MD-11-SP808B4P

Martin O'Malley, *Governor* Anthony G. Brown, *Lt. Governor*



Beverly Swaim-Staley, *Secretary* Neil J. Pedersen, *Administrator*

STATE HIGHWAY ADMINISTRATION

RESEARCH REPORT

LIFE CYCLE AND ECONOMIC EFFICIENCY ANALYSIS PHASE II: DURABLE PAVEMENT MARKINGS

DR. YOUNG-JAE LEE MORGAN STATE UNIVERSITY

PROJECT NUMBER MD-11-SP808B4P

FINAL REPORT

April 2011

The contents of this report reflect the views of the author who is responsible for the facts and the accuracy of the data presented herein. The contents do not necessarily reflect the official views or policies of the Maryland State Highway Administration. This document is disseminated under the sponsorship of the U.S. Department of Transportation, University Transportation Centers Program, in the interest of information exchange. The U.S. government assumes no liability for the contents or use thereof. This report does not constitute a standard, specification, or regulation.

Technical Report Documentation Page

	_	-		
1. Report No. MD-11-SP808B4P	3. Recipient's Catalog No.			
4. Title and Subtitle	5. Report Date			
Life Cycle and Economic Efficiency	April 2011			
Pavement Markings	6. Performing Organization Code			
7. Author/s		8. Performing Organization Report No.		
Dr. Young-Jae Lee				
9. Performing Organization Name and Address		10. Work Unit No. (TRAIS)		
Department of Transportation and U	rban Infrastructure Studies			
School of Engineering		11. Contract or Grant No.		
Morgan State University		SP808B4P		
Baltimore, MD 21251				
12. Sponsoring Organization Name and Address		13. Type of Report and Period Covered		
Maryland State Highway Administra	tion	Final Report		
Office of Policy & Research		14. Sponsoring Agency Code		
707 North Calvert Street		(7120) STMD-MDOT/SHA		
Baltimore, MD 21202				
National Transportation Center				
Morgan State University				
1700 East Cold Spring Lane				
Doltimore MD 21251				
\mathbf{D}				
15. Supplementary Notes				
15. Supplementary Notes 16. Abstract				
15. Supplementary Notes 16. Abstract This report details the Phase II analy	sis of the life cycle and econd	omic efficiency of inlaid tape		
 15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint 	sis of the life cycle and econo was included as a non-durab	omic efficiency of inlaid tape le for comparison purposes		
 15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo 	sis of the life cycle and econo was included as a non-durab mical product for specific tra	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions,		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data v	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide r	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estima	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity.		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of th	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate e data collection period produ	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data ites of future retroreflectivity. uced better estimates. The		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of the results of this research show that snow	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide reference of the results of this research show that snown retroreflectivity. The life cycle of east	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity was collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide results of this research show that snow retroreflectivity. The life cycle of each the installation cost of each material	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated uno-	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of th results of this research show that sno retroreflectivity. The life cycle of eac the installation cost of each material results suggested that specific material	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate e data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom- als should be applied for spec-	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the der different conditions, and nic efficiency analysis. The cific weather and traffic		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of th results of this research show that sno retroreflectivity. The life cycle of each the installation cost of each material results suggested that specific materi conditions. Although inlaid tape's est	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate e data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The cific weather and traffic than thermonlastic's		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econor the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide re- As hoped, a two-year extension of the results of this research show that snown retroreflectivity. The life cycle of each the installation cost of each material results suggested that specific material conditions. Although inlaid tape's est thermoplastic's lower cost made it the	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer be more economical material	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The cific weather and traffic than thermoplastic's, for all conditions		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of th results of this research show that sno retroreflectivity. The life cycle of eac the installation cost of each material results suggested that specific materi conditions. Although inlaid tape's est thermoplastic's lower cost made it th	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer the more economical material to 18. Distribution Statement:	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity was collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The cific weather and traffic than thermoplastic's, for all conditions.		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econor the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide reference of the results of this research show that snown retroreflectivity. The life cycle of each the installation cost of each material results suggested that specific material conditions. Although inlaid tape's est thermoplastic's lower cost made it the 17. Key Words: Durable, Pavement, Marking, Inlaid tape, Thermorelactic	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer the more economical material to 18. Distribution Statement: No restrictions. This docum	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity was collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The cific weather and traffic than thermoplastic's, for all conditions.		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econor the project examined the relationship and input variables. For three to four locations in the state of Maryland. The snowfall they received. Phase I of the collection period could not provide results of this research show that snow retroreflectivity. The life cycle of each the installation cost of each material results suggested that specific material results suggeste	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer the more economical material to No restrictions. This docum Research Division upon rec	pomic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity was collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the der different conditions, and nic efficiency analysis. The cific weather and traffic than thermoplastic's, for all conditions.		
15. Supplementary Notes 16. Abstract This report details the Phase II analy and thermoplastic. Waterborne paint only. In order to find the most econo the project examined the relationship and input variables. For three to four locations in the state of Maryland. T snowfall they received. Phase I of th collection period could not provide r As hoped, a two-year extension of th results of this research show that snor retroreflectivity. The life cycle of each the installation cost of each material results suggested that specific materi conditions. Although inlaid tape's est thermoplastic's lower cost made it th 17. Key Words: Durable, Pavement, Marking, Inlaid tape, Thermoplastic, Life cycle, Efficiency	sis of the life cycle and econo was included as a non-durab mical product for specific tra between the pavement mark years, retroreflectivity data w he sites were selected based of is study was done with one ye easonable and reliable estimate data collection period produ- wfall is a major factor in the ch material was estimated und was estimated for the econom als should be applied for spec- timated life cycle was longer the more economical material 18. Distribution Statement: No restrictions. This docum Research Division upon red	omic efficiency of inlaid tape le for comparison purposes ffic and weather conditions, ing materials' retroreflectivity vas collected from six on the amount of traffic and ear of data, but that data tes of future retroreflectivity. uced better estimates. The deterioration of the ler different conditions, and nic efficiency analysis. The cific weather and traffic than thermoplastic's, for all conditions.		

NoneNone52Form DOT F 1700.7 (8-72) Reproduction of form and completed page is authorized.

TABLE OF CONTENTS

List of Figures	iv
List of Tables	V
List of Equations	vi
Acknowledgements	vii
Executive Summary	1
Introduction	3
Objectives	3
Scope	3
Literature Review	5
Pavement Marking Materials	5
Retroreflectivity	6
Service Life of the Pavement Markings	7
Phase I Results and the Difficulties in the Regression Analysis	8
Methodology	11
Data Selection	11
Data Collection	11
Retroreflectivity Data Collection Methods	11
Retroreflectivity Measuring Equipment	11
Data Entry	14
Regression Analysis	14
Analysis Process	15
Life Cycle Estimation for the Different Materials	15
Cost Estimation for the Different Materials	16
Economic Efficiency Estimation for the Different Materials	19
Research Findings	21
Regression Analysis	21
Life Cycle Estimation	32
Validation of the Regression Analysis and Life Cycle Estimation	33
Economic Efficiency Analysis	34
Sensitivity Analysis	35
Conclusions	39
References	41

LIST OF FIGURES

Figure 1. Field Locations for the Research	4
Figure 2. Glass Bead Retroreflection	6
Figure 3. Examples of the Regression Analysis with Different Basic Equations for the Durab	le
Materials with One Year of Data	9
Figure 4. Typical Retroreflectivity Curves for the Different Pavement Marking Materials	9
Figure 5. Different Life Cycles with Different Estimation Curves	10
Figure 6. Photo of Test Site with Spot Markings	13
Figure 7. Retroreflectivity Measuring Equipment (Delta LTL-X)	13
Figure 8. Flow Chart for the Analysis	15
Figure 9. Regression Curves for White Markings (Low Traffic & Light Snow)	23
Figure 10. Regression Curves for White Markings (Low Traffic & Moderate Snow)	24
Figure 11. Regression Curves for White Markings (Low Traffic & Heavy Snow)	24
Figure 12. Regression Curves for White Markings (Medium Traffic & Light Snow)	25
Figure 13. Regression Curves for White Markings (Medium Traffic & Moderate Snow)	25
Figure 14. Regression Curves for White Markings (Medium Traffic & Heavy Snow)	26
Figure 15. Regression Curves for White Markings (High Traffic & Light Snow)	26
Figure 16. Regression Curves for White Markings (High Traffic & Moderate Snow)	27
Figure 17. Regression Curves for White Markings (High Traffic & Heavy Snow)	27
Figure 18. Regression Curves for Yellow Markings (Low Traffic & Light Snow)	28
Figure 19. Regression Curves for Yellow Markings (Low Traffic & Moderate Snow)	28
Figure 20. Regression Curves for Yellow Markings (Low Traffic & Heavy Snow)	29
Figure 21. Regression Curves for Yellow Markings (Medium Traffic & Light Snow)	29
Figure 22. Regression Curves for Yellow Markings (Medium Traffic & Moderate Snow)	30
Figure 23. Regression Curves for Yellow Markings (Medium Traffic & Heavy Snow)	30
Figure 24. Regression Curves for Yellow Markings (High Traffic & Light Snow)	31
Figure 25. Regression Curves for Yellow Markings (High Traffic & Moderate Snow)	31
Figure 26. Regression Curves for Yellow Markings (High Traffic & Heavy Snow)	32

LIST OF TABLES

Table 1. Specific Information on the Field Locations	4
Table 2. Pavement Marking Materials	5
Table 3. Threshold Retroreflectivity Values Used to Define the End of Pavement Marking	
Service Life	7
Table 4. Estimated Service Life of Yellow Lines by Roadway Type and Pavement Marking	
Material	7
Table 5. Retroreflectivity Data Collection Schedules	12
Table 6. Typical Combinations for Life Cycle Analysis	16
Table 7. Unit Cost Estimation for Inlaid Tape	17
Table 8. Unit Cost Estimation for Thermoplastic	17
Table 9. Unit Cost Estimation for Waterborne Paint	17
Table 10. Installation Costs for the Different Pavement Marking Materials in Maryland	17
Table 11. Summary of Total Installation Cost Estimation	19
Table 12. Regression Results for White Inlaid Tape	22
Table 13. Regression Results for Yellow Inlaid Tape	22
Table 14. Regression Results for White Thermoplastic	22
Table 15. Regression Results for Yellow Thermoplastic	23
Table 16. Estimated Life Cycle of White Pavement Marking Materials	33
Table 17. Estimated Life Cycle of Yellow Pavement Marking Materials	33
Table 18. Summary of the Real Data Values from Data Collection	34
Table 19. Annual Costs for White Pavement Marking Materials	35
Table 20. Annual Costs for Yellow Pavement Marking Materials	35
Table 21. Annual Costs for White Pavement Marking Materials When Inlaid Tape's	
Life Cycle is 50% Longer	36
Table 22. Annual Costs for White Pavement Marking Materials When Inlaid Tape's	
Installation Costs are 40% Lower	37

LIST OF EQUATIONS

Equation 1	8
Equation 2	8
Equation 3	8
Equation 4	8
Equation 5	
-1	

ACKNOWLEDGEMENTS

The Maryland State Highway Administration's Office of Materials Technologies' Pavement Marking Team collected the data for this project. The author would like to thank the following people for their ideas, time, and efforts at various project meetings: Rodney Wynn, Gil Rushton, Ray Johnson, Barbara Adkins, Allison Hardt, Richard Wray, Ralph Smith, Doc Tisdale, Teresa Custer, Deborah Taylor, Donnie Deberry, and Elvis Fohtung. He would also like to express his appreciation for the data handling and analysis done by Morgan State University's Sriram Jayanti and Naveed Shah. Dr. Andrew Farkas, Anita Jones, and the National Transportation Center at Morgan State University also deserve thanks for their administrative support.

EXECUTIVE SUMMARY

This project attempted to estimate the life cycles and economic efficiencies of inlaid tape and thermoplastic. The two durable pavement-marking materials were tested under a variety of weather and traffic conditions for three to four years to find the best-performing product for specific environments. Waterborne paint was included as a non-durable, strictly for comparison purposes.

The materials' retroreflectivity was estimated using four basic regression equations: linear, linear with quadratic, natural log, and natural log with quadratic. The input variables for these equations were cumulative traffic amount, cumulative precipitation, and cumulative snowfall.

Phase I of this study, completed with one year of data, did not provide a reasonable estimation of future retroreflectivity because its data collection period was shorter than the life cycle of the durable materials. That limitation required this Phase II study, which covers an additional two years of data collection.

In order to estimate the life cycles of the durable materials, the research team tested the retroreflectivity equations under various traffic scenarios (i.e., amounts and road design speeds), weather conditions, and threshold values. The traffic and snowfall amounts were specified into three typical categories (high, medium, and low), and the nine combinations of those categories were generated as different conditions for the life cycle estimations.

Because durable materials such as inlaid tape and thermoplastic are known to last more than three years—in some locations they can last more than five years—the data collection period for this research was not long enough to justify various basic functions. Of the four basic regression equations, the linear function best fit the relationship between the collected retroreflectivity data and the input variables. Justification of the log function requires a longer data collection period.

Because of the inconsistent nature of field data, the adjusted R-square values, which show the fitness of the data to the estimated function, were not very high. However, the adjusted R-square values were still higher than those of previous similar research because of the inclusion of weather data in addition to traffic data which has been the sole conventional data for the other previous life cycle studies of the pavement markings.

Snowfall amounts affected the markings' retroreflectivity more than the traffic amounts did. This indicates that snowplow methods must be controlled and regulated in order to minimize the impact of snowplows on pavement markings, and to improve the life cycle and performance of the pavement markings. The regression results fit the real data better for the white pavement markings than they did for the yellow pavement markings. The results also showed that the regression estimates for inlaid tape fit the real data better than those for thermoplastic did. These results indicate that, in general, the performance potential of inlaid tape and the white markings are more stable than that of thermoplastic and the yellow markings. It would also seem to indicate that there are more uncertainties in the performance of thermoplastic and the yellow pavement markings in general.

For this research, the life cycles of the pavement markings were determined with threshold values and estimated retroreflectivity values based on nine weather and traffic conditions.

In general, inlaid tape lasts longer than thermoplastic because the initial retroreflectivity of inlaid tape is higher than that of thermoplastic, and white pavement markings last longer than yellow pavement markings because the initial retroreflectivity of white pavement markings is higher than that of yellow pavement markings. However, in this study, the performance of yellow thermoplastic was very good. Indeed, yellow thermoplastic lasted as long as white thermoplastic and yellow inlaid tape.

Estimated life cycles and total installation costs were used to determine the materials' annual costs (i.e., economic efficiency). The estimated total installation costs (which include monetary installation costs, delay, and accident costs caused by the installation process) were \$3.168 per foot for inlaid tape, \$0.777 per foot for thermoplastic, and \$0.148 per foot for waterborne paint. Although inlaid tape can last longer effectively, thermoplastic is more economical under most conditions because of inlaid tape's higher total installation costs. To make inlaid tape competitive to thermoplastic in terms of economic efficiency, the sensitivity analysis showed that inlaid tape's life cycle had to be increased by 50 percent or its total installation costs had to be reduced by 40 percent.

INTRODUCTION

The Maryland State Highway Administration (SHA) uses different pavement marking materials for roads throughout the state, but it has no specific and proven guideline that indicates the best-performing and most cost-effective product for specific locations, traffic amounts, and weather conditions. As a result, there is no guarantee of performance.

Phase I of this research relied on data collected for one year. However, the life cycle estimates of the durable materials were not reasonable because the materials lasted longer than the study period.

This report shows the results from Phase II, which is based on a total of at least three years of data collection and analysis.

Objectives

SHA is currently evaluating the long-term durability and retroreflectivity of two durable pavement marking materials—thermoplastic and inlaid tape. The objectives of this project were to ensure proper procedure and to evaluate the effect of various inputs (traffic volume, snow, rain, etc.) on the durability and retroreflectivity of the pavement markings. From this analysis, the research team provided general equations for the estimation of retroreflectivity and durability. Those estimated regression equations were then used to estimate the life cycles of the pavement marking materials under different traffic and weather conditions. The most economical material was determined by an economic analysis that used the estimated life cycles and the installation costs of the materials.

Scope

The study sites and data collection methods for this project were established at meetings of the project teams from SHA and Morgan State University. The state of Maryland was divided into three regions—western, central, and eastern—based on historical weather characteristics. In order to generate data that could be more consistent, the research team selected sites with varying traffic amounts from a list of planned resurfacing projects in the regions. The research team ultimately selected four locations in the central zone, one in the eastern region, and one in the western area. It was recommended that the study use more than one location in the western and eastern regions, but the research team found only one location in each area that satisfied the conditions required for this project.

The selected sites are shown in Figure 1 and Table 1. Both straight and curved sections were used in half-mile segments at each of the study locations to account for any geometric issues that might affect retroreflectivity. Thermoplastic and inlaid tape were installed at most locations so their performance could be compared directly under the same conditions (only inlaid tape was installed on I-68).



Figure 1. Field Locations for the Research

REGION	LEGEND	COUNTY	ROUTE	RANGE	MP from:	MP to:	AADT	LANES
Eastern	1	WORCESTER	MD 611	Low AADT	4.49	8.51	10,725	2
	2	HOWARD	MD 175	High AADT	1.54	2.03	44,750	4
	3	HOWARD	MD 216	Medium AADT	0.87	1.55	21,825	4
Central	4	CHARLES	MD 5	Medium AADT	10.44	13.65	23,875	4
	5	HOWARD	MD 32	Medium AADT	19.08	20.19	28,125	4
Western	6	GARRETT	I-68 West- bound	Low AADT	6	7	11,675	2

Note: MP=mile point; AADT=annual average daily traffic

Table 1. Specific Information on the Field Locations

LITERATURE REVIEW

Pavement Marking Materials (Montebello et al., 2000)

The three categories of pavement marking materials—durable, conventional (non-durable), and temporary (removable)—are summarized in Table 2.

Conventional (non-durable) line striping materials, which include latex (waterborne) and alkyd (solvent-based) paint, are typically inexpensive and have a relatively short lifespan.

Category	Products	Estimated Cost per Ft.	Estimated Life	Advantages	Disadvantages
ntional ucts	Latex	\$0.03-0.05	9-36 months	 Inexpensive Quick drying Longer life on low-volume Easy clean-up No hazardous waste products 	 Short life on high-volume Damaged by sands Bead required Not good for concrete Warm weather required
Conver Prod	Alkyd	\$0.03-0.05	9-36 months	 Inexpensive Quick drying Works in cold temperature 	 Short life on high-volume Damage by sands Bead required Not good for concrete Highly flammable Bad smell
	Mid-Durable Paint	\$0.08-0.10	9-36 months	 Inexpensive Quick drying Longer life on low-volume Easy clean-up No hazardous waste products 	 Short life on high-volume Damage by sands Bead required Not good for concrete Warm weather required
urrable roducts	Ероху	\$0.20-0.30	4 years	 Longer life on low- and high- volume More retroreflectivity 	 Slow-drying Coning and flagging required Heavy bead required High initial expense Damage by sands
	Таре	\$1.50-2.65	4–8 years	 Highly retroreflective Long life on low- and high- volume No beads needed 	 High initial expense Best for newly surfaced roads Weak for snowplow
	Preformed Thermoplastic	NA	3–6 years	 Highly retroreflective Long life on low- and high- volume No beads needed Any temperature for application 	 Only used for symbols Damage from sands Weak for snowplow
Temporary Products	Temporary Tape	\$1.10-1.50	Length of construction	 Easy application and removal Last the life of construction Does not damage new pavement 	- Only for construction zones

 Table 2. Pavement Marking Materials (Source: Montebello et al., 2000)

Durable materials, in contrast, are more expensive but have a longer life expectancy. Thermoplastic and tape are in this particular category, as are hi-build paint and epoxy.

Thermoplastic has been used successfully for years. It is made up of glass beads, pigment, binders, and fillers. The glass beads and pigment give the material its retroreflectivity. Inert substances work as fillers that provide bulk, and a mixture of plasticizer and resin hold the components together.

Inlaid tape is very resistant to snowplow damage, particularly when it's inlaid. The tape is rolled into hot, freshly compacted asphalt and pressed into the surface with a finishing roller.

Retroreflectivity

When deciding which pavement marking material to use, one must consider its visibility during the day and night. Retroreflectivity refers to the portion of incident light from a vehicle's headlights that is reflected back toward the driver.

Glass or ceramic beads are added to the surface of most marking materials to make them retroreflective. Figure 2 illustrates how light travels through the beads. These tiny spheres are transparent and act like lenses. They can also be treated for extra adherence, or for moisture resistance. Having a portion of the beads on the surface and in the paint allows for continued retroreflectivity as the paint wears. For best results, the beads on the surface should be approximately 50 to 60 percent embedded. The proper application of beads is crucial to the marking's retroreflectivity (Montebello et al., 2000).



Figure 2. Glass Bead Retroreflection

Service Life of the Pavement Markings

A recent study concluded that the life cycle of a pavement marking is related to its traffic exposure and that the retroreflectivity can be expressed as a logarithmic regression equation (Abboud et al., 2002). However, this data was collected from locations that did not receive snow. Another project detailed the threshold retroreflectivity values that define the end of a pavement marking's service life, and the results can be seen in Table 3 (Migletz et al., 2001). Although that research has been referenced in many recent life cycle studies (Migletz et al., 2001, Zhang et al., 2006), currently, SHA suggests that higher threshold values are necessary to ensure safety and operational efficiency. As shown in Table 4, the project also illustrated how a product's life cycle (elapsed months) can be affected by the type of roadway on which it is placed (cumulated traffic passages).

Color of Marking	Threshold Retroreflectivity Values (mcd/m ² /lux)					
	Non-Freeway	Non-Freeway				
	\leq 40 mph	\geq 45 mph	\geq 55 mph			
	(64 km/hr)	(72 km/hr)	(89 km/hr)			
White	85	100	150			
Yellow	55	65	100			

Table 3. Threshold Retroreflectivity Values Used to Define the End of Pavement Marking
Service Life (Source: Migletz et al., 2001)

	Number of	Service Life	;
Roadway Type and Material	Pavement Marking	Average Cumulative	Elapsed
	Lines	Trips	Months
		(million vehicles)	
Freeway:			
Polyester	1	11.1	39.7
Profiled tape	3	6.9	25.8
Thermoplastic	7	6.1	24.7
Profiled Thermoplastic	4	5.3	23.5
Ероху	7	4.7	23.2
Profiled poly methyl methacrylate	3	6.2	21.1
Poly methyl methacrylate	3	3.0	15.6
Non-Freeway \leq 64 km/hr:			
Profiled Thermoplastic	1	11.4	50.7
Ероху	2	3.6	43.6
Profiled polyester	1	4.7	39.6
Profiled tape	1	3.5	19.6
Non-Freeway \geq 72 km/hr:			
Polyester	1	9.1	47.9
Ероху	6	8.9	44.1
Profiled tape	3	5.1	38.9
Thermoplastic	3	4.5	33.8
Profiled poly methyl methacrylate	2	6.5	31.0
Profiled Thermoplastic	3	3.9	23.0
Poly methyl methacrylate	1	4.8	20.5

Table 4. Estimated Service Life of Yellow Lines by Roadway Type and Pavement Marking
Material (Source: Migletz et al., 2001)

Phase I Results and the Difficulties in the Regression Analysis

In Phase I, the four following basic regression equations were examined to find the function that best fit the data.

- Linear : $Y = a + b_1 X_1 + b_2 X_2 + b_3 X_3$ (1)
- Linear with quadratic: $Y = a + b_1 X_1 + b_2 X_2 + b_3 X_3 + b_4 (X_1)^2 + b_5 (X_2)^2 + b_6 (X_3)^2$ (2)

(3)

- Natural log: $Ln(Y) = a + b_1 Ln(X_1) + b_2 Ln(X_2) + b_3 Ln(X_3)$
- Natural log with quadratic: $Ln(Y) = a + b_1 Ln(X_1) + b_2 Ln(X_2) + b_3 Ln(X_3) + b_4 Ln((X_1)^2) + b_5 Ln((X_2)^2) + b_6 Ln((X_3)^2)$ (4)

where:

 $\begin{array}{l} Y = retrore flectivity\\ a = intercept\\ b_i = coefficient\\ X_1 = cumulative traffic amounts (AADT/lane)\\ X_2 = cumulative precipitation\\ X_3 = cumulative snowfall \end{array}$

The research team expected difficulties in Phase I's regression analysis because the brief data collection period meant that the required estimation would be outside of the data range. For the one-year period, maximum cumulative snowfall was 88 inches and the maximum cumulative traffic per lane was 3 million cars. Since the studied materials are known to last more than 3 years and possibly more than 5 years, there would be too many uncertainties in the performance forecast.

Regression analysis is not good for forecasting outside of the data range (i.e., future events), but it is good for estimating events that have not actually occurred but are within the data range. In order to produce a reasonable estimation, the collected data range must be long enough to include the life cycle.

Because the durable materials' retroreflectivity did not diminish with a clear trend during the one-year data collection period, the regression analysis resulted in different scenarios for each basic function (Figure 3).

The second concern was the shapes of the functions' curves with one year of data. As shown in Figure 4, the retroreflectivity of the durable materials did not change as much in the first year as waterborne paint's did. This characteristic made it difficult to predict the future performance of the durable materials. Additionally, retroreflectivity tends to increase in the first few months after application of the material.



Figure 3. Examples of the Regression Analysis with Different Basic Equations for the Durable Materials with One Year of Data



Figure 4. Typical Retroreflectivity Curves for the Different Pavement Marking Materials

Since the retroreflectivity levels for the durable materials were relatively high (about 300-800 $mcd/m^2/lux$) compared to the threshold values (80-150 $mcd/m^2/lux$) during the first year, the estimation of the life cycles was very sensitive. Figure 5 shows that the life cycle of the durable material can be very sensitive depending on the coefficients of the variables for the estimated curve. In contrast, waterborne paint's life cycle estimation was less sensitive because its retroreflectivity values after the first year were very close to the threshold value. This characteristic means the life cycle variance can be a few years for a durable material and a few months for waterborne paint.

The Phase I results were not prominent for the aforementioned reasons. None of the four regression equations were consistent for any of the conditions, establishing that the research required more data to predict the retroreflectivity of the durable materials.



Figure 5. Different Life Cycles with Different Estimation Curves

METHODOLOGY

Data Selection

The three inputs used in this analysis were cumulated annual average daily traffic (AADT) per lane, cumulated precipitation, and cumulated snowfall. Many studies use total cumulated AADT, but the research team believed that cumulated AADT per <u>lane</u> better represented the chance of exposure to traffic. The research team focused on cumulated precipitation and cumulated snowfall because they can serve as proxy inputs for other weather-related variables. Retroreflectivity was considered the only output of the relationship, and the research team used it to calculate life cycle and economic efficiency.

Data Collection

Retroreflectivity Data Collection Methods

The SHA collected retroreflectivity data at the six locations six or seven times a year for the following marking types: white edge (WE), white skip (WS), yellow center (YC), yellow edge (YE), and yellow skip (YS). In addition to retroreflectivity, SHA recorded the number of lanes and AADT for each test site. Morgan State University collected the daily precipitation and snowfall amounts from each site's nearest weather station. The collection schedule can be seen in Table 5. Data was collected more frequently in the winter because the previous waterborne paint study found that snow removal can be an important factor in the deterioration of a pavement marking's retroreflectivity. As shown in Figure 6, the retroreflectivity data was measured at the exact same five points at each mile point for all five mile points at each location.

Retroreflectivity Measuring Equipment

Retroreflectivity was measured with the LTL-X retrometer (Figure 7). Produced by Delta Company in Denmark, the LTL-X retrometer is a portable field instrument that measures retroreflection in terms of R_L , the coefficient of retroreflected luminance, according to international agreements. The LTL-X illuminates the road at an angle of 1.24°, and the reflected light is measured at an angle of 2.29° that corresponds to an observation distance of 100 feet (30 m). (These measurements mimic a driver's visibility field under normal conditions.)

The instrument's illumination field is approximately 80 inches x 18 inches (200 mm x 45 mm), and the observation field is about 244 inches x 24 inches (610 mm x 60 mm). The tower of the LTL-X contains the illumination and observation system and the control electronics. An optical system at the bottom of the tower directs a beam of light toward the road surface through a dust-protection window. A polymer shielding covers the measuring area for normal operation.

The LTL-X is controlled by multiple microprocessors, and it is operated with an extractable keyboard located at the top of the retrometer. With the push of a button, it executes the measurement and displays the result in plain text. The result is automatically transferred to the internal memory. The measurement—along with its corresponding time, date, and other information—can be printed using the built-in printer.

							(date)
	Route	MD 5	MD 32	MD 175	MD 216	MD 611	I-68
	Date Striped	12/10/2006	06/21/2006	08/01/2006	09/18/2006	11/28/2006	06/26/2007
2006	Jun		23				
	Jul		28				
	Aug		30	4			
	Sep		28	13	26		
	Oct			10	25		
	Nov			15	27		
	Dec		6				
2007	Jan	29	9	17	30	4	
	Feb	27				22	
	Mar	26	9	15	22	29	
	Apr						
	May	22	7	15	18	31	
	Jun				19		
	Jul	25		19		31	
	Aug			-	15		
	Sep	25				7	28
	Oct						31
	Nov		20			1	30
	Dec	12		7	19	-	20
2008	Ian	12		,	17		
2000	Feb	11	21			15	
	Mar	11	21	25	25	15	17
	Apr	15	11	20	20	15	23
	May					1	
	Iun					1	
	Jul	15	10	1	8	23	29
	Ang	10	10	1	0	23	22
	Sen						
	Oct	20	16	1	10	30	
	Nov	20	10	1	10	50	10
	Dec						10
2009	Ian		15		14		
2007	Feb	6	15		11	10	
	Mar	0				10	
	Anr	16	9	2	7		
	May	10	,	2	,	14	
	Iun					17	
	Jul	29	16	22	14	1	
	Δμσ	2)	10	22	11	1	3
	Sent						5
	Oct					8	
	Nov					0	17
	Dec				15		17
2010	Ian	12	7		1.5		
2010	Feb	12	,				
	March						
	April						
	May						13
	Iun	15	3	8	11	17	1.5
	JUII	1 1 2	1.5	10	1 11	1 1/	1

Table 5. Retroreflectivity Data Collection Schedules



Figure 6. Photo of Test Site with Spot Markings



Figure 7. Retroreflectivity Measuring Equipment (Delta LTL-X)

Data Entry

The retroreflectivity data collected by SHA was handwritten, and the data needed to be entered into an electronic file for analysis. The Morgan State University project team entered the retroreflectivity data and the weather-related information into an electronic file on a monthly basis during the data collection period.

Regression Analysis

Regression analysis is the main method for estimating the relationship between the output (retroreflectivity) and inputs in this study. It involves a single dependent variable or response, Y, which is uncontrolled. The response depends on one or more independent or regressor variables that are measured with negligible error and are controlled. The relationship fit to a set of experimental data is characterized by a prediction equation called a regression equation. It is called single variable regression if there is only one regressor or multi-variable regression if there are more than two regressors.

The smaller the variability of the residual values around the regression line relative to the overall variability, the better the prediction. For example, if there is no relationship between the x and Y variables, then the ratio of the residual variability of the Y variable to the original variance is equal to 1.0. If x and Y are perfectly related, then there is no residual variance and the ratio of variance is zero. In most cases, the ratio would fall somewhere between 0 and 1.0. One minus this ratio is referred to as R-square or the coefficient of determination. This value is immediately interpretable in the following manner. An R-square of 0.4 means that the variability of the Y values around the regression line is 1-0.4 times the original variance. In other words, 40 percent of the original variability has been explained and 60 percent residual variability remains. Ideally, most, if not all, of the original variability would be explained. The R-square value is an indicator of how well the model fits the data (i.e., an R-square close to 1.0 indicates that almost all of the variability with the variables specified in the model has been explained).

The adjusted R-square attempts to yield a more honest value to estimate the R-square for the population. The value of the R-square was .4892, and the value of the adjusted R-square was 0.4788. Adjusted R-square is computed using the formula 1 - ((1 - Rsq) ((N - 1) / (N - k - 1))). This formula shows that a small number of observations and a large number of predictors will produce a greater difference between R-square and adjusted R-square because the ratio of (N - 1) / (N - k - 1) / (N - k - 1) will be much greater than one. By contrast, when the number of observations is larger than the number of predictors, the value of R-square and adjusted R-square will be much closer because the ratio of (N - 1) / (N - k - 1) will approach one.

To find the data's correct estimation function, this project used the same four basic regression equations (Equations 1-4) examined in Phase I.

Analysis Process

Figure 8 summarizes the analysis process for this project.



Figure 8. Flow Chart for the Analysis

Life Cycle Estimation for the Different Materials

The proper regression equation and the threshold values in Table 3 will estimate the life cycles of the pavement marking materials. The three input variables used to estimate retroreflectivity were all dependent on the number of days. In order to find the relationship between retroreflectivity

and number of days, the unit values for those variables were fixed as typical low, medium, and high.

The typical low, medium, and high values for daily traffic—1500 AADT per lane, 3000 AADT per lane, and 6000 AADT per lane, respectively—were based on the traffic amounts at the study locations.

The snowfall values were based on the two-year average at the study locations. The typical annual heavy snowfall amount, 88 inches per year, was based on the amounts in the western area. The central region was the basis for the moderate amount (20 inches per year), and the eastern area was the basis for the light amount (13 inches per year). The annual precipitation—30 inches per year—was similar throughout the regions. Table 6 shows the nine typical combinations of traffic and snowfall amounts for life cycle analysis in this research.

Snowfall \rightarrow	Light	Moderate	Heavy
Traffic ↓	(Eastern)	(Central)	(Western)
Low	1500 AADT/lane	1500 AADT/lane	1500 AADT/lane
	13 inches/year	22 inches/year	88 inches/year
Medium	3000 AADT/lane	3000 AADT/lane	3000 AADT/lane
	13 inches/year	22 inches/year	88 inches/year
High	6000 AADT/lane	6000 AADT/lane	6000 AADT/lane
	13 inches/year	22 inches/year	88 inches/year

Annual precipitation is assumed to be 30 inches per year for all nine combinations.

Table 6. Typical Combinations for Life Cycle Analysis

Cost Estimation for the Different Materials

In order to estimate economic efficiency, the research team had to calculate the costs to install each product in terms of money, delay, and potential accidents.

The research team based monetary installation costs on the state of Maryland's application bills from construction companies. In general, the unit cost depended on the total length of the pavement marking applications. Therefore, the best way to estimate the monetary installation costs was to find the regression equation that showed the relationship between the unit cost and the project's installation length.

However, in this research, the unit installation costs were estimated as the average unit costs of the major application projects as shown in Tables 7-10. This was done to minimize the complexity of trying to estimate the installation costs for different project lengths.

Tables 7-9 show the average unit costs for a five-inch-wide piece of inlaid tape, thermoplastic, and waterborne paint from various pavement marking projects. Table 10 compares the unit costs of the three pavement marking materials.

Location	Length of Marking (ft)	Total Cost (\$)	Unit Cost (\$/ft)
MD 32	5,982	27,517.2	4.60
MD 175	3,971	11,913.0	3.00
MD 216	13,359	40,077.0	3.00
US 301	18,066	56,004.6	3.10
US 219	10,560	29,040.0	2.75
Total / Average	51,938	164,551.8	3.168

Table 7. Unit Cost Estimation for Inlaid Tape

Location	Length of Marking (ft)	Total Costs (\$)	Unit Cost (\$/ft)
MD 32	32,942	27,517.2	0.42
MD 216	13,210	5,284.0	0.40
US 1	6,479	4,859.63	0.75
MD 940	6,727	4,036.2	0.60
US 40	6,944.32	8,680.4	1.25
Total / Average	66302.32	50,377.43	0.760

Table 8. Unit Cost Estimation for Thermoplastic

Location	Length of Marking (ft)	Total Costs (\$)	Unit Cost (\$/ft)
MD 135	72,963	10,214.82	0.14
MD 295	24,144	3,757.92	0.16
Total / Average	97,107	13,972.74	0.144

Table 9. Unit Cost Estimation for Waterborne Paint

Material	Installation Costs (\$/ft)
Waterborne Paint	0.144
Thermoplastic	0.760
Inlaid Tape	3.168

Table 10. Installation Costs for the Different Pavement Marking Materials in Maryland

A pavement marking's installation usually causes traffic delays because the installation vehicle is slow and lanes are sometimes blocked. Because each of the materials examined in this research had a different installation process, the research team estimated the delay costs for each product under different conditions.

The basic input variables for estimating delay were the number of lanes, the traffic amount, and the road length of the project. The research team also had to assume the installation vehicle's speed. With those input variables, the delays were estimated through VISSUM, the traffic simulation software. Then, regression analysis was performed to find the relationship between the delay and input variables, so delay can be estimated when the input variables are available. Thus, information about the installation site allows estimation of the installation-caused delay.

Although the research team developed a process to find the delay for specific conditions, this study used one average delay cost in order to simplify the cost estimation. However, if site-specific delay estimation is necessary, it can be found using the regression equation for the site's specific conditions.

The general delay cost was based on a two-lane, half-mile road section with a traffic volume of 1,000 vehicles per hour. Inlaid tape required no additional delay because the material is applied during the paving process.

Temporary tape is installed before thermoplastic is applied to pavement. It was assumed that the installation and removal of the temporary tape took about 30 minutes for a half-mile section. After the tape's removal, thermoplastic was applied at the assumed speed of 10 miles per hour (although it can be slower depending on the thickness of the thermoplastic). Altogether, the thermoplastic installation created an average delay of 13.65 seconds per car, which made the total delay 13,650 seconds. With \$20 per hour of assumed time value, the total delay cost for the thermoplastic installation was \$75.83 or 1.44 cents per foot.

An installation speed of 10 miles per hour meant that waterborne paint created an average delay of 3.83 seconds per car and a total delay of 3,830 seconds. With \$20 per hour of assumed time value, the total delay cost for the installation was \$21.28 or 0.4 cents per foot.

The accident cost is the installation's final expense. It was estimated through the literature review. Although no definitive research shows the exact work zone accident cost, it is believed that there are about 20-30 percent more accidents in a work zone than on the general road. Since the estimated annual accident cost was \$164.2 billion (Clifford, 2008) and the annual vehicle miles traveled (VMT) was 3 trillion miles, annual accident cost was about 5.5 cents for one VMT.

The research team assumed that it took 63 minutes to install thermoplastic (30 minutes each for the temporary tape's installation and removal, and three minutes for thermoplastic's installation on a half-mile section with the installation vehicle moving at 10 miles per hour). As stated earlier, the section's assumed traffic volume was 1,000 vehicles per hour. Thus, the zone's average accident cost for 63 minutes would be about \$28.33 (5.5 cents x 0.5 miles x 1,030 veh/hour). Since \$28.33 is the general accident cost for a half mile with 1,030 vehicles, the additional accident cost would be about 25 percent of the general accident costs, which is \$7.081. If it is distributed to the half-mile section, the unit accident cost caused by the pavement marking installation project will be 0.268 cents per foot.

Waterborne paint's assumed installation time was 3 minutes. As with thermoplastic, the time was based on a half-mile section and a 10-miles-per-hour installation speed. The installation affected only 30 cars. The total general accident cost was 82.5 cents and the total work zone accident cost was 20.63 cents. If it were distributed to the half-mile section, the unit accident cost caused by the pavement marking installation project would be 0.008 cents per foot.

Each material's final unit cost was the sum of its monetary, delay, and accident costs. As shown in Table 11, the total installation cost was \$3.168/ft for inlaid tape, \$0.777/ft for thermoplastic, and \$0.148/ft for waterborne paint.

	Inlaid Tape (\$/ft)	Thermoplastic (\$/ft)	Waterborne Paint (\$/ft)
Installation cost	3.168	0.760	0.144
Delay cost	-	0.0144	0.004
Accident cost	-	0.00268	0.00008
Total installation cost	3.168	0.777	0.148

Table 11. Summary of Total Installation Cost Estimation

Economic Efficiency Estimation for the Different Materials

Because installation costs occur once in a material's life cycle, the costs were distributed throughout the life cycle. As shown in Equation 5, this was done by converting present value to annual value with an assumed interest rate (or simply it can be divided by the life cycle, assuming that there is no interest for distributing the installation costs through the life cycle). The pavement marking material with the lowest annual cost is the most economically efficient material.

$$A = \frac{PV}{\frac{(1+i)^{n} - 1}{i(1+i)^{n}}}$$
(5)

where:

A = annual costs (or monthly costs) PV = present value of installation costs i = interest rate (per year or per month) n = life cycle (number of years or months)

RESEARCH FINDINGS

This research estimated the performance and life cycle of inlaid tape and thermoplastic based on three to four years of data collection. Since the data collection period was long enough, retroreflectivity values at certain locations became close to the threshold values and the resulting regression analysis was more reasonable.

Regression Analysis

Tables 12-15 show the regression results for inlaid tape and thermoplastic. The three variables used in the regression analysis were precipitation, snowfall, and traffic amount. As shown in the tables, because the linear function had the highest R-square value of all the equations, it best fit all four materials (white inlaid tape, yellow inlaid tape, white thermoplastic, and yellow thermoplastic).

White inlaid tape's adjusted R-square values indicate the correctness of the estimation. Not only were white inlaid tape's adjusted R-square values higher than the values of the other materials studied in this project, but they were also higher than the values in other research. However, yellow thermoplastic's R-square value was extremely low, which may indicate that the regression analysis produced imprecise retroreflectivity estimates. The field data caused most of the inconsistency in the data and the regression analysis.

The retroreflectivity curves in Figures 9-26 were based on the nine traffic and snowfall combinations in Table 6. Figures 9-17 show the estimated retroreflectivity curves of white inlaid tape and thermoplastic. The curves had a similar shape and were almost parallel in all nine cases, showing that both materials' basic depreciation characteristics were very similar. The only major difference was the materials' initial retroreflectivity values.

Figures 18-26 show the estimated retroreflectivity curves of yellow inlaid tape and thermoplastic. Unlike the white pavement markings, the shapes of both curves were different. Although yellow inlaid tape had a higher initial retroreflectivity, it deteriorated faster than yellow thermoplastic. After a certain period, yellow thermoplastic's retroreflectivity was higher that yellow inlaid tape's.

The estimates for the yellow markings were not as good as the estimates for the white markings. As shown in the regression tables, the yellow markings' adjusted R-square values were low. In particular, yellow thermoplastic's R-square value was very low. The estimation of the retroreflectivity values may not be correct and reasonable. The yellow markings' low R-square values will be explained in the validation section.

Figures 9-26 show that the retroreflectivity curves were more sensitive to snowfall than traffic amounts (i.e., the snowfall amount, not traffic, was the major factor in retroreflectivity's deterioration). This will be discussed further in the life cycle analysis.

	Linear	Log	Nonlinear	Nonlinear Log
Number of Observations	7603	7603	7603	7603
F-Value	2433.4	1113.27	-	-
Adjusted R-square	0.5015	0.31722	0.334	0.334
Intercept	762.81	6.4379	755.2	6.51
Coef. for cumulative traffic	-1E^-05	0.051837	0.000016	-129.92
Coef. for cumulative traffic square	-	-	1.78X10 ⁻¹²	64.98
Coef. for cumulative precipitation	-0.41259	-0.16495	-860	502.76
Coef. for cumulative precipitation sq.	-	-	0.00042	-251.45
Coef. for cumulative snow	-0.98892	-0.07279	795	-511.76
Coef. for cumulative snow square	-	-	0.00054	255.83

Table 12. Regression Results for White Inlaid Tape

	Linear	Log	Nonlinear	Nonlinear Log
Number of Observations	3121	3121	3121	3121
F-Value	623.438	411.4319	-	-
Adjusted R-square	0.388	0.2948	0.301	0.30089
Intercept	405.66	4.45	434.1	4.36
Coef. for cumulative traffic	4.5E^-6	.1286	.000019	129.18
Coef. for cumulative traffic square	-	-	-7.5X10 ⁻¹³	-64.52
Coef. for cumulative precipitation	.231	02015	023	142.4
Coef. for cumulative precipitation sq.	-	-	.00033	-71.21
Coef. for cumulative snow	-2.938	184	-4.58	-781.21
Coef. for cumulative snow square	-	-	.0068	390.51

Table 13. Regression Results for Yellow Inlaid Tape

	Linear	Log	Nonlinear	Nonlinear Log
Number of Observations	7816	7816	7816	7816
F-Value	794.419	793.92	-	-
Adjusted R-square	0.2748	0.2747	0.140	0.140
Intercept	348.91	11.15	341.7	12.09
Coef. for cumulative traffic	-9.4E^-6	477	000035	201.26
Coef. for cumulative traffic square	-	-	$1.21X10^{-12}$	-100.89
Coef. for cumulative precipitation	.0688	.3395	.804	636
Coef. for cumulative precipitation sq.	-	-	0004	.439
Coef. for cumulative snow	-1.3577	-0.1066	-3.401	589.30
Coef. for cumulative snow square	-	-	.0078	-294.64

Table 14.	Regression	Results for	White	Thermoplastic
1 abic 14.	Regression	ICSUITS IOI	· · mu	1 ner moplastie

	Linear	Log	Nonlinear	Nonlinear Log
Number of Observations	4664	4664	4664	4664
F-Value	172.1843	100.3737	-	-
Adjusted R-square	0.1129	0.0688	0.001	0.00141
Intercept	189.57	4.545	154.7	4.698
Coef. for cumulative traffic	4.96E^-6	0.0453	0.000013	105.23
Coef. for cumulative traffic square	-	-	-8.02X10 ⁻¹³	-52.60
Coef. for cumulative precipitation	.0115	0214	.1274	1230.84
Coef. for cumulative precipitation sq.	-	-	0.000037	-615.42
Coef. for cumulative snow	-0.7233	-0.084	7372	40.60
Coef. for cumulative snow square	-	-	00248	-20.30

 Table 15. Regression Results for Yellow Thermoplastic



Figure 9. Regression Curves for White Markings (Low Traffic & Light Snow)



Figure 10. Regression Curves for White Markings (Low Traffic & Moderate Snow)



Figure 11. Regression Curves for White Markings (Low Traffic & Heavy Snow)



Figure 12. Regression Curves for White Markings (Medium Traffic & Light Snow)



Figure 13. Regression Curves for White Markings (Medium Traffic & Moderate Snow)



Figure 14. Regression Curves for White Markings (Medium Traffic & Heavy Snow)



Figure 15. Regression Curves for White Markings (High Traffic & Light Snow)



Figure 16. Regression Curves for White Markings (High Traffic & Moderate Snow)



Figure 17. Regression Curves for White Markings (High Traffic & Heavy Snow)



Figure 18. Regression Curves for Yellow Markings (Low Traffic & Light Snow)



Figure 19. Regression Curves for Yellow Markings (Low Traffic & Moderate Snow)



Figure 20. Regression Curves for Yellow Markings (Low Traffic & Heavy Snow)



Figure 21. Regression Curves for Yellow Markings (Medium Traffic & Light Snow)



Figure 22. Regression Curves for Yellow Markings (Medium Traffic & Moderate Snow)







Figure 24. Regression Curves for Yellow Markings (High Traffic & Light Snow)



Figure 25. Regression Curves for Yellow Markings (High Traffic & Moderate Snow)



Figure 26. Regression Curves for Yellow Markings (High Traffic & Heavy Snow)

Life Cycle Estimation

To draw the regression curves for retroreflectivity in Figures 9-26, the research team used the assumed traffic and weather conditions. After they estimated retroreflectivity for each condition, the research team calculated a life cycle for each of the three speed-based threshold values in Table 3.

Table 16 shows the estimated life cycles for the three white materials. (Although this project focuses on inlaid tape and thermoplastic, waterborne paint was included in the analysis for comparative purposes.) As stated before, the linear function was used to estimate the retroreflectivity performance and life cycles for inlaid tape and thermoplastic because its adjusted R-square values were higher than the other basic functions'. For consistency, the linear function was also used for the waterborne paint estimates. In Table 17, the same life cycle estimation method was applied to the three yellow pavement marking materials.

Some of the estimated life cycles were not reasonable (e.g., yellow thermoplastic in high traffic and light and moderate snow). In those cases, the estimation produced unreasonably long life cycles and retroreflectivity values that increased with time. The unreasonable estimates may be due to the field data's unreliable characteristics and a data collection period that was too brief. Even though this study's data collection period was longer than this research team's previous pavement marking study, the durable materials' life expectancy still exceeded the study period.

A material's life cycle can vary depending on the time of the installation. Snow has a very significant effect on the visibility and retroreflectivity of any type of pavement marking. After the winter, a material may reach its retroreflectivity threshold, in which case the effective life of

the pavement marking ends. For this project, the life cycle estimates were based on a September installation of the materials. Of course, installations during a different time of the year would yield different life cycle estimates.

Condition	Inlaid Tape	Thermoplastic	Waterborne
			Faint
Low Traffic & Light Snow	240, 258, 264	113, 144, 156	9, 18, 19
Low Traffic & Moderate Snow	201, 218, 223	78, 100, 103	6, 16,16
Low Traffic & Heavy Snow	67, 76, 77	18, 25, 28	3, 4, 4
Medium Traffic & Light Snow	221, 239, 243	91, 114, 126	15, 18, 18
Medium Traffic & Moderate Snow	173, 188, 193	65, 85, 89	6, 16, 17
Medium Traffic & Heavy Snow	64, 72, 73	16, 18, 24	3, 4, 4
High Traffic & Light Snow	157, 172, 176	65, 82, 88	15, 18, 19
High Traffic & Moderate Snow	137, 149, 152	65, 78, 89	6, 16, 17
High Traffic & Heavy Snow	60, 64, 65	16, 18, 19	3, 4, 4

Life cycles are based on thresholds of 150, 100, and 85 mcd/m²/lux, respectively.

Table 16. Estimated Life Cycle of White Pavement Marking Materials

Condition	Inlaid Tape	Thermoplastic	Waterborne
			Paint
Low Traffic & Light Snow	127, 142, 146	170, 242, 262	6, 13, 14
Low Traffic & Moderate Snow	76, 79, 80	66, 90, 100	12, 13, 13
Low Traffic & Heavy Snow	18, 18, 19	7, 18, 18	4, 4, 4
Medium Traffic & Light Snow	140, 157, 162	270, 275, 299	12, 13, 13
Medium Traffic & Moderate Snow	76, 88, 88	114, 156, 167	12, 13, 13
Medium Traffic & Heavy Snow	15, 16, 16	16, 21, 21	4, 4, 4
High Traffic & Light Snow	174, 195, 201	-	12, 13, 13
High Traffic & Moderate Snow	88, 90, 100	-	12, 13, 13
High Traffic & Heavy Snow	15, 16, 16	17, 27, 28	4, 4, 4

Life cycles are based on thresholds of 100, 65, and 55 mcd/m²/lux, respectively.

Table 17. Estimated Life Cycle of Yellow Pavement Marking Materials

Validation of the Regression Analysis and Life Cycle Estimation

The regression analysis produced the estimated life cycles (Tables 16 and 17). In order to validate the estimation, the regression results were compared to the actual collected data.

Inlaid tape showed rather consistent results. The white inlaid tape on MD 611, which is in the eastern area of the state and receives little snow, had the highest average retroreflectivity. At the same time, the white inlaid tape on I-68, which is in the western area of the state and receives the heaviest snowfalls, had the lowest average retroreflectivity.

For the heavy snow and high traffic conditions, white inlaid tape's estimated life cycle was five years and yellow inlaid tape's estimated life cycle was two years. The real data for I-68 shows that the white markings' average retroreflectivity is 166 and the yellow markings' average

retroreflectivity after three years is 73. The real data confirmed the regression analysis and life cycle estimation for inlaid tape.

Thermoplastic showed less consistent and less reasonable results. For the yellow thermoplastic on MD 32, the real data showed that the retroreflectivity after four years was well above the average initial retroreflectivity. Yellow thermoplastic's initial retroreflectivity was 175 and its average retroreflectivity after four years was 140. Because thermoplastic was not installed and evaluated on I-68, the field data made the performance of yellow thermoplastic extremely better than that of the other pavement marking materials. If thermoplastic had been installed, the difference between thermoplastic's initial and final retroreflectivities would be obvious.

Material	Tape White	Tape Yellow	Thermo White	Thermo Yellow
Average initial	700	390	340	175
retroreflectivity				
Average final	270	225	176	140
retroreflectivity				
High retroreflectivity at	453	301	266	250
the final data collection	(MD 611)	(MD 611)	(MD 5)	(MD 32)
Low retroreflectivity at	166	73	117	99
the final data collection	(I-68)	(I-68)	(MD 175)	(MD 5)

Table 18. Summary of the Real Data Values from Data Collection

The real data for both white pavement markings confirmed the accuracy of the regression analysis' retroreflectivity deterioration rates. The real data for the yellow pavement markings also matched the results of the regression analysis: yellow thermoplastic showed relatively better endurance than yellow tape in terms of deterioration rate (Table 18).

Economic Efficiency Analysis

Economic efficiency is typically determined by annual costs. The annual cost is found through the even distribution of the installation costs throughout the estimated life cycle.

As discussed in the previous section, the estimated total installation costs were \$0.148/ft. for waterborne paint, \$0.777/ft. for thermoplastic, and \$3.168/ft. for inlaid tape. Those costs were higher than the material costs used in Phase I (\$0.05/ft, \$0.50/ft and \$2.00/ft, respectively) because they include installation costs (such as material, labor, and equipment) and delay and accident costs caused by the installation. Tables 19 and 20 show the annual costs for the pavement marking materials. To find the monthly cost for each material, the estimated total installation costs (in cents) were divided by the estimated life cycles.

The results showed that thermoplastic is the most economical choice for white pavement markings under most of the conditions included in this study. Unless the road section receives large amounts of snow, thermoplastic is also the most economical choice for yellow pavement markings. Waterborne paint is the most economical material for yellow markings in heavy snow conditions.

Again, the economical analysis was based on the life cycle estimation, and the life cycle estimation was based on the time of the installation. If the installation was done at a different time of year, the life cycles would be different and the most economical material would change. The next section will discuss how changing the input variables would affect the economic efficiency.

Condition	Inlaid Tape	Thermoplastic	Waterborne Paint
Low Traffic & Light Snow	1.32	0.68	1.64
Low Traffic & Moderate Snow	1.58	1.00	2.47
Low Traffic & Heavy Snow	4.73	4.31	4.93
Medium Traffic & Light Snow	1.43	0.85	0.99
Medium Traffic & Moderate Snow	1.83	1.20	2.47
Medium Traffic & Heavy Snow	4.95	4.86	4.93
High Traffic & Light Snow	2.02	1.20	0.99
High Traffic & Moderate Snow	2.31	1.20	2.47
High Traffic & Heavy Snow	5.28	4.85	4.93

Cents per month. Monthly costs based on a threshold of 150 mcd/m²/lux.

Table 19. Annual Costs for White Pavement Marking Materials

Condition	Inlaid Tape	Thermoplastic	Waterborne Paint
Low Traffic & Light Snow	2.49	0.46	2.47
Low Traffic & Moderate Snow	4.17	1.18	1.23
Low Traffic & Heavy Snow	17.60	11.10	3.70
Medium Traffic & Light Snow	4.17	0.29	1.23
Medium Traffic & Moderate Snow	4.17	0.69	1.23
Medium Traffic & Heavy Snow	21.12	4.86	3.70
High Traffic & Light Snow	1.82	-	1.23
High Traffic & Moderate Snow	3.60	-	1.23
High Traffic & Heavy Snow	21.12	4.57	3.70

Cents per month. Monthly costs based on a threshold of $100 \text{ mcd/m}^2/\text{lux}$.

Table 20. Annual Costs for Yellow Pavement Marking Materials

Sensitivity Analysis

The two main inputs for the economic efficiency analysis were life cycle and total installation costs. Life cycles were based on regression curves and threshold values. The total installation costs were based on the monetary installation costs (which depend on the price of material, labor, etc.), delay, and accident costs (which depend on the installation length, traffic amount, number of lanes, etc.).

The analysis would be very complicated if all those variables were included. Therefore, the sensitivity analysis in this research considered the final inputs, life cycle, and total installation

costs. The lower level variables (such as threshold values, monetary installation costs, etc.) can be determined once life cycle and total installation costs are assumed.

In order to be competitive to thermoplastic, inlaid tape must have either a longer life cycle or lower installation costs. Table 21 shows what happened when inlaid tape's life cycle was increased by 50 percent. For the white markings, the increase made inlaid tape competitive to thermoplastic and more economical in high snow conditions. In this case, inlaid tape became more economical than waterborne paint in most scenarios.

Condition	Inlaid Tape	Thermoplastic	Waterborne Paint
Low Traffic & Light Snow	0.88	0.68	1.64
Low Traffic & Moderate Snow	1.06	1.00	2.47
Low Traffic & Heavy Snow	3.17	4.31	4.93
Medium Traffic & Light Snow	0.96	0.85	0.99
Medium Traffic & Moderate Snow	1.22	1.20	2.47
Medium Traffic & Heavy Snow	3.30	4.86	4.93
High Traffic & Light Snow	1.35	1.20	0.99
High Traffic & Moderate Snow	1.55	1.20	2.47
High Traffic & Heavy Snow	3.52	4.85	4.93

Cents per month. Monthly costs are based on a threshold of 150 mcd/m²/lux.

Table 21. Annual Costs for White Pavement Marking Materials When Inlaid Tape's LifeCycle is 50% Longer

Table 22 shows how the annual costs change when inlaid tape's cost is 40 percent lower (\$1.900 instead of \$3.168). For the white pavement markings, the decrease made inlaid tape economically competitive to thermoplastic. In heavy snow conditions, regardless of the traffic amount, inlaid tape was more economical. In moderate snow areas, inlaid tape and thermoplastic were almost the same in terms of economic efficiency. In light snow areas, thermoplastic remained more economical than inlaid tape.

The sensitivity analysis showed that to make the inlaid tape economically competitive, inlaid tape's life cycle should be increased by 50 percent or its total installation costs should be decreased by 40 percent. However, inlaid tape can be more competitive to thermoplastic in heavy snow areas even with less than 50 percent increased life cycle or less than 40 percent decreased total installation cost, because inlaid tape's relative performance to thermoplastic's in heavy snow area is better than that in less snow areas.

Condition	Inlaid Tape	Thermoplastic	Waterborne Paint
Low Traffic & Light Snow	0.79	0.68	1.64
Low Traffic & Moderate Snow	0.95	1.00	2.47
Low Traffic & Heavy Snow	2.84	4.31	4.93
Medium Traffic & Light Snow	0.86	0.85	0.99
Medium Traffic & Moderate Snow	1.10	1.20	2.47
Medium Traffic & Heavy Snow	2.97	4.86	4.93
High Traffic & Light Snow	1.21	1.20	0.99
High Traffic & Moderate Snow	1.39	1.20	2.47
High Traffic & Heavy Snow	3.17	4.85	4.93

Cents per month. Monthly costs are based on a threshold of 150 $mcd/m^2/lux$.

Table 22. Annual Costs for White Pavement Marking Materials When Inlaid Tape'sInstallation Costs are 40% Lower

CONCLUSIONS

Because inlaid tape and thermoplastic are known to last more than three years—in some locations, thermoplastic lasts more than five years and inlaid tape more than eight years—the data collection period for this research was not long enough to justify various basic functions. With the data collection period for this research, the linear function was found to fit the relationship between the collected retroreflectivity data and the input variables.

Because of the inconsistent nature of the field data, the adjusted R-square values, which indicate how well the data fits the estimated function, were not very high. However, the R-square values were higher than the values found in similar research because of the inclusion of weather data and traffic data. Traffic data was the sole conventional variable for the previous life cycle studies of the pavement markings.

Snowfall amounts affected retroreflectivity more than traffic amounts did. This indicates that snowplow use must be well controlled and standardized in order to improve the pavement markings' performance and life cycles. Increased use of rubber blades on the plows may minimize the damage to the pavement markings.

The regression results fit the real data for the white pavement markings, but they did not fit as well for the yellow pavement markings. The regression results also showed that the regression estimates of inlaid tape fit the real data better than that of thermoplastic. These results would seem to indicate that the white markings' and inlaid tape's performance were more stable than the yellow markings' and thermoplastic's. It also means that there were uncertainties in yellow pavement markings' and thermoplastic's performance.

The life cycles for the pavement markings were determined with the estimated retroreflectivity and threshold values. The retroreflectivity estimates were based on nine weather and traffic combinations (which were based on three snowfall amounts and three traffic amounts).

A material's life cycle can vary greatly depending on the time of year of the installation. Snow removal has a significant effect on retroreflectivity. After a severe winter, a material typically hits its retroreflectivity threshold and the life of the pavement marking ends. For this project, the life cycle estimates were based on a September installation of the materials. Installations during a different time of the year would yield much different life cycle estimates and, consequently, different economic efficiencies.

In general, inlaid tape lasts longer than thermoplastic because inlaid tape's initial retroreflectivity is higher than thermoplastic's. In addition, the white pavement markings last longer than yellow pavement markings because the white pavement markings' initial retroreflectivity is higher than the yellow pavement markings'. However, in this study, the performance of yellow thermoplastic was abnormally good. In fact, yellow thermoplastic lasted as long as white thermoplastic and yellow inlaid tape.

Estimated life cycles and total installation costs were used to determine the materials' annual costs (i.e., economic efficiency). The estimated total installation costs were \$3.168 per foot for

inlaid tape, \$0.777 per foot for thermoplastic, and \$0.148 per foot for waterborne paint. Although inlaid tape can last longer effectively, thermoplastic was more economical under most conditions because of inlaid tape's higher installation costs. To make inlaid tape competitive to thermoplastic in terms of economic efficiency, the sensitivity analysis showed that inlaid tape's life cycle had to be increased by 50 percent or its total installation costs had to be reduced by 40 percent. For example, inlaid tape's life cycle would improve if the tape were set deeper in heavy snows areas—either by installing it at a higher asphalt temperature, or by cutting a groove in the pavement so that the tape was slightly below surface. Full-compliment tape projects or longer distance projects could also reduce the installation costs.

This project's two research assistants are currently expanding upon these findings for their theses. One research is about the estimation of total installation costs, and the other examines the life cycle differences among different marking types (such as edge line, skip line, and center line). Once completed, both studies will provide better and more complete information about the life cycles of pavement marking materials.

REFERENCES

Abboud, N., and Nowman, B. Cost- and Longevity-Based Scheduling of Paint and Thermoplastic Striping. *Transportation Research Record 1794*. Transportation Research Board, National Research Council, Washington, D.C., 2002, 55-62.

Clifford, Catherine. U.S. Car Accident Cost: \$164.2 Billion, CNNMoney.com, March 5, 2008.

Jiang, X., and Adeli, H. Freeway Work Zone Traffic Delay and Cost Optimization Model, Journal of Transportation Engineering, Vol. 129, No. 3, May 2003.

Jin, T., Saitoa, M., and Eggett, D. Statistical comparisons of the crash characteristics on highways between construction time and non-construction time, *Accident Analysis & Prevention*, Volume 40, Issue 6, November 2008.

Kopf, J. Reflectivity of Pavement Markings: Analysis of Retroreflectivity Degradation Curves, Washington State Transportation Center, WA-RD 592.1, September 2004

Lee, Y., Randal, R., and Karri, G. Retroreflectivity and Life Cycle Study of Waterborne Paint Pavement Markings: Case Study for the State of Maryland. Transportation Research Board Annual Meeting, Transportation Research Board, Washington D.C., 2008.

Lee, Y. Durability Study: Waterborne Paint Pavement Markings. Maryland State Highway Administration, December 2007.

Lee, Y. Life Cycle and Economic Efficiency Analysis: Durable Pavement Markings, Maryland State Highway Administration, July 2009.

Migletz, J., Graham, J., Bauer, K., and D. Harwood. Service Life of Durable Pavement Markings. Paper 010-447. *Transportation Research Board* 80th Annual Meeting Preprint CD-ROM. Transportation Research Board, National Research Council, Washington, D.C., January 2001.

Migletz, J., Graham, J., Bauer, K., and D. Harwood. Field Surveys of Pavement Marking Retroreflectivity. *Transportation Research Record 1657*. Transportation Research Board, National Research Council, Washington, D.C., 1999, 71-78.

Mohan, S., and Gautam, P. Cost of Highway Work Zone Injuries, *Practice Periodical on Structural Design and Construction*, Vol. 7, No. 2, May 1, 2002.

Mokkapati, Naveen. Determining the Extent and Characteristics of Overrepresentation on Large Truck Crashes in Daytime and Nighttime Work Zones, MS Thesis, Texas A&M University, December 2007.

Montebello, D., and Schroeder, J. Cost of Pavement Marking Materials. Minnesota Local Road Research Board, March 2000.

National Partnership for Highway Quality, Work Zone Fatalities, Web documents.

Pavement Markings Study Nears Completion. Better Roads, Vol. 66, No. 4. April 1996.

Potts, I., Harwood, D., Bokenroger, C., and Hutton, J. Benefit-Cost Evaluation of MoDOT's Total Striping and Delineation Program, OR09.014, Midwest Research Institute and Missouri Department of Transportation, November 2008.

Wang, J., Hughes, W., Council, F., and Paniati, J. Investigation of Highway Work Zone Crashes, Federal Highway Administration, FHWA-RD-96-100, 1996.

Zhang, Y., and Wu, D. Methodologies to Predict Service Lives of Pavement Marking Materials *Journal of the Transportation Research Forum*, Vol. 45, No. 3, 2006.