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**SIMULATION MODELS FOR THE ELECTRIC POWER  
REQUIREMENTS IN AN AUTOMATED GUIDEWAY  
TRANSIT SYSTEM**

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FINAL REPORT

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<p>16. Abstract</p> <p>This report describes a computer simulation model developed at the Transportation Systems Center to study the electrical power distribution characteristics of Automated Guideway Transit (AGT) systems. The objective of this simulation effort is to provide a means for determining the power distribution requirements of AGT systems and for evaluating their performances under varied operating conditions. Typical systems which could be modeled include the Morgantown Personal Rapid Transit System, the Dallas-Fort Worth Airtrans System, or one of the proposed Downtown People Movers.</p> <p>This work was conducted under sponsorship of the Advanced Group Rapid Transit (AGRT) Program of the Office of New Systems and Automation of the Urban Mass Transportation Administration. The purpose of the AGRT program is the development, evaluation, and verification of a second generation AGT technology which is capable of providing transit service in urban areas. The purpose of this report is to provide the reader with a working knowledge of the multi-vehicle AGT simulation model and its application to urban transit systems.</p> <p>This report specifically describes a Fortran computer program which models the electric power requirements of a typical AGT system. The inputs are: 1) the vehicle propulsion system characteristics; 2) the guideway deployment; and 3) the mission profile for each vehicle. The output is a series of tables which show the voltages, power, and harmonic currents in the electric power distribution system. Also included in this report is a complete listing of the Fortran program and an illustrative example of its application to multi-vehicle AGT systems is provided.</p>			
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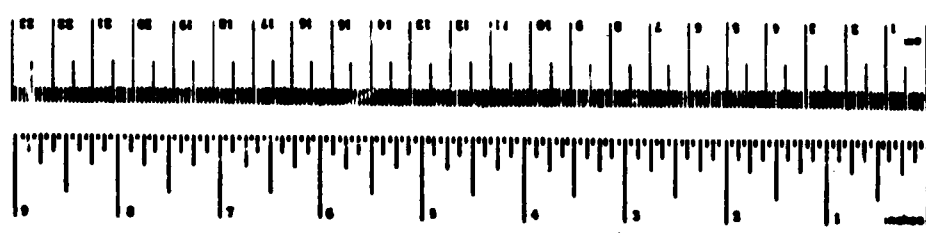
## PREFACE

This report describes a computer model developed at the Transportation Systems Center, Cambridge, Massachusetts, for the simulation of electrical power distribution characteristics of Automated Guideway Transit (AGT) systems. This work was conducted under the sponsorship of the Office of New Systems and Automation of the Urban Mass Transportation Administration (UMTA). The objective of this simulation effort is to provide the necessary software for rapid evaluation and assessment of AGT power system distribution requirements.

The author wishes to acknowledge the assistance of Mr. Roger Flanders of the Systems Development Corporation, Cambridge, Massachusetts for his valuable contributions in the development of certain elements of the computer model.

# METRIC CONVERSION FACTORS

Approximate Conversions to Metric Measures			Approximate Conversions from Metric Measures		
Symbol	When You Know	Multiply by	Symbol	When You Know	Multiply by
<b>LENGTH</b>					
m	meters	2.5	mm	millimeters	0.04
cm	centimeters	39	cm	centimeters	0.4
dm	decimeters	3.9	m	meters	3.9
km	kilometers	1.6	km	kilometers	0.6
<b>AREA</b>					
m <sup>2</sup>	square meters	0.5	m <sup>2</sup>	square meters	0.16
cm <sup>2</sup>	square centimeters	16	cm <sup>2</sup>	square centimeters	1.6
dm <sup>2</sup>	square decimeters	1.6	dm <sup>2</sup>	square decimeters	0.4
km <sup>2</sup>	square kilometers	0.4	km <sup>2</sup>	square kilometers	2.5
<b>MASS (weight)</b>					
g	grams	35	g	grams	0.035
kg	kilograms	2.2	kg	kilograms	2.2
lb	pounds	0.45	lb	pounds	0.45
oz	ounces	1.1	oz	ounces	1.1
<b>VOLUME</b>					
l	liters	0.26	l	liters	0.035
ml	milliliters	35	ml	milliliters	3.5
gal	gallons	0.26	gal	gallons	0.26
qt	quarts	0.95	qt	quarts	0.95
pt	pints	0.47	pt	pints	0.47
cu ft	cubic feet	2.8	cu ft	cubic feet	2.8
cu yd	cubic yards	0.76	cu yd	cubic yards	0.76
<b>TEMPERATURE (exact)</b>					
°C	Celsius temperature	1.8	°C	Celsius temperature	1.8
°F	Fahrenheit temperature	0.56	°F	Fahrenheit temperature	0.56



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## SUMMARY

This report describes a simulation model developed to study the electrical power distribution characteristics of Automated Guideway Transit (AGT) systems. This work was conducted under sponsorship of the Advanced Group Rapid Transit (AGRT) Program of the Office of New Systems and Automation, Urban Mass Transportation Administration (UMTA). The purpose of the AGRT program is the development, evaluation, and verification of a second generation AGT technology which is capable of providing transit service in urban areas. The computer simulation model developed at the Transportation Systems Center provides the required software for rapid evaluation of the complex power distribution of multi-vehicle AGT systems. The application of the computer model provides the system designers with important information on the anticipated power consumption characteristics of AGT systems. Such information is extremely valuable in both the initial design stage of system development as well as in later system evaluation studies aimed at assessing the overall system performance.

The purpose of this report is to provide the reader with a working knowledge of the multi-vehicle AGT simulation model and its application to urban transit systems. Basically the model is comprised of two separate elements which describe (1) the time-varying spatial characteristics of the power distribution network, and (2) the complex power



characteristics of the active (vehicle) loads. These elements are integrated into a comprehensive simulation model which accepts as prescribed input data the vehicle mission profile and computes as output data (in graphical or tabular format) the power consumption characteristics of the vehicle system network. The report includes a complete listing of the FORTRAN program and provides an illustrative example of its application to multi-vehicle AGT systems.

## 1. INTRODUCTION

This document describes a FORTRAN computer program which models the electric power requirements of a guideway transit system. Typical systems which could be modeled include: Morgantown Personal Rapid Transit System, Dallas-Fort Worth Airtrans, or one of the proposed Downtown People-Movers. All of these are Automated Guideway Transit (AGT) systems. The model is designed for studies which examine the impact on power consumption of the following:

- 1) Changing the vehicle propulsion system
- 2) Changing the power distribution system by moving/adding/deleting power substations
- 3) Incorporating regenerative braking
- 4) Altering the vehicles' mission profiles.

The model is general enough so that different AGT systems can be studied. The model is a modular one so that AGT system modifications are made either by changing modules (FORTRAN subroutines) or by changing parameters within a module (FORTRAN statements).

The important features of this model are: (1) the equivalent circuit for the electric power distribution system is automatically updated as the vehicles move, (2) the power flow problem is solved using the efficient Newton-Raphson algorithm, (3) harmonic currents (which are important in sizing power

distribution equipment) are included.

The remainder of this document is structured to serve as both a users' manual and a programmers' reference manual. Section 2 is an overview of the model and it contains a functional description of the model and its component parts. Section 3 contains the analysis used in the model. The simulation output is discussed in Section 4. Section 5 shows the conclusions of a model validation study using the AIRTRANS system.

Finally the procedure for preparing input data, and using the model are included in Section 6.

## 2. MODEL OVERVIEW

The power flow in an AGT system is a complex process. In a simplified form, three-phase electric power enters the AGT system via an electric utility connection. It flows through cables to power substations located along the guideway. At the substation, a step-down transformer converts it to a lower voltage, current is fed to the power rail on the guideway, and current may be fed to other buildings for housekeeping use (heating, cooling, lighting, etc.)

The power rail carries the current to the AGT vehicles on the guideway. Once the electric power reaches the vehicles, most of it is converted into thrust by the propulsion system, but some is used for vehicle housekeeping.

The thrust produced by the propulsion system is a function of time. The vehicle's control system will vary the thrust as it adjusts the velocity of the vehicle. As a result each vehicle's power demand varies with time, and the AGT system's power demand may also vary.

In effect the AGT is a power distribution network with (1) generators (the electric utility connection), (2) transmission lines (cables and power rail), and (3) loads (the AGT vehicles).

The solution to the power demand problem is to model the AGT system as a power distribution network and solve the load-flow problem repeatedly as the time-varying loads change and

as the transmission lines change. One point that needs to be made is that in simplifying the AGT system, we neglected regenerative braking. Regenerative braking means that during braking operations, the AGT vehicles can generate power and feed it back into the power distribution system. Thus our power distribution network has loads which vary in magnitude and sign (negative loads are generators). A block diagram of the AGT power distribution model is shown in Figure 2-1.

Note that the three quantities: (1) the vehicle's position, (2) the vehicle's power demand, and (3) the housekeeping power demand, are the independent variables. Together they determine the systems aggregate power demand.

Each vehicle in the AGT fleet is following a route along the guideway. The characteristics of this route (i.e. the grades, the expected vehicle velocity, and average headwinds encountered) and the characteristics of the vehicle's propulsion system (thrust or tractive force at the wheels vs. electric power into the motor) both determine the vehicle's time-varying power demand. Figure 2-2 shows a block diagram of the AGT vehicle model.

The inputs to the vehicle model, which relate to the guideway route, are functions of time. This set of functions (expected velocity, guideway grade, and headwind encountered) form part of a vehicle's mission profile.

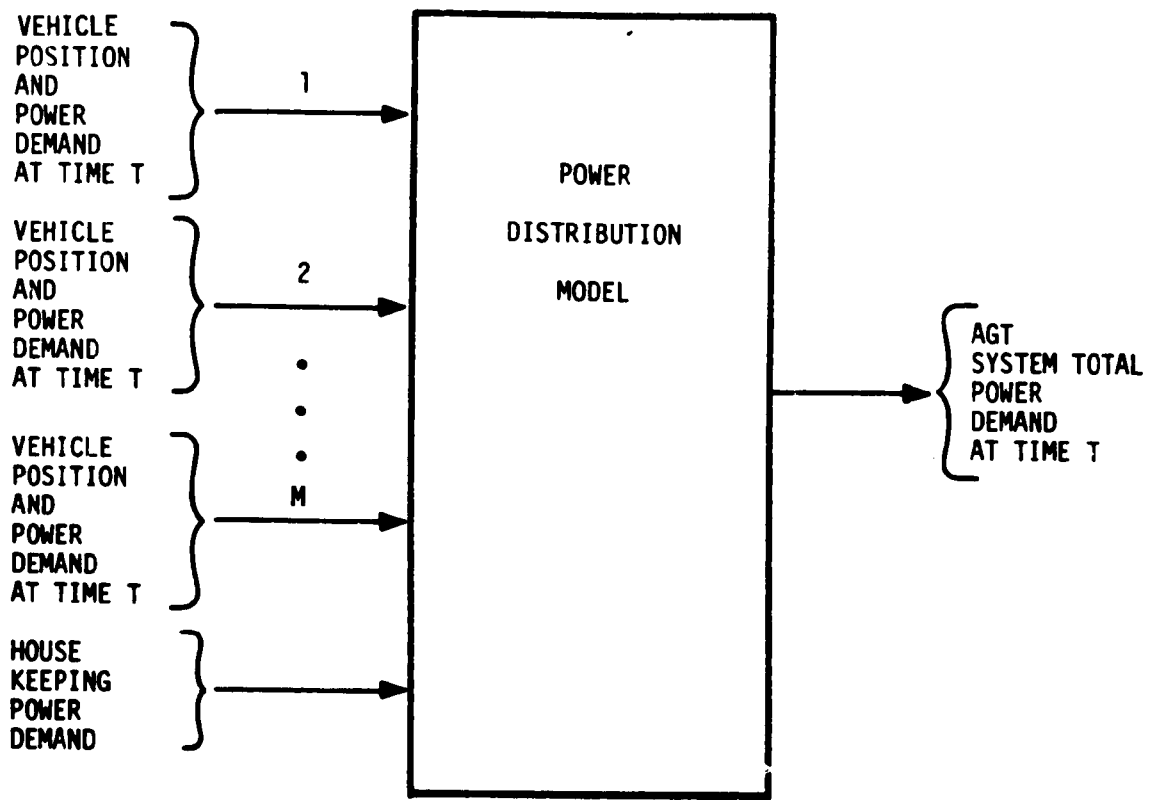


FIGURE 2-1. FUNCTIONAL VIEW OF THE POWER DISTRIBUTION MODEL

So far the propulsion system model has described how much power each vehicle is demanding, but not where in the power distribution network the demand is. After all, some of the AGT vehicles are moving along the power rail somewhere between stations. So we augment the mission profile to include a location code as a function of time. The code has two parts: (1) a prefix part to identify a guideway segment, and (2) a footage part to identify the distance from the segment reference end point.

By using the location code for vehicles and power substations, together with information on the spatial arrangement of guideway segments into the guideway network, the physical length of the power rail which separates vehicles and power substations can be found. (See Figure 2-3 for an example.) This physical length can be converted into the power rail's transmission line admittance for use in the power distribution model.

The transformation from substation and vehicle location codes into power-rail admittances is summarized by the guideway network model. That model is shown functionally in Figure 4.

In summary, the model has three parts:

1. AGT vehicle propulsion system model--it calculates the individual vehicle's power demand versus time.

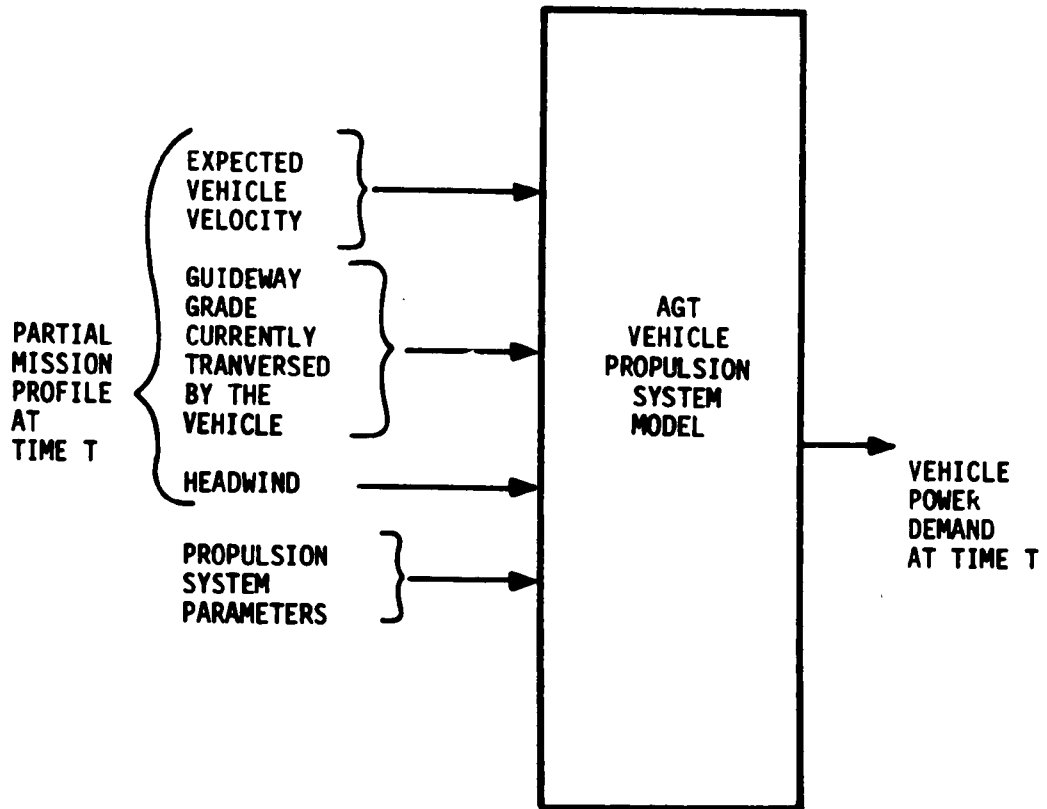
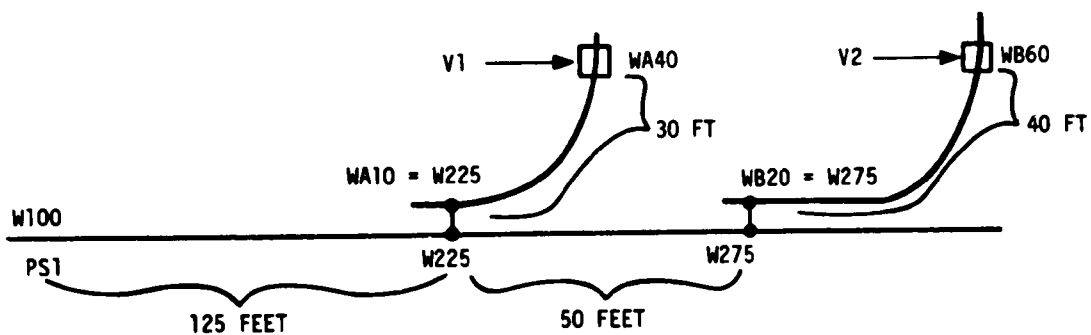


FIGURE 2-2. FUNCTIONAL VIEW OF A SINGLE AGT VEHICLE



KEY

V1 VEHICLE #1  
V2 VEHICLE #2  
W100 100 FOOT ON THE W GUIDEWAY  
P51 POWER SUBSTATION #1



DISTANCE

PS1 to V1  $125 + 30 = 155$   
PS1 to V2  $125 + 50 + 40 = 215$   
V1 to V2  $30 + 50 + 40 = 120$

FIGURE 2-3. THE USE OF LOCATION CODES TO FIND THE LENGTHS OF POWER RAIL AMONG VEHICLES AND POWER SUBSTATIONS

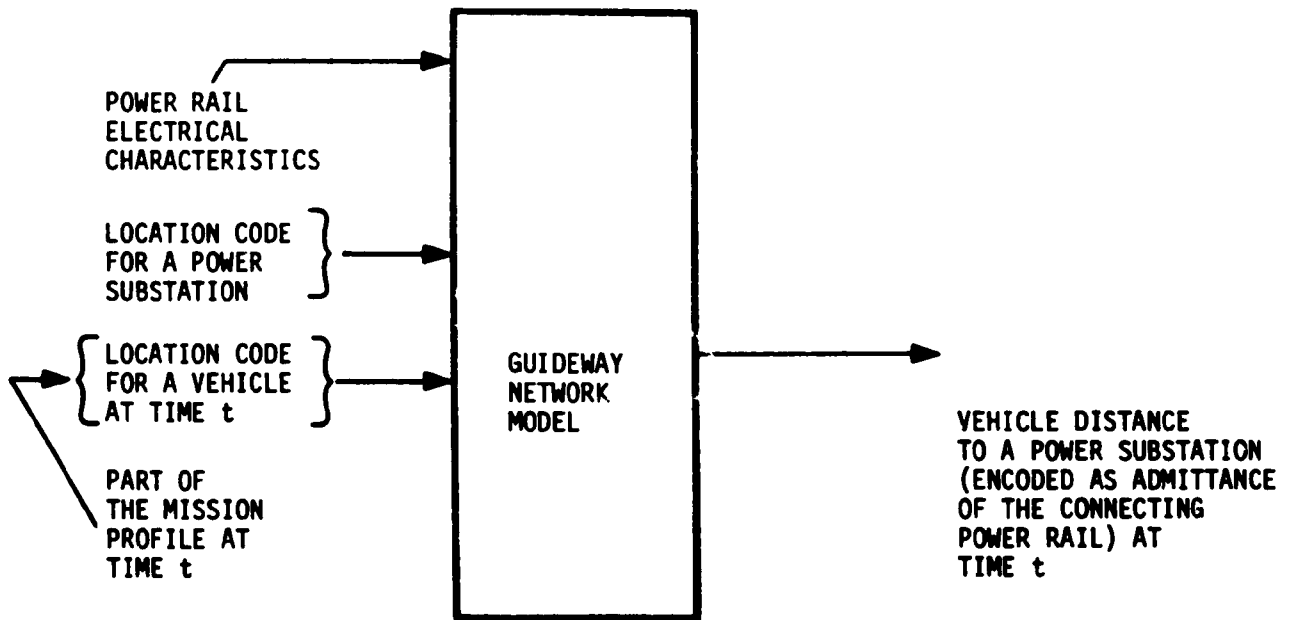


FIGURE 2-4. A FUNCTIONAL DIAGRAM FOR THE GUIDEWAY NETWORK MODEL

2. Guideway Network Model - It calculates the position of the individual vehicle versus time.
3. Power Distribution Model - It combines the individual power demands, based on their magnitude and their location, into a system power demand versus time.

## 2.1 OUTPUT

The model calculates a number of values in addition to the systems' electric power demand at each sample time. In general, the output data will depend on whether the power rail carries ac or dc. A general list of data follows:

1. Active power (P) at the power rail/vehicle interface. P, which is either dc or 60 Hz ac, is the real power used for the vehicles' propulsion system and its auxiliary loads (i.e. heating, lighting, cooling and control systems).
2. Reactive power (Q) at the power rail/vehicle interface. Q, which is present in the ac power rail case, is the quadrature component of the 60 Hz real power.
3. The power rail voltage. This is the voltage present at the power rail/vehicle interface. It is either dc or 60 Hz ac.
4. Distortion current (IO) at the vehicle. It is the RMS value of the harmonic currents which flow across the power rail/vehicle interface.

5. Distortion current at the utility. The RMS value of the harmonic currents which flow from the utility to the AGT system.
6. The active power (P) and reactive power (Q) at the utility.

Assuming that the utility is a "stiff" source and therefore its voltage (E1) is sinusoidal, then the apparent power (U) at the utility is given by Equation 2.1-1 (where \*\* indicates exponentiation).

$$U = \text{SQRT} (P ** 2 + Q ** 2 + E1 ** 2 * ID ** 2) \quad (2.1-1)$$

The above values are summarized in a table printed by the model at each sample time.

## 2.2 INPUT

The simulation involves data from two input files. The first is the guideway deployment data file. It contains information about the guideway which is relevant to the power distribution circuit. Each record in the file describes a branch in the power distribution circuit. The following list shows the type of information in the file:

1. Power feed point locations
2. Power cross-under locations. These are the points at which the two power rails are connected together at a merge or diverge structures.
3. Length of power rail segments between feed point locations and cross-under locations. These are used to calculate the impedance of the branches in the power distribution circuit.

4. Step-down transformer leakage impedance. If the branch between the utility and power feed point contains a step-down transformer, then its impedance plus any cable impedance may be included.

In summary, the guideway deployment data file describes the nodes and branches (in the power distribution circuit) which are geographically fixed.

The second is the mission profile file. It contains information about the vehicles' locations and operating conditions. Each record describes a point on an ideal mission profile. The following list shows the type of information in the file:

1. A time increment. This is the time interval which normally ellapses before the next mission profile point describes the vehicle (i.e., station dwell time).
2. A commanded velocity. This is the velocity which is an ideal velocity, and the vehicle accelerates or decelerates towards it.
3. Encountered grade. This measures the rise or descent in the guideway encountered by the vehicle. Note that if superelevation is present, then it can be combined with the grade to produce a compensated grade.
4. Encountered headwind.

5. Vehicle location. This is the position of the vehicle on the guideway where the mission profile point data becomes effective.

It should be noted that the mission profile is an ideal one from which a vehicle may deviate. For example, if the vehicle's propulsion system cannot provide the necessary tractive effort or if it is jerk-limited, then the current velocity differs from the commanded velocity.

### 2.3 SUBMODELS

This section considers the three submodels and their interfaces. The model can be considered a framework into which modules are inserted. The user creates these modules for a particular vehicle and a particular guideway deployment. Figure 2-5 shows the three models and their interfaces. A functional description for each submodel follows.

#### 2.3.1 Vehicle Propulsion Submodel

This model calculates the electrical power load which the vehicle produces at the power rail. This load is a function of the vehicle dynamics, motor, the power conditioning unit, and the auxiliary loads. The computation of the load rises from the following five steps:

1. Data on a vehicle's commanded mission profile (velocity, acceleration, encountered grade) and data on the vehicle's current state (actual velocity and position) are retrieved from tables.

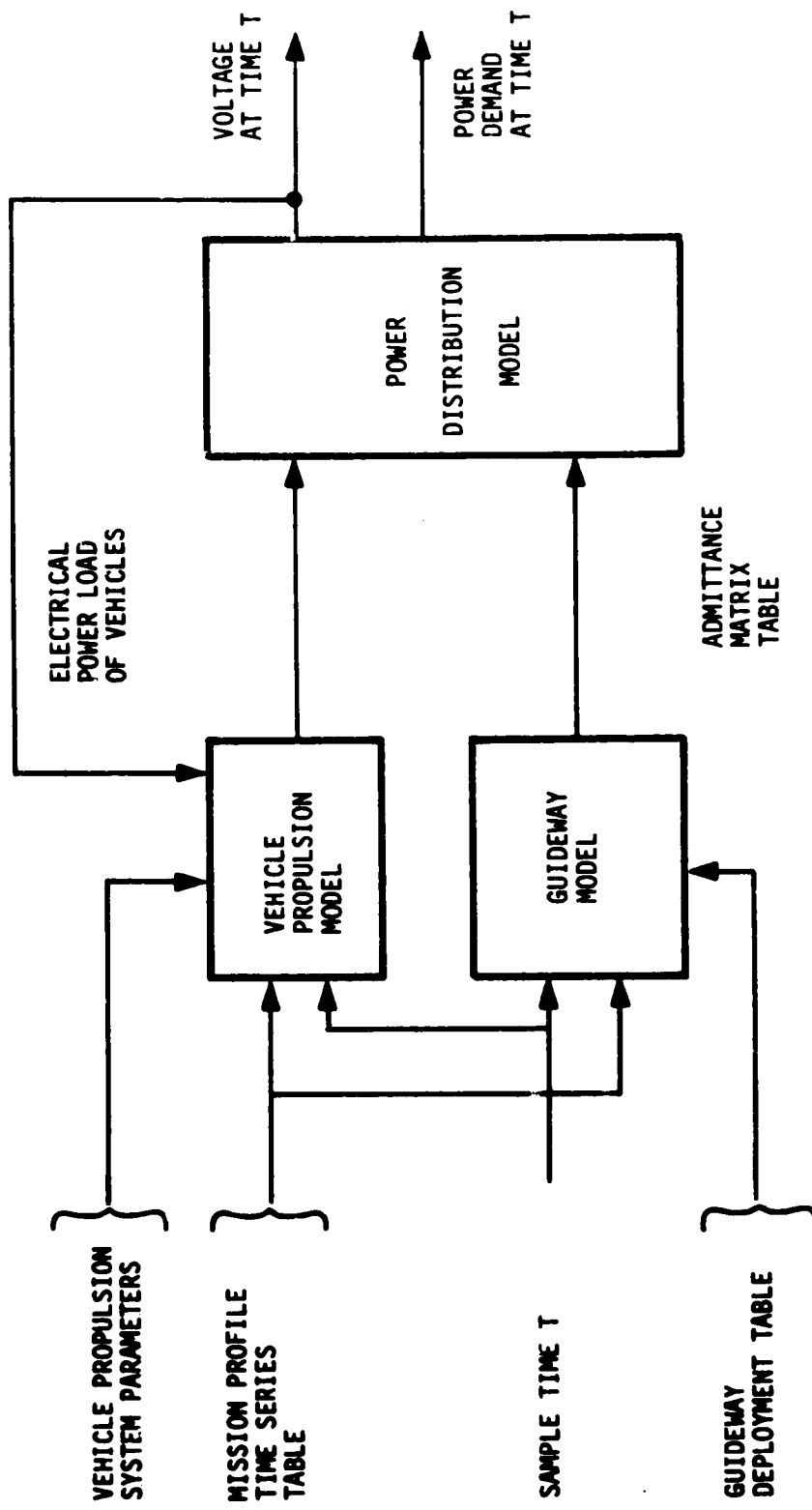


FIGURE 2-5. THREE SUBMODELS AND THEIR INTERFACES

2. The equations of motion for the vehicle (which include a quadratic polynomial in velocity to model tractive resistance) are solved for the mechanical power of the motor.
3. The equations for the motor are solved for the electric power into the motor terminals.
4. The equations for the power conditioning unit are solved for the electric power load at the power rail. These equations use as input the power at the motor terminals.
5. Data on the vehicles' load at the power rail/ vehicle interface and at the motor terminals is entered into tables which are accessible to the other submodels.

It should be noted that steps 1 and 5 are bookkeeping operations required to keep track of a fleet of vehicles. The user is only concerned with providing information about the dynamics, the motor system, and the power conditioning system of a single vehicle. The computations are automatically extended to the fleet of vehicles and tables are used to store the fleet data.

### 2.3.2 Guideway Deployment Submodel

This model is used for bookkeeping. In general, it is a table of power rail segments. The data recorded for each



segment includes its length and its adjoining segments. The computation done by this submodel entails updating a queue of the vehicles on each power rail segment. This is done using the current position of each vehicle.

### 2.3.3 Power Flow Submodel

This model solves the equivalent circuit for the power distribution network. It is an iterative computation, similar to the algorithm used by electric utility companies to simulate their power transmission networks. The difference here is that the loads are dynamic. That is, they vary with the voltage at the vehicle/power rail interface. The power flow submodel involves the following computational steps: (in this model, we use the name "node" where nodes are power feed points, power rail connections, or vehicle/power rail interface points).

1. Using the data from the guideway deployment table (which also specifies the vehicles located on each segment at a given time), calculate the node admittance matrix.
2. Assume initial node voltage values. Calculate the real and reactive power at the vehicle/power rail interface. This is the power needed at each vehicle. Call it the scheduled power.
3. Set an iteration counter to zero.
4. Calculate the power flowing in the power rail. From this the power delivered at each vehicle is determined.

5. Find the largest discrepancy between the power scheduled and power delivered.
6. If the discrepancy is small enough (less than one percent, say), then end the process with step 7. Otherwise go on to step 8.
7. Print-out the voltages and power values. The power distribution computation ends here.
8. Calculate a Jacobian matrix (its elements are partial derivatives of power with respect to voltage).
9. Invert the Jacobian matrix.
10. Use it to calculate the updated node voltages.
11. Recalculate the scheduled power at the power rail/ vehicle interfaces. Continue at step 4.

In Section 3, the details and analysis used for these models are presented.

### 3. ANALYSIS FOR THE MODELS

In this section, the data and analysis for a test case are discussed. The program listings in Appendix A have been set up for this same test case. In general, the vehicle is externally similar to the Morgantown vehicle, but with a 120 horsepower dc motor supplied by three-phase power rail through a variable-voltage rectifier. The guideway is a loop which is based on the Morgantown system. Two vehicles are moving around the loop following a mission profile which approximates the Morgantown operation (but with only two vehicles out of the usual fifteen vehicle fleet running). The analysis is divided into seven parts - one for each major subroutine.

#### 3.1 VEHICLE DYNAMICS

In this section the dissipative and conserved forces acting on the vehicle are used to calculate the real power at the wheels. When positive, this power must be supplied by the propulsion system. When negative, this power must be absorbed by friction brakes or some power source (regenerative braking).

Rolling friction force arises because of the roughness of the contact between the moving vehicle and the guideway. It is linearly proportional to the vehicle weight with an experimentally determined proportionality constant.

VM = 12,000 vehicle weight (lb)

A = 0.025 coefficient of rolling friction (n.d.)

GRADE = encountered grade in percent

FR = VM \* COS (GRADE/100.) \* A where FR is the rolling  
friction force (lb)

Coulombic friction forces arise because of wheel/guideway deformation and wheel bearing resistance. It is proportional to the vehicle weight and speed.

VV = vehicle velocity (mph)

VM = 12,000 vehicle weight (lb)

B = 0.00005 coulombic friction coefficient (n.d.)

FC = VM \* VV \* B where FC is the coulombic friction force (lb)

Aerodynamic drag forces arise because of vehicle motion relative to the air mass. It is proportional to frontal area and the vehicle's relative velocity squared.

C = 0.85 drag coefficient for leading vehicle, use 0.19  
for trailing vehicles

RHO = 0.002331 air density (slugs/ft \*\* 3)

CON1 = 1.46667 ft/sec per mph, conversion factor

VV = vehicle velocity (mph)

HW = encountered headwind (mph)

FD = 0.5 \* RHO \* C \* (VV+HW) \*\* 2 \* CON 1 \*\* 2

where FD is aerodynamic drag force (lb)

The total dissipative force can be found as RFORCE.

RFORCE = FR + FC + FD

The gravitational force arises because of a component of the vehicle's weight retards its uphill motion and advances its downhill motion. It is calculated as the component of weight tangent to the guideway.

VM = 12,000 vehicle weight (lb)

GRADE = encountered grade (%)

FG = VM \* SIN (ATAN (GRADE/100)) where FG is the  
gravitational force (lb)

Inertial force arises when the vehicle must change velocity  
and overcome inertia. It is proportional to the vehicle's  
mass and acceleration.

VM = 12,000 vehicle weight (lb)

KG = 32.174 gravity (lb/slug)

ACC = vehicle acceleration (mph/sec)

CON1 = 1.46667 ft/sec per mph Conversion

FI = VM/G \* ACC \* CON1 where FI is inertial force (lbs)

The total tractive force, FT, can be calculated. It is  
the thrust required at the wheels in order to maintain a given  
velocity and acceleration with an encountered guideway grade  
and headwind.

FT = RFORCE + FG + FI where FT is the tractive force (lb)

The power, PW, required to develop the necessary tractive  
force at the vehicle wheels is the product of that force and  
vehicle velocity.

FT = tractive force at wheels (lb)

VV = vehicle velocity (mph)

CON1 = 1.46667 ft/sec per mph Conversion Factor

CON2 = 1.356 watt per ft lb/sec Conversion factor

PW = FT\*VV\*CON1 CON2 where PW is the power at the  
wheels (watts)

In summary the variable PW is calculated as a function of VV, ACC, HW and GRADE. Subroutine VEHDYN does this computation.

### 3.2 VEHICLE MOTOR

In this section, the real power at the wheels is used to calculate the voltage and current at the motor terminals. These calculations model the motor and drive train components in the propulsion system.

The motor is a separately-excited dc machine rated at 120 horsepower and 600 volts dc. It is connected to the wheels via a gearbox and differential whose efficiency is assumed constant.

Four different modes of operation are considered:

1. Motoring with voltage control,
2. Motoring with field-weakening,
3. Regenerative braking,
4. Friction braking

Modes 2 and 3 are used at higher speeds - those above a 30 mph threshold. Modes 1 and 2 are used if the power at the wheels is positive. More precisely the table below shows the operating conditions for each mode (VV is velocity (mph), PW is power at the wheels (watts)).

<u>MODE</u>	<u>VELOCITY</u>	<u>POWER</u>
1	VV<30	PW>0
2	VV <sub>≥</sub> 30	PW>0
3	VV>30	PW<0
4	VV <sub>≤</sub> 30	PW <sub>≤</sub> 0

The power output at the dc machine shaft is a function of the drive train efficiency and the power at the wheels.

PW = power at wheels (watts)

GREFF = 0.92 gearbox efficiency (n.d.)

PMS = PW/GBEFF power at machine shaft (watts) if mode 1 or 2

PMS = PW\*GBEFF power at machine shaft (watts) if mode 3 or 4

Power losses in the dc machine are either stray load losses or windage losses.

PMS = power at machine shaft (watts)

PL3 = 0.01 ABS(PMS) where PL3 are the stray load loss (watts) computed as one percent of the absolute value of the power at the machine shaft.

VV = vehicle velocity (mph)

PL4 =  $1461.2 * (VV/30.)^{2.5}$  where PL4 are the windage losses (watts)

Note PL4 is modeled as a single term with the vehicle velocity raised to the 2.5 power. For mode 1, the terminal voltage and current are calculated as follows:

CF = 10 where CF is the rated field current (amp)

CON3 = 1.92 where CON3 is a motor constant (volts per mph per amp)

VV = vehicle velocity (mph)

EA = CON3\*V\*CF where EA is the armature back EMF (volt)

PL3 = stray load losses (watt)

PL4 = windage losses (watt)

VBD = 2.0 the comutator brush drop (volts)

PMS = power at motor shaft (watts)

EA = armature back EMF (volts)

CA = (PMS + PL3 + PL4) / (EA - VBD)

The terminal voltage can then be found

RA = 0.15 armature resistance (ohms)

VT = EA+RA\*CA where VT is the terminal voltage (volts)

For MODE 2, which is field weakening, the terminal voltage is held relatively constant at its 30 mph value, while the field current is reduced for speed control above 30.

Writing first an equation for power-in equals power-out plus losses,

CA = armature current

VT = 576 rated terminal voltage (volts)

VBD = 2.0 brush drop (volts)

PMS = power at machine shaft (watts)

PL3 = strong load loss (watts)

PL4 = windage loss (watts)

RA = armature resistance (ohms)

CA\*VT = PMS + CA\* VBD + CA\*\* 2 \* RA + PL3 + PL4

then we can solve it for the armature current.

$$CA = \frac{(VT - VBD) + \text{SQRT}((VT - VBD)** 2 + 4* RA* (PMS+PL3+PL4))}{2*RA}$$

The MODE 3, which is regenerative braking, the dc machine acts as a generator. In this case the armature voltage is greater than the machine terminal voltage, so that reverse armature current flows. Figure 3-1 shows this.



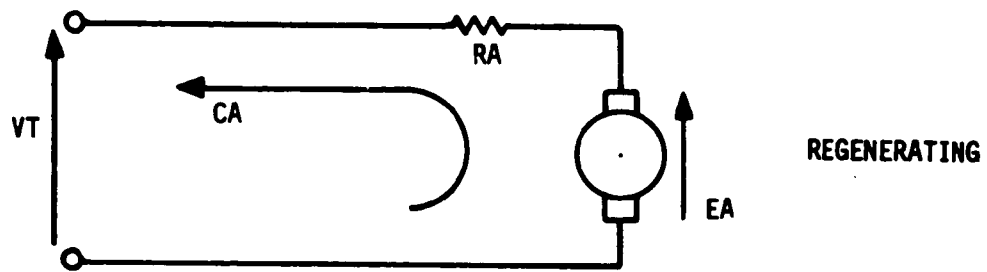
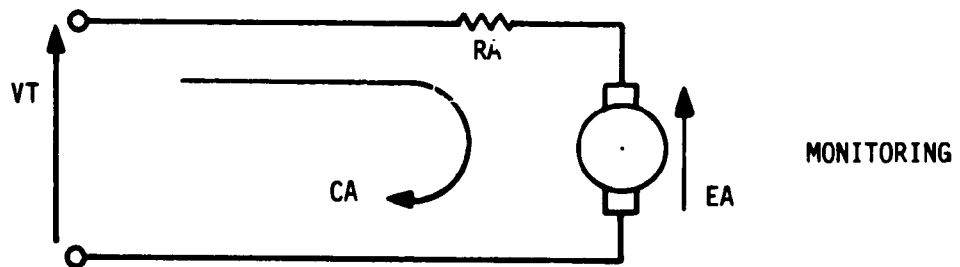


FIGURE 3-1. THE DC MACHINE'S ARMATURE EQUIVALENT CIRCUIT DURING MOTORING AND REGENERATION.

In this case the armature voltage and current are calculated as shown:

CF = 10 rated field current (amp)

CON3 = 1.92 motor constant (volts per mph per amp)

VV = vehicle velocity (mph)

EA = CON3\*VV\*CF armature back EMF (volts)

PMS = power output at machine shaft (watts) - note PMS=0.

PL3 = stray load loss (watts)

PL4 = windage loss (watts)

CA = (PMS + PL3 + PL4) / (EA + VBD)

RA = Armature resistance (ohms)

VT = EA + CA\*RA

For MODE 4, which is friction braking, the motor is disconnected and mechanical brakes dissipate the energy. The voltage and current are set essentially to zero.

VT = 0.01 machine terminal voltage (volts)

CA = 0.01 machine terminal current (amps)

These computations are carried out by subroutine MOTOR. The final step in MOTOR is to calculate the magnitude of VT and CA.

VMTR = ABS (VT)

IMTR = ABS (CA)

TMTR = 0 IF CA<sub>≥</sub>0

TMTR = 180 IF CA<0

In summary the function of the motor simulation is to calculate VMTR, IMTR, and TMTR using PW (the power at the wheels) and VV (the vehicle velocity).

### 3.3 VEHICLE POWER - CONDITIONING UNIT

In this section, the equations used to model the power-conditioning unit (PCU) are discussed. The PCU is a 3-phase fully-controlled bridge rectifier, which interfaces the 3-phase power rail with the dc machine terminals. When real power flows from the power rail to the machine terminals (Mode 1 or 2), the PCU provides a positive terminal voltage as current flows against the machine's back-EMF.

When real power flows from the machine terminals to the power rail (Mode 3), the machine's back-EMF is in the opposite direction from above. The machine's field current is reversed to produce this back EMF change. The machine's back-EMF is larger than the PCU output (which changes size as the firing angle is increased), so the armature current flows in the same direction. Figure 3-3 shows the principle components of the rectifier. It is a six-pulse, bridge circuit with an isolation transformer.

The analysis here follows one used by Schaefer (Schaefer, 1965). The SCR's in the rectifier have a commutation time in which the current flowing through one SCR is switched to another. A voltage drop, EX, is associated with this commutation. It is a function of the leakage reactance (on the secondary) of the transformer and the output current.

CA = output current (amps)

XC = 0.057 transformer leakage reactance on secondary (ohms)

EX = 3 XC \*CA/3.1416 voltage drop due to commutation (volts)



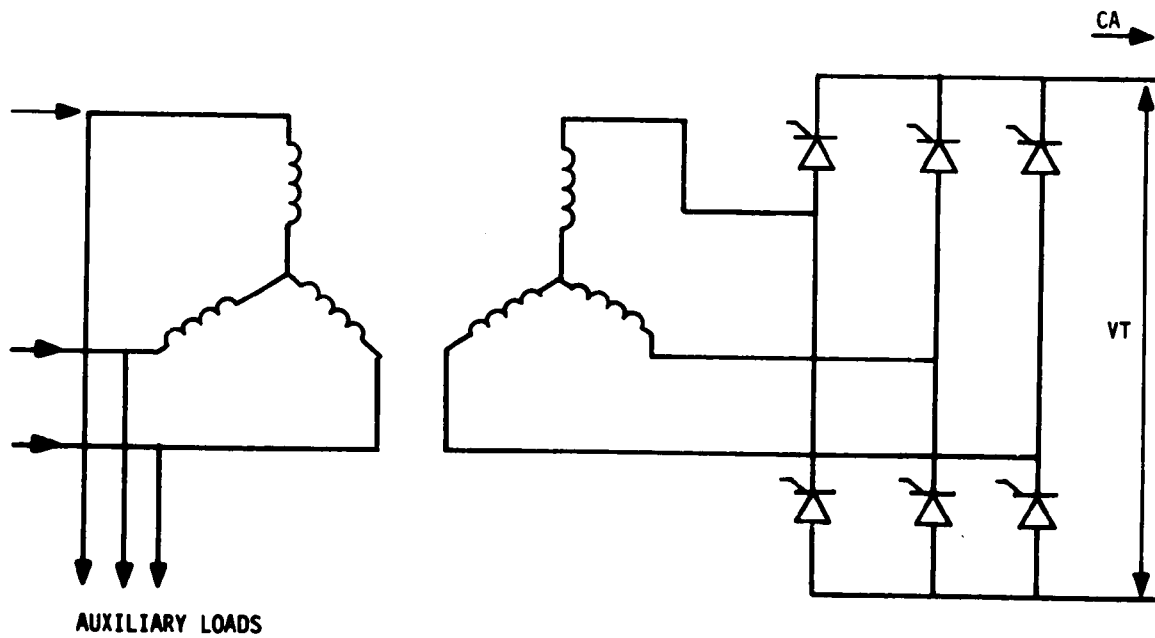


FIGURE 3-3. PCU RECTIFIER

The phase delay angle or thyristor firing angle controls the output voltage. The following equation calculates this angle, ALPHA, as a function of the commutation voltage drop, the desired output voltage, and the uncontrolled output voltage.

EX = commutation voltage drop

VRAIL = complex phase voltage at the power rail (p.u.)

VBASE = base phase voltage (volts)

EDO =  $3 \text{ SQRT}(6.) / 3.1416 \text{ CABS}(VRAIL) VBASE$  the  
uncontrolled output dc voltage (volts)

Note  $\text{SQRT}(X)$  is square root of X,  $\text{CABS}(X)$  is the  
absolute value of the complex quantity X

ED = VT the desired output dc voltage

ALPHA =  $\text{ACOS}((EX + ED)/EDO)$  the SCR firing angle  
(radians)

Note  $\text{ACOS}(X)$  is arc cosine of X

Using this firing angle, we proceed to calculate the power into the PCU. The calculation involves a correction factor to account for the effects of commutation. For this factor, the commutation voltage drop is converted into a commutation angle.

ED = PCU output dc voltage (volts)

EX = commutation voltage drop (volts)

EDO = uncontrolled output voltage (volts)

ALPHA = firing angle (radians)

AMU =  $\text{ACOS}((ED-EX)/EDO) - \text{ALPHA}$  the commutation angle  
(radians)

Note ACOS(X) is arc cosine of X

The correction factor is calculated in three steps:

ALPHA = firing angle (radians)

AMU = commutation angle (radians)

CF1 = .5 \* (COS(ALPHA) + COS(ALPHA + AMU))

CF2 = (2.\*AMU + SIN(2\*ALPHA) - SIN(2\*ALPHA + AMU))/  
(2.\*(COS(ALPHA) - COS(ALPHA + AMU)))

CF = 1./SQRT(CF1\*\*2 + CF2\*\*2)) the final correction  
factor for commutation

The power factor is next calculated.

ALPHA = firing angle (radians)

CF = commutation correction factor

PF = COS(ALPHA)\*CF the power factor at the PCU input

The real power into the PCU is equal to the real power,  
assuming negligible losses.

VT = PCU output voltage (volts)

CA = PCU output current (amps)

REF = VT\*CA real power input to the PCU (watts) in all  
three phases.

The reactive power into the PCU is calculated below.

EDO = uncontrolled output voltage (volts)

CF2 = correction factor for ratio of fundamental  
reactive power to uncontrolled dc power

CA = output current

AIMP = EDO\*CA\*CF2 the reactive power (VA) in all three  
phases.

The final equations are concerned with adding in the auxiliary loads and then normalizing the power values to per unit.

PAUX = 11,520 the real power for the auxiliary load  
(watts) in all 3 phases.

QAUX = 8,640 the reactive power for the auxiliary  
loads (VA) in all 3 phases.

PBASE = 333,000 BASE POWER (VA) for one phase

BP = (REF + PAUX)/PBASE/3 per unit real power at the  
power rail/vehicle interface.

BQ = (AIMP + QAUX)/PBASE/3. per unit reactive power at  
the power rail/vehicle interface.

#### 3.4 ADMITTANCE MATRIX

The power rail segments and power cables each have an impedance which affects the power flow from the utility connection to the vehicles. This impedance is modeled as a linear function of the guideway segment length or as a constant for the power cables (and step-down transformers). The impedance values are calculated as per unit impedances, converted to per unit admittances, and stored in a sparse admittance matrix. The admittance computation is summarized below.

##### CASE 1. A POWER RAIL BETWEEN NODE I AND J

ZGY = complex power rail impedance (per unit ohms per ft  
per phase)



D = distance along the power rail (ft) from node I to  
node J

$YD = 1./(D*ZGY)$

YD = complex power rail admittance (per unit mhos  
per phase) between nodes I and J

CASE 2. A CABLE OR TRANSFORMER BETWEEN NODE I AND J.

GWAY(II,4) = real part of the complex fixed impedance.  
between nodes I and J (see Section 6. using the model.)

GWAY(II,5) = imaginary part of the complex fixed impedance  
between nodes I and J. (See Section 6. using the model.)

$YD = 1./CMPLX(GWAY(II,4), GWAY(II,5))$

YD = complex power rail admittance (per unit mhos per  
phase) between nodes I and J.

The admittance computation involves nodes in the guideway  
network. A numbering convention is adopted for these electrical  
nodes. Node 1 is the electric utility connection. Nodes 2,  
3, ..., NCAR+1 are vehicles.

In summary, the function of the PCU simulation is to  
calculate:

- 1) BP - per unit real power into PCU at power rail/  
vehicle interface
- 2) BQ - per unit reactive power into PCU at the power  
rail/vehicle interface
- 3) ALPHA - SCR firing angle (radians), given as inputs.

- 1) UMTR - magnitude of the motor terminal voltage (volts)
- 2) IMTR - magnitude of the motor terminal current (amps)
- 3) TMTR - has value 0 if motor terminal voltage is greater than 0, has value 180 otherwise
- 4) VRAIL - complex power rail voltage (volts)

This simulation is carried out by the subroutine PCU.

These nodes are usually moving and have a current associated position (a guideway segment and displacement from the segment beginning). Nodes NCAR+2, NCAR+3, ..., SZ-1-1, SZ1 are fixed nodes along the guideway. These nodes include power feed points, diverge or merge power rail connections and power tie points between parallel segments. There are SZ1 nodes in total where SZ1 is a user-supplied parameter.

The admittance matrix is stored in several tables, but only nonzero values are stored in order to save space. The tables are shown in Figure 3-4 and their entries are described below. Note that in the two-dimensional admittance row I and column I are devoted to node number I. The entry  $Y(I,I)$  is the driving point admittance at node I. The entry  $Y(I,J)$ , where  $I \neq J$ , is the transfer admittance. Finally since  $Y(I,J)$  equals  $Y(J,I)$ , the tables of Figure 3-4 have only one entry for those pairs. Again, this is done to save space.

### 3.5 LOAD FLOW ALGORITHM

The equivalent circuit for the power distribution network is described by a set of simultaneous equations. They relate

a)

	1	2	3	4
1	A	0	B	C
2	0	D	0	0
3	B	0	E	F
4	C	0	F	G

b)

	Y	YP	YQ	NATCOL
1	A	1	1	5
2	D	2	2	0
3	E	3	3	7
4	G	4	4	0
5	B	1	3	6
6	C	1	4	0
7	F	3	4	0

FIGURE 3-4. a) AN ADMITTANCE MATRIX AND, b) ITS TABULAR REPRESENTATION

the voltages, current, and power at each node in the network. The load flow algorithm is just the iterative solution technique used on the equations. Many variations exist (Stott, 1974), but the one used here is a power-mismatch version in which a generalized Newton-Raphson method is used. The basic equations are given below. All quantities are fundamental (60HZ) values.

$$DP(k) - jDQ(k) = \text{CONJG}(E(k)) * I(k)$$

DP(k) = real power (per unit) delivered into the network at node k

DQ(k) = reactive power (per unit) delivered into the network at node k

E(k) = line to neutral voltage (per unit) at node k

I(k) = phase current (per unit) into the network at node k.

CONJG(E(k)) = complex conjugate of E(k)

The admittance values are brought into the analysis with the following network performance equation:

$$I(k) = \sum_{n=1}^{SZ1} y(k,n) * E(n)$$

I(k) = phase current (per unit) into the network at node k

y(k,n) = admittance (per unit) value from the admittance matrix. It is either a driving point admittance (if k=n) or a transfer admittance (if k≠n).

E(n) = line to neutral voltage (per unit) at node n.

SZ1 = number of network nodes

By combining these two equations the following set of nonlinear equations results:

$$DP(k) - jDQ(k) = \text{CONJG}(E(k)) \sum_{n=1}^{SZ1} y(k,n) * E(n)$$

The solution involves the following steps:

1. Find the admittance matrix so that  $y(k,n)$  values are known.
2. Assume initial voltages  $(E(k))$  at each node.
3. Find the  $P(k)$  and  $Q(k)$  values at each node in the network where a vehicle needs electric power. Note that the real power could be positive to model a regenerating vehicle or negative to model a power absorbing vehicle. These values are the scheduled power. They are functions of the vehicle's propulsion system, its current mission profile demand, and the node voltage  $E(n)$  at the power rail/vehicle interface.
4. Using the nonlinear system of network equations, with the admittance values  $y(k,n)$  and node voltages  $E(n)$ , find the delivered power. Any mismatch between the scheduled and delivered power can be corrected by revising the voltages  $E(n)$  at each node. Succeeding steps perform this correction.
5. Calculate the differences between scheduled and delivered power,

$$\text{DELTAP}(k) = P(k) - \text{DP}(k)$$

$$\text{DELTAQ}(k) = Q(k) - \text{DQ}(k)$$

$P(k)$  = real power scheduled (per unit) into the network at node  $k$

$\text{DP}(k)$  = real power delivered (per unit) into the network at node  $k$

$Q(k)$  = reactive power delivered (per unit) into the network at node  $k$

$\text{DQ}(k)$  = reactive power delivered (per unit) into the network at node  $k$

$\text{DELTAP}(k)$  = real power (per unit) mismatch at node  $k$

$\text{DELTAQ}(k)$  = reactive power (per unit) mismatch at node  $k$

6. The iteration may stop if the maximum  $\text{DELTAP}(k)$  and  $\text{DELTAQ}(k)$  are below some cutoff,  $\text{EPSIL}$  (Typically 0.10). If the maximum mismatch is too large, then the following steps revise the node voltages.

7. Calculate the current into the network at each node  $I(k)$ .

$$I(k) = (P(k) - jQ(k))/\text{CONJG}(E(k))$$

8. Solve a set of linear equations for the change in node voltages. These equations are shown in Figure 3-5. The Jacobian matrix,  $J$ , is a sparse matrix, so only the nonzero elements are stored in a table. Figure 3-6 depicts these tables. The standard Gauss-Jordan reduction algorithm is used to find the updated  $E(k)$  values.

$$\begin{bmatrix} \text{DELTAP}(k) \\ \text{-----} \\ \text{DELTAQ}(k) \end{bmatrix} = \begin{bmatrix} J_1 & J_2 \\ \text{-----} \\ J_3 & J_4 \end{bmatrix} \begin{bmatrix} \text{REAL}(\text{DELTAE}(k)) \\ \text{-----} \\ \text{IMAG}(\text{DELTAE}(k)) \end{bmatrix}$$

JACOBIAN

$$J_1 \text{ TERMS: } \frac{\partial p(k)}{\partial \text{REAL}(E(k))}$$

$$J_2 \text{ TERMS: } \frac{\partial p(k)}{\partial \text{IMAG}(E(k))}$$

$$J_3 \text{ TERMS: } \frac{\partial Q(k)}{\partial \text{REAL}(E(k))}$$

$$J_4 \text{ TERMS: } \frac{\partial Q(k)}{\partial \text{IMAG}(E(k))}$$

FIGURE 3-5. VOLTAGE CORRECTION EQUATIONS USING THE JACOBIAN MATRIX

a) JACOBIAN MATRIX

	1	2	3	4
1	A	0	E	0
2	0	B	0	F
3	G	0	C	0
4	0	H	0	D

b) TABLES FOR THE JACOBIAN

	JCOB	JCR	JCC	JNC
1	A	1	1	5
2	B	2	2	6
3	C	3	3	0
4	D	4	4	0
5	E	1	3	0
6	F	2	4	0
7	G	3	1	3
8	H	4	2	4

FIGURE 3-6. JACOBIAN MATRIX AS A SPARSE ARRAY.  
 (a) THE MATRIX, (b) THE TABLES



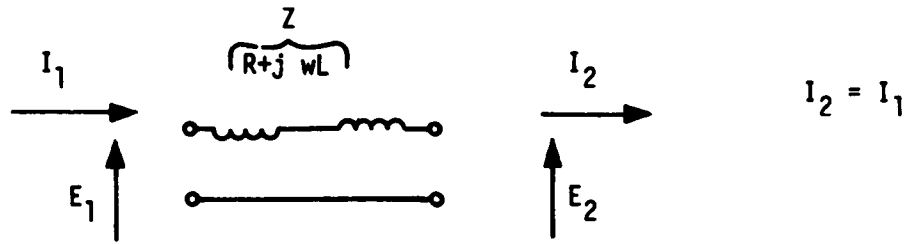


FIGURE 3-7. EQUIVALENT CIRCUIT FOR ONE PHASE OF A POWER RAIL SEGMENT. THE IMPEDENCE  $Z$  IS A FUNCTION OF LENGTH

9. The computation continues at step 3.

This computation is carried out by the subroutine named NR. In addition the subroutine FORMY is used for the admittance matrix formation and subroutines GETJ and PUTJ handle the Jacobian matrix manipulation.

### 3.6 DISTORTION POWER

In this section the high frequency currents are used to calculate the power components which are not included in the fundamental real and reactive power. The analysis of the high frequency currents is concerned with two types of locations in the power distribution network. One is the power rail/vehicle interface where the nonlinear PCU generates the harmonic currents. Second is the utility connection where the currents impact the supply network and where the metering is located.

In order to simplify the analysis, two assumptions are made: (1) the voltage waveform at the utility connection is sinusoidal (i.e., it is a stiff source), and (2) the power rail is a short transmission line (i.e., it is a constant series impedance dependent on rail length). The equivalent circuit for a power rail segment is shown in Figure 3-7.

This analysis involves two steps. First the harmonic currents at each power rail/vehicle interface are calculated. Second these currents are combined into the current at the utility connection.

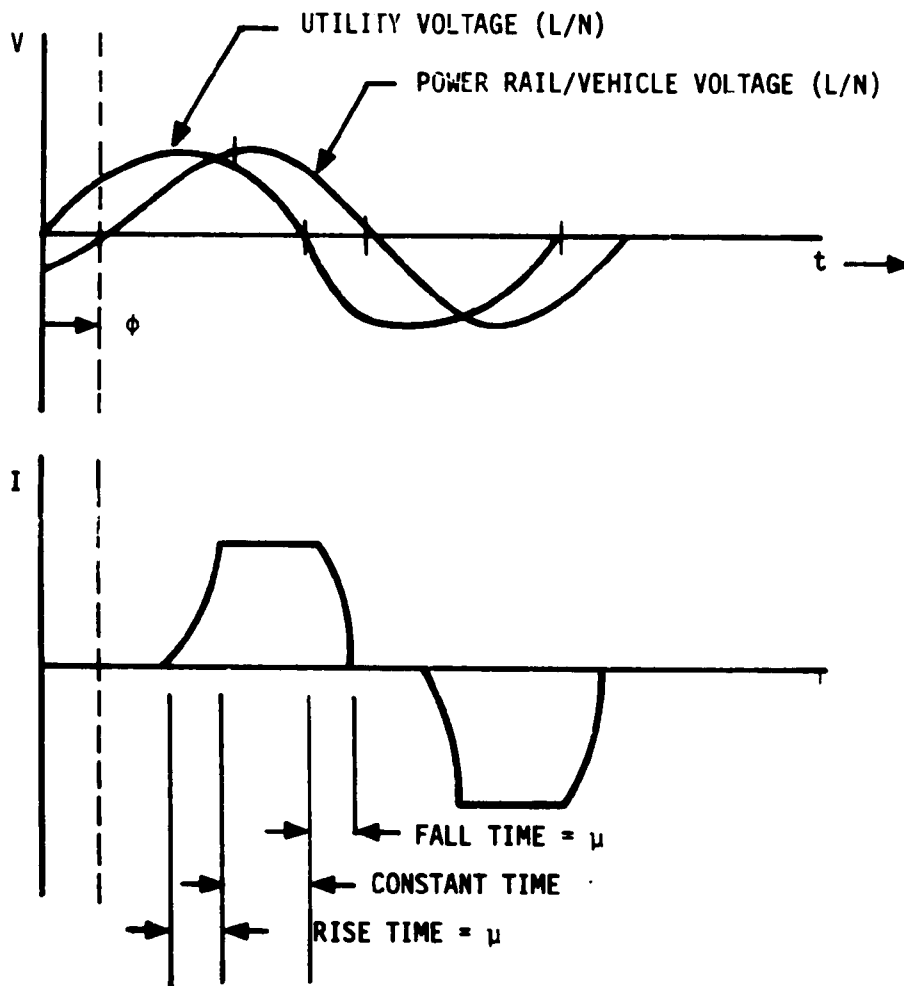


FIGURE 3-8. LINE TO NEUTRAL VOLTAGE AT THE UTILITY AND AT POWER RAIL/VEHICLE INTERFACE

FIGURE 3-9. LINE CURRENT AT THE POWER RAIL/VEHICLE INTERFACE

The harmonic currents are calculated by Fourier analysis on the wave forms. The current wave form used is shown in Figure 3-8. This wave form is discussed in the literature (Schaefer, 1965, p 327-334). It represents the line current for one phase when two effects are present: (1) a delay due to the SCR firing angle  $\alpha$ , and (2) a rise (fall) which is not instantaneous commutation.

The expression to describe the current curve is given below for the three segments (rise, constant, fall).

$\alpha$  = SCR Firing Angle (radians)

$\gamma$  =  $2\pi/3$  Length of current pulse with instantaneous commutation (radians)

$\mu$  = commutation angle (radians)

ID = output dc current from PCU (amp)

IB = per unit base Current (amp)

IR = PCU input line current during Rise Time as a function of  $\omega t$  (per unit amp)

$IR(\omega t) = ID * (\cos(\alpha) - \cos(\omega t + \gamma/2)) / (\cos(\alpha) - \cos(\alpha + \mu)) / IB$

IC( $\omega t$ ) = ID/IB PCU input line current during constant time as a function of  $\omega t$  (per unit amp)

IF = PCU input line current during fall time as a function of  $\omega t$  (per unit amp)

$IF(\omega t) = ID * (1 - (\cos(\alpha) - \cos(\omega t - \gamma/2)) / (\cos(\alpha) - \cos(\alpha + \mu))) / IB$

The Fourier analysis, which yields the harmonic currents, is performed next. Because of the positive/negative symmetry in

the current wave form, the integral is evaluated over a half period.

$I_D$  = output dc current from PCU(amp)

$\alpha$  = SCR firing angle (radians)

$\mu$  = commutation angle (radians)

$I_R(\omega t)$  = PCU input line current during rise time (per unit amp)

$I_C(\omega t)$  = PCU input line current during constant time (per unit amp)

$I_F(\omega t)$  = PCU input line current during fall time (per unit amp)

$A(N) = (\text{SQRT}(2))/\pi^*$

$$\left( \int_{\alpha-\gamma/2}^{\alpha+\mu-\gamma/2} I_R(\omega t) * \sin(N\omega t) d\omega t \right. \\ + \int_{\alpha+\mu-\gamma/2}^{\alpha+\gamma/2} I_C(\omega t) * \sin(N\omega t) d\omega t \\ \left. + \int_{\alpha+\gamma/2}^{\alpha+\mu-\gamma/2} I_F(\omega t) * \sin(N\omega t) d\omega t \right)$$

$A(N)$  = RMS value of the N-th line current harmonic -  
the quadrature component (per unit amp).

$B(N) = (\text{SQRT}(2))/\pi^*$

$$\begin{aligned}
& \int_{\alpha-\gamma/2}^{\alpha+\mu-\gamma/2} IR(\omega t) * \cos(N\omega t) \, d\omega t \\
+ & \int_{\alpha+\mu-\gamma/2}^{\alpha+\gamma/2} IC(\omega t) * \cos(N\omega t) \, d\omega t \\
+ & \int_{\alpha+\gamma/2}^{\alpha+\mu+\gamma/2} IF(\omega t) * \cos(N\omega t) \, d\omega t
\end{aligned}$$

(B/N) = RMS value of the N-th line current harmonic-in phase component (per unit AMP). Appendix C shows the result of evaluating these integrals.

The final step in the analysis is the combining of the harmonic current components at the power rail/vehicle interface into harmonic currents at the utility connection. For this, each  $N^{\text{th}}$  order harmonic is considered separately. So in the discussion that follows the fifth harmonic ( $N=5$ ) is used but  $N$  could be 5,7,11,13,...,6N-1,6N+1. Figure 3-9 shows a small power rail distribution system.

By using superposition, the  $N^{\text{th}}$  harmonic current at the utility connection,  $I_1$ , can be found. Each current source corresponding to a vehicle is treated separately as the others are replaced by their infinite internal impedance. Since  $Z_1$ ,  $Z_2$ , and  $Z_3$  are series impedances for the short transmission line model, the current  $I_1$  is  $I_2 + I_3$ . In general the  $N^{\text{th}}$  harmonic current flowing from the utility into the power rail

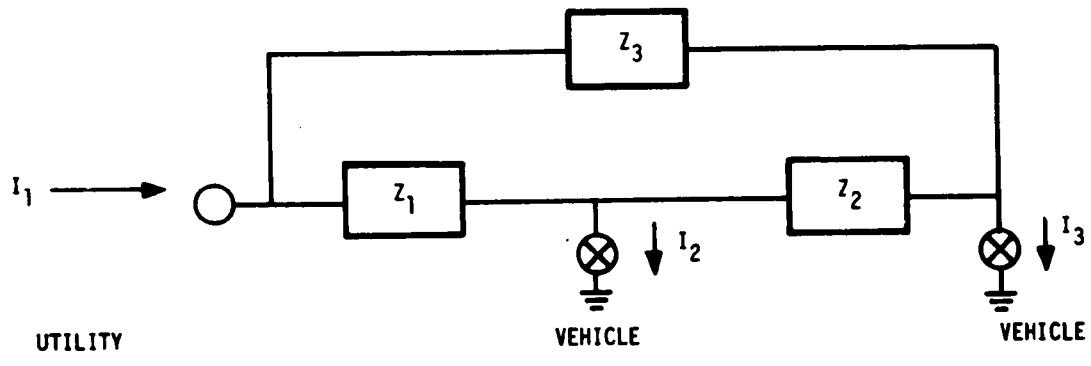


FIGURE 3-10. A SMALL POWER RAIL DISTRIBUTION SYSTEM

network is the sum of the  $N^{\text{th}}$  harmonic currents flowing into the power rail/vehicle nodes. The sum is a vector sum taking into account the phase angles. To illustrate, Figure 3-10 is presented.

Each fifth harmonic at a vehicle has a phase angle shown in Figure 3-10 as  $\phi$ , which is the number of degrees by which it lags the fundamental voltage at the utility (our reference).

The angle  $\phi$  is calculated by the following equation:

$N$  = harmonic number (n.d.)

$B(N)$  = RMS value of the  $N^{\text{th}}$  line current harmonic-in phase component (per unit amp).

$A(N)$  = RMS value of the  $N^{\text{th}}$  line current harmonic-quadrature component ( per unit amp)

$\phi_2 = \text{ATAN}(A(N)/B(N)$

$\phi_2$  = angle by which  $N^{\text{th}}$  harmonic current at vehicle lags fundamental voltage at vehicle (radians)

$\phi_1$  = angle by which fundamental voltage at the vehicle lags fundamental voltage at the utility (radians)

$\phi = N * \phi_1 + \phi_2$

$\phi$  = angle by which the  $N^{\text{th}}$  harmonic current at the power rail/vehicle interface lags the fundamental voltage at the utility (radians)

The fifth harmonic at the electric utility is only one of several harmonics which may be present. The RMS values of all these harmonics can be found from the sum of the squares.



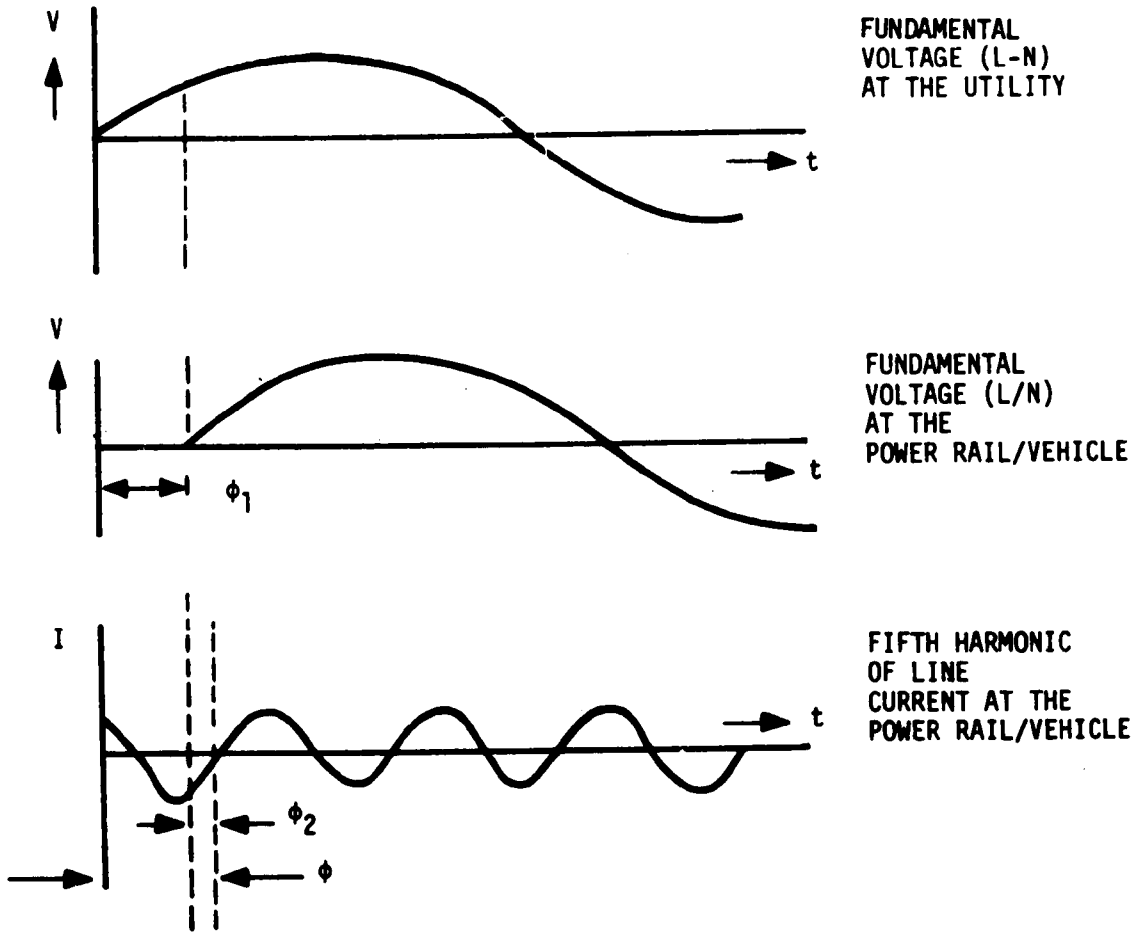


FIGURE 3-11. HARMONIC CURRENT AT THE POWER RAIL/VEHICLES WITH VOLTAGE WAVEFORMS FOR REFERENCE

$I_N$  = RMS value of the  $N^{\text{th}}$  harmonic current at the utility node

$$DC(1) = \text{SQRT} \left( \sum_N I(N)^2 \right)$$

DC(1) = RMS value of the distortion current at the utility node (per unit amp).

The distortion power can be calculated as the product of the utility voltage and distortion current.

DC(1) = RMS distortion current (p.u.)

E(1) = utility voltage (L-N) (p.u.)

DKVA = E(1) \* DC(1)

DKVA = distortion power at the utility (p.u.)

The total apparent KVA may also be calculated.

P(1) = active power at the utility (p.u.)

Q(1) = reactive power at the utility (p.u.)

DKVA = distortion power at the utility (p.u.)

TKVA =  $\text{SQRT}(P(1)^2 + Q(1)^2 + DKVA^2)$

TKVA = total apparent KVA at the utility (p.u.)

The distortion power is calculated from a Fourier analysis of the current wave shape. The parameters of the waveshape are  $\alpha$  (SCR firing angle) and  $\mu$  (commutation angle). The outputs are the distortion power and total apparent KVA at the electric utility connection node. This modeling is done by routine DISTOR.

### 3.7 VEHICLE POSITION UPDATES

Periodically during the simulation, the vehicle positions are updated. This section presents the analysis used to calculate

these updated positions. The analysis involves data for each vehicle from three sources:

1. The commanded mission profile point, which is a requested velocity, and encountered grade, encountered headwind, a position on the guideway and a time interval before the next profile point should be attained.

2. The current vehicle state, which is like the commanded mission profile point but with actual rather than commanded values used.

3. The propulsion system limitations for the maximum acceleration, jerk, thrust and power at the wheels.

The strategy for using this data is illustrated in Figure 3-11. Three commanded mission profile velocity points ( $CV(t)$ ,  $CV(t+1)$ ,  $CV(t+2)$ ) are shown, together with the actual velocity ( $AV(t+1)$ ). Each commanded velocity is treated as a speed limit (which the vehicle accelerates or brakes to achieve). These limits change in two ways. First, if a vehicle passes the guideway position associated with a commanded velocity profile point, the commanded velocity changes. That is, referring to Figure 3-12, each point in time has a position ( $P(t)$ ,  $P(t+2)$ ). It is assumed that the guideway conditions (grade, headwind, speed limit) which are recorded at a time such as  $t+1$  for position  $P(t+1)$  remain constant until position  $P(t+2)$ . A problem arises when a vehicle is dwelling (velocity is zero). In this case it will never pass the next guideway position and

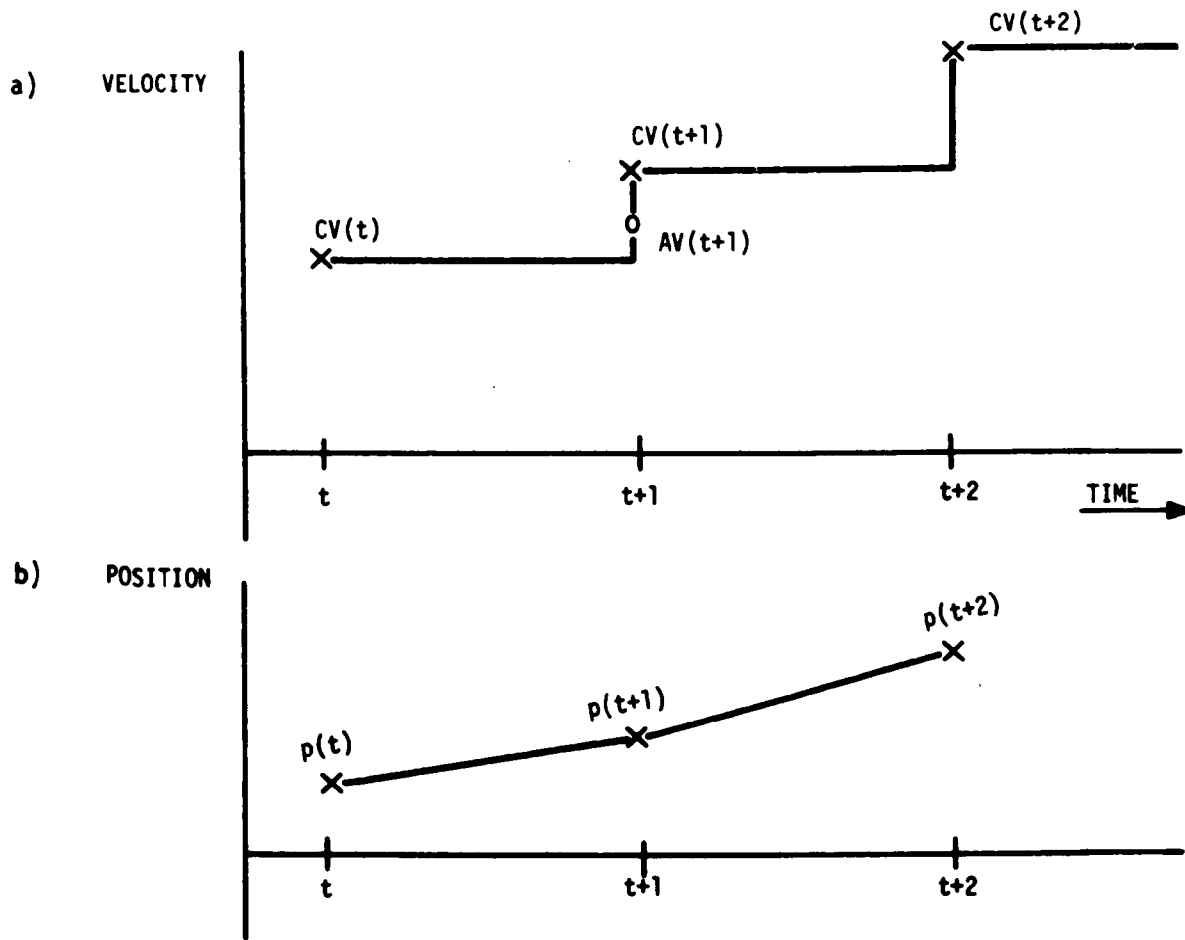


FIGURE 3-12. (a) COMMAND AND ACTUAL VELOCITY PROFILE.  
 (b) POSITION PROFILE POINTS.

"move" to a new commanded mission profile point. To correct for this a second method is employed to change mission profile points. This one says if the velocity is zero and the time interval is exceeded, then use the next profile point. The next point should have a nonzero velocity, which is used to calculate an acceleration to move the vehicle. The position of each vehicle is calculated by the following formula:

DT = time interval (sec)

POS = vehicle displacement (ft) from last guideway reference point. (Its position at some previous time t.)

VVEL = vehicle velocity (mph) at time t (actual velocity achieved)

VACC = vehicle acceleration (mph/sec) during interval DT

C1 = 1.4667 conversion factor to change mph into feet/sec.

NEWPOS =  $POS + VVEL * DT + 0.5 * VACC * C1 * DT * DT$

NEWPOS = vehicle displacement (feet) from last guideway reference point. (Its position at time t + DT)

It should be noted that the acceleration VACC takes into account jerk acceleration and thrust limitations. The new velocity can also be found.

DLEVEL = vehicle velocity (mph) at time t

VACC = vehicle acceleration (mph/sec) during interval DT

DT = time interval (sec)

VVEL = vehicle velocity (mph) at time t + DT

This simulation is done by subroutine NUPNT which uses the mission profile data, current vehicle state information, and subroutine VEHDYN to calculate a new position and velocity for the entire vehicle fleet.

#### 4. SAMPLE OUTPUT - AGRT

In this section, a sample run is described. From this run the reader can see the type of output data produced by the simulation. This data, together with the mission profile input data (Appendix A), provides a complete check case for the program.

The output consists of three parts: (1) a record of the guideway data used for input, (2) a record of the mission profile data used for input (it is a partial listing of only the first 15 lines of the table), (3) output tables showing the vehicles' positions, the power flow from the utility connection, the network node voltages, and the state of the propulsion system for each vehicle. The latter group (3) of output tables are repeated for each sample time.

Table 4-1 is the complete output for two vehicles running along a loop (similar to the Morgantown system). The power rail is pictured in Figure 4-1. In this case the two vehicles become electrical nodes (buses) numbered 2 and 3. The reader should note that the vehicles are identified as vehicle number 1,2,...,NCAR, but once they are included in the equivalent electric circuit, they are node (bus) number 2,3,...,NCAR+1.

The list below describes the output data:

1. Guideway segments at time-n sec. This table displays the guideway input data but appends the node

number for any vehicle on that segment.

2. Power flow summary. This table displays the power flow along each individual cable which is connected to the electric utility connection. It is fundamental P and Q in per unit.
3. Total apparent KVA. This is the apparent power supplied by the utility in per unit.
4. Bus voltages.

This table lists the bus voltage in per unit, the fundamental power into the network in per unit (loads are negative, generators are positive) and the distortion current in per unit.

5. State of the vehicles

For each vehicle number (1 to NCAR) this table lists a vehicle position (a guideway identifier and a footage displacement), current velocity (in MPH), acceleration (in MPH/s) ideal or commanded velocity (in MPH), encountered grade (in percent), encountered headwind (in MPH), motor terminal voltage (volts), motor terminal current (amps) number of passengers, number of cars coupled together, a mode (1-voltage controlled speed, 2-field-weakening controlled speed, 3-regenerative-braking, 4-friction braking), the power conditioning units firing angle (alpha-in radians).

These tables are written by the subroutines named: RITE or VEHSUM. The labels, formats and variables are described there.



TABLE 4-1.

MORGANTOWN GUIDEWAY DATA - THREE LINES

GUIDEWAY DATA									
FROM	TO	SEGMENT	START	END					
6.	7.	E	11650.000	12285.000					
6.	5.	M3	12285.000	17160.000					
5.	4.	M4	17160.000	21903.000					
4.	4.	N	1.000	2050.000					
4.	5.	M1	2050.000	6785.000					
5.	6.	M2	6785.000	11650.000					
1.	4.	TT	0.000	0.025					
1.	5.	TT	0.000	0.025					
1.	6.	TT	0.000	0.025					
AGT 2									
0	746	73	224	0					
0	385	435	584	0					
2	2								
1	413								
0	0								
3.0000	0.0000	0.0000	0.0000W	903.11					
1.0000	1.0200	0.0000	0.0000W	905.35					
1.0000	2.0400	0.0000	0.0000W	908.64					
1.0000	2.1760	0.0000	0.0000W	911.73					
1.0000	2.3120	0.0000	0.0000W	915.23					
1.0000	2.4480	0.0000	0.0000W	918.92					
1.0000	2.5840	0.0000	0.0000W	922.81					
1.0000	2.7200	0.0000	0.0000W	927.74					
1.0000	2.8560	0.0000	0.0000W	932.77					
1.0000	2.9920	0.0000	0.0000W	937.75					
1.0000	3.1280	0.0000	0.0000W	942.73					
1.0000	3.2640	0.0000	0.0000W	947.71					
1.0000	3.4000	0.0000	0.0000W	952.69					
1.0000	3.5360	0.0000	0.0000W	957.67					
1.0000	3.6720	0.0000	0.0000W	962.65					
GUIDEWAY SEGMENTS AT TIME = 0 SEC									
6.	7.	E	11650.000	12285.000	3.	0.	0.	0.	0.
6.	5.	M3	12285.000	17160.000	0.	0.	0.	0.	0.
5.	4.	M4	17160.000	21903.000	0.	0.	0.	0.	0.
4.	4.	N	1.000	2050.000	2.	0.	0.	0.	0.
4.	5.	M1	2050.000	6785.000	0.	0.	0.	0.	0.
5.	6.	M2	6785.000	11650.000	0.	0.	0.	0.	0.
1.	4.	TT	0.000	0.025	0.	0.	0.	0.	0.
1.	5.	TT	0.000	0.025	0.	0.	0.	0.	0.
1.	6.	TT	0.000	0.025	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 0 SEC :

POWER FLOW FROM NODE 1 TO NODE	4 IS	0.0100	-0.0084
POWER FLOW FROM NODE 1 TO NODE	5 IS	0.0044	-0.0030
POWER FLOW FROM NODE 1 TO NODE	6 IS	0.0048	-0.0540

THE TOTAL APPARENT KVA IS 0.073040 IN PER UNIT

BUS	VOLTAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0300	0.0300	0.0119
2	0.9998	-0.0065	-0.0115	0.0000
3	0.9981	-0.0061	-0.0184	0.0119
4	0.9998	-0.0003	0.0000	0.0000
5	0.9999	-0.0001	0.0000	0.0000

TABLE 4-1 (CONT'D)

NO.	STATE OF THE VEHICLES AT 0 SEC	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	MO.
1	W	993.11	0.00	-0.48	0.00	0.00	0.00	0.0	0.00	10	1	4.	1.57	1
2	E	11766.60	5.10	0.34	5.10	0.00	0.00	109.0	63.0	10	1	1.	1.43	2

BUILDWAY SEGMENTS AT TIME = 1 SEC														
0.	0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N3	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N4	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.W	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N2	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	9.000	9.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

BUILDWAY SEGMENTS AT TIME = 2 SEC														
0.	0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N3	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N4	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.W	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N2	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	9.000	9.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	0.WT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 2 SEC

POWER FLOW FROM MODE 1 TO MODE	4 IS	0.4104	-0.0044
POWER FLOW FROM MODE 1 TO MODE	5 IS	0.0022	-0.0019
POWER FLOW FROM MODE 1 TO MODE	6 IS	0.0030	-0.0368

THE TOTAL APPARENT EVA IS 0.059108 IN PER UNIT

BUS	VOLTAGE	POWER SCHEDULED	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	MO.
1	1.0000	0.0000	0.0272	0.0474	0.0272	0.0474	0.0074	0.0074	0.0000	10	1	1.	1.43
2	0.9996	-0.0005	-0.0115	-0.0087	-0.0115	-0.0087	0.0060	0.0060	0.0000	10	1	1.	1.43
3	0.9996	-0.0002	-0.0157	-0.0307	-0.0157	-0.0307	0.0074	0.0074	0.0000	10	1	1.	1.43
4	0.9990	-0.0003	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	10	1	1.	1.43
5	1.0000	-0.0001	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	10	1	1.	1.43
6	0.9991	-0.0003	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	10	1	1.	1.43

STATE OF THE VEHICLES AT 2 SEC														
1	W	913.11	0.00	0.00	0.00	0.00	0.00	0.0	0.00	10	1	4.	1.57	1
2	E	11775.24	5.10	0.00	5.44	0.00	0.00	105.4	39.1	10	1	1.	1.43	2

BUILDWAY SEGMENTS AT TIME = 3 SEC														
0.	0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N3	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N4	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.W	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	0.N2	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

TABLE 4-1 (CONT'D)

LINE	VELOCITY	ACCELERATION	TIME	MODE	ANGLE	CARS	MCDE	M.P.H.A	MO.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 5.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
GUIDEWAY SEGMENTS AT TIME = 4 SEC									
0. 2.1	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 3.1	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 4.1	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 5.1	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 6.1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
0. 7.1	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 5.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

POWER PLAN SUMMARY AT SIMULATED CLOCK TIME OF 4 SEC

MODE	VELOCITY	ACCELERATION	TIME	MODE	ANGLE	CARS	MCDE	M.P.H.A	MO.
POWER PLAN FROM MODE 1 TO MODE 4 IS 0.0100 - 0.0000									
POWER PLAN FROM MODE 1 TO MODE 5 IS 0.0028 - 0.0052									
POWER PLAN FROM MODE 1 TO MODE 6 IS 0.0110 - 0.0000									

THE TOTAL APPARENT KVA IS 0.100370 IN PER UNIT

BUS	VOLTAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0275	0.1027	0.0208
2	0.9400	-0.0157	-0.0937	0.0208
3	0.9770	-0.0115	-0.0115	0.0000
4	0.9770	-0.0003	0.0001	0.0000
5	0.9770	0.0000	0.0000	0.0000
6	0.9900	0.0000	0.0000	0.0000

STATE OF THE VEHICLES AT 4 SEC

NO.	MODE	VELOCITY	ACCELERATION	IDEAL VEL	GRADE	MIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MCDE	M.P.H.A	MO.
1	W	999.35	1.02	1.02	0.00	0.00	30.1	110.2	0.00	10	1	4.	1.51	1
2	E	11791.77	3.54	0.00	3.54	-7.90	0.00	0.0	0.00	10	1	4.	1.57	2

GUIDEWAY SEGMENTS AT TIME = 5 SEC

LINE	VELOCITY	ACCELERATION	TIME	MODE	ANGLE	CARS	MCDE	M.P.H.A	MO.
0. 6.1	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 7.1	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 8.1	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 9.1	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 10.1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 5.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

GUIDEWAY SEGMENTS AT TIME = 6 SEC

LINE	VELOCITY	ACCELERATION	TIME	MODE	ANGLE	CARS	MCDE	M.P.H.A	MO.
0. 6.1	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 7.1	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 8.1	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 9.1	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 10.1	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 5.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

POWER PLAN SUMMARY AT SIMULATED CLOCK TIME OF 6 SEC

MODE	VELOCITY	ACCELERATION	TIME	MODE	ANGLE	CARS	MCDE	M.P.H.A	MO.
POWER PLAN FROM MODE 1 TO MODE 4 IS 0.0100 - 0.0000									
POWER PLAN FROM MODE 1 TO MODE 5 IS 0.0028 - 0.0052									
POWER PLAN FROM MODE 1 TO MODE 6 IS 0.0110 - 0.0000									

TABLE 4-1 (CONT'D)

POWER FLOW FROM NODE 1 TO NODE 4 IS 0.0101 -0.0366  
 POWER FLOW FROM NODE 1 TO NODE 5 IS 0.0034 -0.0021  
 POWER FLOW FROM NODE 1 TO NODE 6 IS 0.0107 -0.0006

THE TOTAL APPARENT KVA IS 0.0012 IN PER UNIT

BUS	VOLTAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0242	0.0473	0.0073
2	0.9999	-0.0126	-0.0126	0.0073
3	0.9999	-0.0115	-0.0087	0.0000
4	0.9991	-0.0003	0.0000	0.0000
5	0.9999	-0.0001	0.0000	0.0000
6	0.9996	-0.0003	0.0000	0.0000

STATE OF THE VEHICLES AT 6 SEC :

NO.	POSITION	VEL	ACC	REAL VEL	GRADE	WIND	MOTOR	VOLTY	CURRENT	ANGLE	PASS	CARS	KCODE	ALPHA	MO.
1	M	900.35	1.02	0.00	0.00	0.00	0.00	27.3	38.6	0.00	10	1	1.	1.53	1
2	E	11897.72	2.35	0.00	0.74	-7.90	0.00	0.0	0.0	0.00	10	1	4.	1.27	2

GUIDEWAY SEGMENTS AT TIME = 7 SEC

0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.
0. 2.03	12205.000	17160.000	0.	0.	0.	0.	0.
0. 4.04	17160.000	21903.000	0.	0.	0.	0.	0.
0. 6.05	1.000	2050.000	2.	0.	0.	0.	0.
0. 8.06	2050.000	6785.000	0.	0.	0.	0.	0.
2. 0.02	6785.000	11650.000	0.	0.	0.	0.	0.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.

GUIDEWAY SEGMENTS AT TIME = 8 SEC :

0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.
0. 2.03	12205.000	17160.000	0.	0.	0.	0.	0.
0. 4.04	17160.000	21903.000	0.	0.	0.	0.	0.
0. 6.05	1.000	2050.000	2.	0.	0.	0.	0.
0. 8.06	2050.000	6785.000	0.	0.	0.	0.	0.
1. 4.17	0.000	0.025	0.	0.	0.	0.	0.
1. 6.17	0.000	0.025	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 8 SEC :

POWER FLOW FROM NODE 1 TO NODE 4 IS 0.0137 -0.0083  
 POWER FLOW FROM NODE 1 TO NODE 5 IS 0.0125 -0.0107  
 POWER FLOW FROM NODE 1 TO NODE 6 IS 0.0421 -0.1120

THE TOTAL APPARENT KVA IS 0.225045 IN PER UNIT

BUS	VOLTAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0000	0.2117	0.0683
2	0.9929	-0.0023	-0.0179	-0.0935
3	0.9953	-0.0005	-0.1181	-0.0500
4	0.9970	-0.0003	0.0000	-0.0001
5	0.9997	-0.0003	0.0000	0.0000
6	0.9972	-0.0011	0.0000	0.0002

STATE OF THE VEHICLES AT 8 SEC :

TABLE 4-1 (CONT'D)

NO.	MODE	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	NO.	
1	M	913.98	2.04	1.02	2.18	0.00	0.00	57.6	110.3	0.00	10	1	1.	1.49	1	
2	E	11843.04	12.84	3.30	13.16	-7.90	0.00	254.9	150.4	0.00	10	1	4.	1.22	2	
GILDRWAY SEGMENTS AT TIME = 9 SEC																
0.	G.	11650.000	12285.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	12285.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	A.M	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	2050.000	6785.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	A.M	6785.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
GILDRWAY SEGMENTS AT TIME = 10 SEC																
0.	G.	11650.000	12285.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	12285.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	A.M	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	2050.000	6785.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	A.M	6785.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 10 SEC 1																
POWER FLOW FROM NODE 1 TO NODE 4 IS 0.0113 -0.0436																
POWER FLOW FROM NODE 1 TO NODE 5 IS 0.0030 -0.0025																
POWER FLOW FROM NODE 1 TO NODE 6 IS 0.0107 -0.0084																
THE TOTAL APPARENT KVA IS 0.00097 IM PER UNIT																
STATE OF THE VEHICLES AT 10 SEC :																
NO.	MODE	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA <td>NO.</td>	NO.	
1	M	920.36	2.31	0.14	2.45	0.00	0.00	53.5	48.3	0.00	10	1	1.	1.50	1	
2	E	11802.47	13.16	0.00	14.28	-7.90	0.00	0.0	0.0	0.00	10	1	4.	1.57	2	
GILDRWAY SEGMENTS AT TIME = 11 SEC																
0.	G.	11650.000	12285.000	3.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	12285.000	17160.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	A.M	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.	S.M	2050.000	6785.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	A.M	6785.000	11650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
1.	S.TT	0.000	0.025	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

TABLE 4-1 (CONT'D)

GUIDEWAY SEGMENTS AT TIME = 12 SEC									
0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 0.E	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME MF 12 SEC :

POWER FLOW FROM MODE 1 TO MODE 4 IS	0.0121	-0.0435
POWER FLOW FROM MODE 1 TO MODE 5 IS	0.0097	-0.0063
POWER FLOW FROM MODE 1 TO MODE 6 IS	0.0258	-0.0221

THE TOTAL APPARENT KVA IS 0.159603 IN PER UNIT

ONE	VOL-TAGE	PCBR SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0675	0.1419	0.0215
2	0.9993	-0.0144	-0.0440	0.0091
3	0.9950	-0.0511	-0.0954	0.0235
4	0.9999	0.0000	0.0001	0.0000
5	0.9998	-0.0022	0.0000	0.0000
6	0.9977	-0.0011	0.0000	0.0000

STATE OF THE VEHICLES AT 12 SEC :

NO.	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	NO.
1	N	927.94	2.58	0.14	2.72	9.00	50.7	40.3	0.90	10	1	1.	1.12	1
2	E	11020.66	10.32	2.04	10.36	-3.85	333.0	124.8	0.00	10	1	1.	1.12	2

GUIDEWAY SEGMENTS AT TIME = 13 SEC

0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 0.E	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

GUIDEWAY SEGMENTS AT TIME = 14 SEC

0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	11650.000	12205.000	3.	0.	0.	0.	0.	0.	0.
0. 0.E	12205.000	17160.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	17160.000	21903.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	1.000	2050.000	2.	0.	0.	0.	0.	0.	0.
0. 0.E	2050.000	6705.000	0.	0.	0.	0.	0.	0.	0.
0. 0.E	6705.000	11650.000	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.
1. 0.17	0.000	0.025	0.	0.	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 14 SEC :

POWER FLOW FROM MODE 1 TO MODE 4 IS	0.0119	-0.0364
POWER FLOW FROM MODE 1 TO MODE 5 IS	0.0076	-0.0039

TABLE 4-1 (CONT'D)

POWER FLOW FROM MODE 1 TO MODE 6 IS 0.0371 -0.0593

THE TOTAL APPARENT KVA IS 0.114258 IN PER UNIT

BUS	VOL TAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0000	0.0563	0.0123
2	0.9942	-0.0139	-0.0138	0.0073
3	0.9972	-0.0419	-0.0404	0.0146
4	0.9991	0.0000	0.0000	0.0000
5	0.9999	-0.0000	-0.0000	0.0000
6	0.9992	0.0000	0.0000	0.0000

STATE OF THE VEHICLES AT 14 SEC

NO.	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	NO.
1	M	936.02	2.72	0.00	4.00	0.00	59.9	38.8	0.00	10	1	1.	1.49	1
2	F	1100.01	19.72	1.36	21.00	-3.85	0.00	31.0	77.7	10	1	1.	1.04	2

INTERVAL SEGMENTS AT TIME = 15 SEC

0.0-0.1	1120.000	1225.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.1-0.2	1225.000	1710.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.2-0.3	1710.000	2195.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.3-0.4	2195.000	2680.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.4-0.5	2680.000	3165.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.5-0.6	3165.000	3650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.6-0.7	3650.000	4135.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.7-0.8	4135.000	4620.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.8-0.9	4620.000	5105.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.9-1.0	5105.000	5590.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

INTERVAL SEGMENTS AT TIME = 16 SEC

0.0-0.1	1120.000	1225.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.1-0.2	1225.000	1710.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.2-0.3	1710.000	2195.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.3-0.4	2195.000	2680.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.4-0.5	2680.000	3165.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.5-0.6	3165.000	3650.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.6-0.7	3650.000	4135.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.7-0.8	4135.000	4620.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.8-0.9	4620.000	5105.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.
0.9-1.0	5105.000	5590.000	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 16 SEC

POWER FLOW FROM MODE 1 TO MODE 4 IS 0.0227 -0.1045  
 POWER FLOW FROM MODE 5 TO MODE 1 IS 0.0099 -0.0069  
 POWER FLOW FROM MODE 1 TO MODE 6 IS 0.0371 -0.0593

THE TOTAL APPARENT KVA IS 0.150626 IN PER UNIT

BUS	VOL TAGE	POWER SCHEDULED	POWER DELIVERED	DISTORTION CURRENT
1	1.0000	0.0000	0.0545	0.0230
2	0.9913	0.0023	-0.1108	0.0234
3	0.9987	-0.0006	-0.0296	0.0059
4	0.9974	-0.0006	0.0000	0.0000
5	0.9999	-0.0002	0.0000	0.0000
6	0.9993	-0.0006	0.0000	0.0000

STATE OF THE VEHICLES AT 16 SEC

NO.	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	NO.
1	M	931.98	5.44	1.36	5.44	0.00	126.3	134.6	0.00	10	1	1.	1.40	1
2	F	1223.83	22.44	1.36	22.44	-0.52	0.00	31.1	93.0	10	1	1.	0.97	2





TABLE 4-1 (CONT'D)

1.	4.84	1710.000	21903.000	0.	0.	0.	0.
2.	4.84	1.000	2050.000	2.	0.	0.	0.
3.	5.81	2050.000	6785.000	0.	0.	0.	0.
4.	6.82	6785.000	11650.000	0.	0.	0.	0.
5.	8.17	0.000	0.025	0.	0.	0.	0.
6.	9.17	0.000	0.025	0.	0.	0.	0.
7.	9.17	0.000	0.025	0.	0.	0.	0.

POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF 20 SEC :

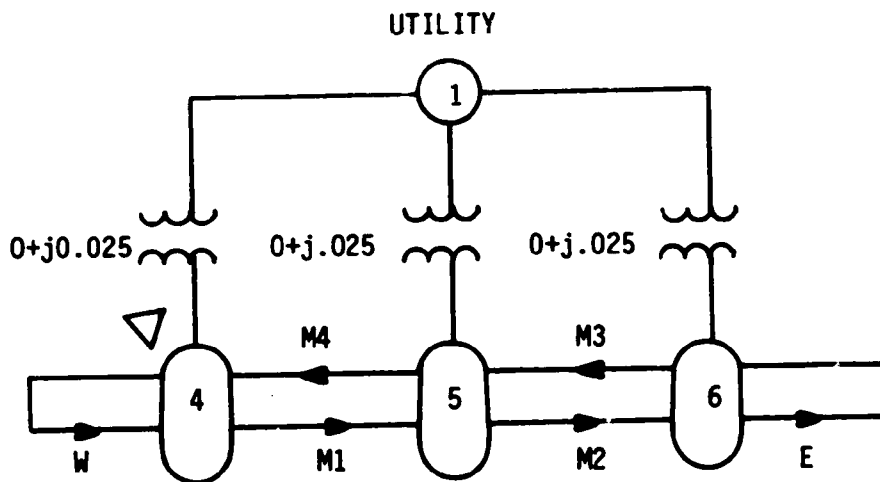
POWER FLOW FROM MODE 1 TO MODE 4 IS	0.0133	-0.0368
POWER FLOW FROM MODE 1 TO MODE 5 IS	0.0036	-0.0020
POWER FLOW FROM MODE 1 TO MODE 6 IS	0.0107	-0.0006

THE TOTAL APPARENT KVA IS 0.055310 IN PER UNITY

BUS	VOLTAGE	POWER SCHEDULED	POWER DELIVERED	DISTURTION CURRENT
1	1.0000	0.0275	0.0474	0.0074
2	0.9967	-0.0159	-0.0306	0.0074
3	0.9997	-0.0003	-0.0007	0.0000
4	0.9991	0.0000	0.0000	0.0000
5	1.0000	0.0000	0.0000	0.0000
6	0.9999	-0.0003	-0.0000	0.0000

STATE OF THE VEHICLES AT 20 SEC :

NO.	W	R	POSITION	VEL	ACC	IDEAL VEL	GRADE	WIND	MOTOR VOLT	CURRENT	ANGLE	PASS	CARS	MODE	ALPHA	NO.
1	W	R	903.89	5.44	0.00	5.44	0.00	0.00	112.0	39.1	0.00	10	1	1.	1.42	1
2	R	R	12105.48	22.64	0.00	22.64	-10.00	0.00	0.0	0.0	0.00	10	1	4.	1.57	2



**KEY:**

① ELECTRICAL NODE

  $0+j0.025$  STEPDOWN TRANSFORMER WITH  $0+j0.025$  PER UNIT IMPEDANCE

 POWER RAIL SEGMENT W


 MILEPOST FROM WHICH ALL VEHICLE POSITIONS ARE MEASURED, AS DISPLACEMENT IN FEET.

FIGURE 4-1 THE TEST CASE POWER RAIL SEGMENTS

## 5. VALIDATION STUDIES

In order to validate the model, two tests were performed. The first compared the program's output to other simulations, while the second compared it to an operating system.

For the first test, we used a model of the Dallas-Fort Worth Airport AIRTRANS system developed by Vought Corporation. Several simulation studies had been done using this model. In essence, the AIRTRANS system consisted of fifteen (one or two car) trains running over fourteen miles of guideway. Four check cases were chosen, and the results of the Vought simulation and our simulation were compared for each case. The results show the electric power values to be similar. Any differences are accounted for by truncation errors (Typically 1%).

For the second test, the four check cases were compared with values measured at the Dallas Fort-Worth Airport. Our check cases are within 10 percent of the typical average real power.

## 6. USING THE MODEL

Three steps are involved in using the model: (1) set up the propulsion system subroutines, (2) create a data file for the guideway, and (3) create a data file for the mission profile.

Step one requires the user to modify the analysis presented in section 3 and then change the subroutines which embed that analysis in the simulation.

Steps two and three involve input data preparation.

Two data files are used by the model. The first contains guideway information; the second contains mission profile information. The size of these data files is recorded in compile-time parameters.

First - consider the guideway file. It is a series of records which are read sequentially into the array GWAY. The parameter GWAYRO specifies the number of records or lines. Each record is read into a row of the array GWAY at columns 1 to 5. The record describes one segment of guideway which connects two points or nodes on the guideway. The following naming convention is used for the guideway: Guideway nodes are integers. Node one is the utility connection. Nodes two and higher are the power cross-unders and power feed points in any order.

The following list describes the record fields:

1. FN - the node number at the beginning of the segment. Vehicles enter the segment at this node.
2. TN - the node number at the end of the segment. Vehicles leave the segment at this node.
3. SI - the two-character segment identifier. This is a unique name for each segment.
4. SD - a distance mark for the FN node. Other points along the guideway are measured with respect to this reference. The units are in feet.
5. ED - a distance mark for the TN node. The length (feet) of the segment is ED-SD.

By convention  $ED > SD$ .

The subrouting SETGW reads in these records and stores them in array GWAY. The compile-time parameter, GWAYRO, defines the number of rows in array GWAY so that the number of rows equals the number of records.

The number of columns in the array GWAY is usually 10. The first five columns are used for the guideway records and the remaining are used for storing the node number of any vehicle which is currently positioned on that guideway segment.

One exception for the guideway data file occurs for the case in which a step-down transformer and/or cables (rather

	FN	TN	SI	SD	ED
2X	3.0	F3.0	A2	F6.0	F6.0

FIGURE 6-1 GUIDEWAY RECORD AND FORMAT

than a power rail) connect two nodes. In that case, the SI field has a special value, "TT". The transformer impedance ( $R+jX$  in per unit) is stored in the SD and ED fields for R and X respectively.

The second data file contains mission profile information. It is a series of records which are read sequentially into the array PFILE. The parameter PFILER specifies the number of records. Each record is read into a row of the array. The record describes one point of the mission profile. An arbitrary number of records are collected together and called a route segment. Figure 6-2 shows this. The data at each mission profile point is described in the following list:



1. DELTA TIME - A NORMAL TIME interval (seconds, between this point and the succeeding profile point. The last record in a route segment has DELTA TIME as 0.
2. VELOCITY - The COMMANDED SPEED UNIT (MPH)
3. GRADE - The encountered grade (%)
4. HEADWIND - The encountered headwind (MPH)
5. LOCATION CODE - A segment identifier (two unique characters) and a distance (feet).

Each such route segment is identified by the row number in PFILE where the first record is. Figure 6-3 shows a collection of route segments in the array PFILE. A complete mission profile data file is contained in Appendix A.

A vehicle's mission is usually a sequence of route segments as Figure 6-4a indicates. So this sequence of route segments is part of a prefix which is included in the mission profile data. The following list describes those data items:

1. Title - a forty character heading which appears on the output
2. ICAR - an array with one column for each vehicle, and an arbitrary number of rows. Column j contains the route segments (by first row number) in the mission profile of vehicle j. The first and last segments are arbitrarily zero.
3. SROW1- a vector with one element for each vehicle.



Its use is as a pointer to ICAR (i.e., vehicle J is initially in route segment ICAR(SROW1(J),J)).

4. SROW2 - a vector with one element for each vehicle. Its use is as a pointer to PFILE (i.e., vehicle J is initially at mission profile point PFILE(SROW2(J), 1 to 6) ).
5. TYM - a vector with one element for each vehicle. Its use is to record remaining station dwell times for the vehicles. It is initialized to 0 usually.

This completes the input data preparation. The program operates with the user providing interaction at a terminal (FORTRAN device TTY). The user is prompted to type in at the terminal the following file names:

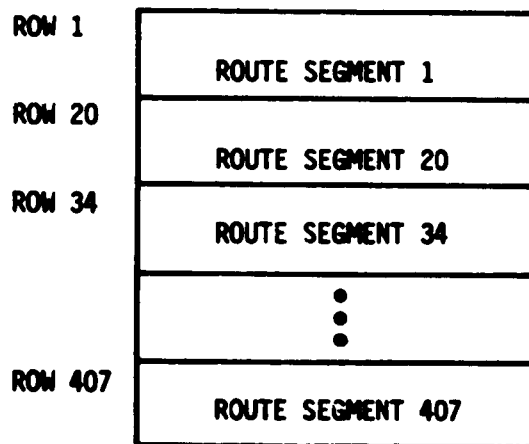
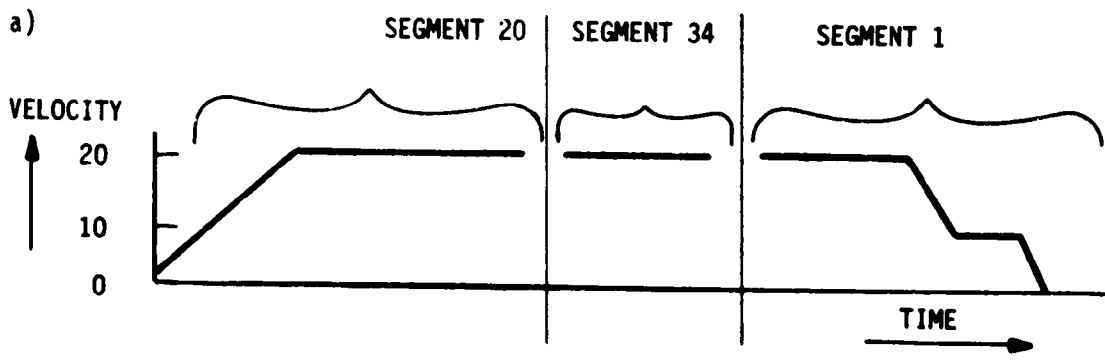


FIGURE 6-3 A COLLECTION OF ROUTE SEGMENTS IN ARRAY PFILE



b)

ICAR	COLUMN J
	0
	20
	34
	1
	0

FIGURE 6-4 THE SEQUENCE OF ROUTES FOR VEHICLE NUMBER  $j$  GRAPHICALLY IN (a) AND AS TABLE ICAR IN (b).

1. a file name for a disk file containing the guide-way data.
2. a file name for a disk file containing the mission profile data.

Subsequent prompting occurs as the user is asked to supply a time interval before the next flow calculations. Entering a negative time terminates the simulation.

All output is written on FORTRAN device number 21.

## 7. CONCLUSIONS

The model described here is capable of simulating a fleet of electric vehicles moving over a guideway network. The output is a discrete and vehicle/power rail interface.

It has been in use for almost one year. It is a useful tool for predicting peak power demand, voltage droop, excessive harmonic currents.

## Appendix A

### A Program Listing (AUGUST 1979)

<u>FILENAME</u>	-	<u>CONTENTS</u>
MAIN2.F4	-	the main program
P. RANR.F4	-	the common block and declarations used in each module
SETUP.F4	-	subroutines SETPEL AND SETGW
VEHDYN.F4	-	subroutine VEHDIN
MOTOR.F4	-	subroutine MOTOR
TEFF.F4	-	block data
NR2.F4	-	subroutine NR
FORMY.F4	-	subroutine FORMV
NEWPQ.F4	-	subroutine NEWPQ
PCU.F4	-	subroutine PCU
GPJ.F4	-	subroutine GETJ,PUTJ
DISTOR.F4	-	subroutine DISTOR
OUTPUT.F4	-	subroutines RITE & VEHSUM
HEDWAY.F4	-	subroutine HEDWAY
NUPNT.F4	-	subroutine NUPNT
NUGWQ	-	subroutine NUGWQ



```

C AND PM POWER AT WHEELS
C CALL VEHICLE
C HAVE ACC, JERR, PT, AND PM APPROPRIATELY LIMITED
VACC(I)=ACC
VACC(I)=VACC
C VACC(I) IS THE ATTAINED ACCELERATION OF VEHICLE II
C FIND THE MOTOR TERMINAL VALUES FOR VEHICLE II
CALL MOTOR
C HAVE VTR, INTR, AND TMR
C HAVE TMR IN A TABLE FOR VEHICLE II
VTR(I)=VTR
TMR(I)=TMR
C VEHICLE II IS UPDATED
CONTINUE
C HAVE ALL NEAR VEHICLES UPDATED
CALL MUGS
C HAVE THE HIGHWAY SEGMENT QUEUES SET UP
CONTINUE
130 SETUP SIMULATED CLOCK TIME
WRITE(LOOPTL,131) TIME
FORMAT(//,23,POWER FLOW SUMMARY AT SIMULATED CLOCK TIME OF,
14,9,23,1,/,)
C SOLVE THE POWER FLOW PROBLEM
CALL NR
C OR "ON THE DC POWER RAIL CABLE CHANGE
C THE ABOVE TO CALL QDC
CALL QDC
C FIND THE DISTORTION CURRENT AT THE BUSES
CALL BISTOR
CALL BITE
C PRINT OUT ON THE LOG FILE A SUMMARY OF THE VEHICLES
CALL VESUM
135 WRITE(77,135)
FORMAT(24,ENTER LOGS TO NEXT SIMUL, IN 13 1')
READ(77,136)
FORMAT(1)
IF(77,LE,0)STOP
9701
140 CONTINUE
CALL MUGS
C HAVE ADVANCED ALL VEHICLES BY 0.1 SECONDS
C SO WE HAVE A NEW FILE # AND ACTUAL POSITION
CALL MUGS
C PRINTED UPDATING THE OUTSTANDING VEHICLE QUEUES
145 IF(77,GT
C IS THE INTERVAL OF TIME BEFORE THE NEXT
C SHAPOT OF THE LOAD FLOW
C VARIABLE IS IN SECONDS
C IF IT IS GREATER THAN 0 THEN ADVANCE THE VEHICLES
IF(77,GT,0) GOTO 140
C FINISHED ADVANCE
C CHECK VEHICLE HIGHWAYS
CALL HIGHWAY
150 150 151,152,153
MUGS(I)
VTR(I)=VTR
ACC=VACC(I)
MUGS(I)=MUGS(I)
MUGS(I)=MUGS(I)
C FIND THE MOTOR TERMINAL VALUES FOR VEHICLE II
CALL MOTOR

```

C HAVE WITH, INTO, AND INTO -  
GIVE THREE IN A TABLE FOR VEHICLE II

TECHNICAL  
TECHNICAL

100

E TAKE MEASUREMENT OF THE LOAD FLOW  
NOTE 130  
END



FRANK, FJ

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DECLARATIONS 6 /0
PARAMETER SS106,SS30,SS300
SS1 = THE NUMBER OF BUSES
SS2 = 2*(SS1-1) THE JACOBIAN MATRIX SIZE
SS3 = 3*(SS1-1) THE NUMBER OF BUSES.
THE NUMBER OF NONZERO TERMS IN
THE ADMITTANCE MATRIX UPPER TRIANGLE
THE SIZE OF Y THE SPARSE ARRAY
IMPLEMENTING THE ADMITTANCE MATRIX

SS4 IS THE SIZE OF THE ARRAY JCOB
USE 100051 OR MORE
PARAMETER SS4000

ICARDO IS THE NUMBER OF ROWS IN ARRAY ICAR
WHICH IS 2 PLUS THE NUMBER OF MISSION PROFILE
SEGMENTS FOR THE LARGEST CAR MOUNT.
PARAMETER ICAR0001

PARAMETER NCA0001,PFIL0002
NCA IS THE NUMBER OF VEHICLES
PFIL IS THE NUMBER OF ROWS IN ARRAY PFIL
I.E. THE NUMBER OF MISSION PROFILE POINTS
PARAMETER QWAT0001
PARAMETER QWAT0010
QWAT0 IS THE NUMBER OF ROWS IN ARRAY QWAT
QWAT0 IS THE NUMBER OF COLUMNS IN QWAT
THE MAX QUEUE SPACE IS QWAT0 NINUS 9
THIS CONTAINS THE MAX NO OF VEHICLES
ON ONE ORIGINWAY SEGMENT

JACOBIAN DATA STRUCTURE FOR NEWTON RAPHSON
USE EITHER SPARSE ARRAY JCOB
OR USE TWO DIMENSIONAL ARRAY JCO

JCO IS THE JACOBIAN MATRIX OF SIZE 3000 OF BUSES
USE A SPARSE ARRAY JCOB FOR THE JACOBIAN
REAL JCOB(004)
JCOB(1) REPRESENTS JACOBIAN(JCB(1),JCC(1))
IF THE ROW IS JCB(1) AND THE COL IS JCC(1)
FOR ELEMENT JCOB(1)
INTEG JCB(004),JCC(004)
JCB(1) IS A POINTER INTO JCOB WHERE JCOB(JCB(1))
IS THE ELEMENT TO THE LEFT OF JCOB(1) AND IN
THE SAME ROW.
INTEG JCB(001)
JCB(1) IS A ROW HEADER AND INDICATES THE
RIGHT MOST ELEMENT IN ROW 11
INTEG JCB(004)
AVAIL IS A POINTER TO THE AVAIL STACK
INTEG AVAIL
REAL JCB(003),JCB2
PUT THEM ALL IN COMMON
COMMON JCB,JCB,JCB,JCB,JCB,JCB,JCB,JCB
COMMON JCO

USE TWO TEMPORARIES FOR THE INVERTER
DIMENSION YINV(003),YINV(003)
DIMENSION P(001),S(001)
P(1) AN, Q(1) ARE THE REAL AND REACTIVE POWER
AT NODE N (OR BUS NUMBER IN N).

```

```

C      COMPLEX E(I,SI)
C      S(M) IS THE COMPLEX VOLTAGE (PER UNIT) AT BUS M
C      INTERG IP(SI),I(ES)
C      YP(M) AND YP(M,SI) ARE THE BUS NUMBERS WHERE
C      ADMITTANCE Y(I,S) IS CONNECTED.
C      COMPLEX Y(ES)
C      Y(M) IS THE COMPLEX ADMITTANCE FROM BUS IP(M) TO
C      BUS Y(M)
C      COMPLEX I(SI)
C      I(M) IS THE COMPLEX PHASE CURRENT (PER UNIT) INTO
C      THE BUS AT BUS NUMBER M.
C      COMPLEX YLC
C      YLC IS THE LINE CHARGING ADMITTANCE AT BUS I
C      IT IS THE SUM OF ALL ADMITTANCES IN ROW I
C      OF THE Y MATRIX
C      REAL Y,YP,Y
C      Y,M,N ARE COEFFICIENTS IN THE EQUATIONS USED
C      FORMED FROM THE JACOBIAN.
C      REAL I,II,I2
C      I1,I2 ARE TEMPORARY VALUES OF CURRENT
C      (PER UNIT) AT THE BUS
C      INTERG I,M,N(I)
C      INTERG I,M,N(II)
C      INTERG I,M,N(I2)
C      IS THE ROW WHERE ANOTHER I,J,K) VALUE IS
C      IF N(I) IS M,N IS 0, THEN
C      YP(I) IS YP(M) THAT IS M IS THE ROW
C      FOR THE NEXT ADMITTANCE CONNECTED TO BUS
C      YP(I)
C      IF N(I) IS 0, THEN NO MORE
C      ADMITTANCE TERMS EXIST IN THE EQUATION
C      FOR NODE YP(I).
C      DIMENSION DP(ES),DO(ES)
C      DP(M) AND DP(M,SI) ARE THE REAL POWER AND
C      REACTIVE POWER SUPPLIED AT BUS NUMBER M.
C      DIMENSION DPWR(ES)
C      DPWR IS A COMPOSITE
C      VECTOR WITH ELEMENTS
C      DP(I),DP(J),DP(SI),DP(II),DP(I2),DO(ES)
C      SHOULD BE USED IN THE VECTOR DISPLAY ROUTINE.
C      DC IS THE DISTORTION CURRENT IN ONE PHASE (PU)
C      DC(M) IS DC AT BUS NUMBER M.
C      DIMENSION DC(ES)
C      INTERG I,I1
C      I1 IS THE LOGICAL OUTPUT DEVICE FOR USER INTERACTION
C      I1, I2 ARE LOG-FILE
C      LOG FILE IS THE LOG FILE FOR THE OUTPUT RECORDS
C      COMPLEX S
C      S IS A TEMPORARY
C      COMMON TIME,VAR,P,Q,E,YP,YO,Y,I,YLC,I,U,V,M,I1,I2
C      COMMON MATRIN,NETCO,DP,DPPOWER,DC
C      COMMON I1,I2,I12
C      DO* THEN ALL IS COMMON
C      THE REGION PROFILE DATA STRUCTURE
C      (CAR(I,J) SUMMARIZES THE
C      ROUTE SEQUENCE FOR CAR J.
C      I01 THE START TIME OF VEHICLE J

```

103,3,0,...ICARNO THE ROW IN PFILE WHERE  
 A ROUTE SEGMENT STARTS. THIS SEQUENCE OF ROUTE  
 SEGMENTS IS FOLLOWED BY CAR J  
 ARROW1(I) IS THE POINTER TO THE ROW IN ICAR COLUMN I WHERE  
 A POINTER TO PFILE EXISTS. THE LATTER POINTER  
 IS TO THE BEGINNING OF VEHICLE I CURRENT ROUTE SEGMENT  
 ARROW2(I) IS A POINTER TO PFILE ROW WHERE THE CURRENT  
 PROFILE POINT FOR VEHICLE I EXISTS.

TIN(I) IS THE NUMBER OF SECONDS LEFT FOR  
 CAR(I) TO REMAIN AT THE MISSION PROFILE  
 POINT INDICATED BY ARROW2(I). TIN(I) IS USEFUL  
 FOR STATION STOPS AND ALLOWING MANY PROFILE  
 POINTS TO BE COMBINED INTO ONE  
 INSTANTANEOUS POINT.

EACH ROW OF PFILE IS A POINT ON THE MISSION  
 PROFILE -

- COL 1 IS DELTA TIME
- COL 2 IS VELOCITY (MPH)
- COL 3 IS MEASURING (MPH)
- COL 4 IS WIDENING GRADE (PERCENT)
- COL 5 IS LOCATION CODE PREFIX- TWO LETTERS
- COL 6 IS LOCATION CODE FIVE DIGITS

ICAR(SICAR) SPECIFIED THE NUMBER OF CARS PER VEHICLE -

PI IS 1-101924  
 PI IS AN INCREMENTAL DISTANCE THAT ALLOWS THE VEHICLES TO  
 OVERSAMPL THE GUIDEWAY SEGMENT DISTANCES  
 INTERM ICAR(ICARNO,ICAR),AROW1(ARCAR),AROW2(ARCAR),TIN(ARCAR)  
 DIMENSION PFILE(PFILE,0),ICAR(SICAR)  
 COMBIN ICAR,AROW1,AROW2,TIN,PFILE,ICARNO,PI,DELTA  
 TIME IS THE TIME INTERVAL BEFORE NEXT CORD FLOW SAMPLED  
 TIME IS THE SIMULATED CLOCK TIME IN SEC,  
 INTERM DT,PT,TIME

WHAT IS THE GUIDEWAY DATA STRUCTURE. EACH  
 ROW IS A LINK BETWEEN GUIDEWAY ROUES. NODES ARE  
 GUIDEWAY NODES, DIVERSIONS, OR POWER FEED POINTS.  
 VEHICLES ARE NOT INCLUDED IN GUIDEWAY NODES.

THE VEHICLE DATA STRUCTURES  
 VEL IS ITS COMMANDED VELOCITY (MPH)  
 VV IS THE ACTUAL VEHICLE VELOCITY IN MPH  
 ACC IS ITS ACCELERATION (MPH/SEC)  
 JACK IS ITS JACK (MPH/SECOND,0)  
 MW IS ITS ENCOUNTERED HEAD WIND (MPH)  
 GRADE IS ENCOUNTERED GRADE (PERCENT)  
 W IS THE VEHICLE MASS IN POUNDS  
 MEAL,JEAR,VEAR  
 COMMON DT,PT,TIME,VEL,ACCL,ACCN,JEAR,JEARN,MW,GRADE,VV,VN

TABLES FOR THE VEHICLE FLEET STATE  
 EACH OF THE FIVE  
 VARIABLES BELOW IS SUBSCRIPTED  
 BY I TO REFER TO VEHICLE NUMBER I.  
 VVEL(I) ACTUAL VELOCITY IN MPH  
 MEAL VVEL(MEAR)  
 VACC(I) ACCELERATION IN MPH PER SEC

REAL VACC(MCAR)  
 POC, (1) TWO LETTER LOCATION CODE  
 POC(2,1) FORTIER IDENTIFICATION CODE  
 REAL POC(3,MCAR)  
 VTYPE(1) MODE OF OPERATION OF VEHICLE  
 1 = VOLTAGE CONTROL; 2 = FELD WEAKENING; 3 =  
 REGENERATIVE BRAKING; 4 = FRICTION BRAKING  
 REAL VMOE(MCAR)  
 VMOE(1) IS THE NUMBER OF PASSENGERS  
 DIMENSION MOWAS(MCAR)  
 MOWAS IS THE NUMBER OF THE VEHICLE UNDER STUDY  
 REAL MOWAS  
 COUPLE(MWTR) IS THE VEHICLE NUMBER TO WHICH NUMBER IS COUPLED  
 INTEGER COUPL(MCAR)  
 PW IS THE PROPULSION POWER IN WATTS  
 PY IS THE REACTIVE POWER IN LOG  
 ALPHA(1) IS THE PHASE DELAY AT VEHICLE 11 (RADIAN)  
 DIMENSION ALPHA(MCAR)  
 PUT THEM ALL IN COMMON  
 COMMON VACC, VMOE, MOWAS, MOWEN, COUPLE, PW, PY, ALPHA

VEHICLE DATA STOPPING  
 COMMON DP, NO, DOC  
 DP IS THE REAL POWER OF SOME VEHICLE (PW)  
 DO IS THE REACTIVE POWER OF SOME VEHICLE (PY)  
 DOC IS THE DISTRIBUTION CURRENT OF SOME VEHICLE (PU)  
 THE MOTOR DATA STRUCTURE  
 MWTR MAGNITUDE OF THE MOTOR TERMINAL VOLTAGE (VOLTS)  
 MWTR MAGNITUDE OF THE MOTOR TERMINAL CURRENT (AMPS)  
 MWTR ANGLE BY WHICH THE LEADS MWTR (DEGREES)  
 THESE THREE ARE FOR ONE PHASE - MWTR IS LINE TO NEUTRAL  
 MWTR IS PHASE CURRENT  
 MWTR MWTR, MWTR, MWTR  
 COMMON MWTR, MWTR, MWTR

A TABLE OF VALUES AT THE MOTOR  
 TERMINALS ON EACH VEHICLE  
 REAL VTM(MCAR), VTM(MCAR), VTM(MCAR)  
 COMMON VTM, VTM, VTM  
 VTM(1) IS THE VOLTAGE AT MOTOR  
 TERMINALS ON VEHICLE NUMBER 11  
 VTM(2) IS THE CURRENT AT THE MOTOR TERMINALS  
 ON VEHICLE NUMBER 11 (AMPS)  
 VTM(3) IS THE ANGLE BY WHICH  
 CURRENT LEADS VOLTAGE AT VEHICLE 11.

EACH ROW OF DATA IS DEVOTED TO A LINE  
 THE COLUMNS ARE  
 1 FROM MODE ITS INTEGER IDENTIFICATION  
 2 TO MODE ITS INTEGER IDENTIFICATION  
 FROM AND TO SHOW TRAVEL DIRECTION OVER THE LINK  
 3 LOCATION CODE PREFIX ON ALL POINTS ALONG THE LINK  
 4 FROM MODE LOCATION CODE SUFFIX  
 5 TO MODE LOCATION CODE SUFFIX  
 6 TO 19 THESE COLUMNS ARE A OVERS OF THE VEHICLES ON  
 THAT LINK EACH VEHICLE IDENTIFIED BY ITS BUGS NUMBER 2 TO MCAR  
 PAGE 11

A SPECIAL CASE IF LOC CODE IS IT THEN IT IS NOT A

C GUIDEWAY LINK BUT A TRANSFORMER OR CABLE LINK  
C THEN COL 4 AND 2 ARE .176 PER UNIT  
C IMPEDANCE REAL AND IMAGINARY PARTS.  
COMMON DATA (CHARTS, GRAPHS)

C TITLE IS A TEN ELEMENT ARRAY FOR  
C TEMPORARY ALPHABETIC IMPEDANCE (ION  
COMMON TITLE(10)

C SET IS THE GUIDEWAY IMPEDANCE PER FOOT IN PER UNIT

COMMON SET(10)

C IS THE GUIDEWAY ADMITTANCE FOR SOME  
C DISTANCE ELEMENT IN WEIGHTS PER UNIT.

COMMON IS(10)

C PUT THEM IN COMMON

COMMON SET(10)

C VRAIL IS THE COMPLEX PHASE VOLTAGE AT SOME VEHICLE

C POSITION ALONG THE POWER RAIL

COMMON VRAIL

COMMON VRAIL



```

C   : * THE SWING BUS, 2 THRU MCA01 ARE THE VEHICLES,
C   AND MCA01 AND UP ARE GUIDEWAY MERGE AND DIVERGE
C   PLATS ON HOSES CONNECTING GUIDEWAY SEGMENTS *
C   1077END3R
C
C   GO 100 11,1, GWAY0
C   CORRECT THE FROM AND TO NODE NUMBERS ON GWAY ROM 11
C   FOR ALL BUT NODE 1 THE SWING BUS *
C   IF(GWAY(11,1),GT,1) GWAY(11,1)GWAY(11,1)+10FF
C   IF(GWAY(11,2),GT,1) GWAY(11,2)GWAY(11,2)+10FF
C   CONTINUE
C   100
C   ALL NODE NUMBERS CONNECTED *
C   WRITE(L06715,200)((GWAY(11,11),JJ),JJ=1,9),1101,GWAY0)
C   FORMAT(12,F12.0,12,F12.0,12,F12.0,12,F12.0)
C   RETURN
C   200
C   CONTINUE
C   1000
C   700 LITTLE DATA *
C   WRITE(L11,200)
C   FORMAT(75,750 LITTLE GUIDEWAY DATA)
C   300
C   STOP
C   END

```









BLOCK DATA  
INCLUDE \*PARAM.F4  
DATA P1/3.151926/DELH/S.O/ CIGARS.II.II.II-1.MCAR.I/MCAR.01/1  
0 (MUNP311) 11-1.MCAR1/MCAR.01/JERUN/10.07.ACCN/5.07  
EMP

44 4441

NR2.FX

```

SUBROUTINE NR
  INCLUDE 'PARAM.F4'
  NUTON RADIOM SOLUTION
  INPUT IS A MATRIX OF ADMITTANCE VALUES Y
  OUTPUT IS THE VOLTAGE AND POWER AT EACH BUS
  BUS ONE IS THE GIVING BUS

  DATA EP01L,01/
  EQUALS IS THE ACCURACY REQUIREMENT FOR
  CONVERGENCE.

  NR CALLS POWER
  IF FULL ARRAY IS USED FOR THE JACOBIAN
  MINVOS (MATRIX INVERTER)
  POWER
  NR IS CALLED BY MAIN
  STEP 1 FORM THE BUS ADMITTANCE MATRIX Y(P,Q),MISOL
  CALL POWER
  STEP 2 ASSUME INITIAL BUS VOLTAGES IS ARRAY E.
  GO TO 101,051.
  101,051.
  CALLS CDBAL(1,0,0,0)
  101,051,051.
  CALLS THE SCHEDULED P AND Q AT EACH NODE,
  CALCULATES THE FUNCTION OF BUS VOLTAGES
  CALL NEWPS
  CALL BITE
  STEP 3 SET THE ITERATION COUNT K TO 0
  NR
  K TIMES THE BUS VOLTAGES HAVE BEEN UPDATED.
  STEP 4 CALCULATE THE SUPPLIED REAL POWER AND REACTIVE
  POWER INTO THE SYSTEM AT NODE N,
  IS DP(N) AND DQ(N)

  FIRST READ OUT DP AND DQ
  PRINTING
  GO TO 101,051
  101,051,051.
  PRINTING
  PRINTING
  CONTINUE
  20 NOW GO THROUGH EACH ADMITTANCE Y IN ANY ORDER
  P= 101,051,051
  IF (Y(P,Q),00,0) GO TO 301
  YP(11) = Y(P,Q) * REAL(S(YQ))
  IF NOT AT THE STARTING POINT WE HAVE
  Y(11) CORRECTED FROM YP(11) TO YQ(11)
  YQ(11)
  YP(11)
  YQ(11)
  SAVE THE BUS MEMBERS
  DCALM(1,1,1)
  DCALM(1,1,1)
  GIVE THE REAL AND IMAG PART OF THE ADMITTANCE
  Y(P,Q) = Y(P,Q) * REAL(S(YQ))
  Y(P,Q) = Y(P,Q) * REAL(S(YQ))
  YP(11) = Y(P,Q) * REAL(S(YQ))
  YQ(11) = Y(P,Q) * REAL(S(YQ))
  DCALM(1,1,1)
  DCALM(1,1,1)
  BUS TO(11) TO YP(11)
  BUS TO(11) TO YQ(11)
  UNLESS IT SHOULD BE THAT IS
  WE HAVE A DRIVING POINT ADMITTANCE

```



```

DO=AIMAG((1,1))
IP0(1,1)=1
IP1(1,1)=1
IP2(1,1)=1
IP3(1,1)=1
IP4(1,1)=1
IP5(1,1)=1
IP6(1,1)=1
IP7(1,1)=1
IP8(1,1)=1
IP9(1,1)=1
IP10(1,1)=1
IP11(1,1)=1
IP12(1,1)=1
IP13(1,1)=1
IP14(1,1)=1
IP15(1,1)=1
IP16(1,1)=1
IP17(1,1)=1
IP18(1,1)=1
IP19(1,1)=1
IP20(1,1)=1
IP21(1,1)=1
IP22(1,1)=1
IP23(1,1)=1
IP24(1,1)=1
IP25(1,1)=1
IP26(1,1)=1
IP27(1,1)=1
IP28(1,1)=1
IP29(1,1)=1
IP30(1,1)=1
IP31(1,1)=1
IP32(1,1)=1
IP33(1,1)=1
IP34(1,1)=1
IP35(1,1)=1
IP36(1,1)=1
IP37(1,1)=1
IP38(1,1)=1
IP39(1,1)=1
IP40(1,1)=1
IP41(1,1)=1
IP42(1,1)=1
IP43(1,1)=1
IP44(1,1)=1
IP45(1,1)=1
IP46(1,1)=1
IP47(1,1)=1
IP48(1,1)=1
IP49(1,1)=1
IP50(1,1)=1
IP51(1,1)=1
IP52(1,1)=1
IP53(1,1)=1
IP54(1,1)=1
IP55(1,1)=1
IP56(1,1)=1
IP57(1,1)=1
IP58(1,1)=1
IP59(1,1)=1
IP60(1,1)=1
IP61(1,1)=1
IP62(1,1)=1
IP63(1,1)=1
IP64(1,1)=1
IP65(1,1)=1
IP66(1,1)=1
IP67(1,1)=1
IP68(1,1)=1
IP69(1,1)=1
IP70(1,1)=1
IP71(1,1)=1
IP72(1,1)=1
IP73(1,1)=1
IP74(1,1)=1
IP75(1,1)=1
IP76(1,1)=1
IP77(1,1)=1
IP78(1,1)=1
IP79(1,1)=1
IP80(1,1)=1
IP81(1,1)=1
IP82(1,1)=1
IP83(1,1)=1
IP84(1,1)=1
IP85(1,1)=1
IP86(1,1)=1
IP87(1,1)=1
IP88(1,1)=1
IP89(1,1)=1
IP90(1,1)=1
IP91(1,1)=1
IP92(1,1)=1
IP93(1,1)=1
IP94(1,1)=1
IP95(1,1)=1
IP96(1,1)=1
IP97(1,1)=1
IP98(1,1)=1
IP99(1,1)=1
IP100(1,1)=1

```



























6  
P.215  
4

```

SUBROUTINE GETJVAL,I,J,K
LOOK UP THE VALUE OF JACOBIAN (I,J)
THE RESULT GOES IN VAL
SAVE THE JACOBIAN ARRAY IN JACOB
SEARCH ARRAY JCOR
K IS A STARTING POINT FOR THE SEARCH
K=0, GET K TO JAC(I)
K=0, START LOOKING AT JCOR(K)
CHECK PARAM, P4
CHECK TRAP PARAMETERS
IF (I.EQ.1 .AND. I.LT.83)
  AND J.EQ.1 .AND. J.LE.83)GOTO 300
WRITE(UNIT=99)I,J
PRINT(UNIT=99)JACOBIAN ARRAY DESCRIPTR ' ,313)
300
CONTINUE
IF (I .AND. J ARE LOCAL JACOBIAN DESCRIPTR
IF (I.EQ.0) K=JAC(I)
K IS NOW POINTING AT A LOCATION IN THE
SEARCH ARRAY. USE IT TO START THE SEARCH.
LOOK AT JCOR(K), AN ELEMENT IN ROW I
CONTINUE
IF (K.EQ.0) .AND. K.EQ.1)GOTO 100
NOT FOUND TRY IN ROW I
K=K+1
IF (I.EQ.0)GOTO 300
K POINTS TO AN ELEMENT IN ROW I
GOTO 10
CONTINUE
PARAM I
WRITE(UNIT=99)K
GOTO 310
CONTINUE
NOT FOUND
310
CONTINUE
HAVE FOUND VAL AND K
IF VAL IS ZERO THEN K IS ZERO
IF VAL IS NOT ZERO THEN VAL IS JCOR(K)
RETURN
END
SUBROUTINE PUTJVAL,I,J,K
GIVE A VALUE VAL AND A POINTER WITH
WHICH TO START SEARCHING LOOK FOR
JACOBIAN(I,J) IN THE SEARCH ARRAY JCOR
STARTING AT JCOR(K) TO K=0
WHEN FOUND STORE VAL IN JACOBIAN(I,J)
IF VAL.EQ.0, THEN SEARCH ARRAY JCOR
DOES NOT STORE IT EXPLICITLY
CHECK PARAM, P4
IF (I.EQ.1 .AND. I.LT.83)
  AND J.EQ.1 .AND. J.LE.83)GOTO 300
WRITE(UNIT=99)I,J
PRINT(UNIT=99)JACOBIAN ARRAY DESCRIPTR ' ,313)
300
CONTINUE

```

1000 IF THE NUMBER OF ELEMENTS EXAMINED  
 1000 IS SET UP POINTERS SO I, J, K, ED, IS THIS  
 1000 THEN ROW I, AND K FOLLOW I.

```

C      IF(I.E.0)M=JMH(I)
C      IF(I.E.0)M=JMC(I)
C      CHECK THE I VALUE
C      IF(I).E.0)GOTO 100
C      HAVE JCOB(K) AS THE PLACE TO START THE SEARCH
C      CHECK THAT THIS IS THE CORRECT ROW
C      CONTINUE
C      IF I7 JACOBIAN(I,J) HAS BEEN FOUND
C      IF(JC(I),0) .AND. JCC(I),0) GOTO 300
C      NOT FOUND ADVANCE LEFT ONE COLUMN
C      IF(JC(I),0) GOTO 100
C      K=I
C      K=JMC(K)
C      IF(I).E.0)GOTO 100
C      POINT TO THE LAST I THAT HAS I
C      IF(JC(I),0) GOTO 17
C      WE HAVE A NEW PLACE JCOB(K) WHICH IS PROMISING
C      IC=I+1
C      IF(I.C.0)GOTO 10
C      CONTINUE
C      WRITE(I7,I7)I7,J,K
C      WRITE(I7,I7)JCOB(K),K
C      WRITE(I7,I7)JCOB(I),JCC(I),JCC(I),
C      NAME(I),M(I),I7,I7,I7,I7,I7,I7,I7,I7,I7,I7
C      FORMAT(9,49)
C      FORMAT(9,49)
C      JACOBIAN PROVIDE SEARCHING FOR '219'
C      ADVANCE BY ONE '14)
C      STOP
C      CONTINUE
C      JACOBIAN(I,J) IS NOT IN THE ROW
C      ITS PREVIOUS VALUE IS ZERO
C      INSERT ITS NEW NONZERO VALUE INTO THE RIGHT OF
C      JCOB(I)
C      IF(AVAIL) LT (I-30)RETURN
C      GET A NEW LOCATION FROM AVAIL
C      IF NONE AVAILABLE EXIT
C      IF(AVAIL)E.0)GOTO 400
C      HAVE A LOCATION AT AVAIL
C      JCOB(AVAIL)
C      JCC(AVAIL)
C      JCC(AVAIL)
C      IF(I.E.0)M(I)=AVAIL
C      IF(I.E.0)M(I)=JMC(AVAIL)
C      K=AVAIL
C      AVAIL=JMC(AVAIL)
C      JMC(I)=I
C      INSERTION AND AVAIL STACK BOOKKEEPING IS DONE
C      RETURN
C      CONTINUE
C      FORM THE JACOBIAN(I,J) AT JCOB(K)
C      IF(I)AVAIL) LT (I-30)M=JCC(I),M=JCC(I)GOTO 300
C      UPDATE THE PREVIOUS NONZERO VALUE TO A NEW
C      NONZERO VALUE
C      JCOB(I)=M
C      K=I
C      RETURN
C      CONTINUE
C      UPDATE THE PREVIOUS NONZERO VALUE TO A NEW VALUE = ZERO
C      IF(I.E.0)M(I)=JMC(K)
C      IF(I.E.0) JMC(I)=JMC(I)

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```

SUBROUTINE BITE
  WRITE(*,*) 'PRINT POWER AND VOLTAGE AT EACH MODE -'
  CALL BITE(1)
  DO 10 I=1,4
    WRITE(*,*) 'MODE', I
    CALL BITE(I)
  10 CONTINUE
  WRITE(*,*) 'END'
  RETURN
END

```

```

SUBROUTINE BITE
  WRITE(*,*) 'PRINT POWER AND VOLTAGE AT EACH MODE -'
  CALL BITE(1)
  DO 10 I=1,4
    WRITE(*,*) 'MODE', I
    CALL BITE(I)
  10 CONTINUE
  WRITE(*,*) 'END'
  RETURN
END

```













NK-645,54

IS THE CURRENT MISSION PROFILE  
IF A IT POSSIBLE SHOW PROFILE TO FILE  
IF A IT POSSIBLE SHOW PROFILE TO FILE  
IF A IT POSSIBLE SHOW PROFILE TO FILE

OF COLUMN 4 TO CHAYCO  
LEFT JUSTIFY THE QUEUE, VEHICLES  
ENTER AT A AND EXIT AT THE END NEAR CHAYCO

THE STRATEGY IS CHOOSE A VEHICLE  
FROM ITS POSITION CODE, FIND WHICH  
VEHICLE IS NEAREST TO IT ON A SCAN THE  
QUEUE OF VEHICLES ALREADY ON THAT SEGMENT  
AND IS IN THE CORRECT SPOT IF ROOM EXISTS

FROM EXPLANATIONS  
INCLUDE SPANISH, PA  
TEMPORARY LOCATION CODES HAVE PREFIX  
PART OF LAB NUMBER PART OF  
LAB, PA, 05  
THROUGH 006

INSERT OUT ALL THE QUEUES  
IN A FILE, CHAYCO  
ON A JUNE, CHAYCO  
CHAYCO, CHAYCO  
CHAYCO, CHAYCO  
CHAYCO

SELECT A VEHICLE  
DO NOT SHOW, CHAYCO  
PLACE VEHICLE JJ  
FROM THE LOCATION CODES FIND  
IF IS THE THE LETTER PREFIX OF IS THE DISTANCE  
FROM(1,1,1)

FROM THE CURRENT SEGMENT FOR VEHICLE JJ  
IF(1,1,1) CHAYCO(1,1,1) INTO 30  
IF(1,1,1) CHAYCO(1,1,1) ON SC OF CHAYCO(1,1,1) GOTO 30  
FROM THE CURRENT SEGMENT AT HOW IT OF CHAY

FROM 30  
CONTINUE  
CALL FROM 17  
WRITE(1,1,1), CHAYCO(1,1,1)  
FROM(1,1,1) HAS PROFILE POINT FOR VEHICLE '1,1,1'  
'1,1,1' (1,1,1)  
CALL FROM  
WRITE(1,1,1), CHAYCO(1,1,1) INTO 30  
WRITE(1,1,1), CHAYCO(1,1,1) ON SC OF CHAYCO(1,1,1)  
'1,1,1' (1,1,1)

FROM 30  
CONTINUE  
FROM THE LOCATION CODES OF VEHICLE JJ  
ON CURRENT SEGMENT CHAYCO(1,1,1)  
INSERT IN THE QUEUE  
IF(1,1,1) CHAYCO(1,1,1) INTO 30  
FROM 30  
FROM THE NEXT SEGMENT 6 COLUMN IN THE QUEUE



## Appendix B

### A Program Concordance

The following table lists the important terms and variables used in the program which is listed in Appendix A:

1. Main program - it prompts the user for input data, sets up the state of the vehicles, initiates the load flow computation and updates the state of the vehicles. The latter two steps can be repeated. Main global symbols:
  - VVEL(II) - vehicle II velocity (MPH)
  - PØS(1,II) - location of vehicle II in terms of a guideway segment identifier
  - PØS(2,II) - vehicle II position (FEET) from a reference
  - TYM(II) - vehicle II dwell time (sec.)
  - VACC(II) - vehicle II acceleration (MPH/sec)
  - TVM(II) - motor terminal voltage at vehicle II (VOLTS)
  - TIM(II) - motor terminal current at vehicle II (AMP)
  - TTM - if POWER FLOW INTO MOTOR THEN 0, ELSE NONZERO.
2. SETPFL - a subroutine which prompts the user for a source (disk file name) of the mission profile input data.
  - IFIL - mission profile data file name
3. SETGW - a subroutine which prompts the user for a source (disk file name) of the guideway input data.
  - IFIL - guideway data file name
4. VEHDYN - a subroutine which handles the vehicle dynamics



5. MOTOR - a subroutine which models a separately excited dc motor
6. TEFF - the block data to initialize values in common
  - ICARS(II) - number of cars coupled together for vehicle II
  - NUMPAS(II) number of passengers on vehicle II
  - JERKM - Maximum jerk limit (MPH/s<sup>2</sup>)
  - ACCM - maximum acceleration limit (MPH/s)
7. NR - the Newton-Raphson load flow subroutine. It will iterate 5 times or until the power mismatch is less than EPSIL
8. FORMY - a subroutine called by NR to calculate the admittance matrix Y
9. NEWPQ - a subroutine called by NR to calculate the scheduled P and Q values for each vehicle.

**GLOBALS**

P(II) - fundamental real power (per unit) at vehicle II.

Q(II) - fundamental reactive power (per unit) at vehicle

II

10. PCU - a subroutine called by NEWPQ to model the power conditioning unit which converts 3 phase power into dc power for the motor

**LOCAL**

PRUX - constant auxiliary load real power at each vehicle (watts)

QUAX - constant auxiliary load reactive power at each vehicle (volt-amp)

AMU - constant commutation angle (radians)

GLOBAL

ALPHA - SCR firing angle (radians)

BP - fundamental real power (per unit) at vehicle under consideration

BQ - fundamental reactive power (per unit) at vehicle under consideration

11. GETJ(VAL,II,J,K) - a subroutine used by NR to look up Jacobian values. It assigns to VAL the Jacobian element at row II, column J. If K is zero then the search for the Jacobian element begins at the end of row. Otherwise the search begins at JCOB(K).
12. PUTJ(VAL,II,J,K) - a subroutine used by NR to update Jacobian values. It assigns to the Jacobian element at row II, column J the value VAL. If K is nonzero, then begin the search for Jacobian element at row II, column J at JCOB(JNC(K)) - otherwise at JCOB(JRH(K)).
13. DISTØR - a subroutine which evaluates the Fourier coefficients of the harmonic currents. Distortion currents at the vehicle/power rail interface and at the electric utility/network interface are calculated.

LOCA-NHAR(I) - a table of harmonics to consider

GLOBAL

DC(I) - RMS harmonic current (per unit) at node I.

14. RITE - a subroutine which prints out the power flow summary
15. VEHSUM - a subroutine which prints out the state (of the vehicles) summary

16. HEDWAY - a subroutine which calculates the distance between vehicles. Its output is a message that the mission profile and vehicle performance have caused some intervehicle distances to shrink below a limit (called HDWY).

LOCAL

HDWY - the limiting distance (feet) in front of a vehicle. It is the vehicle length (feet) plus vehicle velocity (feet per sec) times a reaction time (sec) plus emergency deceleration (feet/sec/sec) times velocity squared divided by 2.

TAU - vehicle reaction time (sec)

EACCEL - emergency deceleration rate (feet/sec/sec)

VLENGTH - vehicle length (feet)

17. NUPNT - a subroutine which advances the vehicle fleet to a new point on the mission profile

GLOBAL

DT - amount of time to advance (sec)

18. NUGWQ - a subroutine which updates all the vehicles' positions on the guideway segments. It changes the vehicle numbers stored in array GWAY columns 6 to 10.

## **Appendix C**

The Fourier analysis integrals described in Section 3.6  
yield the following expressions:

$$\begin{aligned}
A(N) &= \frac{\sqrt{2} I_d}{\pi} \left( \right. \\
&\frac{\cos \alpha}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{-\cos n(\alpha + \mu - \gamma/2)}{n} + \frac{\cos n(\alpha - \gamma/2)}{n} \right] \\
&- \frac{\cos(\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{-\cos(n-1)(\alpha + \mu - \gamma/2)}{2(n-1)} - \frac{\cos(n+1)(\alpha + \mu - \gamma/2)}{2(n+1)} \right] \\
&+ \frac{\cos(\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{\cos(n-1)(\alpha - \gamma/2)}{2(n-1)} - \frac{\cos(n+1)(\alpha - \gamma/2)}{2(n+1)} \right] \\
&+ \frac{\sin(\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{\sin(1-n)(\alpha + \mu - \gamma/2)}{2(1-n)} - \frac{\sin(1+n)(\alpha + \mu - \gamma/2)}{2(1+n)} \right] \\
&+ \frac{\sin(\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{\sin(1-n)(\alpha - \gamma/2)}{2(1-n)} - \frac{\sin(1+n)(\alpha - \gamma/2)}{2(1+n)} \right] \\
&- \frac{\cos n(\alpha + \mu + \gamma/2)}{n} + \frac{\cos n(\alpha + \mu - \gamma/2)}{n} \\
&- \frac{\cos \alpha}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{-\cos n(\alpha + \mu + \gamma/2)}{n} + \frac{\cos n(\alpha + \gamma/2)}{n} \right] \\
&+ \frac{\cos(-\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{-\cos(n-1)(\alpha + \mu + \gamma/2)}{2(n-1)} - \frac{\cos(n+1)(\alpha + \mu + \gamma/2)}{2(n+1)} \right] \\
&- \frac{\cos(-\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{-\cos(n-1)(\alpha + \gamma/2)}{2(n-1)} - \frac{\cos(n+1)(\alpha + \gamma/2)}{2(n+1)} \right] \\
&+ \frac{\sin(-\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{\sin(1-n)(\alpha + \mu + \gamma/2)}{2(1-n)} - \frac{\sin(1+n)(\alpha + \mu + \gamma/2)}{2(1+n)} \right] \\
&+ \frac{\sin(-\gamma/2)}{\cos \alpha - \cos(\alpha + \mu)} \left[ \frac{\sin(1-n)(\alpha + \gamma/2)}{2(1-n)} - \frac{\sin(1+n)(\alpha + \gamma/2)}{2(1+n)} \right] \left. \right)
\end{aligned}$$

$$\begin{aligned}
B(N) = \frac{\sqrt{2} I_d}{\pi} & \left( \right. \\
& \frac{\cos \alpha}{\cos \alpha - \cos(\alpha+\mu)} \left[ \frac{\sin n(\alpha+\mu-\gamma/2)}{n} \quad \frac{\sin n(\alpha-\gamma/2)}{n} \right] \\
+ \frac{\cos \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ \frac{\sin(1-n)(\alpha+\mu-\gamma/2)}{2(1-n)} + \frac{\sin(1+n)(\alpha+\mu-\gamma/2)}{2(1+n)} \right] \\
+ \frac{\cos \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ \frac{\sin(1-n)(\alpha-\gamma/2)}{2(1-n)} + \frac{\sin(1+n)(\alpha-\gamma/2)}{2(1+n)} \right] \\
+ \frac{\sin \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ -\frac{\cos(1-n)(\alpha+\mu-\gamma/2)}{2(1-n)} - \frac{\cos(1+n)(\alpha+\mu-\gamma/2)}{2(1+n)} \right] \\
- \frac{\sin \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ -\frac{\cos(1-n)(\alpha-\gamma/2)}{2(1-n)} - \frac{\cos(1+n)(\alpha-\gamma/2)}{2(1+n)} \right] \\
+ \frac{\sin n(\alpha+\mu+\gamma/2)}{n} - \frac{\sin n(\alpha+\mu-\gamma/2)}{n} & \\
- \frac{\cos \alpha}{\cos \alpha - \cos(\alpha+\mu)} & \left[ \frac{\sin n(\alpha+\mu+\gamma/2)}{n} - \frac{\sin n(\alpha+\gamma/2)}{n} \right] \\
+ \frac{\cos \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ \frac{\sin(1-n)(\alpha+\mu+\gamma/2)}{2(1-n)} + \frac{\sin(1+n)(\alpha+\mu+\gamma/2)}{2(1+n)} \right] \\
+ \frac{\cos \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ + \frac{\sin(1-n)(\alpha+\gamma/2)}{2(1-n)} + \frac{\sin(1+n)(\alpha+\gamma/2)}{2(1+n)} \right] \\
+ \frac{\cos \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ -\frac{\cos(1-n)(\alpha+\mu+\gamma/2)}{2(1-n)} - \frac{\cos(1+n)(\alpha+\mu+\gamma/2)}{2(1+n)} \right] \\
- \frac{\sin \gamma/2}{\cos \alpha - \cos(\alpha+\mu)} & \left[ -\frac{\cos(1-n)(\alpha+\gamma/2)}{2(1-n)} - \frac{\cos(1+n)(\alpha+\gamma/2)}{2(1+n)} \right] \left. \right)
\end{aligned}$$