

# Influence of Wheel Load Shape on Vertical Stress Reaching Subgrade through an Aggregate Layer

Karen S. Henry

March 2001

Approved for public release; distribution is unlimited.

Engineering Laborate

and

**Cold Regions Research** 

Abstract: The U.S. Army design procedure to stabilize low-bearing-capacity soil with geotextiles is based on the assumption that the applied surface load (the wheel load) is in the shape of a circle. The maximum vertical stress that reaches the subgrade through overlying aggregate is then estimated on the basis of the assumption that the aggregate is an elastic, homogeneous, isotropic half-space and, therefore, that the stress distribution can be estimated by using the Boussinesq method. To study the extent to which the shape of the applied load influences the stress that reaches the subgrade through the aggregate layer, the maximum vertical stress at depth predicted by the Boussinesq method was computed and compared for circular and rectangular loads. A comparison of the maximum vertical stress beneath circular and rectangular loads as a function of depth indicated that the differences were insufficient to warrant a change in the design procedure for rectangular load geometries that have length/width ratios of 3 or less, and, furthermore, that assuming that the load is circular is conservative. For length/width ratios of 3 or less, the maximum vertical stress applied by a rectangle is at least 85% of that applied by a circle.

How to get cop	ies of CRREL technical publications:
Department of I tion Center: DTIC-BR 8725 JOH FT BELVO Telephone E-mail	Defense personnel and contractors may order reports through the Defense Technical Informa- SUITE 0944 IN J KINGMAN RD DIR VA 22060-6218 (800) 225-3842 help@dtic.mil msorders@dtic.mil http://www.dtic.mil/
All others may on NTIS 5285 POF SPRINGF Telephone E-mail WWW	Arder reports through the National Technical Information Service: RT ROYAL RD IELD VA 22161 (703) 487-4650 (703) 487-4639 (TDD for the hearing-impaired) orders@ntis.fedworld.gov http://www.ntis.gov/index.html
A complete list of USACRR 72 LYME HANOVE Telephone E-mail For information World Wide We	of all CRREL technical publications is available from EL (CEERD-IM-HL) RD R NH 03755-1290 (603) 646-4338 erhoff@crrel.usace.army.mil n on all aspects of the Cold Regions Research and Engineering Laboratory, visit our b site:
<u></u>	v.oriol.dodoc.drifty.filli

Technical Report ERDC/CRREL TR-01-8



US Army Corps of Engineers® Cold Regions Research & Engineering Laboratory

# Influence of Wheel Load Shape on Vertical Stress Reaching Subgrade through an Aggregate Layer

Karen S. Henry

March 2001

Prepared for OFFICE OF THE CHIEF OF ENGINEERS

Approved for public release; distribution is unlimited.

# PREFACE

This report was prepared by Karen S. Henry, Ph.D., P.E., Research Civil Engineer, Civil Engineering Research Division, U.S. Army Engineer Research and Development Center (ERDC), Cold Regions Research and Engineering Laboratory (CRREL), Hanover, New Hampshire.

The work presented in this report was funded by U.S. Army Corps of Engineers work unit AT42-TO-007, *Cold Regions Theater of Operations Engineering*, under the work unit entitled *Use of Geosynthetics to Rapidly Reinforce Thawing Soils*. The author thanks George Blaisdell, Research Civil Engineer, and Dr. Paul Richmond, Mechanical Engineer, both of CRREL, for technical review of this report.

The contents of this report are not to be used for advertising or promotional purposes. Citation of brand names does not constitute an official endorsement or approval of the use of such commercial products.

# Influence of Wheel Load Shape on Vertical Stress Reaching Subgrade through an Aggregate Layer

KAREN S. HENRY

#### INTRODUCTION

The U.S. Army design procedure to stabilize lowbearing-capacity soil with geotextiles for traffic involves placing aggregate on geotextiles (U.S. Army and U.S. Air Force 1995). It is based on the assumption that the applied surface load (the wheel load) is in the shape of a circle (e.g., Henry 1999). The vertical stress that reaches the subgrade from the applied wheel load is then estimated on the basis of the assumption that the aggregate is an elastic, homogeneous, isotropic half-space and, therefore, that the stress distribution can be estimated by using the Boussinesq method (e.g., Newmark 1942). The stress distribution determined by the Boussinesq approach is assumed to be accurate for the prediction of stresses distributed through compacted crushed rock and through asphalt (e.g., Barenberg et al. 1975, Yoder and Witzcak 1975). However, it is not clear that a circular area accurately predicts stress for non-circular wheel load shapes. For example, a common configuration of dual wheels on a single axle has been modeled as a rectangular area (e.g., Giroud and Noiray 1981). To quantify the extent to which the shape of the applied load influences the stress that reaches the subgrade through the aggregate layer, I analyzed the influence of the shape of the wheel load on the maximum vertical stress at depth predicted by the Boussinesq method.

Since it is the maximum vertical stress (i.e., the stress beneath the center of the loaded area) that is used in the design procedure, I examined the influence of the shape of the applied load on the maximum vertical stress predicted by the Boussinesq approach. If significant differences in the maximum vertical stresses below uniformly loaded rectangles and circles were found, then the wheel load shape (i.e., rectangle or circle) should be accounted for in the design procedure. A comparison of the maximum vertical stress beneath circular and rectangular loads as a function of depth indicated that the differences were insufficient to warrant a change in the design procedure for rectangular load geometries that have length/width ratios of 3 or less, and, furthermore, that assuming that the load is circular is conservative.

The details of the analysis are presented fully in this report. The techniques may be used to examine other load geometries, including those of tracked vehicles.

#### STUDY OBJECTIVES

The goal of this study was to determine whether the shape of the wheel load at the ground surface significantly influences the maximum vertical stress at depth (i.e., that reaches the subgrade) given that the aggregate layer behaves as a linearly elastic material. If a significant difference were to be found between the vertical stresses at depth applied by uniformly loaded circles versus rectangles, then appropriate changes would be made in design guidance developed for vehicles that apply loads that are more accurately modeled as rectangles than circles.

I used the Boussinesq equations to estimate maximum vertical stresses for uniformly loaded circles (Newmark 1942) and rectangles (Newmark 1935). I assumed unit loads and areas, and considered a large range in length-to-width ratios for rectangular wheel loads so that the range of wheel load shapes applied by military vehicles was well represented. The longest rectangle that I studied, at L = 6B, where L is the contact length and B is the contact width, is too extreme to model wheeled vehicles. The range of normalized depths studied represents a range of typical aggregate thicknesses above geotextiles. The technique used can easily be applied to other length/width ratios and other normalized depths.

### VERTICAL BOUSSINESQ STRESS BELOW A RECTANGLE

The vertical stress at depth below the corner of a uniformly loaded rectangle of dimensions  $L \times B$  is estimated as (Fig. 1; Newmark 1935)

$$\sigma_{z} = \frac{w}{4\pi} \left[ \frac{2A_{0}V_{0}}{V_{0}^{2} + A_{0}^{2}} \cdot \frac{V_{0}^{2} + 1}{V_{0}^{2}} + (1a) \right]$$

$$\left( \tan^{-1} \frac{2A_{0}V_{0}}{V_{0}^{2} - A_{0}^{2}} \right) \text{for } A_{0} > Z$$

$$\sigma_{z} = \frac{w}{4\pi} \left[ \frac{2A_{0}V_{0}}{V_{0}^{2} + A_{0}^{2}} \cdot \frac{V_{0}^{2} + 1}{V_{0}^{2}} + (1b)^{*} \right]$$

$$\left( \tan^{-1} \frac{2A_{0}V_{0}}{V_{0}^{2} - A_{0}^{2}} \right) + \pi \text{for } A_{0} < Z$$

where

w = applied uniform pressure

$$Z =$$
 depth below the corner of the rectangle  
for which the vertical stress is desired

$$V_{\rm o}^2 = \frac{L^2 + B^2 + Z^2}{Z^2}$$
$$A_{\rm o} = \frac{LB}{Z^2} \quad .$$

Note that  $V_0$  is the ratio of the radius vector from point Z to the corner of the rectangle to the depth of point Z. To obtain the stress below the center of the rectangle at depth Z, I used superposition and divided the rectangle into four smaller rectangles, such that

and

$$Y = \frac{B}{2}$$

 $X = \frac{L}{2}$ 

and A and V are defined as follows:

$$A = \frac{XY}{Z^2}$$



Figure 1. Notation used in the estimation of vertical stress at depth below the corner and center of a uniformly loaded rectangle.

and

$$V^2 = \frac{X^2 + Y^2 + Z^2}{Z^2} \; .$$

Thus  $I_z$ , or the ratio of the vertical stress below the center of a rectangle at depth Z to the stress applied on the rectangle  $(L \times B)$  at the surface, is equal to

$$I_{z} = \frac{1}{\pi} \left[ \frac{2AV}{V^{2} + A^{2}} \cdot \frac{V^{2} + 1}{V^{2}} + (2a) \right]$$
$$\left( \tan^{-1} \frac{2AV}{V^{2} - A^{2}} \right) \text{for } A > Z$$
$$I_{z} = \frac{1}{\pi} \left[ \frac{2AV}{V^{2} + A^{2}} \cdot \frac{V^{2} + 1}{V^{2}} + (2b) \right]$$

$$\left(\tan^{-1}\frac{2AV}{V^2 - A^2}\right) + \pi \left[ \text{for } A < Z \right].$$

# VERTICAL BOUSSINESQ STRESS BELOW A CIRCLE

The vertical stress at depth Z below the center of a uniformly loaded circle of radius r, divided by the applied stress, is estimated as (Fig. 2; Newmark 1942)

<sup>\*</sup>This form of the equation is not published by Newmark (1935), but it is required to avoid predicting tension (e.g., Bowles 1988).



Figure 2. Uniformly loaded circle, showing notation used in the estimation of vertical stress at depth below the center of the circle.

$$I_{\rm c} = \left[ 1 - \left[ \cos \left[ \tan^{-1} \left( \frac{r}{Z} \right) \right] \right]^3 \right] \quad . \tag{3}$$

I used eq 2 and 3 for a unit uniform load and a unit area to compare the stress reduction at various normalized depths estimated by each equation. I varied the length/width ratio of the rectangles from L = B to L= 6B and the normalized depth Z from 0.05 to 2.0. The range in these parameters reasonably represents the geometry of loads applied by heavy military vehicles. An example of estimating the length-to-width ratio of a wheel load and the values of V and r for a military vehicle follows.

#### WHEEL LOAD GEOMETRY OF THE M1000 TRAILER

On-highway trucks typically have *L*:*B* ratios of 1.4 and off-highway trucks have L:B ratios of 2.0 (Giroud and Noiray 1981). The M1000 trailer of the Heavy Equipment Transporter System (HETS) (Fig. 3) likely has the highest length/width ratio of a wheel load applied by a U.S. military vehicle. Each axle line of this trailer has eight wheels (two sets of dual wheels on each end) (Fig. 4). If we assume that the soil between the tires aligned on one side of the axle will not fail (e.g., Giroud and Noiray 1981), then the load carried on that side of the axle can be assumed to be distributed over a rectangle (Fig. 4). Based on the information given in Figure 4, the L:B ratio of the uniformly loaded rectangle is approximately 3.9. Note that for a 1-m depth of aggregate, V is equal to 1.16 for this vehicle.

#### ANALYTICAL STUDY AND RESULTS

I programmed eq 2 and 3 into a Mathcad 8 programmable worksheet (Mathsoft 1998) and set the area of pressure application equal to one. The results generated include the fraction of the applied vertical stress below the rectangle and the circle,  $I_{rect}$  and  $I_{circ}$ , respectively, and the ratio  $I_{rect}/I_{circ}$ . A factor F represents the L:B ratio that was easily changed to examine its influence on results. Appendix A contains a hard copy of the Mathcad worksheet used, tabulated results, and a copy of the Mathcad worksheet for the reader's use.

The ratios of the stress reduction beneath the center of the rectangles to the stress reduction beneath the center of a circle are shown in Figure 5. The maximum vertical stress beneath the circle is always greater than that beneath the rectangles, including the special case of a square. A circle minimizes the ratio of perimeter to area; thus, the circle maximizes the influence of surface pressure at depths below the center. Therefore, applying the assumption that the surface load is circular is conservative compared to assuming other shapes. Furthermore, for length/width ratios of 3 or less, the maximum vertical stress applied by a rectangle is at least 85% of that applied by a circle. The minimum ratio of the stress beneath a rectangle to a circle for the conditions analyzed occurs at a normalized depth of about 0.6, and is about 0.65 for a length/ width ratio of 6. As mentioned earlier, the length/width ratio of 6 is outside the range of load shapes for wheeled U.S. military vehicles.



Figure 3. M1000 semi-trailer, downloaded from USA TACOM (1999).



Figure 4. Dimensions of wheels on one end of an axle line of the M1000 trailer.\*

#### DISCUSSION

Based on the results of the analytical study, there is no compelling reason to assume any wheel load shape other than circular. However, if a vehicle does produce wheel loads than can be approximated as uniformly loaded rectangles with length/width ratios of about 4 or greater, this question should be reconsidered for purposes of modifying design guidance that may be too conservative. In this case, the spreadsheet shown in Appendix A can be used to calculate the stress reduction at depth below the rectangle simply by changing the F value that is input at the top of the spreadsheet. Keep in mind that this approach assumes that the Boussinesq stress distribution provides a reasonable estimate of vertical stress at depth (i.e., the aggregate behaves in a linearly elastic manner and the stress is uniformly applied).

Although not the topic of this study, whether the aggregate that is placed on top of the geotextile behaves as a linearly elastic material is important; related to this is whether the vertical stresses are accurately predicted by the Boussinesq method. The aggregate type and quality significantly influence the stress distribution at depth. McMahon and Yoder (1960) found that pressures in homogeneous, compacted clay soil subgrades followed the Boussinesq pattern, but were up to 18% higher than those predicted by Boussinesq at shallow depths (e.g., less than the diameter of the loaded area). Further, the presence of compacted crushed limestone base above the clay subgrade reduced the vertical stresses in the subgrade immediately below the interface to values less than those predicted by Boussinesq. Other research indicated that there is a stress concentration in soil layers

containing significant quantities of sand compared to other aggregates. For example, a 45-kN (10-kip) load was applied at 690 kPa (100 psi) to a subgrade through various aggregates, with the result that the stress reaching the subgrade through a 0.6-m (24-in.) layer of sand was about twice that of the stress through a layer of crushed limestone (Herner 1955). Sowers and Vesic (1962) found that vertical stresses in a 203-mm- (8in.-) thick base consisting of 95% subangular quartz sand and 5% asphalt, overlain by a 152-mm- (6-in.-) thick asphalt pavement, were up to 70% higher than the vertical stress predicted by Boussinesq and higher than that in other types of base-many of which had lower vertical stresses than those predicted by Boussinesq. Thus, more effort should focus on accurately modeling stress distribution through the various aggregates that the military may use, indeed may be forced to use, in constructing geotextile-reinforced unsurfaced roads.

#### CONCLUSION

For all wheeled U.S. military vehicles, the wheel load may safely and accurately be assumed to be circular if the aggregate that is loaded can be modeled as a linearly elastic material (e.g., compacted, crushed rock). Because the U.S. Army design procedure to use geotextiles overlain with high-quality aggregate to stabilize low-bearing-capacity soil for trafficking with wheeled vehicles (U.S. Army and U.S. Air Force 1995) assumes that the wheel load applied at the surface is in the shape of a circle, no changes are required in this approach to modeling wheel loads. However, if a vehicle does produce loads than can be approximated as uniformly loaded rectangles with length/width ratios of about 4 or greater, (e.g., tracked vehicles) this ques-



Figure 5. Ratio of the reduction in applied stress with depth for a unit rectangle to a unit circle for various length/width (L:B) ratios of the rectangle.

<sup>\*</sup>Personal communication with R. Dunbar, Test Director, Yuma Proving Grounds, Yuma, Arizona, 1999.

tion should be reconsidered in order to save aggregate material. Furthermore, the Mathcad spreadsheet as shown in Appendix A can be used to calculate the stress reduction at depth below the rectangular loads.

More important than wheel load shape is whether the aggregate that is placed on top of the geotextile can be accurately modeled as a linearly elastic material, and, therefore, whether the vertical stresses are reasonably approximated by the Boussinesq method (as the current design method assumes). Indeed, stress concentrations in sand and in clay soil compared to Boussinesq predictions have been noted. Thus, if low quality aggregate composed of rounded gravel, containing sand or fines, or both, must be used in geotextile reinforcement of low-bearing-capacity soil, this question should be addressed.

### LITERATURE CITED

**Barenberg, E.J., J. Hales, and J. Dowland** (1975) Evaluation of soil-aggregate systems with MIRAFI fabric. University of Illinois Report No. UILU-ENG-75-2020, prepared for Celanese Fibers Marketing Company.

**Bowles, J.E.** (1988) *Foundation Analysis and Design*, 4th edition. New York: McGraw-Hill, Inc.

**Henry, K.S.** (1999) Geotextiles to stabilize unsurfaced roads on thawing, low-bearing capacity soils: A comparison of two design methods for use by the U.S. Army. U.S. Army Cold Regions Research and Engineering Laboratory, Special Report 99–7.

Herner, R.C. (1955) Effect of base course quality on load transmission through flexible pavement. In *Proceedings, Highway Research Board*, p. 224–233.

Mathsoft (1998) *Mathcad 8 Professional*. Cambridge, Massachusetts: MathSoft Inc.

McMahon, T.F., and E.J. Yoder (1960) Design of a pressure-sensitive cell and model studies of pressure in a flexible pavement subgrade. In *Proceedings, Highway Research Board, 39th Annual Meeting*, National Academy of Sciences–National Research Council, Washington, D.C., p. 650–682.

Newmark, N.M. (1935) Simplified computation of vertical pressures in elastic foundations. *University of Illinois Bulletin*, **33**(4).

Newmark, N.M. (1942) Influence charts for computation of stresses in elastic foundations. *University of Illinois Bulletin*, **40**(12).

**Sowers, G.F., and A.B. Vesic** (1962) Vertical stresses in subgrades beneath statically loaded flexible pavements. In *Stress Distribution in Earth Masses*. Highway Research Board Bulletin 342, NAS-NRC, Washington, DC, p. 90–120.

**U.S. Army TACOM** (1999) http://www.tacom.army. mil/dsa/pm htv/programs.html.

**U.S. Army and U.S. Air Force** (1995) Engineering use of geotextiles. TM5-818-8/AFJMAN 32-1030, Headquarters, Departments of the Army and the Air Force, Washington, D.C.

**Yoder, E.J., and M.W. Witczak** (1975) *Principles of Pavement Design*, 2nd edition. New York: John Wiley and Sons.

#### APPENDIX A: ANALYTICAL STUDY OF MAXIMUM VERTICAL STRESSES UNDER UNIFORMLY LOADED RECTANGLES AND CIRCLES

This worksheet,nrmlshapestudymatrix.mcd, prepared by Karen S. Henry of The U.S. Army Cold Regions Research and Engineering Laboratory, Hanover, NH, compares the distributions of vertical stress at depth of uniformly loaded circles and rectangles by the respective Boussinesq equations. F can be varied to study the influence of the length/width ratio. z may also be varied to determine the stress at various depths.

Assume unit Areas:

Area := 1 
$$r := \sqrt{\frac{Area}{\pi}}$$
  $r = 0.564$   $F := 6$ 

F is the ratio of the length, L to the width, B of the rectangle unit area. Note that z is a vector.

$$i := 0..19$$
  
 $B(F) := \sqrt{\frac{Area}{F}}$   $L(F) := F \cdot B(F)$   $z_i := \frac{i}{10} + 0.1$   $L(F) \cdot B(F) = 1$ 

Divide the rectangle into four sections:

$$X(F) := \frac{L(F)}{2}$$
  $Y(F) := \frac{B(F)}{2}$   $X(F) = 1.225$   $Y(F) = 0.204$ 

Define V and A for use in Newmark's rectangle equation.

$$V(z,F) := \sqrt{\frac{X(F)^{2} + Y(F)^{2} + z^{2}}{z^{2}}} \qquad A(z,F) := \frac{X(F) \cdot Y(F)}{z^{2}}$$

This expression, of the fraction of the applied load at z, is for the sum of four rectangles of dimension X by Y.

$$Irect1(z,F) := \frac{1}{\pi} \cdot \left[ \left( \frac{2 \cdot A(z,F) \cdot V(z,F)}{V(z,F)^2 + A(z,F)^2} \cdot \frac{V(z,F)^2 + 1}{V(z,F)^2} \right) + \operatorname{atan} \left( \frac{2 \cdot A(z,F) \cdot V(z,F)}{V(z,F)^2 - A(z,F)^2} \right) \right]$$
$$Irect2(z,F) := \frac{1}{\pi} \cdot \left[ \left( \frac{2 \cdot A(z,F) \cdot V(z,F)}{V(z,F)^2 + A(z,F)^2} \cdot \frac{V(z,F)^2 + 1}{V(z,F)^2} \right) + \operatorname{atan} \left( \frac{2 \cdot A(z,F) \cdot V(z,F)}{V(z,F)^2 - A(z,F)^2} \right) + \pi \right]$$

Irect(z,F) := if(A(z,F) > V(z,F), Irect2(z,F), Irect1(z,F))

 $\operatorname{Icirc}(z) := \left[1 - \left(\cos\left(\operatorname{atan}\left(\frac{r}{z}\right)\right)\right)^3\right]$ 

Results:

F = 6		r			$\operatorname{Irect}(z_i, F)$
z. =	$V(z_i, F) =$	$\frac{-}{z_{i}} = \frac{z_{i}}{1}$	$\operatorname{Irect}\left(\mathbf{z}_{i}, \mathbf{F}\right) =$	Icirc(z) =	$\frac{1}{\operatorname{Icirc}(z_i)} =$
0.1	12.457	5.642	0.961	0.995	0.967
0.2	6.288	2.821	0.824	0.963	0.856
0.3	4.258	1.881	0.675	0.897	0.753
0.4	3.261	1.41	0.556	0.807	0.689
0.5	2.677	1.128	0.465	0.708	0.657
0.6	2.298	0.94	0.396	0.613	0.646
0.7	2.036	0.806	0.343	0.528	0.649
0.8	1.846	0.705	0.299	0.454	0.659
0.9	1.704	0.627	0.264	0.392	0.674
1	1.594	0.564	0.235	0.339	0.692
1.1	1.508	0.513	0.21	0.296	0.71
1.2	1.439	0.47	0.189	0.259	0.729
1.3	1.383	0.434	0.17	0.228	0.747
1.4	1.337	0.403	0.154	0.202	0.764
1.5	1.298	0.376	0.141	0.18	0.781
1.6	1.266	0.353	0.128	0.161	0.796

Note that the augment function pastes matrices next to each other. The arrays generated by the computations that were not already vectors have to first be "vectorized with the vectorize function (z and functions of z are vectors, but not functions containing both z and F). This is done so that all elements in the matrix generated by the results can be exported to a spreadsheet.

$$M := augment\left(z, augment\left(\overrightarrow{V(z, F)}, augment\left(\overrightarrow{r}, augment\left(\overrightarrow{Irect(z, F)}, augment\left(\overrightarrow{Icirc(z)}, \overrightarrow{\overrightarrow{Irect(z, F)}}\right)\right)\right)\right)\right)$$



REPOR	Form Approved OMB No. 0704-0188				
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing this collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Department of Defense, Washington Headquarters Services, Directorate for Information Operations and Reports (0704-0188), 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302. Respondents should be aware that notwithstanding any other provision of law, no person shall be subject to any penalty for failing to comply with a collection of information if it does not display a currently valid OMB control number. PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.					
1. REPORT DATE (DD-MM-YY) March 2001	2. REPORT TYPE Technical Report	3. DATES COVERED (From - To)			
4. TITLE AND SUBTITLE		5a. CONTRACT NUMBER			
Influence of Wheel Load Shape of	5b. GRANT NUMBER				
Layer	5c. PROGRAM ELEMENT NUMBER				
6. AUTHOR(S)		5d. PROJECT NUMBER			
Karen S. Henry	5e. TASK NUMBER				
		5f. WORK UNIT NUMBER			
7. PERFORMING ORGANIZATION NAME(	8. PERFORMING ORGANIZATION REPORT NUMBER				
U.S. Army Engineer Research ar	d Development Center				
Cold Regions Research and Engi	neering Laboratory				
72 Lyme Road	1200	ERDC/CRREL TR-01-8			
Hanover, New Hampshire 03733					
9. SPONSORING/MONITORING AGENCT	NAME(3) AND ADDRESS(E3)	10. SPONSOR / MONITOR S ACRONTM(S)			
Office of the Chief of Engineers					
Washington, DC		11. SPONSOR / MONITOR'S REPORT NUMBER(S)			
12. DISTRIBUTION / AVAILABILITY STATE	MENT				
Approved for public release; dist	ribution is unlimited.				
Available from NTIS, Springfield	d, Virginia 22161.				
13. SUPPLEMENTARY NOTES					

#### 14. ABSTRACT

The U.S. Army design procedure to stabilize low-bearing-capacity soil with geotextiles is based on the assumption that the applied surface load (the wheel load) is in the shape of a circle. The maximum vertical stress that reaches the subgrade through overlying aggregate is then estimated on the basis of the assumption that the aggregate is an elastic, homogeneous, isotropic half-space and, therefore, that the stress distribution can be estimated by using the Boussinesq method. To study the extent to which the shape of the applied load influences the stress that reaches the subgrade through the aggregate layer, the maximum vertical stress at depth predicted by the Boussinesq method was computed and compared for circular and rectangular loads. A comparison of the maximum vertical stress beneath circular and rectangular loads as a function of depth indicated that the differences were insufficient to warrant a change in the design procedure for rectangular load geometries that have length/width ratios of 3 or less, and, furthermore, that assuming that the load is circular is conservative. For length/ width ratios of 3 or less, the maximum vertical stress applied is at least 85% of that applied by a circle.

15. SUBJECT TERMS	Boussinesq Stress distribution	Wheel lo	pad		
16. SECURITY CLASSIFICATION OF:			17. LIMITATION OF OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
a. REPORT	b. ABSTRACT	c. THIS PAGE			19b. TELEPHONE NUMBER (include area code)
U	U	U	U	13	