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IMPROVING FOUNDATION DESIGN IN ROCK: LOAD TEST AT BURMA ROAD OVERPASS

By:

Department of Civil and Architectural Engineering University of Wyoming 1000 E. University Avenue Laramie, Wyoming 82071 December 2009

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Abstract		Less data a The test	t and the stand in			
conjunction with construction of a new bridge at Burma	test on a drilled snaft foundation in wea Road Overpass on I-90 in Gillette, Wyor	k sandstone. The test ming. The purpose wa	as to provide much			
needed information on side resistance and base resistar	nce in weak sandstone of the Tertiary W	asatch Formation. Lo	bad test results are			
compared to design equations for both soil and rock. Des	sign equations based on treating the weatory the load test. Design equations base	ak sandstone as cohes ad on treating the sand	ionless soil provide			
provide reasonable agreement with the load test results,	but comparisons were limited by the in	ability to obtain repres	entative intact core			
samples suitable for measuring the uniaxial compressive	strength of the sandstone. Unit base res	istance mobilized in the	e load test exceeds			
response of the test shaft is analyzed by fitting to an ar	nalytical model, providing a practical too	of for evaluation of tria	l designs to satisfy			
service limit states. Finally, results of the load test are used to illustrate the application of AASHTO LRFD methodology to de						
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Approx	ximate Conversio	ns <mark>from</mark> SI U	Inits		Approximate Conversions to SI Units						
Symbol	When You Know	Multiply By	To Find	Symbol	Symbol	When You Know	Multiply By	To Find	Symbol		
Length					Length						
mm	millimeters	0.039	inches	In	in	inches	25.4	millimeters	mm		
m	meters	3.28	feet	Ft	ft	feet	0.305	meters	m		
m	meters	1.09	yards	Yd	yd	yards	0.914	meters	m		
km	kilometers	0.621	miles	Mi	mi	miles	1.61	kilometers	km		
Area					Area						
mm ²	square millimeters	0.0016	square inches	in ²	in ²	square inches	645.2	square millimeters	mm ²		
m²	square meters	10.764	square feet	ft ²	ft ²	square feet	0.093	square meters	m²		
m²	square meters	1.195	square yards	Yd ²	yd²	square yards	0.836	square meters	m²		
ha	hectares	2.47	acres	Ac	ac	acres	0.405	hectares	ha		
km ²	square kilometers	0.386	square miles	Mi ²	mi²	square miles	2.59	square kilometers	km ²		
Volume					Volume						
ml	milliliters	0.034	fluid ounces	fl oz	fl oz	fluid ounces	29.57	milliliters	ml		
I	liters	0.264	gallons	gal	gal	gallons	3.785	liters	I		
m³	cubic meters	35.71	cubic feet	ft ³	ft ³	cubic feet	0.028	cubic meters	m³		
m³	cubic meters	1.307	cubic yards	Yd ³	yd ³	cubic yards	0.765	cubic meters	m³		
Mass					Mass						
g	grams	0.035	ounces	Oz	oz	ounces	28.35	grams	g		
kg	kilograms	2.202	pounds	Lb	lb	pounds	0.454	kilograms	kg		
Mg	megagrams	1.103	short tons (2000 lbs)	т	Т	short tons (2000 lbs)	0.907	megagrams	Mg		
Tempera	ture (exact)				Tempera	ture (exact)					
°C	Centigrade	1.8 C + 32	Fahrenheit	°F	°F	Fahrenheit	5(F-32)/9	Celsius	°C		
	temperature		temperature			temperature	or (F-32)/1.8	temperature			
Illuminati	on				Illuminati	ion					
lx	lux	0.0929	foot-candles	Fc	fc	foot-candles	10.76	lux	lx		
cd/m ²	candela/m ²	0.2919	foot-Lamberts	FI	fl	foot-Lamberts	3.426	candela/m ²	cd/m ²		
Force an	d Pressure or Stress				Force an	d Pressure or Stress					
Ν	newtons	0.225	poundforce	Lbf	lbf	pound-force	4.45	newtons	Ν		
kPa	kilopascals	0.145	pound-force per square inch	psi	psi	pound-force per square inch	6.89	kilopascals	kPa		

SI* (Modern Metric) Conversion Factors

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EXECUTIVE SUMMARY

Load testing of a drilled shaft foundation at the site of a new bridge provided the opportunity to evaluate design methods employed by the Wyoming DOT for foundations in rock.

Selection of design values of side and base resistance for drilled shaft foundations in rock is a challenge to engineers and geologists responsible for design of bridges and other structures. Rock mass can exhibit large variability in strength and quality. Rock is often difficult to sample when it is highly fractured or weathered. The boundary between soil and highly weathered rock can be hard to define and the design equations for soil will produce different side and base resistance values than the design equations for rock. One approach to reducing uncertainty is to conduct a load test for the purpose of verifying values of side and base resistances. The Wyoming DOT conducted a drilled shaft load test for this purpose at the Burma Road Overpass site near Gillette, WY, in September, 2009. This load test provided an opportunity to research the behavior of drilled shafts in rock in order to improve the reliability and cost-effectiveness of WYDOT foundation design methods.

This report provides a review of design methods for drilled shafts in rock under axial loading (Chapter 1). This is followed by a summary of the field load test conducted at the Burma Road Overpass (Chapter 2). In Chapter 3, the load test results are compared to current design methods and the measured resistances are used to illustrate the application of LRFD design methods to the design of drilled shafts for the bridge at Burma Road Overpass.

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CHAPTER 1: INTRODUCTION AND BACKGROUND

1.1 Introduction

Properly designed and constructed drilled shaft foundations can provide cost-effective and reliable support for highway bridge structures. A drilled shaft is a reinforced concrete member constructed by excavating a cylindrical hole in the ground followed by placement of a reinforcing cage and backfilled with concrete. Use of drilled shafts can be particularly advantageous at sites underlain by rock because large axial and lateral loads can be supported and foundation deformations can be limited to tolerable levels. Tools and equipment for excavating in rock have undergone many improvements in recent years and design methods for shafts in rock also have advanced significantly. Nevertheless, selection of appropriate design values of side and base resistance for rock sockets can still be very challenging. Reasons include the following: (i) rock mass can exhibit large variability in strength and quality, (ii) rock is often difficult to sample and test when it is highly fractured, weak, or weathered, and (iii) the boundary between soil and highly weathered rock can be hard to define and the design equations for soil will produce different side and base resistance values than the design equations for rock.

Load testing of drilled shafts provides a means to verify design assumptions and/or to measure ultimate values of side and base resistance. The Wyoming DOT conducted a drilled shaft load test for this purpose at the Burma Road Overpass site near Gillette, WY, in September of 2009. This load test provided an opportunity to the Principal Investigator and WYDOT to research the behavior of drilled shafts in rock in order to improve the reliability and cost-effectiveness of WYDOT foundation design methods. Evaluation of the load test with the objective of improve design is the topic of this report.

1.2 Objectives

The objectives of this project are to use the load test results at Burma Road Overpass to evaluate design equations for side and base resistance in a weakly-cemented sandstone and to apply a model that predicts the axial load-settlement behavior of drilled shafts in rock. These research activities maximize the benefits of conducting the load test. Comparison of measured side and base resistances against design equations given by AASHTO and FHWA enable WYDOT engineers and geologists to determine their applicability to the subsurface conditions at the Burma Road Overpass and to sites with similar geology on future projects. Modeling the load-displacement response of the test shaft enables direct evaluation of AASHTO service limit states for the overpass project. The model can now be used by WYDOT engineers on future projects that require predictions of axial load-settlement response of drilled shafts in rock. The principal benefits to WYDOT are increased confidence in design methods for drilled shafts, the introduction of a new analytical tool for predicting foundation deformations used in service limit state evaluations, and more cost-effective foundation designs.

1.3 Design Considerations for Rock Sockets

Current AASHTO design specifications (AASHTO 2007) require that both superstructure and substructure elements, including foundations, be designed in the format of LRFD (Load and Resistance Factor Design). The basic design criterion that must be satisfied for all applicable limit states can be stated as:

the summation of factored force effects may not exceed the summation of factored resistances.

In equation form:

$$\sum \eta_i \gamma_i Q_i \le \sum \varphi_i R_i \tag{1}$$

where:

η_{i}	=	a load modifier to account for ductility, redundancy, and
		operational importance of the bridge or other structure
γ_i	=	load factor; a multiplier applied to force effects
Q_i	=	force effect
ϕ_i	=	resistance factor for resistance component i
$\mathbf{R}_{\mathbf{i}}$	=	nominal value of resistance component i

The left side of the inequality given by Equation 1 represents the summation of factored force effects while the right side represents the summation of factored resistances. A force effect is defined as an axial load, shear, or moment caused by loads acting on the structure. AASHTO specifies the load combinations under which the bridge must be analyzed, for each limit state.

When applied to a drilled shaft under axial force effects, the resistance (right-hand side of Eq. 1) consists of several components, including side resistance (uplift or compression) and base resistance (compression only). To illustrate, consider the case of a rock-socketed drilled shaft of length L and diameter B under a compressive force Q_c as shown in Figure 1 (a). The compressive force is transferred to the ground through (a) shearing stress that develops at the concrete-rock interface along the sides of the shaft and (b) the bearing stress that develops between the tip of the shaft and the underlying rock. The resultants of these two components of resistance are shown in the figure as: (1) side resistance R_s and (2) base resistance R_b .

The load transfer response can be illustrated by considering a generalized axial load versus displacement curve as shown in Figure 1 (b). Upon initial loading, shearing stress develops along the vertical shaft-rock interface. For relatively small load, displacement is small and the stress-strain behavior at the shaft-rock interface is linear (line OA). There is no relative displacement ("slip") between the concrete shaft and surrounding rock and the system may be modeled as being linearly elastic. With increasing load, the shear strength along some portion of the shaft sidewall is exceeded, initiating rupture of the "bond" and relative slip at the shaft-rock interface. The load-displacement curve





Figure 1. Drilled shaft in rock under axial compression

becomes nonlinear as rupture and slip progress and a greater proportion of the applied load is transferred to the base (line AB). At some point, the full side resistance is mobilized, there is slip along the entire surface ("full slip" condition), and a greater proportion of the applied load is transferred to the shaft base (beyond point B in Figure 1 b). If loading is continued to a displacement sufficient to cause failure of the rock mass beneath the base, a peak compressive load may be reached. In practice, design of drilled shafts in rock requires consideration of (1) geotechnical and structural capacity (strength limit states) and (2) deformation limits (service limit states). Geotechnical capacity in compression is evaluated in terms of limiting values of side and base resistances.

Load transfer in uplift involves the same mechanisms of side resistance mobilization as described above for compression. The uplift force Q_u is resisted by the weight of the shaft (W) and the side resistance (R_s), both of which act downward. Base resistance is assumed to be zero.

1.3.1 Evaluation of Strength Limit States

Considering the two components of resistance for axial compression loading (side and base), the summation of factored resistances (right side of Equation 1) for evaluation of LRFD strength limit states is given by:

$$\sum \phi_{i} R_{i} = \sum_{i=1}^{n} \phi_{S,i} R_{SN,i} + \phi_{B} R_{BN}$$
(2)

where $R_{SN,i}$ = nominal side resistance for layer *i*, $\varphi_{S,i}$ = resistance factor for side resistance in layer *i*, *n* = number of layers providing side resistance, R_{BN} = nominal base resistance, and φ_B = resistance factor for base resistance.

The total nominal side resistance for a specific geomaterial layer is the product of the nominal unit side resistance (f_{SN}) and the cylindrical surface area over which side resistance develops, expressed as the product of the layer thickness (Δz_i) and the shaft circumference, or:

$$\mathbf{R}_{\rm SN} = \pi \mathbf{B} \Delta z_{\rm i} f_{\rm SN} \tag{3}$$

where B = shaft diameter, Δz_i = thickness of layer *i*, and f_{SN} = nominal unit side resistance. Nominal unit side resistance for shafts in rock may be evaluated on the basis of mean uniaxial compressive strength of the rock, as follows:

$$\frac{f_{SN}}{p_a} = C \sqrt{\frac{q_u}{p_a}} \tag{4}$$

in which q_u = mean value of uniaxial compressive strength for the rock layer, p_a = atmospheric pressure in the same units as q_u , and C = a regression coefficient used to analyze load test results. Studies relating side resistance to rock compressive strength include those of Horvath and Kenney (1979), Rowe and Armitage (1987), Kulhawy and Phoon (1993), and others. The most recent regression analysis of available load test data is reported by Kulhawy et al. (2005) and demonstrates that the mean value of the coefficient *C* is approximately equal to 1.0. The authors recommend the use of Equation 4 with C = 1.0 for design of "normal" rock sockets. A lower bound value of C = .63 was shown to encompass 90% of the load test results. For design, the value of q_u used in Equation 4 should not exceed the compressive strength of the drilled shaft concrete, unless load testing is conducted and the results verify that a higher value of side resistance can be achieved.

The term "normal" as used above applies to sockets constructed with conventional equipment and resulting in nominally clean sidewalls without resorting to special procedures or artificial roughening. Rocks that may be prone to smearing or rapid deterioration upon exposure to atmospheric conditions, water, or slurry, are outside the "normal" range and may require additional measures to insure reliable side resistance. Rocks exhibiting this type of behavior include clay shales and other argillaceous rocks. Rock that cannot support construction of an unsupported socket without caving is also outside the "normal" and will likely exhibit lower side resistance than given by Equation 4 with C = 1.0.

The expression for unit side resistance in rock as given in the FHWA Drilled Shaft Manual (O'Neill and Reese 1999) and adopted in the AASHTO (2007) LRFD specifications has the same form as Equation 4 but with a recommended value of the coefficient C = 0.65. This is referred to as the "Horvath and Kenney" method based on their 1979 paper. O'Neill and Reese (1999) also applied an empirical reduction factor α_E to account for the degree of fracturing. The resulting expression is:

$$\frac{f_{SN}}{p_a} = 0.65\varphi \sqrt{\frac{q_u}{p_a}} \tag{5}$$

where the coefficient φ is estimated from the RQD of the rock. The relationships between RQD and φ are given in Table 1.

Considering the more recent research on side resistance in rock, in particular the work cited above by Kulhawy et al. (2005) that incorporates the original data of Horvath and Kenney (1979) plus additional data compiled over the ensuing 25+ years, Equation 4 with C = 1.0 is recommended for routine design of rock sockets. For rock that cannot be drilled without some type of artificial support, such as casing or by grouting ahead of the excavation, the reduction factors given in Table 1 are recommended for application to the resistance calculated by Equation 4. Additional research is needed to establish reliability-based resistance factors for use with this approach.

Nominal base resistance is the product of the nominal unit base resistance (q_{BN}) and the cross-sectional area of bearing at the shaft base (A_{base}) , or:

$$R_{\rm BN} = \frac{\pi B^2}{4} q_{\rm BN} \tag{6}$$

Base resistance in rock is complex because of the wide range of possible rock mass conditions. Various failure modes are possible depending upon whether rock mass strength is governed by intact rock, fractured rock mass, or structurally controlled by

	Joint Modification Factor, φ						
RQD (%)	Closed joints	Open or gouge-filled joints					
100	1.00	0.85					
70	0.85	0.55					
50	0.60	0.55					
30	0.50	0.50					
20	0.45	0.45					

Table 1. Side Resistance Reduction Factor for Rock

shearing along dominant discontinuity surfaces. In practice, it is common to have information on the uniaxial compressive strength of intact rock (q_u) and the general condition of rock at the base of a shaft. Empirical relationships between nominal unit base resistance (q_{BN}) and rock compressive strength can be expressed in the form:

$$q_{BN} = N_{cr}^* q_u$$
⁽⁷⁾

where N_{cr}^{*} is an empirical base resistance factor for rock. Studies relating q_{BN} to q_u are reported by Zhang and Einstein (1998) and Prakoso and Kulhawy (2002). There is overlap in the data used in each study although the authors used different interpretations of load test results to establish q_{BN} . Prakoso and Kulhawy used a consistent definition of ultimate base resistance and limited the data to tests that exhibited failure. Results of the Prakoso and Kulhawy study are shown in Figure 2 in which the base resistance factor is plotted against shaft diameter. The data base included 14 load tests at 9 sites in several rock types, mainly fine-grained sedimentary rocks. The mean value of N_{cr}^{*} is 3.38 with a coefficient of variation COV = 35.4%. A lower bound value of N_{cr}^{*} = 2.5 incorporates most of the points shown in Figure 2 and is consistent with work by Rowe and Armitage (1987) in which a value of N_{cr}^{*} = 2.5 is recommended for competent rock. Considering these three studies, a value of N_{cr}^{*} = 2.5 is recommended for design when q_u is the sole parameter for establishing q_{BN} and the following conditions are met:

- 1. The shaft base is bearing on rock which is either massive or tightly jointed (no compressible seams or joints) to a depth of at least one diameter beneath the base.
- 2. No solution cavities or voids exist beneath the base, and.
- 3. A clean base can be achieved and verified using conventional clean-out equipment. Equation 7 with $N_{cr}^* = 2.5$ is recommended in AASHTO (2007). Values of N_{cr}^* greater than 2.5, which clearly are possible based on Figure 2, are justified when they can be verified by local experience or load testing.



Figure 2. Base resistance factor for rock (Prakoso and Kulhawy 2002)

1.3.2 Side Resistance in Cohesionless Soils

The site of the drilled shaft load test that is the subject of this report is underlain by sandstone which is described as being weathered and poorly-cemented. Over most of the depth corresponding to the test shaft, Drivepoint Penetration and Standard Penetration Tests (SPT) were conducted. Results of SPT tests, given in terms of N-values, are typically used to evaluate resistances in cohesionless soils such as sands and gravels. The availability of SPT data at Burma Road Overpass makes it possible to compare the load test results to design equations for side resistance based on field N-values. The applicable design equations are presented below and are evaluated against the load test results in Chapter 3.

The nominal side resistance of a drilled shaft in cohesionless soil can be expressed as the frictional resistance that develops over a cylindrical shear surface defined by the soil-shaft interface. As illustrated in Figure 3, the unit side resistance is directly proportional to the normal stress acting on the interface. Nominal side resistance is then given by:

$$\mathbf{R}_{\rm SN} = \pi \mathbf{B} \Delta \mathbf{z} f_{\rm SN} = \pi \mathbf{B} \Delta \mathbf{z} \left(\boldsymbol{\sigma}_{\nu}^{\prime} \, \mathbf{K} \, \mathrm{tan} \delta \right) \tag{8}$$

in which R_{SN} = nominal side resistance, B = shaft diameter, Δz = thickness of the soil layer over which resistance is calculated, σ'_v = average vertical effective stress over the depth interval $\Delta z_{,}$ K = coefficient of horizontal soil stress (K = σ'_h / σ'_v), σ'_h = horizontal effective stress, and δ = effective stress angle of friction for the soil-shaft interface. For convenience, the following terms may be combined:



Figure 3. Frictional model of side resistance, drilled shaft in cohesionless soil

$$\beta = K \tan \delta \tag{9}$$

and

$$f_{\rm SN} = \sigma'_{\rm v} \beta \tag{10}$$

in which β = side resistance coefficient (hence the name 'beta method') and f_{SN} = nominal unit side resistance. Several design models have been proposed for evaluating the β term in Equation 13-7. The approach currently recommended in AASHTO (2007) is the "O'Neill and Reese (1999)" method, in reference to equations presented in the 1999 version of the FHWA Drilled Shaft Manual. In this approach, β is calculated solely as a function of depth below the ground surface, without explicit consideration of soil strength or the in-situ state of stress. A more rational approach, as presented for example by Chen and Kulhawy (2002), is to evaluate separately values of K and δ which are then combined to determine β . This approach is applicable to all cohesionless soils, including those identified previously as cohesionless intermediate geomaterials.

The resulting expression for β is as follows:

$$\beta \approx \left(1 - \sin\phi'\right) \left(\frac{\sigma'_p}{\sigma'_v}\right)^{\sin\phi'} \tan\phi' \tag{11}$$

where $\phi' = \text{soil friction angle}$, $\sigma'_p = \text{effective vertical preconsolidation stress}$, and $\sigma'_v = \text{effective vertical in-situ stress}$. The value of soil friction angle (ϕ') can be determined through correlation to SPT N-values as follows:

$$\phi' = 27.5 + 9.2 \log[(N_1)_{60}]$$
(12)

in which $(N_1)_{60}$ = N-value corrected for effective overburden stress and corresponding to 60 percent energy efficiency of the hammer. A practical estimate for preconsolidation stress can be made using the following correlation suggested by Mayne (2007):

$$\frac{\sigma_p'}{p_a} \approx 0.47 \left(N_{60}\right)^m \tag{13}$$

where m = 0.6 for clean quartzitic sands and m = 0.8 for silty sands to sandy silts, and N₆₀ is the field N-value (not corrected for overburden stress).

For each cohesionless soil layer, the value of β evaluated by Equation 13-15 is substituted into Equation 13-7 for determination of unit side resistance and this value is substituted into Equation 13-5 for determination of nominal side resistance R_{SN}. This model accounts for site-specific variations in horizontal stress and soil strength in a rational manner.

The method described above, commonly referred to as the beta-method, is generally applicable to non-cemented cohesionless soils. The sandstone at Burma Road Overpass is weakly cemented; however, the fact that Standard Penetration Testing was possible suggests that it may behave more like soil than rock for engineering purposes.

1.3.3 Evaluation of Service Limit States

An approximate method given by Kulhawy and Carter (1992) provides simple closedform expressions that compare reasonably well to more sophisticated nonlinear finite element analyses. The basic problem is depicted in Figure 4a and involves predicting the relationship between an axial compression load (Q_c) applied to the top of a socketed shaft and the resulting axial displacement at the top of the socket (w_c). The concrete shaft is modeled as an elastic cylindrical inclusion embedded within an elastic rock mass. The cylinder of depth L and diameter B has Young's modulus E_c and Poisson's ratio v_c . The rock mass surrounding the cylinder is homogeneous with Young's modulus E_r and Poisson's ratio v_r while the rock mass beneath the base of the shaft has Young's modulus E_b and Poisson's ratio v_b . The solution (Figure 4b) approximates the actual nonlinear load-deformation response of an axially loaded rock socket (see Fig. 1b) as consisting of two linear segments: (1) the initial linear elastic response and (2) the full slip condition. The maximum load is limited to the nominal axial resistance.



Figure 4. Simplified Model of Axial Load-Deformation Behavior, Drilled Shaft in Rock

The complete analytical solution for modeling the load-displacement curve as described above is presented in Appendix A. The equations have been implemented into a spreadsheet by the author and the spreadsheet has been provided to WYDOT as part of the technology transfer component of this research.

The above method is best applied in conjunction with load testing of rock sockets. The analytical solution can be fit to the measured axial load displacement curve from the load test providing a means to back-calculate the rock mass strength and stiffness properties. Where borings verify that the rock mass has similar characteristics, the analysis can then be used to evaluate load-deformation behavior of trial designs. In Chapter 3, this type of analysis is presented to illustrate the evaluation of Service Limit State I for the bridge at Burma Road Overpass.

CHAPTER 2: LOAD TEST AT BURMA ROAD OVERPASS

A proposed new bridge crossing I-90 near Gillette, WY, required drilled shafts in weathered sandstone to resist uplift forces at the abutments. The uncertainty associated with strength properties of the sandstone and uplift resistance of the foundations led the Wyoming DOT to conduct a field load test on a full-size drilled shaft at the site of the bridge. This chapter provides an overview of the key features of the bridge followed by a description of the site conditions and the drilled shaft load test.

2.1 Bridge and Structural Considerations

The bridge was designed for a new overpass crossing Interstate 90 and connecting an existing road (Burma Road) to a proposed extension to the south. An elevation view is shown in Figure 5. The overall length of the structure is 280 ft and includes three spans. The superstructure consists of continuous composite plate girders. The interior span, which is 190 ft in length, is supported by two four-column bents. Each column is supported on a single spread footing (eight footings total). Each abutment is supported by eight deep foundations, consisting of 36-inch diameter drilled shafts with embedded H-piles. The H-piles extend above the drilled shafts and are connected to a pile cap at the abutments.

Structural modeling of the bridge was used to establish axial force effects acting on the deep foundations. The AASHTO limit states considered by the structural designer included Service I, Strength I, and Strength IV. For each limit state, the bridge was analyzed under several different load combinations. The load combinations and resulting axial forces acting on each of the eight foundations supporting the abutment are presented in Table 2. Positive values indicate compression while negative values indicate tension (uplift). The maximum axial forces on a single foundation are highlighted in Table 2.



Figure 5. Elevation view of bridge at Burma Road Overpass (WYDOT 2008)

For foundation design, the following forces will govern:

- Service I: Factored axial compression = 86.1 kips (Piles 1 and 8, Load Case 2) Factored axial uplift = 84.8 kips (Piles 1 through 8, Load Case 3)
- Strength I: Factored axial compression = 61.2 kips (Piles 1 and 8, Load Case 4) Factored axial uplift = 162.5 kips (Piles 2 and 7, Load Case 3)

Axial force effects for the Strength IV limit state are less than those listed above for Strength I, and therefore do not require further consideration (*i.e.*, Strength I governs the foundation design). In Chapter 3, the axial forces given above are used to illustrate the application of LRFD design methods to the foundations for the bridge at Burma Road Overpass.

Load	Description Items in brackets [] indicate uplift											
1	Cap Weight											
2	Cap Weight + Wingwalls + Diaphragm + [Girder Weight + Cross-Frames + Stay-in-Place Forms]											
3	[deck + curbs + traffic rail + pedestrian safety fence + drain system]											
4	[future wearing surface]											
5	[live load]											
6	live load											
Service I Lir	nit State:	Axial	Force Effect	s (kips)								
Load	Pile 1	Pile 2	Pile 3	Pile 4	Pile 5	Pile 6	Pile 7	Pile 8	Σ			
1	40.122	28.002	36.513	34.385	34.385	36.513	28.002	40.122	278.044			
2	86.133	38.907	62.957	57.071	57.071	62.957	38.907	86.133	490.136			
3	-84.779	-84.779	-84.779	-84.779	-84.779	-84.779	-84.779	-84.779	-678.232			
4	-7.988	-7.988	-7.988	-7.988	-7.988	-7.988	-7.988	-7.988	-63.904			
5	-53.252	-53.252	-53.252	-53.252	-53.252	-53.252	-53.252	-53.252	-426.016			
6	37.216	37.216	37.216	37.216	37.216	37.216	37.216	37.216	297.728			
2+3+4	-6.634	-53.860	-29.810	-35.695	-35.695	-29.810	-53.860	-6.634	-251.998			
Strength Lin	nit States: Lo	oad Combina	ations and L	oad Factors								
Load Case	Description			Limit State		γdc	γdw	γ _{LL+IM}				
1	Load 1			Strength IV		1.50						
2	Load 2 + Loa	d 3 + Load 4		Strength IV		1.50	1.50					
3	Load 2 + Loa	d 3 + Load 4	+ Load 5	Strength I		1.25	1.50	1.75				
4	Load 2 + Loa	d 3 + Load 4	+ Load 6	Strength I		0.90	0.65	1.75				
Service Lim	Limit States I and IV: Axial Force			Effects (kips)								
Load Case	Pile 1	Pile 2	Pile 3	Pile 4	Pile 5	Pile 6	Pile 7	Pile 8	Σ			
1	60.183	42.002	54.769	51.578	51.578	54.769	42.002	60.183	417.064			
2	-9.951	-80.789	-44.715	-53.543	-53.543	-44.715	-80.789	-9.951	-377.996			
3	-103.480	-162.512	-132.450	-139.807	-139.807	-132.450	-162.512	-103.480	-1076.498			
4	61.154	18.651	40.295	34.999	34.999	40.295	18.651	61.154	310.198			

Table 2. Results of Structural Modeling: Foundation Force Effects(Data from B. Rentner, WYDOT Bridge)

A notable outcome of the structural analysis is that uplift force effects are the dominant design consideration for the abutment foundations. Design of drilled shafts founded in rock under uplift means that a single component of resistance, side resistance, must be relied upon, in contrast to compression for which both side and base resistances are mobilized. This reliance on side resistance makes it important for the designer to have reliable estimates of unit side resistance for the rock. This was the primary consideration that led WYDOT Bridge and Geology personnel to consider conducting a foundation load test for this project.

2.2 Site Conditions

Subsurface conditions are described in an internal WYDOT memo from R. Johnson, Engineering Geologist (WYDOT 2008), referred to herein as "Foundation Memo". Bedrock in the area is Tertiary Wasatch Formation, described as "drab sandstone and drab to variegated claystone" (Love and Christiansen 1985). Based on four borings made at the site the subsurface consists of "up to 67 ft of very dense, poorly cemented slightly moist sandstone to very dense, poorly cemented silty sandstone". Occasional blue-gray clay lenses were encountered, ranging in thickness from 0.5 to 1 foot. All of the gomaterials are believed to be derived from weathering of the Wasatch Formation. Unweathered bedrock was not observed in any of the borings.

Figure 6 shows a portion of the boring log sheet showing subsurface profiles at two borings located on the north side of the bridge. The north abutment of the bridge is approximately mid-way between the two borings. The boring on the left, at Station 19+10, is believed to be most representative of the load test location. Information shown on the log includes drivepoint penetration values (in blows per foot) from the surface to elevation 4,646 ft (borehole depth = 17 ft). The drivepoint test involved a 140-lb hammer with a 30-inch drop height acting on a 2-inch diameter conical penetrometer. At depth = 17 ft, the blows per foot exceeded 300 at which point driving was terminated. There is no reliable correlation between the strength of sandstone and the drivepoint resistance. However, refusal can be indicative of stronger, less weathered rock, while the material above this depth is indicative of cemented soil-like material. Below this depth the Standard Penetration Test (SPT) was conducted and the values shown represent the number of blows per foot (N), or, if the number of blows exceeds 100, the distance of penetration. For example, 100/10" represents 100 blows over a penetration of 10 inches. Achieving 100 blows in less than 1 ft of penetration is considered refusal. The values shown range from N = 85 to refusal, which is indicative of weak rock or strongly cemented soil.

Beginning at elevation 4,220 ft (borehole depth = 43 ft) rock coring was initiated. On the boring log, numbers below this depth indicate core samples and percent recovery. As can be observed, rock core runs numbered 4 through 10 show percent recovery ranging from zero (no recovery) to 50% with a mean value of 20%. Rock Quality Designations (RQD), for the core runs with sufficient recovery, range from zero to 10%. Taken at face value, these low values of recovery and RQD are considered indicative of 'very poor'



Figure 6. Boring logs along the northern alignment of Burma Road Overpass (WYDOT 2008)

rock mass. Alternatively, this may suggest that the weathered sandstone is highly prone to disturbance caused by the coring operation and that percent recovery and RQD are not meaningful parameters for assessing the in-situ behavior of these materials for foundation design. As noted in the next section, excavation for drilled shaft construction produced a competent borehole with no observed caving or other signs of instability.

Very few of the samples obtained using the split spoon sampler with the Standard Penetration Test or from rock coring were adequate for performing laboratory strength tests. In Boring 19+10 a single value of undrained shear strength is reported for core run No. 8., corresponding to borehole depth interval = 63 to 68 ft. The undrained shear strength $c_u = 7.2$ kips/ft². In the borehole at Station 19+85 two samples of rock were tested in uniaxial compression, corresponding to core runs No. 22 and No. 23. From the boring log it can be seen that core run No. 22 is located in weathered poorly cemented sandstone and this sample yielded $q_u = 5.5 \text{ kips/ft}^2$. Core run No. 23 is shown as corresponding to gray, sandy clay shale and yielded $q_u = 17.1$ kips/ft². Several points are noted regarding the available strength values. First, the number of measurements is small and does not lend itself to statistical evaluation by parameters such as mean and standard Second, the reported values vary over a wide range and correspond to deviation. different materials (sandstone versus clay shale) making it difficult to select design values of strength applicable to evaluation of side resistance over the full length of a drilled shaft. Third, the low recovery rates observed in most of the core runs raise the question of sample disturbance. Combined with the low number of intact test specimens, it is difficult to assess the degree to which sample disturbance may have affected the measured strengths.

The values of uniaxial compressive strength, 5.5 ksf and 17.1 ksf, fall in a range that straddles the boundary between soil and rock. Compressive strength of $q_u = 5.5$ ksf falls in a range that corresponds to 'very stiff' when applied to cohesive soils, while $q_u = 17.1$ corresponds to 'very weak' rock. Since sandstone is the predominant material providing side and base resistance of the drilled shaft at the test site, it could be argued that design methods based on treating the weathered sandstone as soil may be most appropriate. This issue is considered further in Chapter 3.

In summary, the subsurface investigation provides useful information on the site stratigraphy and overall conditions (weakly cemented sandstone with interbedded shale layers), but somewhat ambiguous information that can be used for selection of strength parameters of the subsurface materials for foundation design. Data on the uniaxial compressive strength of the sandstone is limited to a single value corresponding to a sample depth that is below the base of the test shaft. This topic is considered further in Chapter 3 of this report. This uncertainty in the selection of appropriate strength values was an additional factor supporting the decision to conduct a foundation load test.

2.3 Test Shaft Installation

A single drilled shaft was constructed for the purpose of conducting a field load test. The objective of the test was to make direct measurements of side and base resistances considered to be representative of those expected in the drilled shafts supporting the abutments of the bridge at Burma Road Overpass.

The load test was conducted using the Osterberg load cell (commonly referred to as the O-cell test). This method involves bi-directional loading of a drilled shaft. Force is applied to the shaft by means of an embedded hydraulic jacking system. The expendable jack is sandwiched between steel plates and cast within the test shaft. The portion of the shaft above the O-cell provides a reaction for loading against the portion below the O-cell and vice versa, thus eliminating the need for a separate structural reaction system. A schematic diagram of the O-cell loading system is shown in Figure 7. The O-cell loading system is provided in the U.S. exclusively by Loadtest, Inc.

After a shaft has been cast and the concrete has been allowed to gain sufficient strength for testing, the O-cell is pressurized to break the tack weld holding the cell together and to "crack" the shaft into an upper and a lower portion. Pressure is then applied incrementally to load the upper and lower shaft sections. During the test, upward and downward movements of each section of the shaft are also measured and recorded, enabling the calculation of a load-displacement curve. Strain gages attached to 'sister bars', or sections of rebar embedded in the shaft, make it possible to calculate the axial force at the strain gage locations, thus providing numerical values of load transfer and average side resistance over portions of the shaft between strain gage elevations.



Figure 7. Bi-Directional (O-cell) testing schematic (courtesy LoadTest, Inc.)

The maximum test load is limited to the maximum axial resistance of the shaft above or below the cell or the maximum capacity of the cell, whichever is smaller. It is therefore important that the O-cell be located at or near a point in the shaft where the axial resistance above and below the cell are approximately equal. If the side resistance exceeds the base resistance, the O-cell should be located such that the combined base and side resistances of the lower section are approximately equal to the side resistance of the upper section. If the objective of the test is focused on one component of resistance (side or base) the O-cell should be located to insure that component of resistance will be mobilized fully. For the test at Burma Road Overpass, the primary objective was to measure side resistance, since this controls uplift capacity; however it was also desirable to mobilize as much base resistance as possible while still assuring the shaft would fail in shear.

Construction of the test shaft, including installation of the O-cell, was carried out on August 18, 2009. Shaft excavation was made using a 36-inch diameter, four-flight rock auger as shown in Figure 8. The auger was equipped with drag-bit teeth at the cutting

end, which is a highly efficient method for excavating soft to medium strength sedimentary rock such as sandstone and shale. The resulting borehole was stable with no observed caving or other problems that would require temporary support by casing the hole. Figure 9 is a photo of the borehole showing the excavation with rough sidewall surfaces, ideal conditions for developing side resistance in rock. This favorable condition would not be predicted by the parameters obtained from core drilling, which yielded low recovery and low RQD values, as noted in Section 2.2 above.



Figure 8. Drilling operation for installation of the test shaft (Photo by S. Cooney)



Figure 9. Photo of the drilled shaft borehole prior to concrete placement (Photo by S. Cooney)

The reinforcing cage was fabricated on site and the O-cell was attached to the bottom of the cage by personnel from Loadtest, Inc. and the general contractor. Figure 10 shows the rebar cage with the O-cell attached to its base as it was being transported to the borehole. The holes in the upper and lower plates of the O-cell apparatus are intended to allow fluid concrete to flow around the O-cell. The steel plates are 2 inches thick. The rebar cage consists of eleven No. 9 longitudinal bars with No. 3 spirals on a 4-inch pitch. The base of the O-cell is 7 ft above the base of the shaft. This location was chosen on the basis of preliminary estimates of side and base resistance to assure the shaft would fail by reaching the limiting side resistance of the section above the O-cell while still mobilizing significant base resistance in the portion below the O-cell.

The top elevation of the test shaft is 4,661 feet. Strain gages were placed on sister bars at two locations along the rebar cage. One is at a depth of 22 feet (S.G. Level 1) and the other is at a depth of 12 feet (S.G. Level 2). The bottom of the O-cell is at a depth of 34 feet and the tip of the shaft is at a depth of 41 feet (elevation = 4,620 feet).

When the borehole was excavated to the target depth of 41 feet, fluid concrete was placed into the bottom 7 feet of the shaft. The reinforcing cage and O-cell apparatus were then lowered into the excavation while suspended from a crane. Figure 11 shows the suspended cage while concrete was being placed by pump truck into the lower portion of the shaft. Once the cage was in place concrete was placed by tremie up to the ground surface to complete the test shaft.



Figure 10. Test shaft reinforcing cage with attached O-cell (Photo by S. Cooney)



Figure 11. Concrete placement in the bottom of the shaft prior to placement of the reinforcing cage (Photo by S. Cooney)

2.4 Load Test and Results

The load test was conducted on September 2, 2009, by personnel from Loadtest, Inc. WYDOT Geology and Bridge personnel were present to observe the test, as was the author. Test results are presented in a report provided by Loadtest, Inc. (Loadtest, Inc. 2009). The maximum bi-directional sustained force applied to the test shaft was 1,457 kips and corresponded to the maximum resistance provided by the upper section of the shaft, as anticipated. At this load, the downward movement of the O-cell base was 0.74 inches and the upward displacement was 2.18 inches. The calculated unit side resistance averaged over the upper section of the shaft (from the O-cell to the ground surface) is 4.4 kips/ft². At the maximum load, the mobilized base resistance is estimated to be 171 kips/ft².

Load displacement behavior of the shaft can be displayed in two ways. Figure 12 shows the O-cell load versus upward displacement of the upper portion of the shaft and load versus downward movement of the lower part of the shaft. These curves represent the actual measured behavior and are used to calculate mobilized side and base resistances. In this case, the peak side resistance of the upper section appears to have been reached. The resistance of the lower portion of the shaft has not been mobilized fully.



Figure 12. Load-displacement curve from O-cell test (Loadtest, Inc. 2009)

Second, by adding values of load at common values of displacement (upward and downward) it is possible to construct a "Equivalent Top Load versus Settlement Curve" from the O-cell test results. This curve, shown in Figure 13, represents an approximation of the load-settlement behavior of the test shaft subject to an axial compressive force applied at the top of the shaft. Two curves are shown, one using the actual values of displacement measured during the O-cell test and a second curve that accounts for the elastic compression of the concrete shaft expected to occur during top-down loading.

Strain gage measurements allow the average unit side resistance to be estimated over the depth intervals between strain gages and between the O-cell and S.G. Level 1. Figure 14 shows curves of mobilized unit shearing resistance (kips/ft²) versus upward movement of the shaft above the O-cell. Table 3 summarizes the maximum observed values of unit side resistance for the three depth intervals and the unit side resistance averaged over the upper portion of the shaft.

(
Depth Interval	Upward Displacement (inches)	Mobilized Unit Side Resistance (kips/ft ²						
O-cell to Ground Surface (average)	2.13	4.4						
S.G. Level 2 to Ground Surface	2.10	5.0						
S.G. Level 1 to S.G.Level 2	2.13	4.5						
O-cell to S.G. Level 1	2.16	3.8						

Table 3. Summary of Mobilized Unit Side Resistances (Data from Loadtest, Inc. 2009)



Figure 13. Equivalent top load versus settlement curve, Burma Road Overpass (Loadtest, Inc. 2009)



Figure 14. Mobilized unit side resistance versus displacement curves (Loadtest, Inc. 2009)

CHAPTER 3: APPLICATION TO ROCK SOCKET DESIGN

3.1 Evaluation of Drilled Shaft Resistances

In Chapter 1 design equations were presented for calculating nominal values of side and base resistance for drilled shafts in rock. In each case, the equations depend on measured values of uniaxial compressive strength of intact core specimens. It was noted in Chapter 2 that a very limited number of intact specimens were available for uniaxial compression testing. Despite this limitation, the load test results provide an opportunity to compare measured values of resistance to resistances calculated by the design equations.

3.1.1 Side Resistance

Nominal unit side resistance for shafts in rock is evaluated by the following expression (Equation 4 in Chapter 1):

$$\frac{f_{SN}}{p_a} = C_v \sqrt{\frac{q_u}{p_a}} \tag{4}$$

in which q_u = mean value of uniaxial compressive strength for the rock layer, p_a = atmospheric pressure in the same units as q_u (e.g. 2.116 ksf), and C = a regression coefficient used to analyze load test results. It was noted in Chapter 1 that the mean value of the coefficient C is approximately equal to 1.0 for "normal" rock, defined as rock which can be excavated using conventional drilling tools while remaining stable. The excavation for the test shaft clearly fits this definition. In Chapter 2 it was noted that uniaxial compressive strength of the sandstone is limited to a single value measured on an intact specimen obtained by rock coring in Boring 19+85 over the elevation interval of 4,613 ft to 4,618 feet. The base of the test shaft is at elevation 4,620 feet. The uniaxial compressive strength of the specimen $q_u = 5.5$ ksf. Substituting this value into Equation 4 yields the following:

$$\frac{f_{SN}}{2.116} = 1.0\sqrt{\frac{5.5}{2.116}} = 1.612$$
(14)

$$f_{\rm SN} = 2.116 \, \text{ksf} \, (1.612) = 3.41 \, \text{ksf}$$
 (15)

All of the measured side resistance values for various intervals of the shaft, as presented in Table 3, exceed the side resistance predicted above in Equation 15. This very limited data suggests that side resistance calculated using Equation 4 provides a safe value of nominal side resistance for design. It is also noted that the calculated value of f_{SN} exceeds the value actually used to design the drilled shafts at Burma Road Overpass, which is 2 ksf, as recommended in the Foundation Memo (WYDOT 2008). Alternatively, a value of C = 1.29 would correctly predict the average measured unit side resistance (4.4 ksf).

For comparison, the average value of q_u given in the Foundation Memo, denoted as "Average Uniaxial Compressive Strength", $q_u = 11.3$ ksf, can be used with Equation 4 and C = 1. This calculation yields a design unit side resistance of 4.89 ksf, which is in close agreement with the measured values presented in Table 3. This 'average' value of q_u is based on two measured values (5.5 ksf and 17.1 ksf) which is not a statistically valid mean. This comparison, therefore, should be considered as an exercise and not a rigorous test of the design equation. The higher of the two strength values (17.1 ksf) was measured on a rock core specimen of shale, which is not the predominant rock type along the side of the test foundation.

The comparisons presented above between side resistance values measured in the load test and those predicted using current design equations suggest that Equation 4 with the recommended value of C = 1.0 provides a valid tool for designing drilled shafts in rock when it is possible to obtain specimens of rock core that are suitable for conducting uniaxial compression tests. The data that support this conclusion are quite limited, but nevertheless show good agreement with the load test results at Burma Road Overpass. An important caveat is that the shaft excavation at the test site was stable, fitting the definition of a 'normal' rock socket, despite the observation that core recovery and RQD values indicated a poor quality rock mass.

A alternative approach to evaluation of side resistance in geomaterials that exhibit characteristics of both soil and rock is to utilize measured N-values from the Standard Penetration Test (SPT). Both borings in the vicinity of the test shaft (Borings 19+10 and 19+85) include N-values to depths that cover the depth range of the test shaft. The equations used to compute values of unit side resistance from N-values are presented in Chapter 1 (see Equations 11 through 13, referred to as the beta-method). Values of unit side resistance f_{SN} calculated by these equations are tabulated in Table 4 below. All of the data points correspond to depths that are above the tip elevation of the test shaft. The mean value of side resistance from the six available data points is $f_{SN} = 4.6$ ksf. This value is remarkably close to the average measured unit side resistance over the shaft depth of 4.4 ksf. This exercise strongly suggests that N-values provide an alternative means to calculating design values of unit side resistance for weak rock in which Standard Penetration Testing is possible.

An important point to note is that the beta method, as applied above, was not developed for use with cemented sands. One reason for this limitation is the lack of useful data (load tests) on drilled shafts in cemented materials. However, at least for the conditions at Burma Road Overpass, the method appears to have merit in sandstone that is weathered to a degree that makes it possible to obtain N-values.

Boring	Sample No.	Elevation (ft)	Depth (ft)	σ _v ' (psf)	N-value	Beta	f _{sn} (psf)
19+10	1	4,644.0	19.0	2,280	85	2.02	4,597
19+10	2	4,634.0	29.0	3,480	100	1.63	5,677
19+85	12	4,647.0	4.0	480	71	6.06	2,909
19+85	14	4,642.0	9.0	1,080	92	3.81	4,116
19+85	16	4,637.0	14.0	1,680	100	2.81	4,726
19+85	19	4,628.0	23.0	2,760	100	1.94	5,635
						Mean:	4,610

Table 4. Unit Side Resistances from Field N-Values

3.1.2 Base Resistance

The mobilized unit base resistance during the O-cell test is estimated to be 171 kips per square foot (Loadtest Inc., 2009). From Figure 11 (Chapter 2) it can be observed that the load-deformation behavior of the section of drilled shaft below the O-cell is approximately linear up to the maximum load applied in the test. There is no sign of yielding or that a limiting value of base resistance was developed. For design of the production shafts a value of $q_{BN} = 40$ ksf was used, as recommended in the Foundation Memo. The mobilized value of $q_B = 171$ ksf can also be compared to values predicted by design equations.

In Chapter 1, the following equation was presented for calculating nominal base resistance of drilled shafts in competent rock:

$$q_{\rm BN} = N_{\rm cr}^* q_{\rm u} \tag{7}$$

in which q_{BN} = nominal unit base resistance, N_{cr}^* = a bearing capacity factor for rock and q_u = uniaxial compressive strength of intact rock over a depth interval of two shaft diameters below the base of the shaft. As shown in Figure 2 (Chapter 1) data from load tests to failure yield a mean value of N_{cr}^* = 3.38. A lower bound value of N_{cr}^* = 2.5 incorporates most of the points shown in Figure 2 and is recommended for design when it can be verified that the base of the shaft is free of loose debris and is underlain by competent rock. It was noted further that higher values of N_{cr}^* are clearly possible, but that they should be verified by load testing before being used in design.

Values of uniaxial compressive strength are limited to the two values noted previously: $q_u = 5.5$ ksf for a single specimen of sandstone and $q_u = 17.1$ ksf for a single specimen of shale. Using Equation 7 with $N_{cr}^* = 2.5$, this yields nominal bases resistance values of 13.8 ksf and 42.8 ksf, respectively. Regardless of which value is used, the mobilized unit base resistance of 171 ksf exceeds the computed nominal values by a substantial margin. The measured resistance is a lower-bound value because the full base resistance was not reached. In fact, the value of N_{cr}^* that would correspond to the mobilized base resistance is $N_{cr}^* = 31.0$ for $q_u = 5.5$ ksf and $N_{cr}^* = 10.0$ for $q_u = 17.1$ ksf. If the material beneath the base is treated as cohesionless soil, the design equation in the current FHWA Drilled Shaft manual is:

$$q_{BN} (tsf) = 0.60 (N_{60}) \le 30 tsf$$
 (16)

in which N_{60} is the field (uncorrected) N-value over a depth of two diameters below the base of the shaft. Equation 16 is limited to N-values less than 50 which corresponds to the upper limit of 30 tsf (60 ksf) for q_{BN} . All of the field N-values exceed 50, therefore the maximum nominal unit base resistance that could be justified using Equation 16 is $q_{BN} = 60$ ksf. This value exceeds those computed above by Equation 7, which are based on uniaxial compressive strength of the rock, but is still less than the mobilized base resistance mobilized during the load test by a factor of 2.9.

The overall conclusion is that base resistance of the test shaft exceeds any value that would be calculated using currently recommended design equations in AASHTO (2007) or as given in the current FHWA Drilled Shaft Manual (O'Neill and Reese 1999). One possible explanation is that the rock beneath the base of the test shaft might have much higher strength than indicated by the two available values of uniaxial compressive strength. Neither of the tested core samples was obtained at the exact location of the test shaft is unknown. A test boring at the exact location of a load test is a highly recommended practice for future load tests.

3.2 Load-Deformation Response

Current AASHTO LRFD design specifications require that bridges and other structures be designed for applicable service limit states. For bridge foundations, this requires analysis of vertical deformations under service loads. The general LRFD criterion (Equation 1 in Chapter 1) must be satisfied. For service limit states this means that the summation of factored force effects may not exceed the summation of factored resistances, where those resistances correspond to the tolerable deformation of the foundation.

The drilled shaft foundation tested at Burma Road Overpass has the same dimensions (depth and diameter) as the actual production shafts that will be used to support the bridge abutments. Therefore, the equivalent top load versus settlement curve, shown as Figure 13 in Chapter 2, can be used to evaluate expected settlement under various force effects. However, the curve is for compression only and cannot be used directly for estimating deformations under uplift, which is the critical loading condition for the Burma Road Overpass. Furthermore, one of the objectives of this research is to demonstrate how load test results can be used to develop a model of the load-deformation behavior of a rocket socket, which can then be used to evaluate trial designs with dimensions that are different than those of the test shaft.

The model presented in Appendix A, developed by Kulhawy and Carter (1992) provides a rational interpretation of load test results in which the load-deformation response is idealized as consisting of three distinct regions: linear elastic, full slip, and nominal total resistance, as illustrated in Figure 4 (Chapter 1). To model the results of a load test, the slopes of various portions of the measured load-settlement curve are used to calculate values of the rock mass strength and stiffness properties, as illustrated in Figure 15. The equations relating the curve parameters (consisting of slopes S_1 , S_2 , and S_3 and the intercept Q_i) to the strength and stiffness properties of the rock are as follows:

$$\mathbf{E}_{\mathrm{r}} = \left[\frac{(1+\nu_{\mathrm{r}})\zeta}{\pi \mathrm{L}}\right] (\mathbf{S}_{1} - \mathbf{S}_{3}) \tag{17}$$

$$E_{b} = \left[\frac{(1-\nu_{b}^{2})\zeta}{B}\right]S_{3}$$
(18)

$$\tan\phi \cdot \tan\psi = \left(\frac{1}{2\zeta}\right) \left(\frac{S_2 - S_3}{S_1 - S_2}\right) \tag{19}$$

$$c = (2\zeta \tan\phi \cdot \tan\psi + 1) \frac{Q_i}{\pi BL}$$
(20)

$$\zeta = \ln\left[5(1 - \nu_{\rm r})\frac{\rm L}{\rm B}\right] \tag{21}$$



Figure 15. Interpretation of a compression load test on a complete rock socket (Kulhawy and Carter 1992)

in which: E_r = average rock mass modulus over the length (L) of the shaft, E_b = rock mass modulus beneath the base of the shaft, c = cohesion of the rock-shaft interface, ϕ = interface friction angle, ψ = interface angle of dilation, and B = shaft diameter.

In Figure 16, the overall load-settlement curve and a tip load-settlement curve are shown for the load test at Burma Road Overpass. The following parameters were determined from the two curves:

$$S_1 = 6,900$$
 kips/inch $S_2 = 1,900$ kips/inch $S_3 = 1,650$ kips/inch $Q_i = 850$ kips

Substituting the above values into Equations 17 through 21, and making minor adjustments to obtain good agreement with the load test results in the following values;

 $E_r = 20 \text{ kips/inch}^2$ $E_b = 55 \text{ kips/inch}^2$ $c = 17 \text{ kips/inch}^2$ $\phi = 22 \text{ degrees}$ $\psi = 1 \text{ degree}$

The above values are then used as input to the model presented in Appendix A, which has been programmed into a spreadsheet by the author, to calculate and plot the modeled load displacement curve. The spreadsheet analysis is given in Appendix B and the resulting curve is shown in Figure 17 along with the actual measured load-displacement curve. The model shows a very good fit with the measured curve. Neither curve shows a total nominal resistance because the load test did not reach the nominal (ultimate) resistance.

Once a model such as that shown in Figure 17 has been developed, it can be used to evaluate trial designs with dimensions that differ from that of the test shaft, assuming the rock mass properties are approximately the same. For example the shaft diameter could be increased or decreased in order to evaluate the effect of diameter on load-settlement response.

The uplift load-displacement behavior can also be modeled using parameters backcalculated from the load test. The analysis utilizes the same values of modulus and strength along the sides of the shaft but does not involve any properties of the rock beneath the base of the shaft. The spreadsheet analysis is presented in Appendix B and the resulting curve is shown in Figure 18.



Figure 16. Complete and base load versus settlement curves from O-cell test



Figure 17. Measured (in red) and modeled load versus settlement curve for drilled shaft at Burma Road Overpass



Figure 18. Modeled uplift load-displacement curve

3.3 Application of Results to LRFD Design of Drilled Shafts

The load test results, including the measured and modeled load displacement curves, can be used to perform limit state checks for the drilled shaft design at Burma Road Overpass. For each applicable limit state, the basic LRFD inequality (Equation 1) must be satisfied; this constitutes a 'check'. The applicable limit states identified by the Bridge Engineer include Strength I, Strength IV, and Service I. Since the Strength I force effects are greater than the Strength IV force effects, checks are conducted for Strength I only. For each limit state, checks are conducted for both compression and uplift. Each case is described below.

Strength I

For the Strength I compression case, resistances will be the values reported by Loadtest, Inc. (2009). The net side resistance above the O-cell is reported to be 1,420 kips. The side resistance below the O-cell is estimated to be 246 kips. These values are added to obtain the nominal side resistance of 1,666 kips. The mobilized base resistance is estimated to be 1,211 kips. This value does not correspond to a nominal (ultimate) resistance; however it will be used in this analysis because it is the maximum value of base resistance that can be verified. The limit state check is conducted as follows:

Strength I Factored Force Effect (compression) = $\underline{61.2 \text{ kips}}$ (Piles 1 and 8, Load Case 4)

As noted above, the nominal side resistance $R_{SN} = 1,666$ kips and nominal base resistance $R_{BN} = 1,211$ kips. The resistance factor specified by AASHTO (2007) for all strength limit states in which the resistance is based on a load test is $\varphi = 0.7$. Applying Equation 1:

$$\sum \eta_i \gamma_i Q_i \le \sum \varphi_i R_i \tag{1}$$

$$61.2 \text{ kips} \le 0.70 (1,666) + 0.70 (1,211 \text{ kips})$$
(22)

61.2 kips < 2,013.9 kips
$$\sqrt{}$$
 (23)

The LRFD inequality is satisfied and the drilled shaft design therefore satisfies the Strength I Limit State criterion for compression (*i.e.*, checks).

For uplift:

Strength I Factored Force Effect (uplift) = $\underline{162.5 \text{ kips}}$ (Piles 2 and 7, Load Case 3)

The nominal side resistance in uplift $R_{SN} = 1,666$ kips and nominal base resistance in uplift $R_{BN} = 0$. The resistance factor specified by AASHTO (2007) for all strength limit states in which the resistance is based on a load test, for uplift is $\varphi = 0.6$. Applying Equation 1:

$$162.5 \text{ kips} \le 0.60 (1,666) + 0 \tag{24}$$

162.5 kips < 999.6 kips
$$\sqrt{}$$
 (25)

The LRFD inequality is satisfied and the drilled shaft design therefore satisfies the Strength I Limit State criterion for uplift ($\sqrt{}$).

Results of the Strength I limit state checks are summarized in Table 5

Table 5. Summary of Strength I Limit State Check, Drilled Shaft, B = 3 ft, L = 41 ft

	Σ Factored Axial Force Effect (kips)	Nominal Side Resistance, R _{SN} (kips)	Resistance Factor, φs	Factored Side Resistance (kips)	Nominal Base Resistance, R _{SN} (kips)	Resistance Factor, φ _B	Factored Base Resistance (kips)	Σ Factored Resistances (kips)	Σ Factored Force Effects ≤Σ Factored Resistances ?
Compression	61.2	1,666.0	0.70	1166.2	1,211.0	0.70	847.7	2013.9	V
Uplift	162.5	1,666.0	0.60	999.6	0	0	0	999.6	V

Service I

The bi-directional load test conducted at Burma Road Overpass was used to develop an equivalent top load versus displacement curve for axial compression, shown as Figure 13 in Chapter 2. Since the test shaft has the same dimensions as the production shafts, this

curve can be used directly to perform a service limit state check for compression, as follows. For illustrative purposes only, it will be assumed that the Bridge Engineer has established a tolerable settlement of $\frac{1}{2}$ inch for each drilled shaft foundation at the abutment, for both compression and uplift. From Table 2:

Service I: Factored axial compression = $\underline{86.1 \text{ kips}}$ (Piles 1 and 8, Load Case 2)

Entering Figure 13, the axial compressive resistance corresponding to $\frac{1}{2}$ inch settlement is approximately equal to 1,850 kips. The resistance factor specified for Service I Limit State analysis is $\varphi = 1.0$. Applying Equation 1:

$$\sum \eta_i \gamma_i Q_i \le \sum \phi_i R_i \tag{1}$$

$$86.1 \text{ kips} \le 1.0 (1,850 \text{ kips}) \tag{26}$$

86.1 kips < 1,850 kips
$$\sqrt{}$$
 (27)

The LRFD inequality is satisfied and the drilled shaft design therefore satisfies Service I Limit State criterion for compression ($\sqrt{}$).

In addition to the limit state check, it is useful to determine the expected settlement under the service force effect. From the compression load-settlement curve, the expected downward settlement under a force of 86.1 kips is approximately 0.014 inches.

For uplift loading, Figure 18 is used to determine that the axial resistance corresponding to $\frac{1}{2}$ inch of uplift displacement is approximately 1,060 kips. The limit state check is satisfied because the factored uplift force effect of 84.8 kips is well within the factored uplift resistance of 1,060 kips. Figure 18 can also be used to estimate the expected uplift displacement under the service force effect. For an uplift force of 84.8 kips the expected uplift displacement is approximately 0.016 inches, which is well within the tolerable deformation.

Results of the Service I limit state check are summarized in Table 6.

Table 6. Summary of Service I Limit State Check, Drilled Shaft, B = 3 ft, L = 41 ft

	Σ Factored Axial Force Effect (kips)	Tolerable Vertical Deformation (inches)	Nominal Resistance at Tolerable Deformation (kips)	Resistance Factor, φs	Σ Factored Resistances (kips)	Σ Factored Force Effects < Σ Factored Resistances ?	Expected Deformation Under Service I Force Effect
Compression	86.1	0.5	1,850.0	1.00	1,850.0	V	.01 inch
Uplift	84.8	0.5	1,060.0	1.00	0.0	V	.02 inch

CHAPTER 4: CONCLUSIONS AND RECOMMENDATIONS

4.1 Conclusions

A bi-directional load test on a single drilled shaft at Burma Road Overpass provided a unique opportunity to evaluate design methods for rock-socketed foundations used to support highway bridges in Wyoming. The test foundation was constructed in weakly-cemented weathered sandstone. The full side resistance of the section of drilled shaft above the O-cell was mobilized and measured. This enabled the author to compare the measured unit side resistance to nominal values predicted by design equations given in current AASHTO and FHWA design codes. While the test did not result in mobilization of the full base resistance, a very high value of base resistance was measured and this also provides a lower bound value that is compared to values given by current design equations.

The principal findings of this study are as follows.

- 1. Design equations based on N-values from the Standard Penetration Test provide nominal values of side resistance that are close to the measured average unit side resistance measured by the load test. The mean value of unit side resistance predicted using the 'beta-method' is $f_{SN} = 4.61$ kf. The average measured value of unit side resistance from the load test is $f_S = 4.4$ ksf. The equations upon which the nominal values are calculated involve several empirical relationships between N-values and soil properties. The method was developed for non-cemented sands and gravels, yet appears to provide a reasonable estimate of side resistance in the weakly-cemented sandstone encountered at the test site.
- 2. Evaluation of design equations for unit side resistance in rock was limited by the inability to obtain intact core samples suitable for measuring the uniaxial compressive strength of the sandstone. Only two values of uniaxial compressive strength (q_u) were obtained. Both specimens were taken from a boring that is not at the exact location of the test shaft and both were taken from an elevation that is lower than the base of the shaft. One of the core specimens was sandstone and yielded $q_u = 5.5$ ksf, while the second core specimen was shale and yielded $q_u = 17.1$ ksf. Nominal unit side resistance based on the strength of the single sandstone specimen yields $f_{SN} = 3.41$ kf. Nominal unit side resistance based on the 'average' strength of the two specimens (sandstone and shale) yields $f_{SN} = 4.89$ kf. While these nominal values fall within a range that agrees with the average measured unit side resistance (4.4 ksf) and with the range of values established for various depth intervals along the shaft (3.8 ksf to 5.0 ksf), it is not sufficient data upon which to base a strong conclusion.
- 3. All of the nominal side resistance values based on design equations are greater than the value used to design the drilled shafts (2 ksf) at Burma Road Overpass.

The load test was successful, therefore, in demonstrating that higher values of side resistance are justified than those currently being used by WYDOT for drilled shafts in weak rock.

- 4. Unit base resistance mobilized in the load test is estimated to be 171 ksf. This value exceeds by a significant amount the value of unit base resistance used to design the drilled shafts (40 ksf) as well as nominal values predicted using AASHTO and FHWA design equations. Unit base resistance (q_{BN}) calculated from N-values yields $q_{BN} = 60$ ksf. Equations that are based on uniaxial compressive strength of rock yield values of q_{BN} ranging from 13.8 to 42.8 ksf. A possible reason for the much higher observed base resistance is that the sandstone below the base of the test shaft may be of much higher strength than the specimens tested in uniaxial compression. No specimens were obtained and tested at the exact location of the test shaft.
- 5. Modeling the load-displacement response of rock-socketed drilled shafts can be accomplished by fitting the results of a load test to an analytical model. The resulting model provides a powerful tool for evaluation of trial designs to satisfy AASHTO LRFD design criteria. The as-designed shafts at Burma Road overpass easily satisfy LRFD criteria for Strength I, Strength IV, and Service I limit state. Calculations illustrating limit state check for all applicable loading cases are presented in Chapter 3.

4.2 Recommendations

The load test conducted at Burma Road overpass demonstrates that realistic values of side resistance can be predicted using design equations published in current AASHTO and FHWA publications. The following are recommended:

Side Resistance

For subsurface conditions that permit Standard Penetration Testing (SPT) in granular geomaterials, nominal values of side resistance for design can be calculated using the beta-method as presented in Chapter 1 of this report. Granular geomaterials include all soils classified as clean sands and gravels, silty sands and gravels, as well as material described as rock, such as sandstone or conglomerate, which is weak and/or weathered to a degree that makes it possible to penetrate using SPT.

For strata of rock which cannot be penetrated by SPT, rock coring and laboratory testing of intact cores to measure uniaxial compressive strength is recommended. Side resistance for design of rock sockets can then be established using Equation 4 presented in Chapter 1. At the Burma Road Overpass site, rock core samples were insufficient for this purpose, however, even the very limited test results, consisting of only a single value of q_u for the sandstone, provide a unit side resistance that would result in a safe design

but which is more realistic and allows for higher side resistance than the design value actually used.

Base Resistance

Where Standard Penetration Testing is possible in cohesionless soils or in weathered sandstone, values of design unit base resistance (q_{BN}) can be calculated using:

$$q_{BN}(tsf) = 0.60 (N_{60}) \le 30 tsf$$
 (16)

This expression places an upper limit of 60 ksf on nominal unit base resistance and clearly underestimates the base resistance measured in the load test at Burma Road Overpass. Where SPT penetration is not possible, it is recommended to obtain intact cores in the zone of tip bearing and to perform uniaxial compression tests. In this case, the following expression is recommended:

$$q_{\rm BN} = 2.5 \ q_{\rm u}$$
 (28)

this corresponds to Equation 7 with $N*_{cr} = 2.5$. This equation is limited to sites where the base is underlain by competent rock, as defined in Chapter 1.

Where it is not possible to obtain intact core samples or to penetrate using SPT, load testing may be the most effective way to justify the use of higher values of base resistance, as demonstrated by the load test at Burma Road overpass.

Finally it is recommended that WYDOT consider load testing of drilled shafts in rock in conjunction with future bridge projects. The information obtained from the load test at Burma Road Overpass shows that both side and base resistances far exceed the nominal values recommended in the Foundation Memo and actually used to design the drilled shafts for this project. Results of load testing conducted during the design phase would allow for the use of higher resistance factors and more cost-effective designs. Collection and analysis of multiple tests over time will certainly lead to more reliable designs for a wide range of geomaterials and could allow WYDOT to develop in-house calibrations for establishing resistance factors for specific geomaterials.

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APPENDIX A: Model for Axial Load-Displacement Response of a Rock Socket

This approximate method, given by Kulhawy and Carter (1992), provides simple closedform expressions that compare reasonably well to more sophisticated nonlinear finite element analyses reported by Pells and Turner (1979) and Rowe and Armitage (1987). The basic problem was depicted in Figure 4 and involves predicting the relationship between an axial compression load (Q_c) applied to the top of a socketed shaft and the resulting axial displacement at the top of the socket (w_c). The concrete shaft is modeled as an elastic cylindrical inclusion embedded within an elastic rock mass. The cylinder of depth L and diameter B has Young's modulus E_c and Poisson's ratio v_c . The rock mass surrounding the cylinder is homogeneous with Young's modulus E_r and Poisson's ratio v_r while the rock mass beneath the base of the shaft has Young's modulus E_b and Poisson's ratio v_b . The solution (Figure 4b) approximates the load-deformation response of an axially loaded rock socket as consisting of two linear segments: (1) the initial linear elastic response and (2) the full slip condition. The maximum load is limited to the nominal axial resistance.

For compression loading, two cases are treated by Kulhawy and Carter: (1) a "complete socket", for which full contact is assumed between the base of the concrete shaft and the underlying rock, and: (2) a shear socket, for which a void is assumed to exist beneath the base. Uplift is also considered and was applied to analyze the test shaft under the expected uplift force effects at the overpass project. For illustrative purposes only the complete socket under compression case will be presented here.

1. For the linearly elastic portion of the load-displacement curve.

$$w_{c} = \frac{2Q_{c}}{G_{r}B} \frac{1 + \left(\frac{4}{1 - \nu_{b}}\right)\left(\frac{1}{\pi\lambda\xi}\right)\left(\frac{2L}{B}\right)\left(\frac{\tanh[\mu L]}{\mu L}\right)}{\left(\frac{4}{1 - \nu_{b}}\right)\left(\frac{1}{\xi}\right) + \left(\frac{2\pi}{\zeta}\right)\left(\frac{2L}{B}\right)\left(\frac{\tanh[\mu L]}{\mu L}\right)}$$
A-1

in which: $w_c = axial deformation (settlement)$

$$(\mu L)^2 = \left(\frac{2}{\zeta\lambda}\right) \left(\frac{2L}{B}\right)^2$$
A-2

$$\zeta = \ln \left[5(1 - v_r) L/B \right]$$
A-3

$$\lambda = E_{\rm c}/G_{\rm r}$$
 A-4

$$G_{\rm r} = E_{\rm r} / [2(1 + v_{\rm r}]] = {\rm elastic shear modulus of rock mass}$$
 A-5

$$\xi = G_{\rm r}/G_{\rm b}$$
 A-6

$$G_{\rm b} = E_{\rm b} / [2(1 + v_{\rm b})]$$
 A-7

The magnitude of load transferred to the base of the shaft (Q_b) is given by:

$$\frac{Q_b}{Q_c} = \frac{\left(\frac{4}{1-\nu_b}\right)\left(\frac{1}{\xi}\right)\left(\frac{1}{\cosh[\mu D]}\right)}{\left(\frac{4}{1-\nu_b}\right)\left(\frac{1}{\xi}\right) + \left(\frac{2\pi}{\zeta}\right)\left(\frac{2D}{B}\right)\left(\frac{\tanh[\mu D]}{\mu D}\right)}$$
A-8

2. For the full slip portion of the load–displacement curve.

$$w_c = F_3 \left(\frac{Q_c}{\pi E_r B}\right) - F_4 B$$
A-9

in which:

$$F_3 = a_1(\lambda_1 B C_3 - \lambda_2 B C_4) - 4a_3$$
 A-10

$$F_4 = \left[1 - a_1 \left(\frac{\lambda_1 - \lambda_2}{D_4 - D_3} \right) B \right] a_2 \left(\frac{c}{E_r} \right)$$
A-11

$$C_{3,4} = \frac{D_{3,4}}{D_4 - D_3}$$
A-12

$$D_{3,4} = \left[\pi \left(1 - v_b^2\right) \left(\frac{E_r}{E_b}\right) + 4a_3 + a_1 \lambda_{2,1} B\right] \exp[\lambda_{2,1} D]$$
A-13

$$\lambda_{1,2} = \frac{-\beta \pm \left(\beta^2 + 4\alpha\right)^{\frac{1}{2}}}{2\alpha}$$
A-14

$$\alpha = a_1 \left(\frac{E_c}{E_r}\right) \left(\frac{B^2}{4}\right)$$
A-15

$$\beta = a_3 \left(\frac{E_c}{E_r}\right) B$$
A-16

$$a_1 = (1 + v_r)\zeta + a_2$$

A-17

$$a_{2} = \left[\left(1 - \nu_{c} \right) \left(\frac{E_{r}}{E_{c}} \right) + \left(1 + \nu_{r} \right) \right] \left(\frac{1}{2 \tan \phi \tan \psi} \right)$$
A-18

$$a_{3} = \left(\frac{v_{c}}{2\tan\psi}\right) \left(\frac{E_{r}}{E_{c}}\right)$$
A-19

The magnitude of load transferred to the base of the shaft (Q_b) is given by:

$$\frac{Q_b}{Q_c} = P_3 + P_4 \left(\frac{\pi B^2 c}{Q_c}\right)$$
A-20

in which:

$$P_{3} = a_{1}(\lambda_{1} - \lambda_{2}) B \exp[(\lambda_{1} + \lambda_{2})D] / (D_{4} - D_{3})$$
A-21

$$P_4 = a_2(\exp[\lambda_2 D] - \exp[\lambda_1 D]) / (D_4 - D_3)$$
A-22

Note that the point of intersection between the linear elastic portion of the curve and the full slip segment, defined by point (Q_{C1} , w_{C1}) in Figure 3b, can be calculated by setting Equation A-1 equal to Equation A-9, solving for the resulting value of axial load (Q_{C1}) and using this value to compute the corresponding displacement w_{C1} .

Numerical solutions to Equations A-1 through A-22 are implemented conveniently by spreadsheet, thus providing designers a simple analytical tool for assessing the likely ranges of behavior for trial designs. The user of this method should be familiar with the assumptions made in its development. The modulus of the rock mass is assumed to be constant over the depth of shaft embedment and beneath the base. Rock mass modulus and its variation with depth must, therefore, be assessed carefully (see Chapter 3 of

Turner 2006) and determined to satisfy the assumption of uniformity. Strength of the rock mass is required in terms of its Mohr-Coulomb parameters (c, ϕ , and ψ) where $\psi =$ angle of dilatancy. In the absence of laboratory testing of the rock-concrete interface, for example by constant normal stiffness direct shear tests, Kulhawy and Carter (1992) suggest the following correlations between the Mohr-Coulomb strength parameters and uniaxial compressive strength (q_u) of intact rock:

$$\frac{c}{p_a} = 0.1 \left(\frac{q_u}{p_a}\right)^{\frac{2}{3}}$$
A-23

 $\tan\phi\tan\psi = 0.001 \left(\frac{q_u}{p_a}\right)^{\frac{2}{3}}$ A-24

APPENDIX B: Axial Load-Displacement Model for Burma Road Overpass

This Appendix presents two figures, each of which illustrates the results of the loaddisplacement analysis of the test shaft at Burma Road Overpass. The equations presented in Appendix A, developed by Kulhawy and Carter (1992), were programmed by the author into a spreadsheet. Input parameters include the geometry of the foundation (depth and diameter) and strength and stiffness properties of the rock and the drilled shaft foundation. The program then executes the calculations corresponding to the equations given in Appendix A. Results are presented as a graph showing the axial loaddisplacement calculated by the model.

Figure B-1 shows the spreadsheet analysis of the test shaft plotted alongside the equivalent top load-settlement curve developed by Loadtest, Inc. (2009) and presented in their report of the load test. Fitting the model to match the results of the load test is presented and discussed in Chapter 3. This fitting is the method by which the strength and stiffness parameters of the rock mass were established. Figure B-2 shows the spreadsheet analysis for modeling the uplift load-displacement curve of the as-designed drilled shafts at Burma Road Overpass. This curve is used to evaluate the design for Service Limit State I, also described and discussed in Chapter 3.

A 'live' version of the spreadsheet solution has been provided to Wyoming DOT as part of this research project and can also be obtained by contacting the author.

Liasue Load-Settlement Anal	ysis, Ro	ck So	cket in Compression								
by Kulhawy & Carter (1992)											
Shaft diameter B (in):	36			Linear Flastic	oad-Displa	cement Calcu	lations	Full-Slip Lo	ad-Displacem	ent Calculation	
Shaft depth D (in):	492			Einour Eidouo	Loud Diopid	oomon oulou	anono	0	aa Diopiacoini		
Modulus of concrete, E_c (kip/in ²):	4408			Q _c (kips)	Complete Socket wc (in)	Tip Load Q _{tip} (kips)		Q _c (kips)	Complete Socket w _c (in)	Tip Load Q _c (kips)	
Poissons ratio, y _c :	0.25			0	0.00	0.0		1160	0.194	254.5	
Shear modulus, G _c (kip/in ²):	1763.2			1160	0 189	252.5		2600	0.89	1463.3	
				86.1	0.014			2600	1.20		
								1785	0.50		
ROPERTIES OF SIDE ROCK MASS											
Rock mass modulus <i>E</i> _r (k/in ²):	20										
Rock mass Poissons ratio, vr:	0.25										
Shear modulus, Gr (k/in ²):	8										
cohesion, c (lb/in ²)	16										
friction angle, (degrees)	22					3000 -					
dilation angle, w (degrees)	1										
						t					
ROPERTIES OF BASE ROCK MASS	<u>s</u>					L L					
Rock mass modulus E _b (k/in ²):	55					2500 -					
Rock mass Poissons ratio, vb:	0.3					1					
Shear modulus, G _b (k/in ²):	21.154					-					
									9	Complete Soc	ket
					୍ଚ	2000				L = 4111 R = 3 ft	
DIMENSIONLESS CONSTANTS					ä	- F				0 - 5 it	
OR LINEAR ELASTIC calculated)			CALCULATED CONSTANTS FOR FULL SLIP		ad (k	1500			i I	E _r = 20 k/in ² E _b = 55 k/in2 v _r = 0.25	
$\frac{OR LINEAR ELASTIC}{calculated}$ $\lambda = E_{\sigma}/G_{r}$	551		CALCULATED CONSTANTS FOR FULL SLIP a ₃	0.0325	oad (k	1500				E _r = 20 k/in ² E _b = 55 k/in2 v _r = 0.25 v _b = 0.30	
$\frac{\text{COR LINEAR ELASTIC}}{(calculated)}$ $\lambda = E_{c}/G,$ $\zeta = \ln[5(1-\gamma_{t}) D/B]$	551 3.9367		CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂	0.0325 88.8648	l Load (k	1500				E _r = 20 k/in² E _b = 55 k/in2 v _r = 0.25 v _b = 0.30	
$\frac{\text{OR LINEAR ELASTIC}}{\lambda = E_{\sigma}/G_{r}}$ $\zeta = \ln[5(1-\gamma_{r}) D/B]$ $\xi = G_{r}/G_{b}$	551 3.9367 0.3782		CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂ a ₁	0.0325 88.8648 93.7857	ial Load (k	1500				E _r = 20 k/in² E _b = 55 k/in2 v _r = 0.25 v _b = 0.30	
COR LINEAR ELASTIC calculated) $\lambda = E_d/G_r$ $\zeta = \ln[5(1-v_r) D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$	551 3.9367 0.3782 0.6889		CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂ a ₁ B	0.0325 88.8648 93.7857 257.8048	Axial Load (k	1500 1000			d-Settleme	$E_r = 20 \text{ k/in}^2$ $E_b = 55 \text{ k/in2}$ $v_r = 0.25$ $v_b = 0.30$	
$cor LINEAR ELASTICcalculated)\lambda = E_{J}G,\zeta = ln[5(1-v_{t}) D/B]\xi = G_{t}/G_{b}(\mu D)^{2}\mu$	551 3.9367 0.3782 0.6889 0.0017		CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂ a ₁ β α	0.0325 88.8648 93.7857 257.8048 6697197.6	Axial Load (k	1500 1000	/_	S Load	d-Settleme	$E_r = 20 k/in^2$ $E_b = 55 k/in2$ $v_r = 0.25$ $v_b = 0.30$ nt	
FOR LINEAR ELASTIC calculated) $\lambda = E_{o}/G_{r}$ $\zeta = ln[5(1-v_{r}), D/B]$ $\xi = G_{r}/G_{b}$ $(\mu D)^{2}$ μ for complete socket: $G_{r}Bw_{c}/2Q_{c}$	551 3.9367 0.3782 0.6889 0.0017 0.0235		CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂ a ₁ β α λ ₁	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004	Axial Load (k	1500 1000	/_		d-Settleme ve, O-cell T	E _r = 20 k/in ² E _b = 55 k/in2 v _r = 0.25 v _b = 0.30 nt est 2009	
$\frac{\text{OR LINEAR ELASTIC}}{\lambda = E_{i}/G_{r}}$ $\frac{\zeta = \ln[5(1-v_{r}) D/B]}{\xi = G_{i}/G_{b}}$ $\frac{\zeta = G_{i}/G_{b}}{(\mu D)^{2}}$ for complete socket: G_{r}Bw_{c}/2Q_{c} for shear socket: E_{i}Bw_{c}/2Q_{c}	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699		CALCULATED CONSTANTS FOR FULL SLIP a3 a2 a1 β α λ1 λ2	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004	Axial Load (k	1500 1000	/	Curv Load	d-Settleme /e, O-cell T dtest, Inc.,	$E_{r} = 20 k/in^{2}$ $E_{b} = 55 k/in2$ $v_{r} = 0.25$ $v_{b} = 0.30$ nt est 2009	
FOR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = ln[5(1-v_r), D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ μ for complete socket: $G_rBw_c/2Q_c$ for shear socket: $E_rBw_c/2Q_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699		$\frac{CALCULATED CONSTANTS}{FOR FULL SLIP}$ a_{3} a_{2} a_{1} β α λ_{1} λ_{2} C_{1}	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584	Axial Load (k	1500 1000 500	/_	Curv Load	d-Settleme /e, O-cell T dtest, Inc.,	$E_r = 20 k/in^2 E_b = 55 k/in2 v_r = 0.25 v_b = 0.30 nt est 2009$	
$ \begin{array}{l} \hline \text{OR LINEAR ELASTIC} \\ \hline \text{calculated} \\ \hline \lambda = E_{i}/G_{r} \\ \hline \zeta = \ln[5(1-v_{r}) D/B] \\ \hline \xi = G_{i}/G_{b} \\ (\mu D)^{2} \\ \mu \\ for complete socket: G_{r}Bw_{c}/2Q_{c} \\ \hline for shear socket: E_{r}Bw_{c}/2Q_{c} \\ \hline \text{Equivalent Linear Spring} \\ \hline \text{Onstants K (force/length)} \end{array} $	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699		$ \begin{array}{c} \begin{array}{c} \textbf{CALCULATED CONSTANTS} \\ \hline \textbf{FOR FULL SLIP} \\ \textbf{a}_3 \\ \textbf{a}_2 \\ \textbf{a}_1 \\ \textbf{\beta} \\ \textbf{\alpha} \\ \textbf{\lambda}_1 \\ \textbf{\lambda}_2 \\ \textbf{C}_1 \\ \hline \textbf{C}_2 \end{array} $	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -3.1584	Axial Load (k	1500 1000 500	/_	Curv Load	d-Settleme /e, O-cell T dtest, Inc.,	$\begin{array}{l} F_{\rm c} = 20 \; k/in^2 \\ F_{\rm b} = 55 \; k/in2 \\ v_{\rm p} = 0.25 \\ v_{\rm b} = 0.30 \end{array}$	
FOR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = ln[5(1-v_r), D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ for complete socket: $E_rBw_c/2Q_c$ for shear socket: $E_rBw_c/2Q_c$ Equivalent Linear Spring Constants K (force/length) complete socket: $K_c = Q_c/w_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127	k/in	$\begin{array}{c} \begin{array}{c} \text{CALCULATED CONSTANTS} \\ \hline \text{FOR FULL SLIP} \\ a_3 \\ a_2 \\ a_1 \\ \beta \\ \alpha \\ \lambda_1 \\ \lambda_2 \\ C_1 \\ \hline \\ C_2 \\ C_3 \end{array}$	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -3.1584 -0.0541	Axial Load (k	1500 1000 500	/	Curv Load	d-Settleme /e, O-cell T dtest, Inc.,	E,= 20 k/in ² E _b = 55 k/in2 v _b = 0.30 nt Cest 2009	
COR LINEAR ELASTIC calculated) $\lambda = E_c/G_c$ $\zeta = \ln[5(1-v_c) D/B]$ $\xi = G_c/G_b$ $(\mu D)^2$ μ for complete socket: $G_cBw_c/2Q_c$ for shear socket: $E_cBw_c/2Q_c$ Equivalent Linear Spring Constants K (force/length) complete socket: $K_c = Q_c/w_c$ shear socket: $K_c = Q_c/w_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 0.0699 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.000000	k/in k/in	CALCULATED CONSTANTS FOR FULL SLIP a3 a2 a1 β α λ1 λ2 C1 C2 C3 C4	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -3.1584 -0.0541 0.9459	Axial Load (k	1500 1000 500 0.00	0.25	Curv Load	d-Settleme ve, O-cell T dtest, Inc.,	E,= 20 k/in ² E _b = 55 k/in ² v _b = 0.30 nt 	2.00
The second seco	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 0.0699 0.0000 0.000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.000000	k/in k/in		0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -2.1584 -3.1584 -0.0541 0.9459 -0.1652	Axial Load (k	1500 1000 500 0.00	0.25	Curr Curr Load	d-Settleme re, O-cell T dtest, Inc., i 1.00 1.2	E,= 20 k/in ² E _b = 55 k/in2 w _b = 0.35 w _b = 0.30 nt est 2009	2.00
COR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = \ln[5(1-v_r) D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ μ for complete socket: $G_rBw_c/2Q_c$ for shear socket: $E_rBw_c/2Q_c$ equivalent Linear Spring Constants K (force/length) complete socket: $K_s = Q_c/w_c$ shear socket: $K_s = Q_c/w_c$ Proportion of Load Transferred to ip	551 3.9367 0.3782 0.03782 0.0017 0.0235 0.0235 0.0699 6127 5150.4	k/in k/in	CALCULATED CONSTANTS FOR FULL SLIP a ₃ a ₂ a ₁ β α λ ₁ λ ₂ C ₁ C ₂ C ₃ C ₄ D ₃	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -3.1584 -3.1584 -0.0541 0.9459 -0.1652 2.8888	Axial Load (k	1500 1000 500 0.00	0.25	Curv Load	d-Settleme re, O-cell T dtest, Inc., 5 1.00 1.2 acement (E,= 20 k/in ² E,= 55 k/in2 v,= 0.25 v _b = 0.30 nt est 2009 5 1.50 1.75 inches)	2.00
$ \begin{array}{l} \hline \begin{array}{l} \hline \begin{array}{l} \hline \begin{array}{l} \hline \begin{array}{l} \hline \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} \end{array} \\ \hline \end{array} $ \\ \hline \end{array} \\ \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \hline \end{array} \\ \\ \hline \end{array} \\ \\ \\ \hline \end{array} \\ \\ \hline \end{array} \\ \\ \\ \\ \end{array} \\ \\ \\ \\ \end{array} \\ \\	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127 5150.4 0.2176	k/in k/in	CALCULATED CONSTANTS FOR FULL SLIP a1 a2 a1 β a C1 C2 C3 C4 D3 D4	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801	Axial Load (k	1500 1000 500 0.00	0.25	Curr Load	d-Settleme re, O-cell T dtest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E _b = 55 k/in2 v _p = 0.25 v _b = 0.30 nt est 2009 5 1.50 1.75 inches)	2.00
FOR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = \ln[5(1-v_r) D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ μ for complete socket: $G_rBw_c/2Q_c$ for shear socket: $E_rBw_c/2Q_c$ Equivalent Linear Spring Constants K (force/length) complete socket: $K_s = Q_c/w_c$ shear socket: $K_s = Q_c/w_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127 5150.4	k/in k/in	CALCULATED CONSTANTS FOR FULL SLIP a1 a2 a1 β α C1 C2 C3 C4 D3 D4 F1 F2	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -0.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801 0.0711	Axial Load (k	1500 1000 500 0.00	0.25	S Load Curr Load 0.50 0.75 Displa	d-Settleme ve, O-cell T ittest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E _b = 55 k/in2 w _b = 0.30 nt est 2009 5 1.50 1.75 inches)	2.00
FOR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = \ln[5(1-v_r), D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ μ for complete socket: $G_rBw_c/2Q_c$ for shear socket: $E_rBw_c/2Q_c$ Equivalent Linear Spring Constants K (force/length) complete socket: $K_s = Q_c/w_c$ shear socket: $K_s = Q_c/w_c$ complete socket: $K_s = Q_c/w_c$	551 3.9367 0.3782 0.03782 0.0017 0.0235 0.0699 6127 5150.4	k/in	CALCULATED CONSTANTS FOR FULL SLIP a3 a2 a1 β α λ1 λ2 C1 C2 C3 C4 D3 D4 F1 F2 F3	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -3.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801 0.0711 1.1000	Axial Load (k	1500 1000 500 0.00	0.25	Curr Load	d-Settleme ve, O-cell T dtest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E,= 55 k/in2 v,= 0.25 v _b = 0.30 nt eest 2009 5 1.50 1.75 inches)	2.00
FOR LINEAR ELASTIC calculated) $\lambda = E_c G_r$, $\zeta = \ln[5(1-v_r) D/B]$ $\xi = G_c / G_b$, $(\mu D)^2$ μ for complete socket: $C_r Bw_c / 2Q_c$ for shear socket: $E_r Bw_c / 2Q_c$ iquivalent Linear Spring Donstants K (force/length) complete socket: $K_s = Q_c w_c$ shear socket: $K_s = Q_c w_c$ roportion of Load Transferred to ip complete socket: $Q_{up}/2Q_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127 5150.4	k/in k/in	$\begin{array}{c} \begin{array}{c} {\rm CALCULATED CONSTANTS} \\ \hline {\rm FOR FULL SLIP} \\ {a_3} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {a_2} \\ {a_1} \\ {a_2} \\ {$	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801 0.0711 1.1000 0.0103	Axial Load (k	1500 1000 500 0.00	0.25	Load Curr Load 0.50 0.75 Displa	d-Settleme re, O-cell T dtest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E _b = 55 k/in2 v _p = 0.25 v _b = 0.30 nt est 2009 5 1.50 1.75 inches)	2.00
FOR LINEAR ELASTIC calculated) $\lambda = E_c/G_r$ $\zeta = \ln[5(1-v_r) D/B]$ $\xi = G_r/G_b$ $(\mu D)^2$ μ for complete socket: $G_rBw_c/2Q_c$ for shear socket: $E_r, Bw_c/2Q_c$ iquivalent Linear Spring Sonstants K (force/length) complete socket: $K_s = Q_c/w_c$ shear socket: $K_s = Q_c/w_c$	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127 5150.4 0.2176	k/in k/in	$\begin{array}{c} \begin{array}{c} {\rm CALCULATED CONSTANTS} \\ \hline {\rm FOR FULL SLIP} \\ {a_3} \\ {a_2} \\ {a_1} \\ {\beta} \\ {\alpha} \\ {\alpha} \\ {\lambda_1} \\ {\lambda_2} \\ {C_1} \\ \\ {C_2} \\ {C_3} \\ \\ {C_4} \\ {D_3} \\ \\ \hline {D_4} \\ \\ {F_1} \\ \\ {F_2} \\ \\ {F_3} \\ \\ {F_3} \\ \\ {F_4} \\ \\ {P_3} \end{array}$	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -2.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801 0.0711 1.1000 0.839395482	Axial Load (k	1500 1000 500 0.00	0.25	Load Curr Load 0.50 0.75 Displa	d-Settleme ve, O-cell T titest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E _b = 55 k/in ₂ w _b = 0.35 w _b = 0.30 nt est 2009 5 1.50 1.75 inches)	2.00
$ \begin{array}{l} \hline \text{OR LINEAR ELASTIC} \\ \hline \text{calculated} \\ \hline \lambda = E_c G_r \\ \hline \zeta = \ln [5(1-v_r), D/B] \\ \hline \xi = G_r / G_b \\ \hline (\mu D)^2 \\ \mu \\ \hline \text{for shear socket: } G_r Bw_c / 2Q_c \\ \hline \text{for shear socket: } E_r Bw_c / 2Q_c \\ \hline \text{quivalent Linear Spring} \\ \hline \text{complete socket: } K_s = Q_c / w_c \\ \hline \text{shear socket: } K_s = Q_c / w_c \\ \hline \text{roportion of Load Transferred to} \\ \hline \text{toportion of Load Transferred to} \\ \hline \end{array} $	551 3.9367 0.3782 0.6889 0.0017 0.0235 0.0699 6127 5150.4 0.2176	k/in	$\begin{array}{c} \begin{array}{c} \text{CALCULATED CONSTANTS} \\ \hline \text{FOR FULL SLIP} \\ \hline a_3 \\ a_2 \\ a_1 \\ \hline a_1 \\ \hline a_2 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\ \hline a_2 \\ \hline a_2 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\ \hline a_1 \\ \hline a_2 \\$	0.0325 88.8648 93.7857 257.8048 6697197.6 0.0004 -0.0004 -2.1584 -0.0541 0.9459 -0.1652 2.8888 6.8801 0.0711 1.1000 0.839395482 -11.03983924	Axial Load (k	1500 1000 500 0.00	0.25	C Load Curv Load	d-Settleme ve, O-cell T dtest, Inc., i 1.00 1.2 acement (E,= 20 k/in ² E,= 55 k/in2 v,= 0.25 v _b = 0.30 nt eest 2009 5 1.50 1.75 inches)	2.00

Figure B-1. Spreadsheet Analysis of Load-Displacement Model, Shaft in Compression



Figure B-2. Spreadsheet Analysis of Load-Displacement Model, Shaft in Uplift