changing conditions without permanent loss
<p>Design Objectives</p> <ul style="list-style-type: none"> – Minimization of consequences of failure and rapid recovery times
<p>Design Strategies</p> <ul style="list-style-type: none"> – Diversity, adaptability, cohesion, flexibility, and renewability
<p>Relation to Sustainability</p> <ul style="list-style-type: none"> – Recovery, renewal, and innovation – Modes of analysis – Possible consequences of analysis involving scenarios with unidentified causes

Figure 35 presents the general perspective, topics, and methodology for resilience.

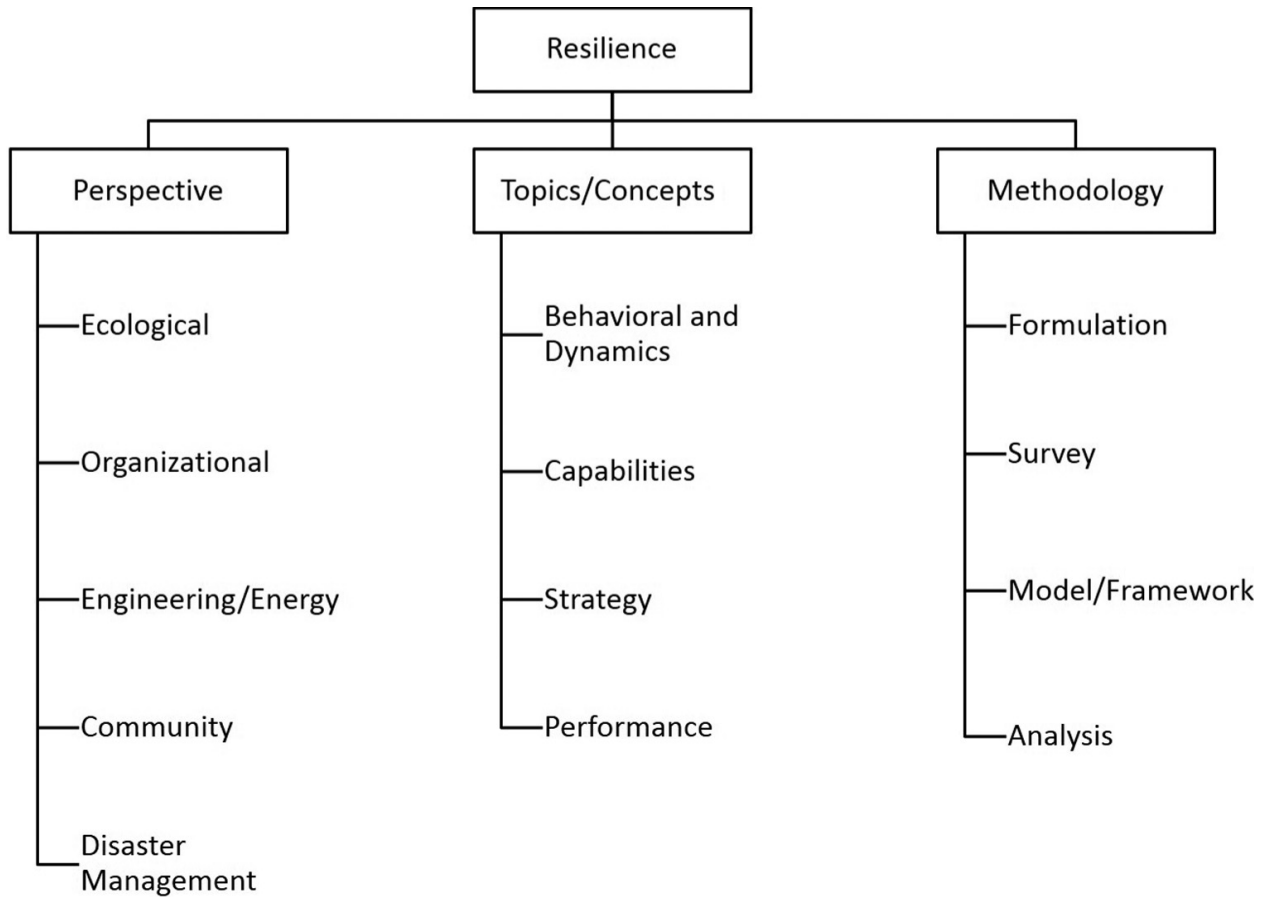


Figure 35. Perspectives, concepts, and methodologies in resilience engineering.

Transportation Resilience

Transportation systems and networks are critical infrastructure for the growth and development of communities at various levels, this include local, regional, national or international [20]. The transportation systems are also characterized by complex and nonlinear relations and interdependencies between their several internal and external components [20]. Because of the dependencies and interdependencies, there are various types of risks:

- a) Cascading effect: when disruption in one of transportation infrastructure causes disruption in a second.
- b) Escalating effect: when a disruption in one of transportation infrastructure exacerbates an independent disruption of a second transportation infrastructure.
- c) Common cause: more prevalent during natural disaster when there is disruption of two or more infrastructures at the same time [21].

Summarized the key principles of resilience for the transportation system: the principle defines resilience in two dimensions: a) technical and b) organizational as shown in Table 6.

Table 6. Proposed principles of resilience for the transport system [21].

Dimension	Principle	Definition and Justification
Technical	Robustness	Strength, or the ability of elements, systems, and other units of analysis, to withstand a given level of stress or demand without suffering degradation or loss of function [22].
	Redundancy	The extent to which elements, systems, or other infrastructure units exist that are substitutable, i.e., capable of satisfying functional requirements in the event of disruption, degradation, or loss of functionality [22]. For simplification, this is assumed to include considerations of ‘diverse’ and ‘reserve capacity’. The concept of ‘independent/autonomous’ is included here, only in the context of back-up provision, as discussed above.
	Safe-to-fail	The extent to which innovative design approaches are developed, allowing (where relevant) controlled, planned failure during unpredicted conditions, recognising that the possibility of failure can never be eliminated. This may involve new approaches to design, to complement traditional, incremental risk-based design [19].
Organizational	Change readiness*	The ability to sense and anticipate hazards, identify problems and failures, and to develop a forewarning of disruption threats and their effects through sourcing a diversity of views, increasing alertness, and understanding social vulnerability [23]. Also involves the ability to adapt (either via redesign or planning) and learn from the success or failure of previous adaptive strategies [19]. This learning is also conceptualised by Manyena et al. [24] who in their ‘bounce-forward’ idea of resilience, identify moving from single-loop or error-corrective learning, to double-loop, organisational learning, where the values, assumptions and policies that led to the actions in the first place are questioned.
		The capacity to mobilise resources when conditions exist that threaten to disrupt some element, system, or other unit of analysis; resourcefulness can be further conceptualised as consisting of the ability to apply material (i.e., monetary, physical, technological, and informational) and human resources to meet established priorities and achieve goals [22].

	Networks	The ability to establish relationships, mutual aid arrangements and regulatory partnerships, understand interconnectedness and vulnerabilities across all aspects of supply chains and distribution networks, and; promote open communication and mitigation of internal/external silos [23].
	Leadership and culture	The ability to develop an organisational mind-set/culture of enthusiasm for challenges, agility, flexibility, adaptive capacity, innovation and taking opportunity [23].

* Readiness encompasses the change-ready concepts developed by Resilient Organisations [23], along with the concept of ‘resourcefulness’ developed by Bruneau et al. [22] and Park et al. [19].

The authors also proposed a table summarizing qualitative and quantitative measurements approaches that can be used in resilience of transportation systems (Table 7).

Table 7. Summary of qualitative and quantitative measurement approaches [21].

	Qualitative approach	Quantitative approach
Flexibility	Provides a flexible approach that can be adapted to a range of situations, scales and conditions.	Is typically applied only at a smaller geographical scale and at a more detailed level.
Data requirements	Can be applied with complete or incomplete data sets. Relies on subjective assessments in many cases.	Typically requires large, accurate data sets.
Computational requirements	None/minimal.	Requires significant computational effort.
Results	A relative, subjective assessment – often using a ranking scale	Typically delivers a discrete resilience index or measure by way of network modelling or fuzzy logic modelling.
Ease of implementation	Simple	Difficult
Use in targeting resilience improvements	Useful; however, is very much related to the design of the framework, how it is implemented, and subjectivity of the scores given.	Can be accurate for the network analysed.
Useful in wider organizational resilience assessments and	Yes	No

engagement		
Useful in assessing physical network asset resilience	Yes	Yes

Cox et al. [25] define categories specific to static and dynamic transportation resilience:

- *Conservation* is maintaining service with fewer inputs (e.g. railroad cars, employees) on the supply side or doing with less transportation on the demand side.
- *Input substitution* is shifting input combinations or transportation modes to achieve the same function or level of productivity.
- *Inventories* include both emergency stockpiles and ordinary working supplies of production inputs for both the transportation system and for economic activities dependent on transportation.
- *Excess capacity* refers to idle plant and equipment. A special case is *redundancy* that refers to back-up systems that do not increase productive capacity, but rather compensate for damaged capital (e.g. multiple tracks).
- *Relocation* is changing the site of business activity in terms of travel routes or end-user sites.
- *Resource unimportance* refers to the portion of business operation that can continue without a critical input like transportation.
- *Import substitution* is importing resources from other regions. This might be imports for the transportation system itself or the employment of the transportation system in doing so.
- *Export substitution* refers to selling goods to other regions that cannot be sold otherwise to local customers.
- *Technological change* allows for easier manipulation to restore function, to increase production, change hours of operation, and to respond to altered service demands.
- *Production recapture* refers to working overtime or extra shifts to catch up on lost production or service.

- *Logistics refinement* refers to reducing impediments to the delivery of goods and services.

Dynamic resilience strategies to speed recovery include:

- *Removing operating impediments* involves debris removal and related complications, and streamlining paperwork for insurance claims and government assistance.
- *Management effectiveness* refers to skills that promote restoration, repair and reconstruction.
- *Speeding restoration* refers to a range of options such as alternative means of access to repair sites and incentive contracts.
- *Input substitution, import substitution, inventories*, as above, also speed restoration, but pertain to materials and labor needed for repair activities rather than normal production operations.

Coastal Resilience Analysis

4.1 Introduction

The Mid-Atlantic region is recognized as one of the most vulnerable regions of the USA to the impacts of global climate change and sea level rise. One of the main concerns is the effect of sea level rise on the transportation infrastructure network. Also, the sea level rise can affect marine present areas along the coast. For example, the Chesapeake Bay area is experiencing both absolute (rising water) and relative (sinking land) [26]. Some of the predicted impacts of a rise in sea level poses a major risk to various infrastructures along the coast, community development, watershed, and saltwater intrusion into surface and groundwater. There are also some ecological impacts including coastal erosion and some changes in intertidal areas in inundation of island and coastal wetlands. In general, the sea level rise impacts on the coastal areas can be classified as shown in Figure 36.

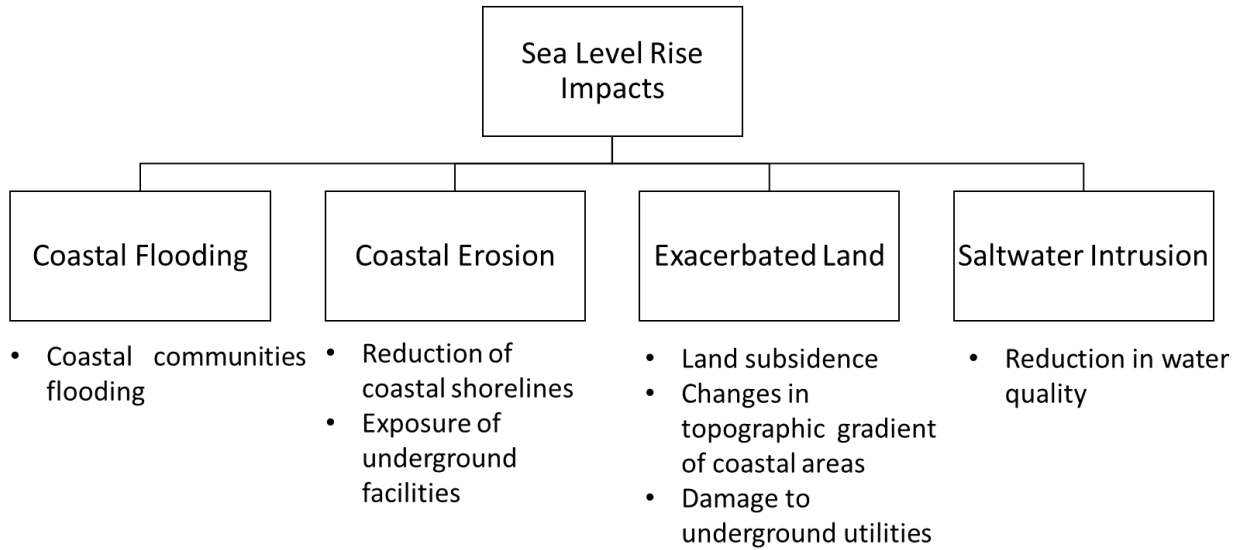


Figure 36. Sea level rise impacts.

The Department of Defense presented a climate change adaptation roadmap, which clearly demonstrate the effect of coastal flooding on transportation systems.

Table 8. Summary of five key indicators of climate change [27].

Climate Change Indicator	Transportation System Impacts and Consequences
<p>Rising Temperatures</p> <ul style="list-style-type: none"> • More days with temperatures above 95° F • Melting permafrost and ice sheets • Changes in incidence or distribution of vector-borne diseases • More wildfires • Warmer soil 	<ul style="list-style-type: none"> • Degrading transportation infrastructure and increased maintenance costs • Increased energy costs for transport facility operations • Creating infrastructures that can stand weather extremes • Stress on electrical grids • Opening of Arctic waters • Longer ice-free seasons • More seasonal Arctic commerce and transit
<p>Changes in Precipitation Patterns</p> <ul style="list-style-type: none"> • Seasonal increases and decreases in precipitation • More drought, and more severe drought • More extreme precipitation events 	<ul style="list-style-type: none"> • Higher maintenance costs • Higher costs for flood control and erosion prevention • Stream bank erosion • Desertification—the creation of new

	<ul style="list-style-type: none"> deserts • Soil and water supply loss • Poorer quality groundwater • Spread of invasive species
<p>Increasing Storm Frequency and Severity</p> <ul style="list-style-type: none"> • Changes in flood patterns, soil, and vegetation 	<ul style="list-style-type: none"> • Increased coastal and inland flooding • Poorer water quality • Loss of soil and vegetation • Wind damage • Damage to coastal infrastructure • Increased costs of flood control and erosion prevention
<p>Rising Sea Levels and Storm Surges</p> <ul style="list-style-type: none"> • Loss of coastal land • Reduced capacity of protective barrier islands and coastal wetlands against storm surges 	<ul style="list-style-type: none"> • Degradation of coastal infrastructure • Increased cost of retrofit structures • Supply chain impacts • Scarcity of available land for transportation services • Road and rail infrastructure damage • Equipment damage from salt water
<p>Changes in Ocean Temperatures</p> <ul style="list-style-type: none"> • Coral reef losses • Loss of ocean protection from storm surge and wave damage 	<ul style="list-style-type: none"> • Coastal stations and infrastructure more vulnerable to severe weather • Reduced commercial fishing

5. Resilience: Coastal Flooding and Transportation System

5.1 Introduction

The current changes in weather patterns have significant impact of various transportation infrastructure. In the near future, sea level rise and coastal flooding will have major threat on communities around the Mid-Atlantic region. The impact of sea level on roads will include:

- a) The erosion and subsidence of the pavement subsurface. It will affect the deterioration rate, hence the maintenance budget allocation of the road network.
- b) Flood of underground tunnels and low-lying formation.
- c) Inundation of rail lines (both regional and local transportation). This will have major economic impact of the region.
- d) The tendency to have traffic congestion and uncontrollable traffic patterns since most of the roads will be impassable.

Azevedo de Almeida and Mostafavi [28] present the interdependencies between various infrastructures showing the cascading impact of sea level rise (Figure 37).

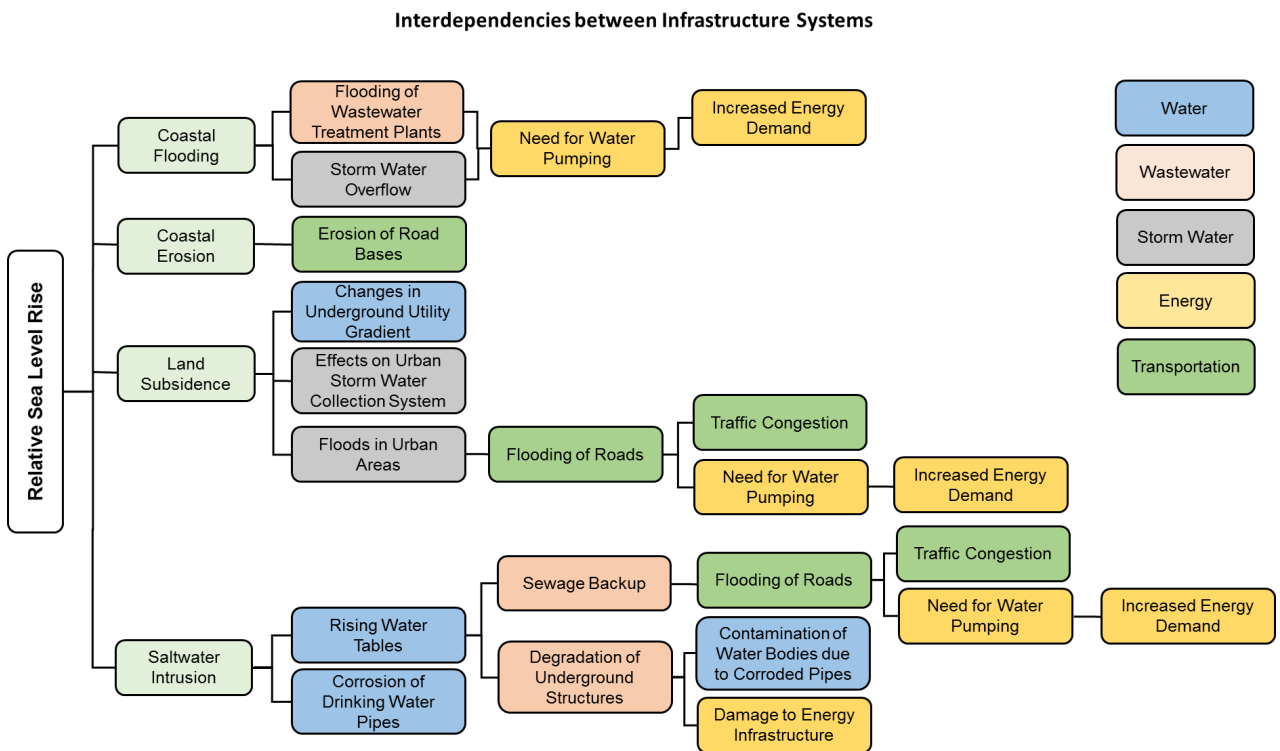


Figure 37. Cascading impacts of sea level rise on infrastructure systems [28].

Melillo et al. [29] presented the adaptation impacts of coastal flooding and its impact on transportation systems (Figure 38).

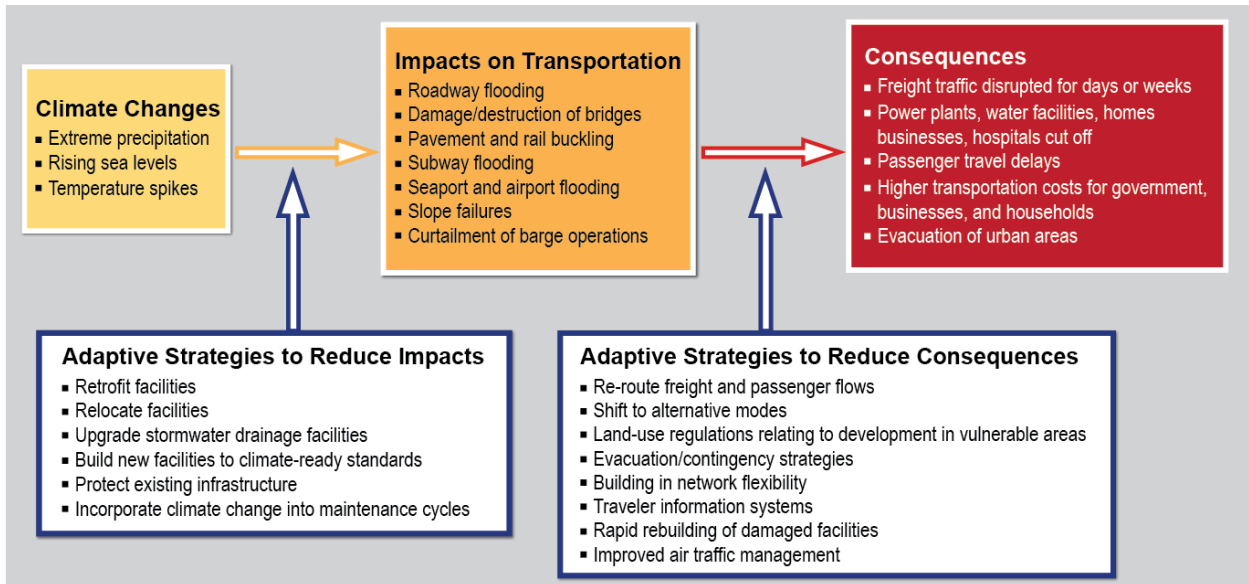


Figure 38. Role of adaptive strategies and tactics in reducing impacts and consequences [29].

6. Concluding Remarks

- Development of an appropriate resilience index or indices is highly dependent on the types of system.
- Most of the resilience indices developed so far are highly based on the network systems, where graph network has been the technique used to develop resilience.
- The effect of resilience on transportation systems based on coastal flooding consists of both networked and non-networked systems.
- There is a need to develop the resilience index of combine networked and non-networked systems.
- The method should also be capable of handling incomplete or complete information, subjective information, structured and/or unstructured data. The achievement of combine resilience index of networked/non-networked is therefore needed.

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